1. Cauchy-Schwarz inequality:  $|u \cdot v| \leq |(u|| ||v|| \quad \text{or} \quad \left(\sum_{i=1}^{n} u_i \cdot v_i\right)^2 \leq \left(\sum_{i=1}^{n} u_i^2\right) \left(\sum_{i=1}^{n} v_i^2\right)$ where the equality holds iff u. v are linearly dependent. Proof:  $\sum_{i=1}^{n} \sum_{j=1}^{n} (u_i v_j - u_j v_i)^2 = \sum_{i=1}^{n} u_i^2 \sum_{j=1}^{n} v_j^2 + \sum_{i=1}^{n} v_i^2 \sum_{j=1}^{n} u_i^2 - \sum_{i=1}^{n} u_i v_i \sum_{j=1}^{n} u_i v_j$ = 2 ( \( \frac{\sigma}{\( \text{Lin} \) \) \( \frac{\sigma}{\( \text{Lin} \) \) \( \frac{\sigma}{\( \text{Lin} \) \) \( \text{Lin} \) \( \text Since LMS 30. we have  $(\sum_{i=1}^{n} u_i^*)(\sum_{j=1}^{n} v_j^*) > (\sum_{i=1}^{n} u_i v_j^*)^2$ .

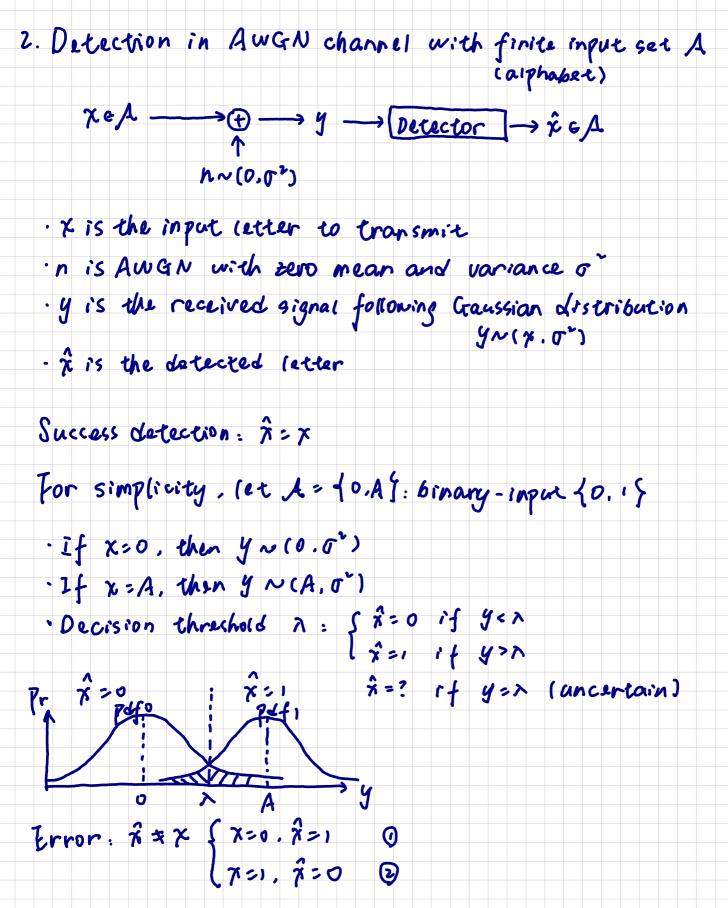
The equality holds off  $u_i v_j = u_j v_i$ , i.e.  $u_i^* > v_i^* = v_i v_j^* = 1...n$  (linearly dependent). 0.E.D.It can be generalized by replacing oil finite sams to integrals:

 $\left|\int_{-\infty}^{+\infty} \phi_{1}(x) \phi_{2}(x) dx\right| \leq \int_{-\infty}^{+\infty} \left|\phi_{1}(x)\right|^{2} dx \int_{-\infty}^{+\infty} \left|\phi_{2}(x)\right|^{2} dx$ 

The proof is similar and thus omitted here.

Hölder's inequality generalizes Cauchy-schwartz inequality.  $|u\cdot v| \in ||u||_{\mathcal{P}} ||v||_{\mathcal{Q}} ||v||_{\mathcal{Q}} ||v||_{\mathcal{Q}} = \left(\sum_{i=1}^{n} |u_i v_i| \in \left(\sum_{i=1}^{n} |u_i v_i|^{p}\right)^{\frac{1}{p}}$ where p.q.e[1.00] and ++ +==1.

Note that (as norm reduces to 11711 == max 1761.



(): 
$$x = 0$$
.  $\hat{\chi} = 1$  input probability Gaussian w. pefo  
 $Peo=P(x=0, \hat{\chi}=1) = P(x=0) P(\hat{\chi}=1 \mid \chi=0)$   
 $P(\hat{\chi}=1(\chi=0)) = \int_{\lambda}^{\infty} \frac{1}{\sigma_1 t_{\pi}} e^{-\frac{\hbar^2}{2\sigma_2}} dn$  is a function of  $\lambda \cdot \sigma$ .

$$\begin{array}{ll}
\text{($\chi : \chi : 1. $\hat{\chi} : 0)$} & = P(\chi : 1) P(\hat{\chi} : 0) P(\hat{\chi} : 0) | \chi : 1) \\
P(\hat{\chi} : 0 | \chi : 1) = \int_{-\infty}^{N} \frac{(n-A)^2}{\sigma_1 f_{WL}} Q_{WL} Q$$

$$\frac{\partial P_{A}}{\partial \lambda} : 0 \Rightarrow \lambda^{\frac{1}{2}} = -\frac{\sigma^{2}}{A} \left( n \frac{P_{i}}{i - P_{i}} + \frac{A}{2} \right), depends on the input probability.$$

Consider equipment input 
$$P(x=0) = P(x=1) = 0.5$$
.  
 $\lambda^{4} = \frac{A}{2}$  ensures  $Pe = Peo = Pei$ .  
 $Z = \frac{A}{\sigma} = Peo = \frac{1}{\sqrt{2\sigma}} \int_{\Delta \sigma}^{\Delta \sigma} e^{-\frac{2\sigma}{\sigma}} ds$   $Q(\pi) = \frac{1}{\sqrt{2\sigma}}$ .