

Figures: Snowflake Workload Timeseries Patterns

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1 Introduction

This file includes figures and analysis for Section 2.2 on the Snowflake Workload User Demand Patterns. All figures and analysis are generated from the public dataset.

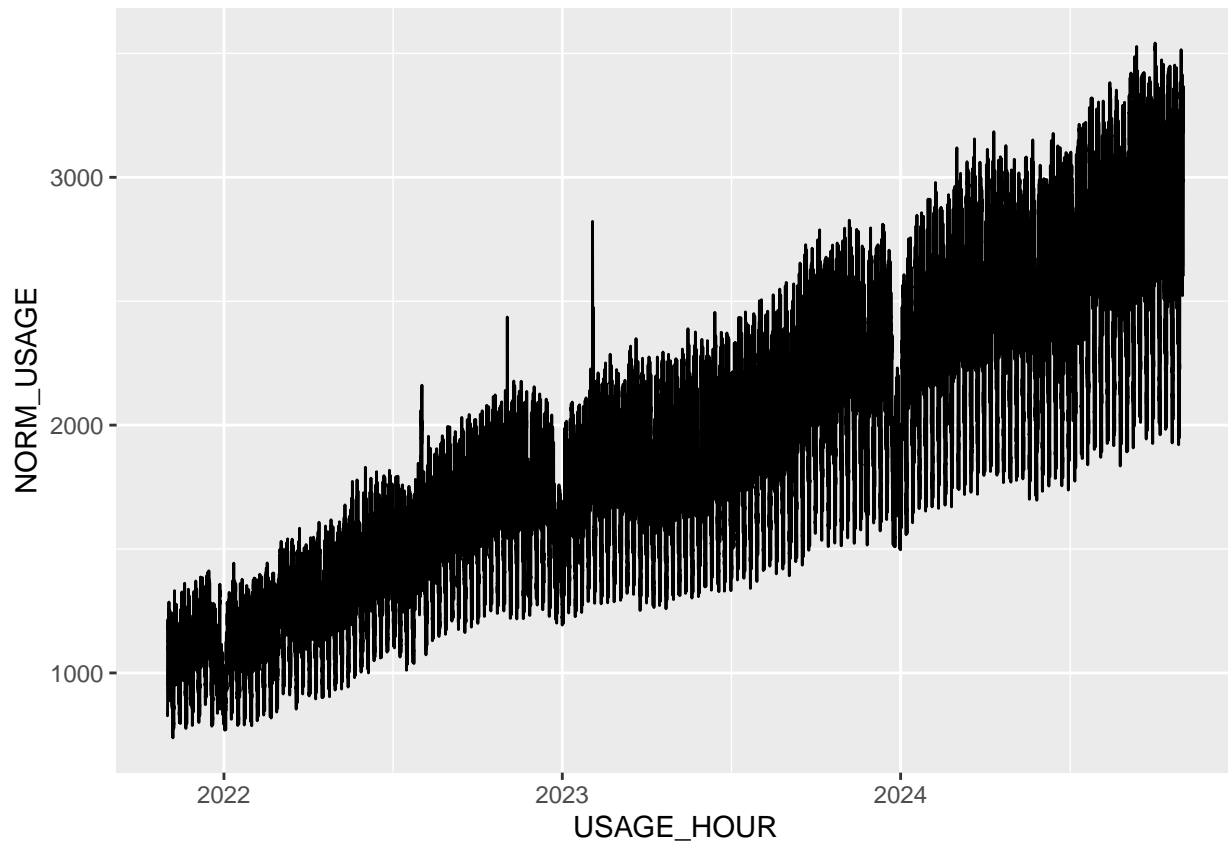
2 Full-Granularity Aggregated Hourly Timeseries

All regions and SKU types aggregated together at full hourly granularity and plotted over the full time range of the data set.

```
data <- read_parquet("../hourly_normalized.parquet")
data.all <- data %>% group_by(USAGE_HOUR) %>% summarise(across(NORM_USAGE, sum))
head(data.all)
```

```
## # A tibble: 6 x 2
##   USAGE_HOUR      NORM_USAGE
##   <dtm>          <dbl>
## 1 2021-11-01 00:00:00      845
## 2 2021-11-01 01:00:00      827
## 3 2021-11-01 02:00:00      841
## 4 2021-11-01 03:00:00      871
## 5 2021-11-01 04:00:00      898
## 6 2021-11-01 05:00:00      940
```

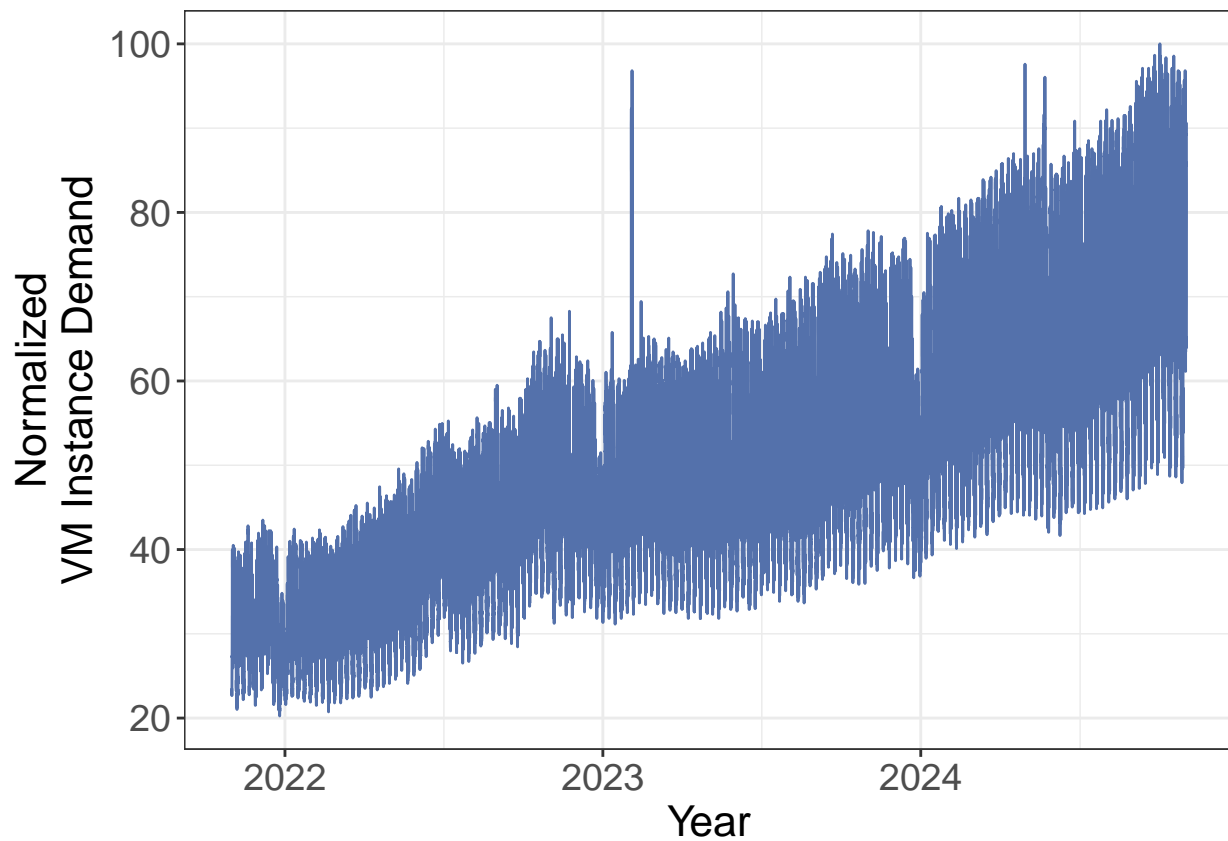
```
ggplot(data.all, aes(x=USAGE_HOUR, y=NORM_USAGE)) + geom_line()
```



2.1 Normalized Full-Granularity Aggregated Hourly Timeseries

All regions and SKU types aggregated together at full hourly granularity and plotted over the full time range of the data set. Normalized with the largest data point at 100.

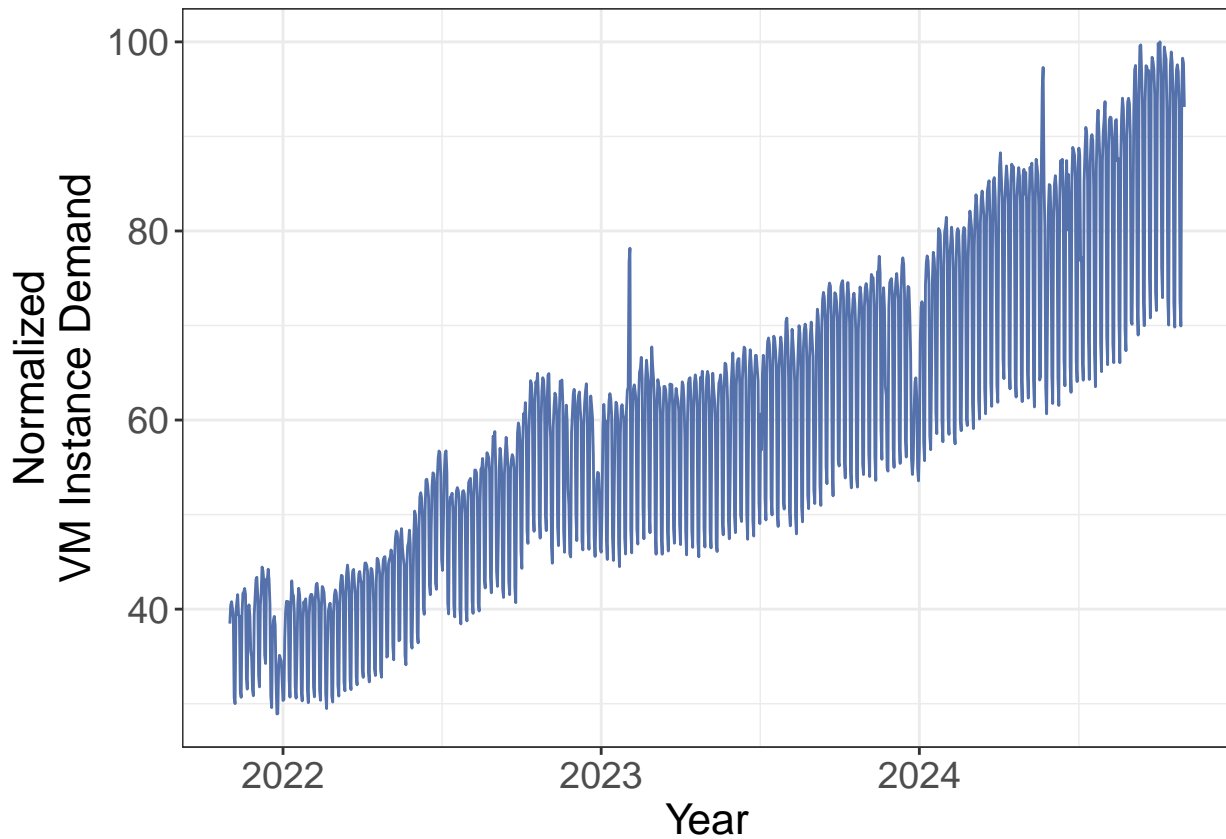
```
data.p1 <- data %>% subset(REGION_NUM == 2) %>% group_by(USAGE_HOUR) %>%
  summarise(across(NORM_USAGE, sum))
data.p1$TOTAL_COMPUTE = data.p1$NORM_USAGE
data.p1$day <- as.Date(data.p1$USAGE_HOUR)
data.p1$TOTAL_COMPUTE = (100*data.p1$TOTAL_COMPUTE) / max(data.p1$TOTAL_COMPUTE)
p1 <- ggplot(data.p1, aes(x=USAGE_HOUR, y=TOTAL_COMPUTE)) + geom_line(color="#5471AB") + theme_bw() + t
old.mai <- par("mai")
par("mai"= c(1,0.9,2,0.4))
p1
```



2.2 Normalized Timeseries of the Daily Means

Plot of the normalized daily means.

```
data.p2 <- data.p1 %>% group_by(day) %>% summarize(DAILY_MEAN = mean(TOTAL_COMPUTE))
data.p2$DAILY_MEAN = (100*data.p2$DAILY_MEAN) / max(data.p2$DAILY_MEAN)
p2 <- ggplot(data.p2, aes(x=day, y=DAILY_MEAN)) + geom_line(color="#5471AB") + theme_bw() + theme(axis.
old.mai <- par("mai")
par("mai"= c(1,0.9,2,0.4))
p2
```



3 Weekly Pattern Analysis

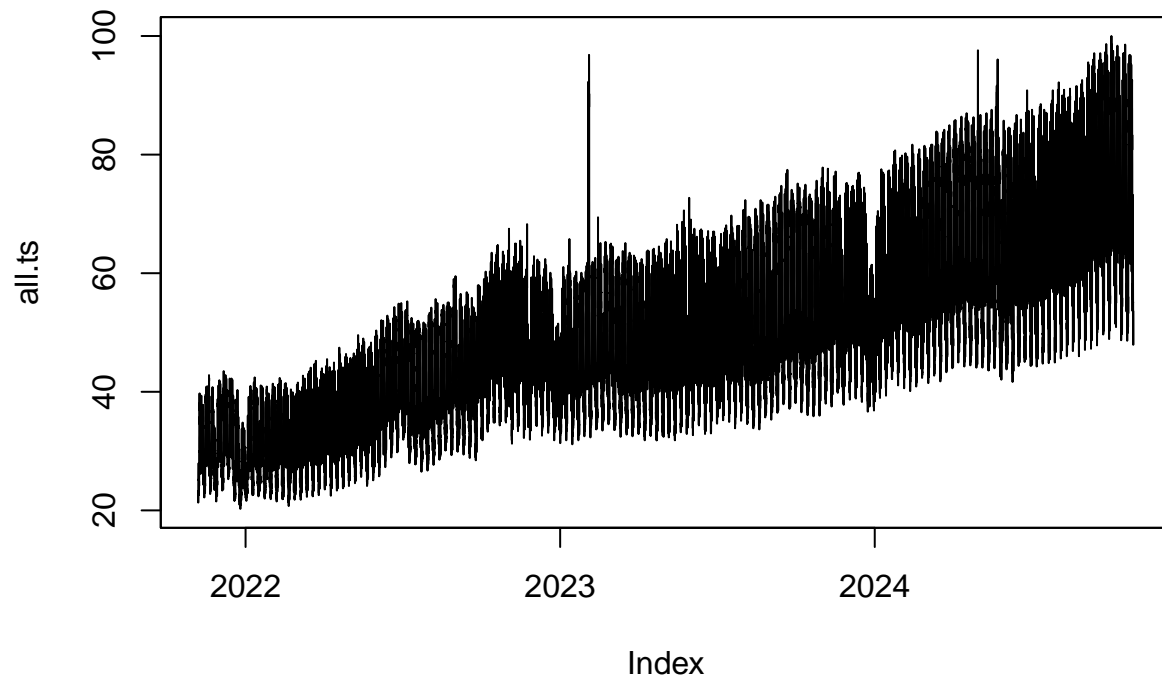
We trim the start and end of our timeseries to align our dataset with Sunday through Saturday weeks so we can split it up in 7 day chunks and look at the distribution of weekly patterns.

We then generate timeseries of the maximum, minimum, and mean of each day.

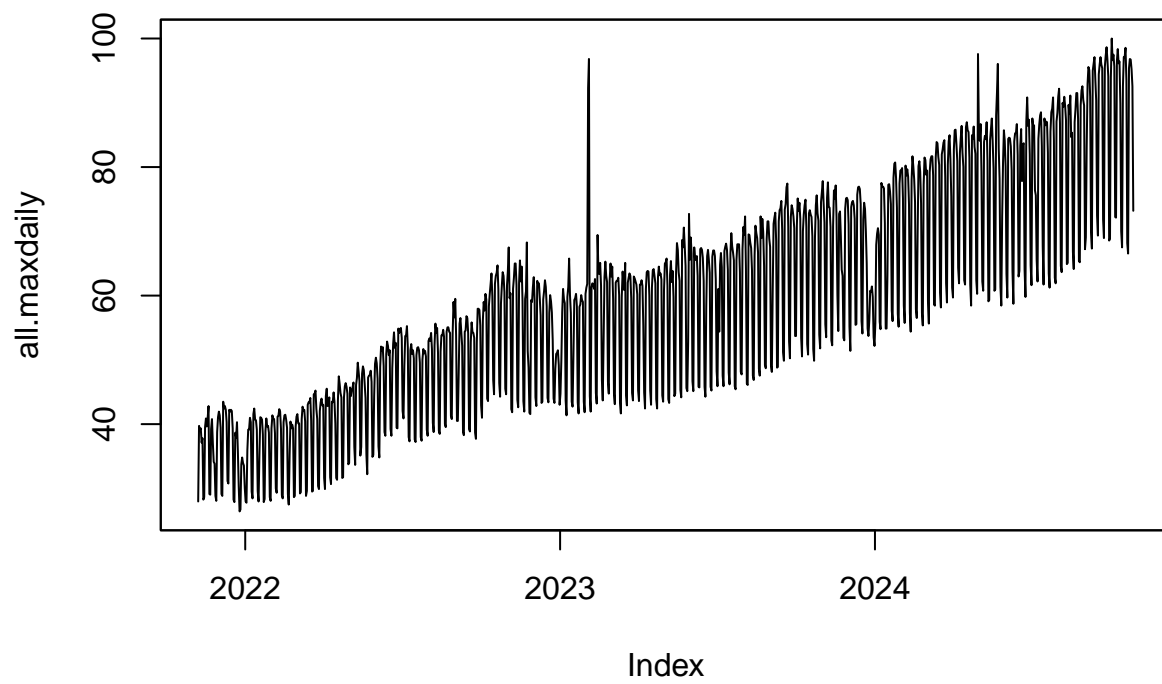
```
all <- data.p1 %>% subset(USAGE_HOUR >= as.POSIXct("2021-11-07", tz="UTC")) %>%
  subset(USAGE_HOUR < as.POSIXct("2024-10-27", tz="UTC"))
range(all$USAGE_HOUR)
```

```
## [1] "2021-11-07 00:00:00 UTC" "2024-10-26 23:00:00 UTC"
```

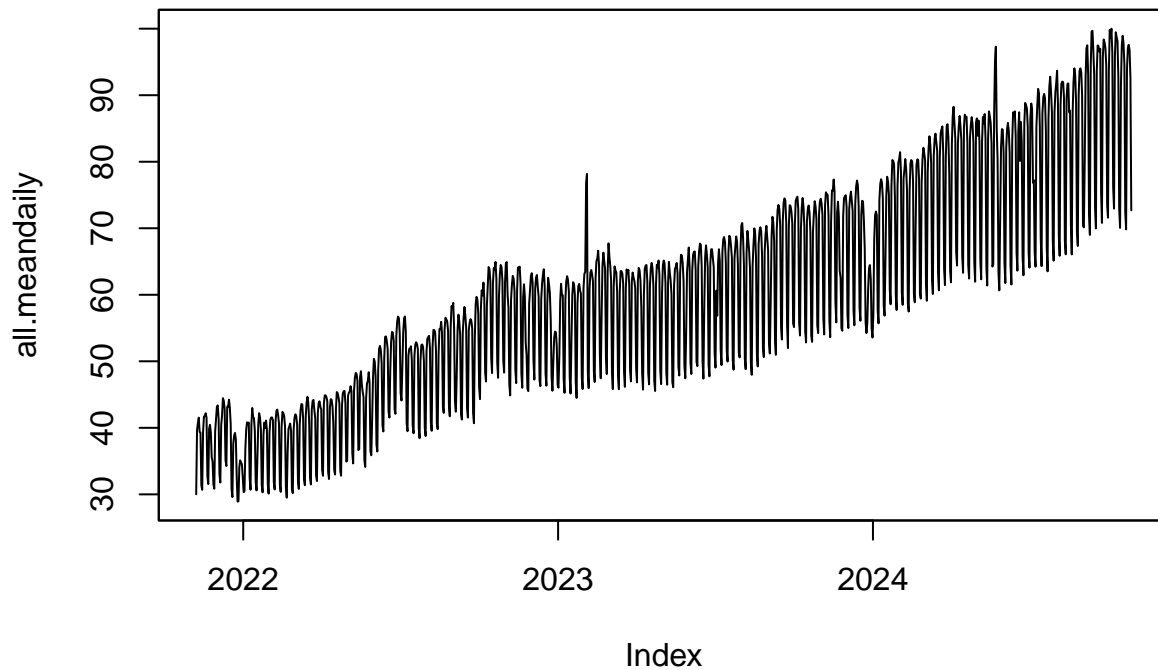
```
all.ts <- zoo(all$TOTAL_COMPUTE, all$USAGE_HOUR)
# Compute the maximums over each day.
all.maxdaily <- rollapply(all.ts, width=24, by=24, FUN=max)
all.meandaily <- rollapply(all.ts, width=24, by=24, FUN=mean)
all.mindaily <- rollapply(all.ts, width=24, by=24, FUN=min)
plot(all.ts)
```



```
plot(all.maxdaily)
```



```
all.meandaily <- 100*all.meandaily/(max(all.meandaily))  
plot(all.meandaily)
```



Next we plot the first two weeks of our dataset to examine the different weekly periodicity.

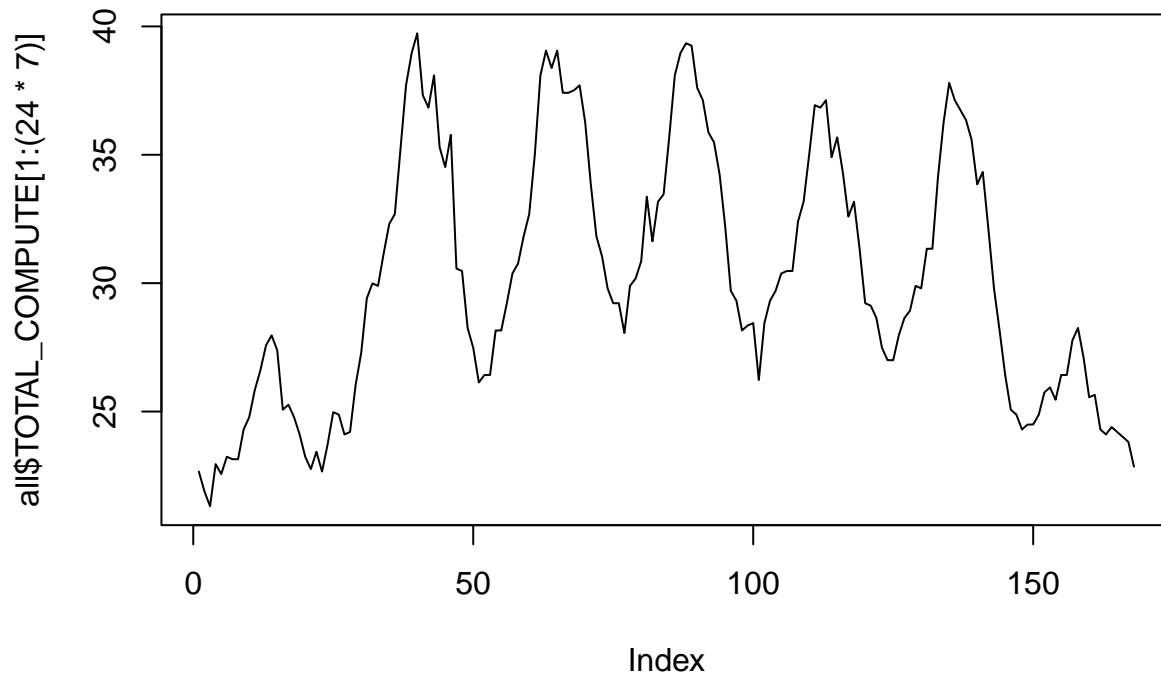
```
range(all$USAGE_HOUR)
```

```
## [1] "2021-11-07 00:00:00 UTC" "2024-10-26 23:00:00 UTC"
```

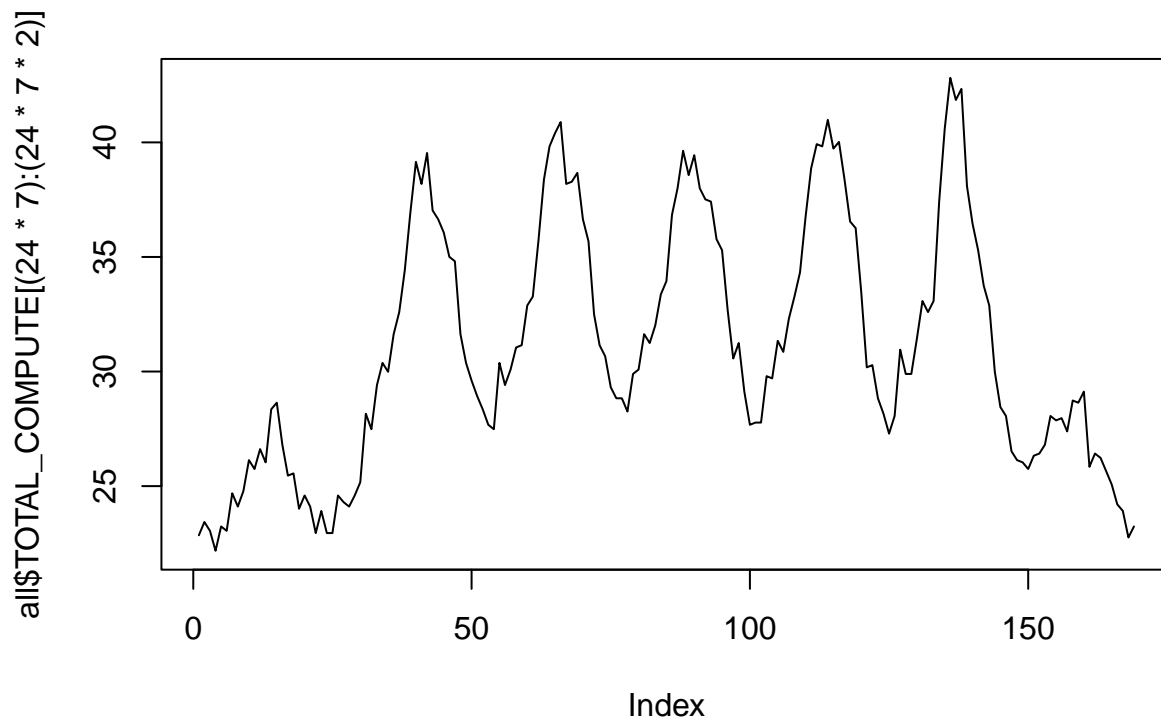
```
head(all)
```

```
## # A tibble: 6 x 4
##   USAGE_HOUR      NORM_USAGE TOTAL_COMPUTE day
##   <dtm>          <dbl>         <dbl> <date>
## 1 2021-11-07 00:00:00      235          22.7 2021-11-07
## 2 2021-11-07 01:00:00      227          21.9 2021-11-07
## 3 2021-11-07 02:00:00      221          21.3 2021-11-07
## 4 2021-11-07 03:00:00      238          23.0 2021-11-07
## 5 2021-11-07 04:00:00      234          22.6 2021-11-07
## 6 2021-11-07 05:00:00      241          23.2 2021-11-07
```

```
plot(all$TOTAL_COMPUTE[1:(24*7)], type="l")
```



```
plot(all$TOTAL_COMPUTE[(24*7):(24*7*2)], type="l")
```



Now we break up the timeseries into 7 day partitions, calculate the quantiles at each time offset within the partitions to compute the range of weekly patterns.

```
weeks <- rollapply(all$TOTAL_COMPUTE, width=24*7, by=24*7,
  FUN=function(x) return(x))
```

*# Now we have a matrix. Each row is one of the 1 week periods of time.
Each 1-week period should be normalized separately to the peak demand that week.*

```

weeks.norm <- apply(weeks, 1, function(x) { return ((100*x)/max(x)) })

# Now for each week, return a data frame and concat them together.
tmp.df <- do.call(rbind, lapply(1:ncol(weeks.norm), function(i) return (
  data.frame(x=weeks.norm[,i], y=1:length(weeks.norm[,i]),
    dow=rep(c("Su", "M", "T", "W", "R", "F", "S"), each=24, times=1))))))

# Now we generate a single data.frame of hourly quantiles. One row for
# each hour in the week (24*7 = 168 rows) with a column for each of 7 different
# percentiles.

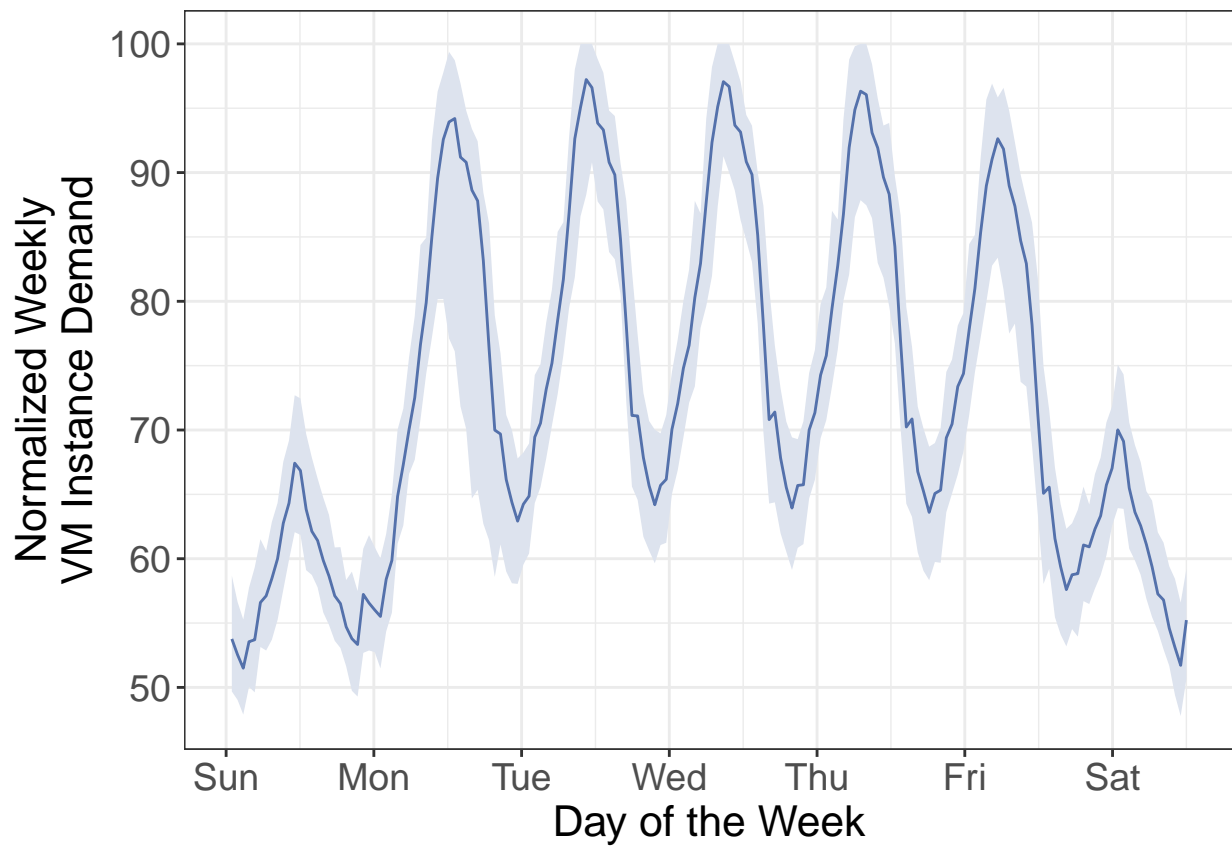
hourly.quantiles <- tmp.df %>% group_by(y) %>%
  summarize(p90 = quantile(x, probs=0.9),
    p95 = quantile(x, probs=0.95),
    p99 = quantile(x, probs=0.99),
    p10=quantile(x, probs=0.1),
    p5=quantile(x, probs=0.05),
    p1=quantile(x, probs=0.01),
    med=quantile(x, probs=0.5))

# Nice x-axis labels for the days of the week.
days <- c("Sun", "Mon", "Tue", "Wed", "Thu", "Fri", "Sat")

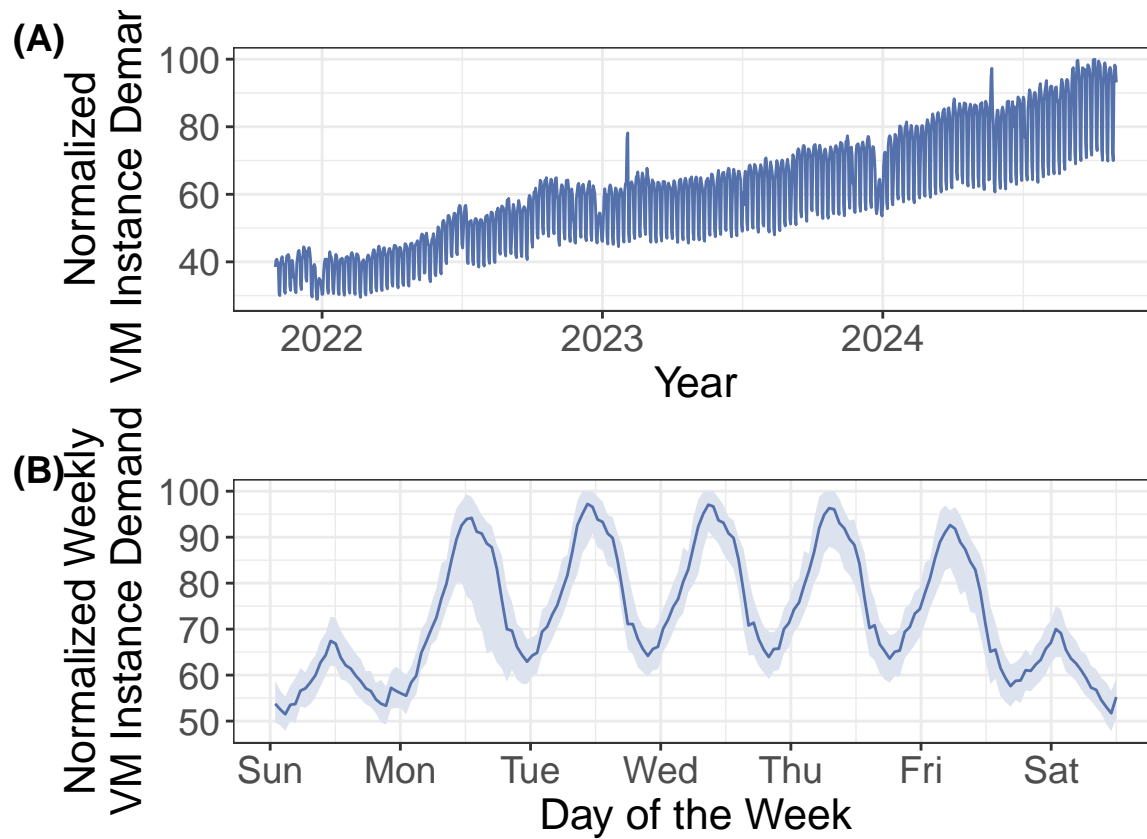
p3 <- ggplot(hourly.quantiles, aes(x=y, y=med)) +
  geom_ribbon(aes(ymin=p5, ymax=p95), fill="#DDE3EE") +
  geom_line(color="#5471AB") + theme_bw() +
  theme(axis.text = element_text(size=14),
    axis.title.x = element_text(size=16),
    axis.title.y = element_text(size=16)) +
  xlab("Day of the Week") + ylab("Normalized Weekly\nVM Instance Demand") +
  scale_x_continuous(breaks=seq(from=0, to=24*14, length.out=14),
    labels=rep(days, 2))

```

p3



```
plot_grid(p2, p3, labels=c("(A)", "(B)"), scale=0.9, ncol=1)
```

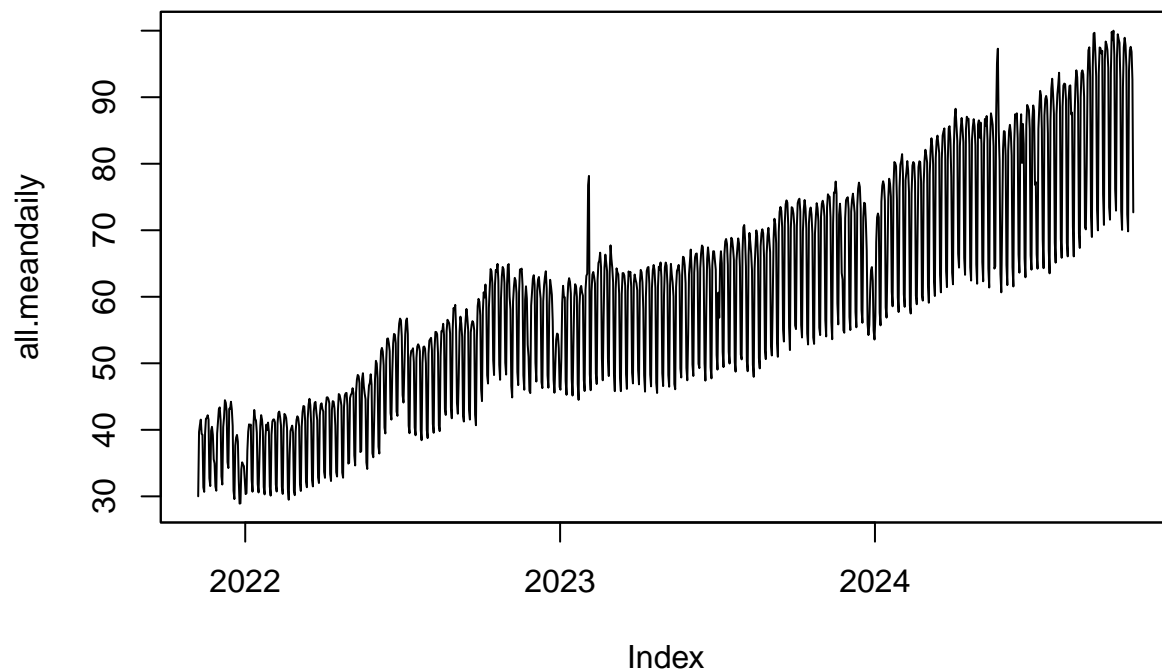


```
pdf("dailypattern.pdf", width=7, height=5.5)
plot_grid(p2, p3, labels=c("(A)", "(B)"), scale=0.9, ncol=1)
dev.off()
```

```
png("dailypattern.png", width=700, height=550)
plot_grid(p2, p3, labels=c("(A)", "(B)"), scale=0.9, ncol=1)
dev.off()
```

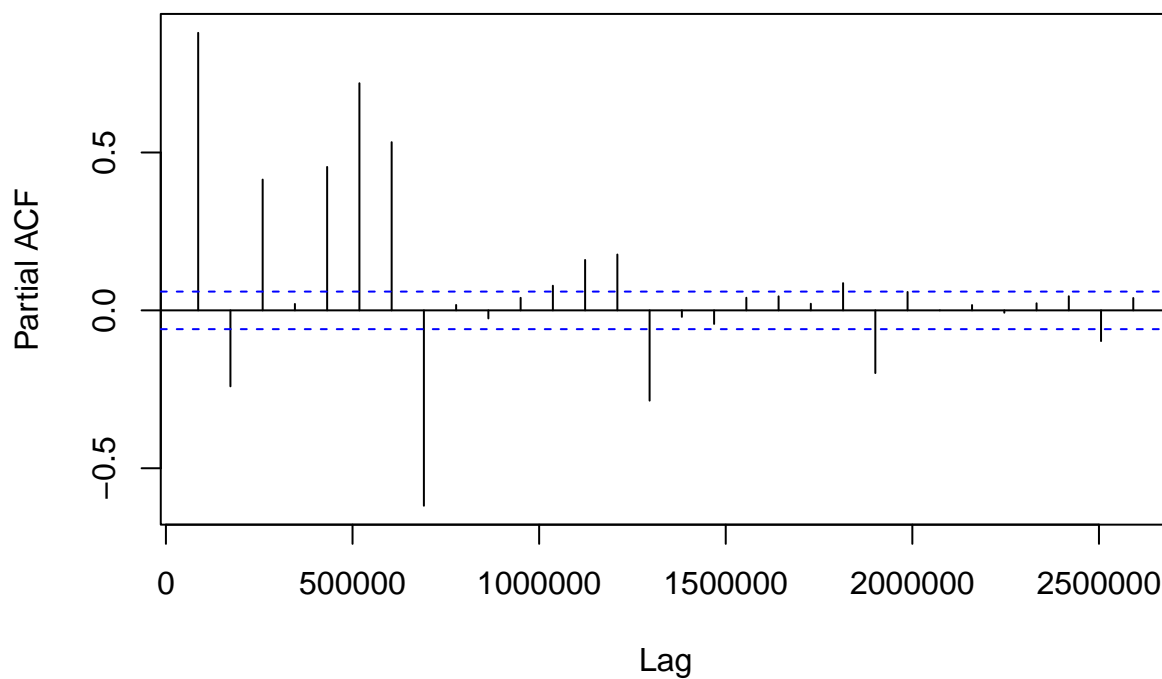
4 Autocorrelation Analysis

```
plot(all.meandaily)
```



```
pacf(all.meandaily)
```

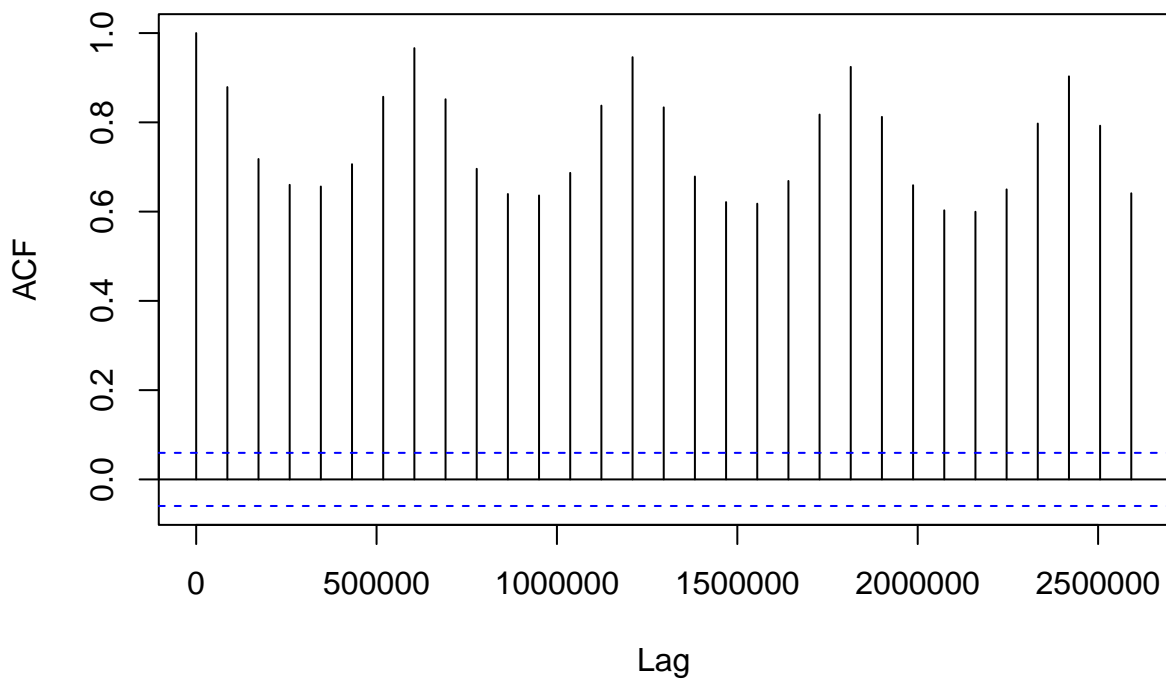
Series all.meandaily



```
#data.zoo <- zoo(all$NORM_USAGE, all$USAGE_HOUR)
#data.sub
#data.sub.zoo <- zoo(data.sub$TOTAL_COST, data.sub$day)
#data.sub.zoo
#plot(data.zoo)
#pacf(data.sub.zoo)
```

```
#acf(data.sub.zoo)
z = acf(all.meandaily)
```

Series all.meandaily

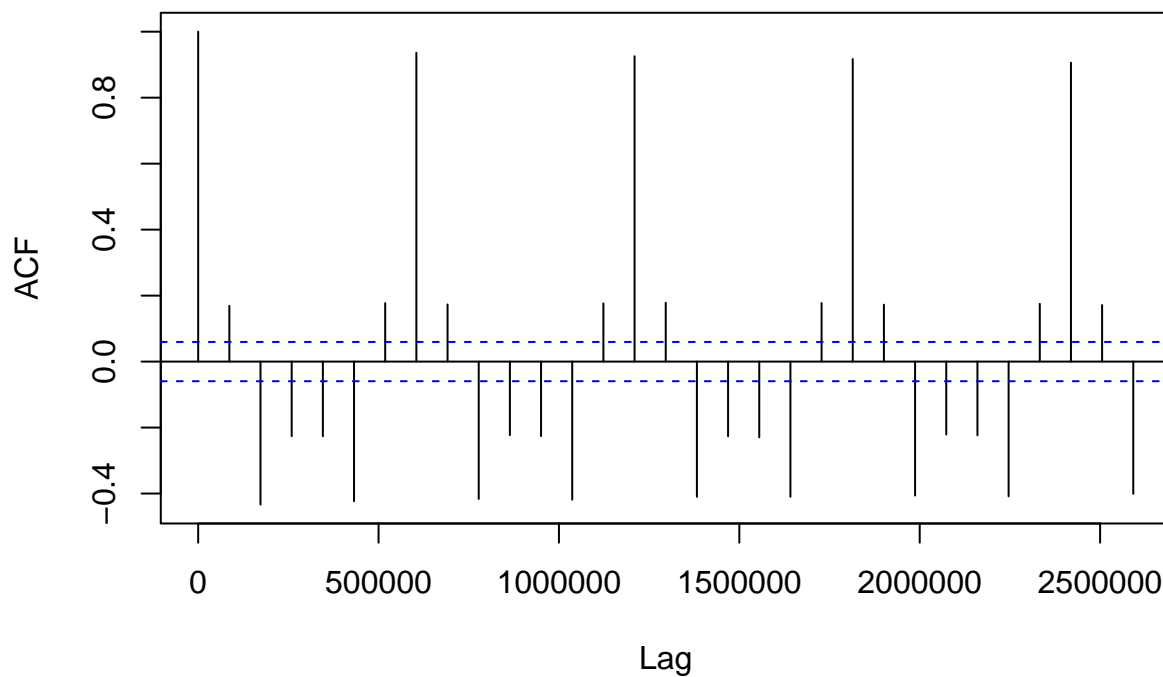


```
z
```

```
##
## Autocorrelations of series 'all.meandaily', by lag
##
##      0   86400  172800  259200  345600  432000  518400  604800  691200  777600
## 1.000  0.879   0.718   0.660   0.656   0.706   0.857   0.966   0.852   0.696
## 864000 950400 1036800 1123200 1209600 1296000 1382400 1468800 1555200 1641600
## 0.639  0.636   0.687   0.837   0.946   0.834   0.679   0.621   0.618   0.669
## 1728000 1814400 1900800 1987200 2073600 2160000 2246400 2332800 2419200 2505600
## 0.817  0.924   0.812   0.659   0.603   0.600   0.650   0.797   0.903   0.792
## 2592000
## 0.641
```

```
y = acf(diff(all.meandaily))
```

Series diff(all.meandaily)

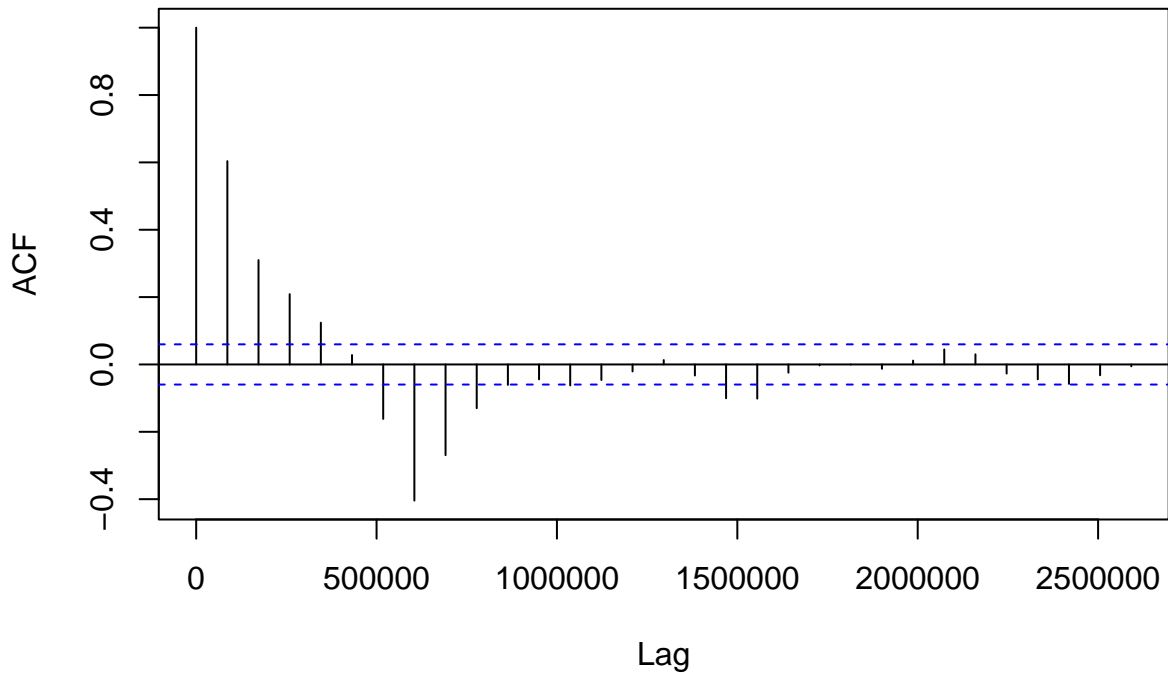


y

```
##
## Autocorrelations of series 'diff(all.meandaily)', by lag
##
##      0   86400  172800  259200  345600  432000  518400  604800  691200  777600
## 1.000  0.169 -0.433 -0.226 -0.226 -0.423  0.177  0.936  0.173 -0.416
## 864000 950400 1036800 1123200 1209600 1296000 1382400 1468800 1555200 1641600
## -0.223 -0.226 -0.419  0.176  0.926  0.179 -0.410 -0.226 -0.230 -0.410
## 1728000 1814400 1900800 1987200 2073600 2160000 2246400 2332800 2419200 2505600
##  0.178  0.917  0.173 -0.406 -0.221 -0.224 -0.408  0.175  0.906  0.171
## 2592000
## -0.401
```

```
x = acf(diff(all.meandaily,7))
```

Series diff(all.meandaily, 7)



x

```
##
## Autocorrelations of series 'diff(all.meandaily, 7)', by lag
##
##      0   86400  172800  259200  345600  432000  518400  604800  691200  777600
## 1.000  0.604   0.310   0.209   0.124   0.028  -0.162  -0.404  -0.269  -0.130
## 864000 950400 1036800 1123200 1209600 1296000 1382400 1468800 1555200 1641600
## -0.061 -0.044 -0.062 -0.046 -0.021  0.013  -0.033  -0.100  -0.101  -0.024
## 1728000 1814400 1900800 1987200 2073600 2160000 2246400 2332800 2419200 2505600
## -0.003  0.000 -0.013  0.011  0.045  0.030  -0.027  -0.044  -0.058  -0.032
## 2592000
## -0.005
```

5 Hourly daily maximum vs daily minimum

```
all.maxweekly <- rollapply(all.meandaily, width=7, by=7, FUN=max)
all.minweekly <- rollapply(all.meandaily, width=7, by=7, FUN=min)
head(all.maxweekly)
```

```
## 2021-11-10 11:00:00 2021-11-17 11:00:00 2021-11-24 11:00:00 2021-12-01 11:00:00
##           41.53539           42.18843           40.45364           43.37488
## 2021-12-08 11:00:00 2021-12-15 11:00:00
##           44.45165           44.22233
```

```
head(all.minweekly)
```

```
## 2021-11-10 11:00:00 2021-11-17 11:00:00 2021-11-24 11:00:00 2021-12-01 11:00:00
##           30.00499           30.67298           31.47557           30.84247
## 2021-12-08 11:00:00 2021-12-15 11:00:00
```

```
##          31.77468          30.82752
head(all.maxweekly / all.minweekly)

## 2021-11-10 11:00:00 2021-11-17 11:00:00 2021-11-24 11:00:00 2021-12-01 11:00:00
##          1.384283          1.375427          1.285239          1.406336
## 2021-12-08 11:00:00 2021-12-15 11:00:00
##          1.398965          1.434508
mean(all.maxweekly / all.minweekly)

## [1] 1.387805
head(all.maxdaily)

## 2021-11-07 11:00:00 2021-11-08 11:00:00 2021-11-09 11:00:00 2021-11-10 11:00:00
##          27.96528          39.72999          39.05497          39.34426
## 2021-11-11 11:00:00 2021-11-12 11:00:00
##          37.12633          37.80135
head(all.mindaily)

## 2021-11-07 11:00:00 2021-11-08 11:00:00 2021-11-09 11:00:00 2021-11-10 11:00:00
##          21.31148          24.10800          26.13308          28.06172
## 2021-11-11 11:00:00 2021-11-12 11:00:00
##          26.22951          27.00096
head(all.maxdaily/all.mindaily)

## 2021-11-07 11:00:00 2021-11-08 11:00:00 2021-11-09 11:00:00 2021-11-10 11:00:00
##          1.312217          1.648000          1.494465          1.402062
## 2021-11-11 11:00:00 2021-11-12 11:00:00
##          1.415441          1.400000
mean(all.maxdaily/all.mindaily)

## [1] 1.513287
```

Average daily maximum is 34% higher than average daily minimum.

6 Holiday Effect Analysis

```
holidays.2022 <- subset(data.all, (USAGE_HOUR > as.POSIXct("2021-12-15") &
                                USAGE_HOUR < as.POSIXct("2022-01-15")))
# Normalize this holiday period to 100 over the holidays.
holidays.2022$NORM_USAGE <- (100 * holidays.2022$NORM_USAGE) /
  max(holidays.2022$NORM_USAGE)
label.1 <- "2021-2022"
label.2 <- "2022-2023"
label.3 <- "2023-2024"
holidays.2022$year = label.1
holidays.2022$weekend.start = as.POSIXct("2021-12-18")
holidays.2022$weekend.end = as.POSIXct("2021-12-20")
holidays.2022$ts <- holidays.2022$USAGE_HOUR

highlights <- data.frame(year=c(rep(label.1, 4), rep(label.2, 5),
                                rep(label.3, 5)),
                        weekend.start=c(as.POSIXct("2021-12-18"),
```

```

        as.POSIXct("2021-12-25"),
        as.POSIXct("2022-01-01"),
        as.POSIXct("2022-01-08"),
        as.POSIXct("2021-12-17"),
        as.POSIXct("2021-12-24"),
        as.POSIXct("2021-12-31"),
        as.POSIXct("2022-01-07"),
        as.POSIXct("2022-01-14"),
        as.POSIXct("2021-12-16"),
        as.POSIXct("2021-12-23"),
        as.POSIXct("2021-12-30"),
        as.POSIXct("2022-01-06"),
        as.POSIXct("2022-01-13")),
weekend.end=c(as.POSIXct("2021-12-20"),
              as.POSIXct("2021-12-27"),
              as.POSIXct("2022-01-03"),
              as.POSIXct("2022-01-10"),
              as.POSIXct("2021-12-19"),
              as.POSIXct("2021-12-26"),
              as.POSIXct("2022-01-02"),
              as.POSIXct("2022-01-09"),
              as.POSIXct("2022-01-15"),
              as.POSIXct("2021-12-18"),
              as.POSIXct("2021-12-25"),
              as.POSIXct("2022-01-01"),
              as.POSIXct("2022-01-08"),
              as.POSIXct("2022-01-15")))

holidays.2023 <- subset(data.all, (USAGE_HOUR > as.POSIXct("2022-12-15") &
                                USAGE_HOUR < as.POSIXct("2023-01-15")))
holidays.2023$ts <- holidays.2023$USAGE_HOUR - dyears(1)

holidays.2023$NORM_USAGE <- (100 * holidays.2023$NORM_USAGE) /
  max(holidays.2023$NORM_USAGE)
holidays.2023$year = label.2
holidays.2023$weekend.start = as.POSIXct("2021-12-17")
holidays.2023$weekend.end = as.POSIXct("2021-12-19")

holidays.2024 <- subset(data.all, (USAGE_HOUR > as.POSIXct("2023-12-15") &
                                USAGE_HOUR < as.POSIXct("2024-01-15")))
holidays.2024$ts <- holidays.2024$USAGE_HOUR - dyears(2)

holidays.2024$NORM_USAGE <- (100 * holidays.2024$NORM_USAGE) /
  max(holidays.2024$NORM_USAGE)
holidays.2024$year = label.3
holidays.2024$weekend.start = as.POSIXct("2021-12-16")
holidays.2024$weekend.end = as.POSIXct("2021-12-18")

holidays.all <- rbind(holidays.2022, holidays.2023, holidays.2024)
head(holidays.all)

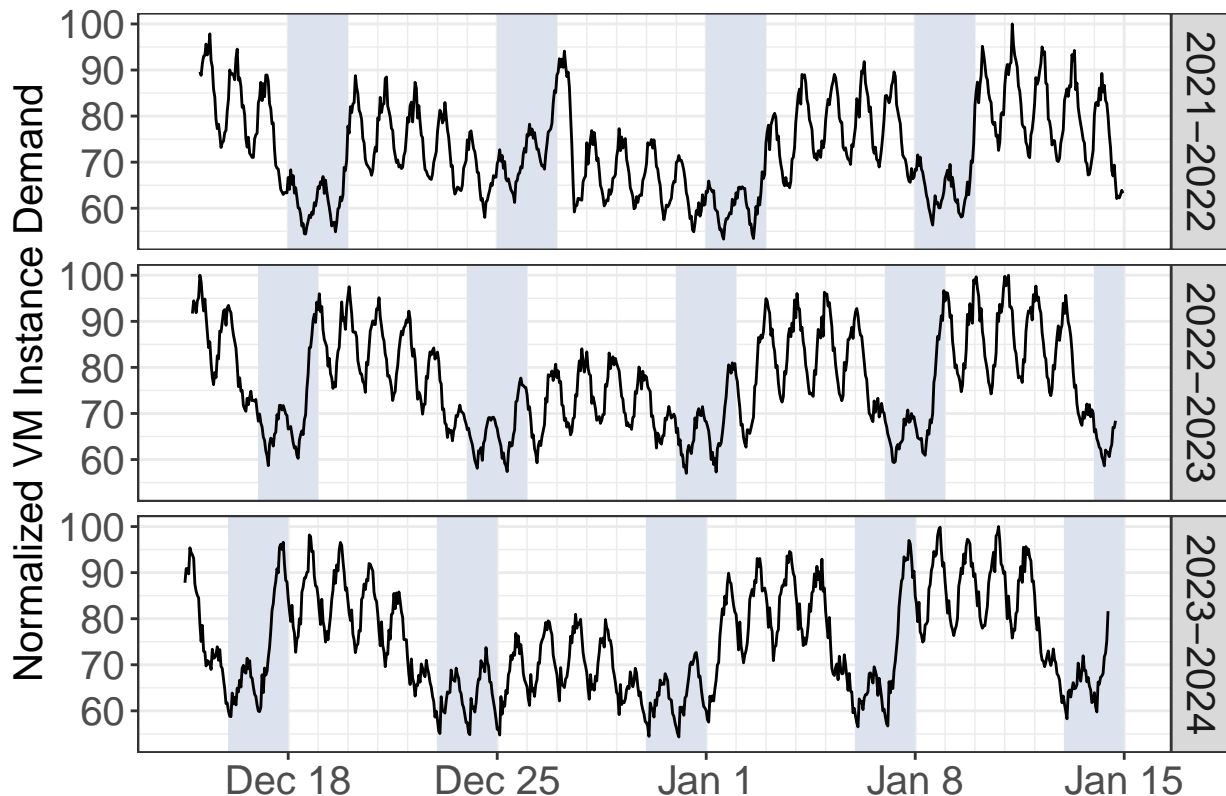
## # A tibble: 6 x 6
##   USAGE_HOUR      NORM_USAGE year weekend.start weekend.end
##   <dtm>          <dbl> <chr>   <dtm>      <dtm>

```



```
## 1 2021-12-15 09:00:00      89.6 2021-2~ 2021-12-18 00:00:00 2021-12-20 00:00:00
## 2 2021-12-15 10:00:00      88.8 2021-2~ 2021-12-18 00:00:00 2021-12-20 00:00:00
## 3 2021-12-15 11:00:00      91.4 2021-2~ 2021-12-18 00:00:00 2021-12-20 00:00:00
## 4 2021-12-15 12:00:00      93.0 2021-2~ 2021-12-18 00:00:00 2021-12-20 00:00:00
## 5 2021-12-15 13:00:00      93.1 2021-2~ 2021-12-18 00:00:00 2021-12-20 00:00:00
## 6 2021-12-15 14:00:00      95.6 2021-2~ 2021-12-18 00:00:00 2021-12-20 00:00:00
## # i 1 more variable: ts <dtm>
```

```
holidayPlot <- function() {
  highlights$ts <- min(holidays.all$ts)
  highlights$NORM_USAGE <- min(holidays.all$NORM_USAGE)
  ggplot(data=holidays.all, aes(x=ts, y=NORM_USAGE)) +
    geom_rect(data=highlights, aes(xmin=weekend.start, xmax=weekend.end,
                                   ymin=-Inf, ymax=Inf),
              fill="#DDE3EE",alpha=1.0) +
    geom_line() + facet_grid(rows = vars(year)) + theme_bw() +
    theme(axis.text=element_text(size=15), axis.title=element_text(size=15),
          strip.text=element_text(size=15), legend.text = element_text(size=15),
          legend.title = element_text(size=15)) +
    ylab("Normalized VM Instance Demand") + xlab("") +
    scale_x_continuous(breaks=c(as.POSIXct("2021-12-18"), as.POSIXct("2021-12-25"),
                                  as.POSIXct("2022-01-01"), as.POSIXct("2022-01-08"),
                                  as.POSIXct("2022-01-15")),
                      labels=c("Dec 18", "Dec 25", "Jan 1", "Jan 8", "Jan 15"),
                      minor_breaks=seq(from=as.POSIXct("2021-12-19"),
                                       to=as.POSIXct("2022-01-15"), by=86400))
}
holidayPlot()
```



pdf
2

pdf
2