```
- MAKING OUR OWN TYPES AND TYPECLASSES --
module Shapes (
            Point(..)
             Shape(..),
             surface,
             nudge,
            baseCircle.
            baseRectangle
) where -- Export types like [TYPE]([Constructors]|..)
 import qualified Data.Map as Map
-- ALGEBRATC DATA TYPES INTRO --
-- data Bool = False | True
-- We use 'data' to say that we're defining a new data type. The part before the = is the name of the type, and the parts after are the value -- constructors. They're the different values the type can have.
-- We define data Int = -2147483648 | -2147483647 | ... | -1 | 0 | 1 | 2 | ... | 2147483647 (it doesn't actually have the ...).
-- How can we represent a shape in Haskell? We can use a tuple (x-cord, y-cord, radius), but that only works for circles, and it's not exactly -- very specific about what value is what. This could also represent a 3-D vector or a bunch of other things. It's better to use a bunch of
-- different things to represent a shape.
-- data Shape = Rectangle Float Float Float Float Float Float Float Float Geriving (Show) -- OLD -- data Point = Point Float Float deriving (Show) data Shape = Circle Point Float | Rectangle Point Point deriving (Show)
-- The Shape type is made up of two different constructors (Rectangle and Circle). Rectangle takes four Floats, the first two are coordinates -- of the lower left corner and the last two are coordinates of the upper right corner. With the Cirle, the first two are the coordinates of -- the center, and the last is the radius.
-- An important thing to see is the type declaration here. We take a SHAPE. Not a Circle or a Rectangle. The only thing that's a type is Shape.

-- Just like we can't write a function with True -> Int

surface :: Shape -> Float
cutrace :: Shape -> Float
-- surface (Circle _ r) = pi * r ^ 2 -- OLD --
-- surface (Rectangle x1 y1 x2 y2) = (abs $ x1 - x2) * (abs $ y1 - y2)
surface (Rectangle (Point x1 y1) (Point x2 y2)) = (abs $ x1 - x2) * (abs $ y1 - y2)
surface (Circle _ r) = pi * r ^ 2
-- We can also pattern match against constructors. Because we aren't worried about the positioning of the Circle, we only need the radius.
-- If we just try to give Haskell "Circle 5 5 10", we get an error because it doesn't know how to display that on the screen.
-- We can add 'deriving ([TYPE])' to the data declaration in order to tell Haskell that it can be shown.
-- Since value constructors are functions, we can map them and partially apply them. mapFunction :: Float -> Float -> [Shape]
mapFunction a b = map (Circle (Point 5.0 4.0)) [a,b,5,6,7]
-- We have a good Shape data type, but we can make it better by implimenting a Point data type (line 14)
  - How about a function that nudgs a shape?
nudge :: Shape -> Float -> Float -> Shape
nudge (Circle (Point x y) r) a b = Circle (Point (x+a) (y+b)) r
nudge (Rectangle (Point x1 y1) (Point x2 y2)) a b = Rectangle (Point (x1+a) (y1+b)) (Point (x2+a) (y2+b))
-- If we don't want to have to deal directly with points, we can define a function that wil create a base circle or a base rectangle and then
-- just nudge that.
baseCircle :: Float -> Shape
baseCircle r = Circle (Point 0 0) r
baseRectangle :: Float -> Float -> Shape
baseRectangle width height = Rectangle (Point 0 0) (Point width height)
-- Now we can just nudge in order to declare the new position without having to type out Point all the time.
-- RECORD SYNTAX --
-- If we want to make a person, we could define it as
-- data Person = Person String String Int Float String String deriving (Show)
-- But then we would have to define a lot of different functions to get a specific value, and the placement of the different types doesn't make
-- it apparent what value goes where.
-- Instead, we can define it like this
--data Person = Person {
             firstName :: String,
--
            lastName :: String
             age :: Int,
--
            height :: Float
            phoneNumber :: St
flavor :: String
--} deriving (Show)
 -- Now, Haskell already made functions for firstName, lastName, etc. to return the values.
 -- There's also another benefit to using record syntax. If we just define a Car as
-- data Car = Car String String Int deriving (Show)
-- Then when we try to show a car, it only prints out "Car "Ford" "Mustang" 1967"
-- If we define a car as
data Car = Car {
            company :: String,
             model :: String,
            year :: Int
} deriving (Show)
  - Then we show a car
doCar :: Car
doCar = Car {company = "Ford", model = "Mustang", year = 1967}
-- It will display like this:
-- Car {company = "Ford", model = "Mustang", year = 1967}
-- We also don't have to put the specific names in a certain order because we are assigning using a key-value-ish system.
 -- TYPE PARAMETERS --
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-- A value constuctor can take a few parameters and return a result. As an example, Car takes three values and produces a car value.

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-- Type constuctors can also take values just like value constuctors to create new types.
     data Maybe a = Nothing | Just a
-- data Maybe a = Nothing | Just a
-- Here, the a is the type parameter. Because there is a type parameter involved, we call this a type constuctor. Depending on what
-- we want this type constuctor to hold, it can produce Maybe Int, Maybe Car, etc. No value will have a type of just Maybe because it's not
-- exactly a type. It's a type constuctor. In order for it to be a type, it needs to have all of its parameters filled up.
-- So if we pass in a Char to Maybe, we get Maybe Char.
-- We used a type that has a type parameter before Maybe. Lists have a type parameter. [Int], [Char], [[String]]. However you can't just have []
-- Type parameters are useful because ti allows us to make different types based on what you want contained. If the a in Just a is a String,
-- then the a in Maybe a is also a String.
-- The type of Nothing is Maybe a because its type is polymorphic. If some funciton requires Maybe Int, we can give it Nothing because Nothing -- doesn't contain any values anyway, so it doesn't matter. The type Maybe a can act as Maybe Int or Maybe Double just like 5 can act as
-- an Int or Double. An empty list can act as a list of anything. That's why we can do [1,2,3] ++ [].
-- Using type parameters is very beneficial, but only when using them makes sense. For example, we wouldn't define Car as
-- {company :: a, model :: b, year :: c} because company and model will always be a String and the year will always be an Int. If our type
-- acts as some kind of a box, it's good to use them.
-- Here's a funciton to show the properties of a car.
tellCar :: Car -> String
tellCar (Car {company = c, model = m, year = y}) = "This " ++ c ++ " " ++ m ++ " was made in " ++ show y
-- This function would have to be made if the car was declared with types a, b, and c.
-- tellCar' :: (Show a) => Car String String a -> String
-- tellCar' (Car {company = c, model = m, year = y}) = "This " ++ c ++ " " ++ m ++ " was made in " ++ show y
-- As you can see the type declaration is very gross looking and only benefits us in that we can use any data type that is of the Show typeclass
-- So we would rather just use Car String String Int to make it simple. We usually use type parameters when the type inside of the value doesn't -- really need to be a certian one for the type to work. A list of stuff is just a list of stuff. If we want it to be a list of integers,
-- we can specify that in the function's type declaration. The same goes for Maybe values. Maybe represents having either nothing or have one -- of something. It doesn't matter what the type of that thing is.
  - Another example of a parameterized type that we've met is Map k v from Data.Map. The k is the key in the map, and the v is the value. This
-- is an example of where type parameters are useful. This allows us to have two types, but it doesn't matter what types they actually are.
-- So you can have a key that's an Int and a value that's a String. Or the other way around. Having maps parameterized allows us to have
-- mappings from any type to any other type as long as they key is within the Ord typeclass.
-- data (Ord k) => Map k v =
-- It's a very strong convention to never add typeclass constraints in data declarations because we don't benefit a lot. We just end up writing -- more class constraints. If we do have the Ord k in the data delcaration, then we won't have to write Ord k when writing a function that uses
-- Map, but if we don't put it in, we don't need to have Ord k in our function type delcaration.

-- An example of this is toList. It's defined like toList :: Map k v -> [(k,v)]

-- If we had Ord k in our data declaration, we would need to write toList :: (Ord k) => Map k v -> [(k,v)] even though the function does nothing
-- with comparing by order.
-- So don't put typeclass constraints into data declarations even if it makes sense at the time because you'll have to put them into the -- function declarations either way.
-- Here'd a 3D vector type
data Vector a = Vector a a a deriving (Show)
vector to add two vectors.

vplus :: (Num t) => Vector t -> Vector t -> Vector t
(Vector a b c) `vplus` (Vector d e f) = Vector (a+d) (b+e) (c+f)
-- Function to multiply two vectors together
vmult :: (Num a) => Vector a -> Vector a
(Vector a b c) `vmult` (Vector d e f) = Vector (a*d) (b*e) (c*f)
-- Function to add together the products of the scalar values of two vectors
 scalarMult :: (Num a) => Vector a -> Vector a -> a
(Vector a b c) `scalarMult` (Vector d e f) = (a*d) + (b*e) + (c*f)
-- Notice how we didn't put the Num a constraint in the data declaration because we would need to do the same thing in the funciton declaration.
scalarMult :: (Num a)
(Vector a b c)
-- DERIVED INSTANCES -
-- Typeclasses are somewhat like Java interfaces, but not exactly. A type can be made an instance of a typeclass if it supports that behavior. -- Example: The Int type is an instance of the Eq typeclass because the Eq typeclass defines behavior for stuff that can be equated. And -- because Integers can be equated, Int is a part of the Eq typeclass. The real usefulness comes with the functions that act as the interface
-- for Eq, namely == and /=. If a type is a part of the Eq typeclass, we can use the == function with values of that type. That's why -- 4 == 4 or "foo" /= "bar" typecheck.
-- Let's look at how Haskell can automatically make our type an instance of Eq, Ord, Enum, Bounded, Show, and Read. Haskell can derive
-- the behavior of our types if we use teh deriving keyword in our data declaration.
-- Consider the Person data type
--data Person = Person {
-- firstName :: String,
             lastName :: String,
             age :: Int
-- Say we have a list of persons, and none of them are the same. Would it make sense to have to compare two persons to see if two references
-- are the same person? Yes. So we would add on a "deriving (Eq)" to the data declaration so that we can compare two Persons with
-- When we try to an an ==, Haskell will look to see if the value constructors match.
-- ALL VALUES INSIDE OF THE CONSTRUCTOR MUST ALSO BE OF THE EQ TYPECLASS
-- Since String and Int are both of the Eg typeclass, we're good to go.
data Person = Person {
    firstName :: String,
             lastName :: String,
              age :: Int
} deriving (Eq, Show, Read)
-- Let's test out how People are compared.
comparePeople :: Bool
comparePeople = mike == joe
                                                      mike = Person {firstName = "Mike", lastName = "Pike", age =
joe = Person {firstName = "Joe", lastName = "Bob", age = 36}
-- Of course, since Person is of type Eq, we can use it as the a in functions that have Eq a in their type signature. Such as elem. -- If we had a list of people and wanted to see if a certain one was a part of that list, then we could simply do
-- [person] `elem` [listofpeople]
-- If we add a derivation of Show to the Person type, we can print it out to the terminal. If we tried to Show before we added it, then
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-- Haskell would have complained about us trying to show something that it claims it doesn't know how to show.
-- When we add Read to the Person type, we can read in a value like "let mike = read "Person {firstName=\"Mike\", lastName=\"Diamond\",
-- age = 43}" :: Person" and it would read in Mike as a Person
-- We can also read in parameterized types like Maybe values
                               :: Maybe Char
-- The way we can derive instances of the Ord typeclass are by order of definition. Say we define the data type of Bool.
-- data Bool = False | True deriving (Ord)
-- What's cool about this is that the value that's defined first is considered the least, and the one that's defined last is considered
-- to be the greatest. So True is considered to be greater than False.
-- In the Maybe a datatype, the Nothing value is defined before the Just a value, so the value of Nothing is less than Just a. However,
-- if we compare two Just a values, it just compares the 'a' value. We can't do something like Just (*3) > Just (*2) because those are
-- functions
-- We can use algebraic data types to make enumerations and the Enum and Bounded typeclasses can help us with that.

data Day = Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday deriving (Enum, Bounded, Eq, Ord, Show, Read)

-- Because all of the value constructors are nullary (take no parameters), we can make these a derivation of the Enum typeclass.

-- the Enum typeclass is for things that have predicessors and successors. We also can give it Bounded type because Bounded is for things that

-- have a definite upper and lower bound. While we're at it, let's make it an instance of a bunch of different typeclasses.

-- Because it's a part of the Show and Read typeclass, we can easily change things to and from Strings.
doWed :: Day
doWed = Wednesday
readDay :: String -> Day
readDay a = read a :: Day
    Because Day is a part of the Eq and Ord typeclass, we can equate and compare two days.
eqDay :: Day -> Day -> Bool
eqDay a b = a == b
compareDay :: Day -> Day -> Ordering
compareDay a b = a `compare` b
-- We can also get maxBound :: Day and minBound :: Day. Also we can see what the successors and predicessors are.
-- Because String and [Char] are the same thing, that's done with type synonyms.
-- type String = [Char]
-- type string = [that]
-- We aren't defining a new type here. We're simply making what is essentialy an alaias.
-- In Data.Map, we first represented a phonebook with an association list before converting it to a map. Let's look at the phonebook we made.
-- phoneBook :: [(String, String)]
-- We see that the type is [(String, String)], but tells us that it maps from Strings to Strings, but not much else.
-- type PhoneBook = [(String, String)]
-- Now the type of our phoneBook can be
-- phoneBook :: PhoneBook
-- Let's make a type synonym for String as well.
type PhoneNumber = String
type Name = String
type PhoneBook = [(Name, PhoneNumber)]
-- Using type synonyms in code is good because it lets people know more about what the code should do and how certain things should be made.

-- Here's a function to check if a phone number and name is in a phone book.

inPhoneBook :: Name -> PhoneNumber -> PhoneBook -> Bool
inPhoneBook name pn pb = (name,pn) `elem` pb
-- If we decided not to use type synonyms, our type would be String -> String -> [(String, String)] -> Bool, which is more confusing.
-- It's important to remember not of go overboard with type synonyms though. They're good when you're working with stuff that is long and
-- can be confusing, but they shouldn't be used to just replace a simple Int or Char every here and there.
  - Type synonyms can also be parameterized!
type Assoclist k v = [(k,v)]
-- Now a function that has the type signature of (Eq k) => k -> Assoclist k v -> Maybe v because Assoclist is a type constructor that
-- can take stuff like Int String
-- Just like we can partially apply functions, we can also partially apply type parameters to get what we want. Like this:
type IntMap v = Map.Map Int
   - or we could do it like this
-- data IntMap = Map Int
-- Either way, the IntMap constructor takes one parameter and that is the type that the Int will point to in the map.
-- The difference between value constructors and type constructors is that we can use a value constructor to make a value, but we can't use
-- a type constructor to make a new value. We just are changing the way we can interpret a type. We can't do AssocList [(1,2), (3,4)] but -- we can do [(1,2), (3,4)] :: AssocList Int Int, which will make the numbers inside assume the type of Int.
  - Another cool data type is the Either data type
- data Either a b = Left a | Right b deriving (Eq. Ord, Show, Read)
- It has two value constructors. If Left it used, then the contents are of type a, and if Right is used, its contents are of type b. So we
- can use this type to encapsulate a value of one type or another and then we get a value that's Either a or b. We usually will pattern match
- on both Left and Right and we get different stuff based on which one of them it was.
-- We've used Maybe a to represent the results of computations that could have either failed or not. Sometimes Maybe a isn't good enough because
-- Nothing doesn't really tell us much other than something has failed. It's good for functions that can only fail one way or if we don't care
-- if they fail or not. We can use Either a b to tell us about errors. Left values are used for errors, while Right values are used for results.
-- Here's a little example with lockers.
data LockerState = Taken | Free deriving (Eq. Show)
type Code = String
type LockerMap = Map.Map Int (LockerState, Code)
lockerLookup :: Int -> LockerMap -> Either String Code
lockerLookup lockerNum mapp =
     case Map.lookup lockerNum mapp of
          Nothing -> Left $ "Locker " ++ show lockerNum ++ " doesn't exist."
                           Just (state, code) -> if state == Free
                                                                                                           then Right code
 else Left $ "Locker " ++ show lockerNum ++ " is already taken."
-- So calling lockerLookup 5 $ Map.fromList [(5,(Free, "382938"))] will return Right "382938".
-- We could have used Maybe a to represent out results, but then we wouldn't know why they failed.
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-- Because we create data types with fields that are of some concrete type, we can also define types that take the same type as a parameter. -- Let's use algebraic data types to impliment our own list then
-- data List a = Empty | Cons a (List a) deriving (Show, Read, Eq, Ord)
-- The Cons is basically using :, so we're adding to the list. We take a head value and the rest of the list, or we take an empty list.
-- Typing "Cons 5 (Cons 4 (Cons 3 Empty))" will give us something like a list where Cons is :. Just like 5:4:3:[]
 -- We can define functions to be automatically infix by making them only comprised of special characters, so we can also do the same to
 -- constructors.
 infixr 5 :-:
infixr 5:-:
data List a = Empty | a :-: (List a) deriving (Show, Read, Eq, Ord)
-- The infix_ makes something right associative or left associative. infixr and infixl. The number defines the fixity. The higher the number,
-- the more presidence is gets over the others. So * has 7, and + has 6. If you write 4 * 5 + 7, it's the same as (4 * 5) + 7.
-- Otherwise we just wrote a :-: instead of Cons a.
-- Writing 5 :-: 5 :-: 4 :-: Empty give us ("5 :-: (5 :-: (4 :-: Empty))"
-- When we derive the Show typeclass, Haskell is treating this as a prefix function, so it puts parenthesis around the operator.
-- Penember 4 + 4 and (+) 4 are the same.
 -- Remember 4 + 4 and (+) 4 4 are the same.
 -- Let's make a function to add two of our new lists together.
 -- This is how ++ is defined for normal lists.
 -- infixr 5 ++
-- (++) :: [a] -> [a] -> [a]
-- [] ++ ys = ys
 ...(x:xs) ++ ys = x : (xs ++ ys)
infixr 5 .++
(.++) :: List a -> List a -> List a
Empty .++ ys = ys
(x:-:xs) .++ ys = x :-: (xs .++ ys)
   - And it works. If we wanted, we could write all of the functions that operated on list types.
-- Now it's time to make a binary search tree.

-- Here is what we can say about trees: It's either empty, or it's an element that contains a value and two trees.

data Tree a = EmptyTree | Node a (Tree a) (Tree a) deriving (Show, Eq. Read)

-- Our furst function is a utility function for just making a new tree with just one node.
 singleton :: a -> Tree a
singleton x = Node x EmptyTree EmptyTree
   - Our second function is one that will insert an element into a tree.
treeInsert :: (Ord a) => a -> Tree a -> Tree a
treeInsert x EmptyTree = singleton x
treeInsert x (Node a left right)
                 x == a = Node x left right
x < a = Node a (treeInsert x left) right
x > a = Node a left (treeInsert x right)
-- Function for determining if an element is in a tree treeElem :: (Ord a) => a -> Tree a -> Bool treeElem _ EmptyTree = False treeElem x (Node a left right) | x == a = True
                 x < a = treeElem x left
x > a = treeElem x right
 -- Build a tree with "foldr treeInsert EmptyTree nums" where EmptyTree is the starting value, nums is the list, and treeInsert is our function.
 -- TYPECLASSES 102 --
 -- So far, we've learned how to use typeclasses, but we haven't learned how to make our own typeclasses.
 -- Typeclasses are like interfaces in Java. It defines some behavior, and then, some types that can behave in that way are made instances of -- that typeclass. So when we say a type is an instance of a typeclass, that means that we can use functions that typeclass defines with that
 -- type (Show, Eq, Read, Ord, etc.).
 -- Typeclasses have nothing to do with classes in things like Java or PHP or Python.
 -- This is how the Eq typeclass is written.
 --class Eq a where
              (==) :: a -> a -> Bool
(/=) :: a -> a -> Bool
-- (/=) :: a -> a -> Bool
-- x == y = not (x /= y)
-- x /= y = not (x == y)
-- we define classes like "class [CLASSNAME] [TYPEVARIABLES] where" and then we state the functions of the typeclass. It's not manditory to
-- impliment the function bodies themselves but we need the type declarations.
-- We can't do much with a class once we have it, but once we start making some instances of that class, there is some nice funcitonality.
data TrafficLight = Red | Yellow | Green
-- This defines the different states of a traffic light. We didn't derive any classes for it because we are going to write up an instance by
-- hand
 instance Eq TrafficLight where
              Red == Red = True
Yellow == Yellow = True
              Green == Green = True
               _ == _ = False
-- So 'class' is for making a new Typeclass, but 'instance' is for making a data type an instance of a typeclasss.
-- In our example, we just replaced 'a' with 'TrafficLight' since it was the type.
 -- Because == was defined along with /= in the Eq typeclass, we only needed to overwrite one of them in our instance declaratio because it
-- knows that in order to be true, it need to not be not true. -- If Eq a where defined like \,
 class Eq a where
        (==) :: a -> a -> Bool
(/=) :: a -> a -> Bool
    Then we would have to implement both == and /= in our instance.
 -- Now let's make an instance of Show my hand.
 instance Show TrafficLight where
              show Red = "Red light!"
show Yellow = "Yellow light!
               show Green = "Green light!"
 -- We can also make a typeclass that is an extention of another typeclass. Like Num.
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-- class (Eq a) => Num a where
-- So this is like writing "class Num a where" only our 'a' is a part of the Eg typeclass.
-- The difference between Maybe and TrafficLight is that Maybe isn't a concrete type, so it can be Maybe Int, Maybe String, or Maybe etc.
-- So how it is Eq'd since all functions need to use concrete types?
-- We can define Maybe as a non-concrete type, but the 'a' part of it is concrete.
instance Eq (Maybe a) where
           Just x == Just y = x == y
Nothing == Nothing = True
           _ == _ = False
-}
-- This is basically saying that we want to make all tyes that are Maybe a a part of Eq. This is how Haskell would derive the instance too.
-- Most of the time, class constraints in class declarations are sued for making a class a subclass of another class, while type constraints
-- in instance declarations are used for making sure that a certian requirements are met.
-- When you see that there is a type parameter used in a class declaration, you need to surround it with parenthesis to keep it a part of where -- you want it.
-- If you want to see what instances your typeclass has, type :info TYPECLASS for information.
-- A YES-NO TYPECLASS --
  - Let's make a class that will give us True or False based on if a value is considered to be "0" or not.
class YesNo a where
    yesno :: a -> Bool
 -- Now let's define some instances.
-- Now let's define some instance YesNo [a] where yesno [] = False yesno _ = True instance YesNo Int where
yesno 0 = False
yesno _ = True
instance YesNo Bool where
yesno = id -- The 'id' returns the same parameter that it was given.
instance YesNo (Maybe a) where
yesno (Just _) = True
            yesno Nothing = False
instance YesNo (Tree a) where
yesno EmptyTree = False
yesno _ = True
instance YesNo TrafficLight where
           yesno Red = False
           yesno _ = True
-- Let's make a function that returns something based on what you put in.
yesnoIf :: (YesNo y) => y -> a -> a -> a
yesnoIf yesNo yesV noV = if yesno yesNo then yesV else noV
-- THE FUNCTOR TYPECTASS --
-- The Functor typeclass is for things that can be mapped over, such as lists. Lists are a part of the Functor typeclass.
class Functor f where
            fmap :: (a -> b) -> f a -> f b
-}
-- This is how it's implimented.
-- It's just like the map function, which takes a function (a -> b) and a list [a] and returns a list of the second type [b].
-- fmap is the same as map, but map is only for lists.
instance Functor [] where
            fmap = map
-}
-- We didn't write [a] or something because the class definition doesn't ask for a concrete type. It's asking for a type constructor.
-- The [] is a type constructor, so it can work. But we can't involve 'a', 'b', etc.
-- Since fmap is the same as map, w fmapTest :: (a -> b) -> [a] -> [b] fmapTest = fmap
                         the same as map, we get the same results when operating on lists.
mapTest :: (a -> b) -> [a] -> [b]
-- The Functor typeclass can work on anything that's like a box. So anything that can holds a value or any number of values.
-- Maybe can be put into it as well.
instance Functor Maybe where
           fmap f (Just x) = Just (f x)
fmap f (Nothing) = Nothing
-}
-- Once again, we wrote it as a type constructor instead of a type parameter with an 'a' or 'm' or whatever because it takes a type constructor.
functorTest :: Maybe String
functorTest = fmap (++ "Hello there") (Just "hi.")
\begin{array}{lll} & fmap \ f \ \hbox{\bf EmptyTree} = \hbox{\bf EmptyTree} \\ & fmap \ f \ (\hbox{\bf Node} \ x \ \hbox{\bf lTree} \ \hbox{\bf rTree}) = \hbox{\bf Node} \ (f \ x) \ (fmap \ f \ \hbox{\bf lTree}) \ (fmap \ f \ \hbox{\bf rTree}) \\ -- \ implementing \ an \ instance \ of \ the \ Functor \ typeclass \ over \ Trees. \end{array}
instance Functor (Either a) where
fmap f (Right x) = Right (f x)
           fmap _ (Left x) = Left x
-}
-- Here's how the Either type is instanced. Bebause it takes two type parameters, but Functor only wants one, we can give it one so that the
-- other is left unknown. We only apply the function to the Right value because the Right and Left are usually of two different types. If we
-- wanted to apply a function over both L and R, then they would have to be of the same type.
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