

Which of the following equations specify a linear Gaussian POMP model for which the observable variable $Y_{1:N}$ is an ARMA(1,1) model? Here, ϵ_n and η_n are Gaussian white noise. X_n is 1-dimensional in (1) and 2-dimensional in (2) and (3).

- (A) (1), (2) and (3)
- (B) (1) and (2) but not (3)
- (C) (2) and (3) but not (1)
- (D) (1) and (3) but not (2)

$$\left. \begin{aligned} X_n &= aX_{n-1} + \epsilon_n \\ Y_n &= X_n + \eta_n \end{aligned} \right\} \quad (1)$$

$$\left. \begin{aligned} X_n &= \begin{pmatrix} a & 1 \\ 0 & 0 \end{pmatrix} X_{n-1} + \begin{pmatrix} 0 \\ 1 \end{pmatrix} \epsilon_n \\ Y_n &= (1, 0) X_n + \eta_n \end{aligned} \right\} \quad (2)$$

$$\left. \begin{aligned} X_n &= \begin{pmatrix} a & 1 \\ 0 & 0 \end{pmatrix} X_{n-1} + \begin{pmatrix} 1 \\ b \end{pmatrix} \epsilon_n \\ Y_n &= (1, 0) X_n \end{aligned} \right\} \quad (3)$$