

$$1. \text{ FM signal: } x(t) = A \cos(2\pi f_c t + 2\pi k_f \int_0^t m(\tau) d\tau) \\ = 10 \cos(10000\pi t + 4000\pi \int_0^t m(\tau) d\tau)$$

$$\therefore \int_0^t m(\tau) d\tau = \frac{5}{4} t \Rightarrow m(t) = \frac{5}{4}$$

$$2. \text{ SNR}_{\text{FM}} = 3\beta^2 \frac{P}{m_p^2} \text{SNR}_{\text{baseband}}$$

$$m(t) = A_m \cos(2\pi f_m t)$$

$$a) m_p = A_m. P = \frac{1}{2} A_m^2 \Rightarrow \text{SNR}_{\text{FM}} = \frac{3}{2} \beta^2 \text{SNR}_{\text{baseband}}$$

$$b) \text{SNR}_{\text{FM}} = \frac{M^2}{2 + M^2} \text{SNR}_{\text{baseband}} \stackrel{M=1}{=} \frac{1}{3} \text{SNR}_{\text{baseband}}$$

$$\frac{3}{2} \beta^2 > \frac{1}{3} \Rightarrow \beta > \frac{\sqrt{2}}{3}$$

$$3. P = \sigma_m^2. m_p = 4\sigma_m.$$

$$\text{SNR}_{\text{FM}} = 3\beta^2 \frac{P}{m_p^2} \text{SNR}_{\text{baseband}}$$

$$= \frac{3}{16} \beta^2 \text{SNR}_{\text{baseband}}$$

$$1. f_s \geq 2f_{\max} = 20 \text{ KHz}.$$

$$\text{bit rate} = 16 \times 20 = 320 \text{ kbps}$$

$$\text{nbits} = 60^2 \times 320 = 1152 \text{ Mbits} = 144 \text{ Mbytes}.$$

$$2. \sigma_q^2 = \int_{-\frac{\Delta}{2}}^{\frac{\Delta}{2}} q^2 \frac{1}{\Delta} dq = \frac{\Delta^2}{12} \quad \text{Uniform quantizer has MSE} = \frac{\Delta^2}{12}.$$

a) need to quantize $\pm 4\sigma$ into 2^n levels

$$\Delta = \frac{8\sigma}{2^n}$$

$$\therefore P_N = \frac{1}{12} \left(\frac{8\sigma}{2^n} \right)^2 = \frac{16}{3} \frac{\sigma^2}{2^{2n}}$$

$$P_S = \sigma^2 \quad \therefore \text{SNR} = \frac{P_S}{P_N} = \frac{3}{16} 2^{2n}$$

$$\text{SNR}_{\text{dB}} = 10 \log_{10} \frac{3}{16} 2^{2n} = -7.3 + 6.02n$$

$$b) P(|X| > 4\sigma) = 2 \int_{4\sigma}^{\infty} \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{x^2}{2\sigma^2}} dx = 2Q\left(\frac{4\sigma}{\sigma}\right) = 6.3 \times 10^{-3}$$

3. Consider first quarter.

$$P_S = \frac{1}{\frac{1}{4}} \int_0^{\frac{1}{4}} x^2 dx = \frac{1}{3}$$

$$P_N = \frac{\Delta^2}{12} = \frac{1}{12} \left(\frac{2}{2^n} \right)^2 = \frac{2^{-2n}}{3}$$

$$\therefore \text{SNR} = \frac{P_S}{P_N} = 2^{2n}$$

$$\text{SNR}_{\text{dB}} = 10 \log_{10} 2^{2n} = 6.02n$$

