

*Ph.D. Thesis*

**Probing Electroweakly Interacting  
Massive Particles  
with Drell-Yan Process  
at 100 TeV Colliders**

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## Abstract

(♣ To be written ♣) The main part of this thesis is based on our works [1, 2].

# Acknowledgments

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(♣ Appreciate more ♣)

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# Section 1

## Introduction

### 1.1 Overview

There are many models that extend the standard model (SM) of the particle physics by introducing weakly interacting massive particles (WIMPs), which have interactions with SM particles whose size is comparable to the electroweak gauge coupling. We have many theoretical and phenomenological motivations to introduce WIMPs, some of which are listed below.

- One of the motivations is the existence of the dark matter (DM) in our universe. When we assume a stable WIMP, its thermal relic abundance agrees with the observation if its mass is of  $\mathcal{O}(\text{TeV})$  or so.
- Such  $\mathcal{O}(\text{TeV})$  new particle is likely to be discovered by many kinds of experiments such as the dark matter searches and the particle colliders.
- Such  $\mathcal{O}(\text{TeV})$  WIMPs often appear in well-motivated ultraviolet (UV) completions of the SM. For example, the following two models contain such WIMPs: the minimally supersymmetric standard model (MSSM) introduced to solve the hierarchy problem and the minimal dark matter (MDM) model that can explain the existence and stability of the DM in a minimal extension of the SM.

Considering the third point, many of the WIMPs in the UV completions mentioned above have non-zero electroweak charges, which explain its weak interaction with SM particles. In this thesis, we would like to focus on such kind of WIMPs and seek ways to search for them.<sup>[b1](#)</sup>

In the MSSM, it is known that the supersymmetric (SUSY) partner of the electroweak gauge bosons or the Higgs boson can be the lightest supersymmetric particles (LSP) and are natural DM candidate. In particular, there are well motivated scenarios where the so-called Higgsino or Wino play the role of the LSP, which transform as doublet and triplet under the weak  $SU(2)_L$  gauge symmetry, respectively; light Higgsino is preferred to reduce the amount

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<sup>b1</sup>The word “WIMPs” is usually used in a broader sense that includes particles with some unknown weak interactions with SM particles. To distinguish this usage with ours, which only denotes some particles with non-zero electroweak charge, it may be better to call them as “WIMPs”, abbreviation of electroweakly interacting massive particles. However, within this thesis, we will just use “WIMPs” in a narrow sense obeying the widely spread custom.

of the fine-tuning of the electroweak scale as in the “natural SUSY” set up [3–6], while the so-called “mini-split” spectrum [7–12] with anomaly mediation [13, 14] makes Wino LSP. Another example, the MDM scenario, introduces a larger  $SU(2)_L$  multiplet, whose stability is automatically ensured by the charge assignment. In particular, a 5-plet Majorana fermion with hypercharge zero is a good DM candidate that escape from the DM search experiments so far.

To search for WIMPs, several different approaches are adopted. One way is to rely on DM search experiments, assuming that the WIMPs are the dominant component of the DM. Firstly, there exist several direct detection experiments that utilize a scattering between the DM and the nucleon [15–17]. Wino is the most promising target of these experiments, whose spin independent scattering cross section with nucleon is almost mass independently given as  $\sigma_{\text{SI}} \simeq 2.3 \times 10^{-47} \text{ cm}^2$  [18–22], which is still an order of magnitude below the current experimental limit. It is unlikely to detect Higgsino DM in this way since its small  $SU(2)_L$  charge makes scattering cross section comparable to or below the neutrino floor [19]. The detection of MDM may also be difficult [23] since its possibly larger mass of  $\mathcal{O}(10) \text{ TeV}$  weakens the sensitivity of direct detection experiments.

Secondly, a lot of effort is devoted to detecting cosmic rays resulting from DM annihilation, namely the DM indirect detection [24–27]. Although the results suffer from some astrophysical uncertainties, they have already excluded, for example, Wino with mass less than 400 GeV and also around 2 TeV [28]. On the other hand, the corresponding Higgsino bound is weaker and it has been probed only up to 350 GeV [29] again due to the smallness of its  $SU(2)_L$  charge. For the MDM, 5-plet fermion is analyzed as an example in [30] and the mass less than 2 TeV and several narrow regions are excluded. Note again that the WIMPs must be the dominant component of the DM for these approaches to be sensitive.

Another way of probing WIMPs is the direct production at the large hadron collider (LHC). The main strategy is to use the disappearing charged track, which indicates a long-lived charged particle, the charged components of the WIMP in the current case. Both ATLAS and CMS collaborations announced a result of this method with the data of  $\sqrt{s} = 13 \text{ TeV}$  LHC [31–33]. The current lower bound on the mass of the pure Higgsino-like (Wino-like) state is 152 (460) GeV at 95 % C.L. We can obtain a similar bound for the MDM using the same method [34]. In this method, however, the bound strongly depends on the lifetime of the charged component, which is sensitive to the mass difference between the charged and the neutral components. In particular, it is often the case in the SUSY model that the Higgsino-like LSP and its charged counterpart possess a non-negligible fraction of Wino, which significantly enhances the mass difference compared to the pure Higgsino case. In such a case, the lifetime of the charged component is extremely short, making the disappearing track method challenging. There is another option called mono-X search to search for a new physics signal in general. However, the corresponding bound is usually very weak due to the

large SM background and no bound is imposed on Higgsino at  $\sqrt{s} = 14 \text{ TeV}$  LHC [35].

To acquire somewhat stronger bounds on the WIMPs, independent of the decay product or the lifetime and whether they are the dominant component of the DM or not, it has been discussed that indirect search of WIMPs at collider experiments is useful [36–40]. It utilizes the WIMP loop effect on various observables. We pursue this possibility and study the effects of WIMPs on the oblique correction to the electroweak gauge bosons. In particular, in this paper, we study the prospect of the indirect search method at future 100 TeV hadron colliders such as FCC-hh at CERN [41–43] or SppC in China [44, 45]. We concentrate on the Drell-Yan process that has two leptons in the final state since it provides a very clean signal without any hadronic jets at least from the final state particles. We will show that it provides a comparable or better experimental reach for Higgsino compared to the direct production search of WIMPs at future colliders [46–49]. This method also provides independent and additional information about Wino and the MDM. Besides, we will reveal that this method is useful to investigate WIMP properties, such as charges, masses, and spins.



## 1.2 Organization of this thesis

This thesis is organized as follows.

In Sec. 2, we briefly review models with WIMPs considered in the thesis. Sec. 2.1 is devoted to the minimally supersymmetric standard model, while Sec. 2.2 to the minimal dark matter model. The mass splitting among the multiplet, which is a phenomenologically important property of WIMPs, is described in Sec. 2.3. The WIMP properties are summarized in Sec. 2.4.

In Sec. 3, we summarize the WIMP properties as a DM candidate. We show the calculation of thermal relic abundance and derive the required mass for WIMP DMs in Sec. 3.1. (**♣ More later ♣**)

In Sec. 4, we study the WIMP production at the hadron collider experiments and its detection. Possible production processes and the kinematics of the produced WIMPs are summarized in Sec. 4.1. Using the production processes described here, the current status and the prospect at the future 100, TeV colliders are reviewed in the following subsections. Sec. 4.2 is devoted to the description of the most promising way for the WIMP search called the disappearing track search. (**♣ More later ♣**)

In Sec. 5, we discuss our own ideas [1, 2] to probe the one-loop effect of WIMPs on the lepton pair production processes through the precise measurement at 100 TeV colliders. Here, we will describe our statistical analysis, show the obtained reach for WIMPs, and see the possibility to determine the WIMP properties after its discovery. Conclusions of the thesis are presented in Sec. 6.

In Appendices, we first summarize the conventions and notations used in the thesis in A. Then, we briefly review the  $\mathcal{N} = 1$  supersymmetry in Appendix B, the properties of the so-called transverse mass used in our analysis in Appendix C, and the statistical analysis method called the profile likelihood method in Sec. D.

## Section 2

# Models with WIMPs

There are several examples of models that contain WIMP DM candidates. In this section, two of them are briefly reviewed, which are intensely studied in this thesis: the minimally supersymmetric model (MSSM) described in Sec. 2.1 and the minimal dark matter (MDM) model described in Sec. 2.2. Sec. 2.4 is devoted to the summary table of properties of WIMPs frequently considered below.

### 2.1 Minimally supersymmetric standard model

**(♣ Summary of SUSY particle names somewhere ♣)**

The MSSM is the simple extension of the SM with  $\mathcal{N} = 1$  supersymmetry (SUSY).<sup>‡2</sup> One of the motivations to introduce SUSY is to solve the so-called hierarchy (or naturalness) problem [50–52] in the SM. The problem is related to the quantum correction to the SM Higgs boson mass from heavy new physics particles. For example, we can consider the one-loop correction to the Higgs mass from a Weyl fermion  $f$  and a complex scalar  $S$  as illustrated in Fig. 1. The corrections to the Higgs mass is given by

$$\Delta m_h^2 = -\frac{|\lambda_f|^2}{8\pi^2} \left[ \Lambda_{\text{UV}}^2 - 2m_f^2 \ln \left( \frac{\Lambda_{\text{UV}}}{m_f} \right) + \dots \right] \quad (\text{fermion}), \quad (2.1)$$

$$\Delta m_h^2 = \frac{\lambda_S}{16\pi^2} \left[ \Lambda_{\text{UV}}^2 - 2m_S^2 \ln \left( \frac{\Lambda_{\text{UV}}}{m_S} \right) + \dots \right] \quad (\text{scalar}), \quad (2.2)$$

**(♣ Check! Derive MSbar formula? ♣)** where  $\lambda_f$  and  $m_f$  are the Higgs-fermion coupling constant and the fermion mass, respectively, while  $\lambda_S$  and  $m_S$  are those for the scalar  $S$ .

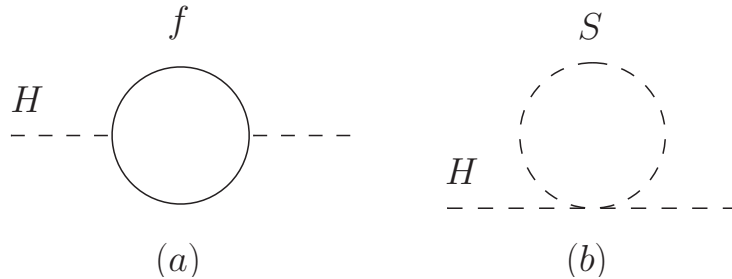


Figure 1: One-loop correction to the Higgs mass from (a) a Weyl fermion  $f$  and (b) a complex scalar  $S$ .

<sup>‡2</sup>For a brief review of the  $\mathcal{N} = 1$  SUSY, see Sec. B.

Notation	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	boson	fermion
$\hat{Q}_i$	<b>3</b>	<b>2</b>	1/6	squark	left-handed quark
$\hat{L}_i$	<b>1</b>	<b>2</b>	-1/2	slepton	left-handed lepton
$\hat{U}_i$	$\bar{\mathbf{3}}$	<b>1</b>	-2/3	squark	right-handed up-type quark
$\hat{D}_i$	$\bar{\mathbf{3}}$	<b>1</b>	1/3	squark	right-handed down-type quark
$\hat{E}_i$	<b>1</b>	<b>1</b>	1	slepton	right-handed lepton
$\hat{H}_u$	<b>1</b>	<b>2</b>	1/2	Higgs	Higgsino
$\hat{H}_d$	<b>1</b>	<b>2</b>	-1/2	Higgs	Higgsino

Table 1: Notations and quantum numbers of the chiral superfields in the MSSM. Also shown are names of bosonic and fermionic components of each suprefield used in this thesis.

Notation	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	boson	fermion
$\hat{g}$	<b>8</b>	<b>1</b>	0	gluon	gluino
$\hat{W}$	<b>1</b>	<b>3</b>	0	$W$ boson	Wino
$\hat{B}$	<b>1</b>	<b>1</b>	0	$B$ boson	Bino

Table 2: Notations and quantum numbers of the vector superfields in the MSSM. Also shown are names of bosonic and fermionic components of each suprefield.

We take the cut-off scale of the theory to be  $\Lambda_{UV}$  to regularize the otherwise divergent loop integral and neglect the lower order terms of  $\Lambda_{UV}$ . Eqs. (2.1) and (2.2) show the quadratic dependence of  $\Delta m_H^2$  on  $\Lambda_{UV}$ , which means that the Higgs mass is sensitive to the energy scale of the beyond the SM physics. However, there is at least one extremely high energy scale physics in nature, gravity at the Planck scale  $M_{\text{pl}} \sim 10^{18-19} \text{ GeV}$ . By substituting  $\Lambda_{UV} = M_{\text{pl}}$  in Eqs. (2.1) and (2.2) and assuming  $\lambda_f \sim \lambda_S \sim \mathcal{O}(1)$ , we notice that orders-of-magnitude fine-tuning is required to obtain the correct Higgs mass  $m_h = 125.10 \text{ GeV}$  [53], which is unnatural.

SUSY provides a nice solution to this fine-tuning problem. As is summarized in Appendix B, each Weyl fermion in a supersymmetric model is accompanied by two complex scalars with the same mass  $m_f = m_S$ . In addition, their coupling constants to the Higgs boson should have a relationship  $|\lambda_f|^2 = \lambda_S$  due to the fact that  $\lambda_S$  is a coupling constant in the F-term potential sourced by a superpotential term proportional to  $\lambda_f$ . By using both equations and summing the corrections (2.1) and (2.2) with a factor of two multiplied to the latter, we obtain a result independent of the cut-off scale  $\Lambda_{UV}$  without fine-tuning. This cancellation is ensured by the so-called non-renormalization theorem. [54, 55]

We now summarize the notations and quantum numbers of the chiral and vector su-

perfields in the MSSM in Table 1 and 2, respectively. In the tables, we also summarize the names of bosonic and fermionic components of each superfield used in this thesis. The supersymmetric part of the MSSM Lagrangian is described by the superpotential<sup>‡3</sup>

$$W = Y_u^{ij} \hat{U}_i \hat{Q}_j \hat{H}_u - Y_d^{ij} \hat{D}_i \hat{Q}_j \hat{H}_d - Y_e^{ij} \hat{E}_i \hat{L}_j \hat{H}_d + \mu \hat{H}_u \hat{H}_d, \quad (2.3)$$

where  $i, j = 1, 2, 3$  labels the quark and lepton generation, while  $Q, L, U, D, E$  are superfields that contain the left-handed quark, left-handed lepton, right-handed up-type quark, right-handed down-type quark, and right-handed charged lepton, respectively. In Eq. (2.3), proper contraction of  $SU(3)_C$  and  $SU(2)_L$  indices is assumed. Note that two Higgs doublets  $H_u$  and  $H_d$  with opposite values of  $U(1)_Y$  hypercharges are introduced, which is needed to cancel the contributions to the gauge anomaly from fermionic partners of the Higgs doublets.

Postulating SM gauge symmetries as a unique guideline to construct a model, there are a few more terms allowed in the superpotential:

$$W_{\Delta L=1} = \lambda^{ijk} \hat{L}_i \hat{L}_j \hat{E}_k + \lambda'^{ijk} \hat{L}_i \hat{Q}_j \hat{D}_k + \mu^i \hat{L}_i \hat{H}_u, \quad (2.4)$$

$$W_{\Delta B=1} = \lambda''^{ijk} \hat{U}_i \hat{D}_j \hat{D}_k, \quad (2.5)$$

where  $\Delta L = 1$  and  $\Delta B = 1$  represents the breaking of the lepton and baryon numbers by one, respectively. These terms with a lepton or baryon number breaking are phenomenologically problematic since they may cause a too fast proton decay, depending on parameters (see for example [57]). To avoid this problem, we often rely on a symmetry called the R-parity [58] or the matter parity [57, 59–61]. Charges of the R-parity, which is basically a  $Z_2$  symmetry, are calculated as

$$P_R = (-1)^{3(B-L)+2s}, \quad (2.6)$$

where  $B, L$ , and  $s$  are the baryon number, lepton number, and spin of the particle, respectively. According to the definition, we can see that all the SM particles have even parity ( $P_R = +1$ ), while all the supersymmetric particles have odd parity ( $P_R = -1$ ). Then it is easy to check that Eqs.(2.4) and (2.5) lead to the R-parity violating terms in the Lagrangian and thus are forbidden, while all the terms in Eq. (2.3) are allowed. From now on, we only focus on the R-parity preserving MSSM.

Since no superpartner of any SM particle is observed yet, SUSY should be broken at some scale to give large masses to superpartners. The SUSY breaking part of the Lagrangian is

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<sup>‡3</sup>For a more detailed review of the MSSM, see for example [56].

expressed as

$$\begin{aligned}
\mathcal{L}_{\text{soft}} = & -\frac{1}{2} \left( M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + \text{h.c.} \right) \\
& - \left( A_u^{ij} \tilde{U}_i \tilde{Q}_j H_u - A_d^{ij} \tilde{D}_i \tilde{Q}_j H_d - A_e^{ij} \tilde{E}_i \tilde{L}_j H_d \right) \\
& - m_Q^{2ij} \tilde{Q}_i^\dagger \tilde{Q}_j - m_L^{2ij} \tilde{L}_i^\dagger \tilde{L}_j - m_U^{2ij} \tilde{U}_i^\dagger \tilde{U}_j - m_D^{2ij} \tilde{D}_i^\dagger \tilde{D}_j - m_E^{2ij} \tilde{E}_i^\dagger \tilde{E}_j \\
& - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{h.c.}), \tag{2.7}
\end{aligned}$$

where the tilde is used to express the superpartner of the SM particle contained in a superfield, while fields without hat nor tilde denote particles in the SM. An exception is two Higgs doublets, where  $H_u$  and  $H_d$  express the scalar components, while  $\tilde{H}_u$  and  $\tilde{H}_d$  express their superpartners called Higgsinos. The SM-like Higgs doublet  $H$  corresponds to a linear combination of  $H_u$  and  $H_d$ , while the other combination becomes heavy.

It is known that, within the MSSM, almost all SUSY breaking mechanisms, such as the F-term (O’Raifeartaigh) [62] or D-term (Fayet-Iliopoulos) SUSY breaking [63, 64], fail to generate masses of superpartners with remaining the SM gauge group in the low energy effective theory. Thus, we need a so-called hidden sector in addition to the MSSM sector, in which SUSY is spontaneously broken. For the MSSM sector to have Lagrangian terms (2.7), we also need some mediation mechanism of the SUSY breaking. The relative size of the SUSY breaking parameters in Eq. (2.7) and thus the phenomenology of the model highly depends on the mediation mechanism. Among many mediation mechanisms of SUSY breaking, the anomaly mediated SUSY breaking [13, 14] leads to an interesting phenomenology with relatively light WIMPs, so it will be reviewed later.

## Dark matter candidate in the MSSM

There is another motivation to consider the R-parity preserving MSSM; it naturally contains the candidate for DM. Since there is a sizable amount of DM in the current universe, a DM candidate should be stable or have a sufficiently small decay width. In many models, the stability of DM is ensured by imposing a symmetry and/or by kinematically forbidding the DM decay. In the MSSM, the role of stabilizer can be played by the R-parity described above. Recalling that all the SM (supersymmetric) particles have even (odd) parity, each interaction vertex in the MSSM Lagrangian should contain an even number of supersymmetric particles. If we consider the lightest supersymmetric particle (LSP), such vertices can not construct the kinematically allowed LSP decay chain and, as a result, the LSP becomes a stable DM candidate.

The DM phenomenology, such as the production and annihilation of DM in the universe and processes that allow us to efficiently detect it, highly depends on which species of the supersymmetric particle becomes the LSP. Hereafter, we only focus on the cases where one

Value	Description	Reference
$M_W = 80.384 \pm 0.014 \text{ GeV}$	Pole mass of the W boson	[65, 66]
$M_Z = 91.1876 \pm 0.0021 \text{ GeV}$	Pole mass of the Z boson	[67]
$M_h = 125.15 \pm 0.24 \text{ GeV}$	Pole mass of the Higgs	[68, 69]
$M_t = 173.34 \pm 0.82 \text{ GeV}$	Pole mass of the top quark	[70]
$(\sqrt{2}G_\mu)^{-1/2} = 246.21971 \pm 0.00006 \text{ GeV}$	Fermi constant for $\mu$ decay	[71]
$\alpha_3(M_Z) = 0.1184 \pm 0.0007$	$\overline{\text{MS}}$ $SU(3)_C$ gauge coupling	[72]

Table 3: Experimentally measured SM parameters used for the derivation of Eq. (2.9).

of the gauginos and Higgsinos becomes the LSP, whose motivations are described below. Besides, all the LSP candidates described below (*i.e.*, Wino and Higgsino) have non-zero electroweak charges and they can be viewed as examples of the WIMPs.

### Higgs mass in the MSSM

Under the spontaneously or softly broken SUSY, the cancellation of the quantum correction to the Higgs boson mass discussed above is not exact. One obvious consequence of the SUSY breaking in Eqs. (2.1) and (2.2) is the hierarchy between  $m_f$  and  $m_S$  that appear in the second term of each contribution. In the case of the MSSM, the largest contribution comes from the superpartner of the top quark, stop, which has the largest Yukawa coupling with the Higgs boson.

When there is a large hierarchy between the SUSY breaking scale  $M_S$ , which is comparable to stop masses, and the top mass  $M_t$ , the stop contributions to the Higgs mass contains a large logarithm of the form of  $\log(M_S^2/M_t^2)$ . To resum the large logarithm and obtain a precise result, it is easy to rely on the renormalization group equation (RGE). In this framework, the value of the Higgs self-coupling  $\lambda$  at the electroweak scale is closely related to the Higgs mass. We define the potential for the SM Higgs doublet  $H$  as

$$V(H) = -\frac{m^2}{2}|H|^2 + \lambda|H|^4, \quad (2.8)$$

and assume the SM parameters summarized in Table 3. Then, according to [73], we obtain the relationship<sup>‡4</sup>

$$\lambda(M_t) = 0.12604 + 0.00206 \left( \frac{M_h}{\text{GeV}} - 125.15 \right) - 0.00004 \left( \frac{M_t}{\text{GeV}} - 173.34 \right), \quad (2.9)$$

<sup>‡4</sup>Although the values listed in Table 3 are different from the latest ones given in [53], we use older ones because the change in input values may cause the slight change in coefficients of second and third terms of Eq. (2.9). The latest central values of the Higgs and top masses are  $M_h = 125.10 \text{ GeV}$  and  $M_t = 173.1 \text{ GeV}$ , with which we can estimate  $\lambda(M_t) = 0.12595$ .

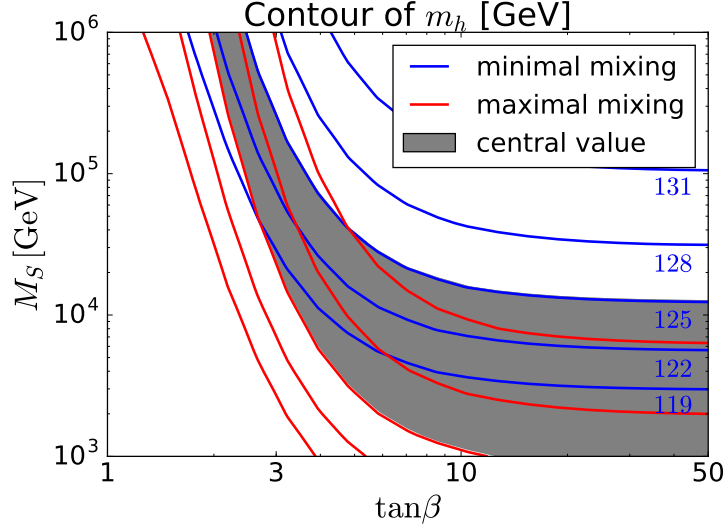


Figure 2: Contour of the Higgs mass  $m_h$  in the  $\tan\beta$  vs.  $M_S$  plane. The universal mass  $M_S$  is assumed for all the SUSY particles. Blue (red) lines correspond from top to bottom to the contours of  $m_h = 131, 128, 125, 122, 119$  GeV for the minimal (maximal) stop mixing. Gray shade corresponds to the region where  $m_h = 125.10$  GeV can be explained.

where the  $\overline{\text{MS}}$  scheme is used to renormalize the divergence of loop integrals.

In the MSSM, the value of  $\lambda$  at the SUSY breaking scale  $M_S$  is given by

$$\lambda(M_S) = \frac{g_1^2(M_S) + g_2^2(M_S)}{8} \cos^2 2\beta + \delta\lambda, \quad (2.10)$$

where  $g_1$  and  $g_2$  are  $U(1)_Y$  and  $SU(2)_L$  gauge coupling constants, respectively, while  $\beta$  parametrizes the ratio of the vacuum expectation values

$$\frac{\langle H_u^0 \rangle}{\langle H_d^0 \rangle} = \tan \beta, \quad (2.11)$$

with  $H_u^0$  and  $H_d^0$  being electromagnetically neutral components of the corresponding Higgs doublets. In Eq. (2.10), the first term shows the tree-level contribution from the D-term potential and  $\delta\lambda$  denotes the threshold correction from heavy superpartners.  $M_S$  is often chosen to be the geometric mean of stop masses to minimize the largest contribution to  $\delta\lambda$  from stops. Once the spectrum of the MSSM particles is fixed, we can evaluate the Higgs self-coupling using Eq. (2.10), calculate its running according to the RGE, and obtain the prediction for the Higgs mass through Eq. (2.9).

In Fig. 2, we show the contour plot of the Higgs mass  $m_h$  in the  $\tan\beta$  vs.  $M_S$  plane. We assume the universal mass  $M_S$  for all the SUSY particles. Under this assumption, the

largest contribution to the threshold correction  $\delta\lambda$  from stops is expressed as

$$\delta\lambda \simeq \frac{9y_t^2(M_S)}{16\pi^2} \tilde{X}_t \left[ 1 - \frac{\tilde{X}_t}{12} \right], \quad (2.12)$$

$$\tilde{X}_t \equiv \frac{(A_t - \mu \cot \beta)^2}{M_S^2}, \quad (2.13)$$

with  $y_t \equiv Y_u^{33}$  and  $A_t \equiv A_u^{33}$ . It is obvious from Eq. (2.12) that, for a moderate value of  $\tilde{X}_t \lesssim \mathcal{O}(1)$ ,  $\tilde{X}_t = 0$  ( $\tilde{X}_t = 6$ ) corresponds to the case with minimum (maximum) threshold correction, often called as the minimal (maximal) stop mixing.<sup>5</sup>

The red (blue) lines in Fig. 2 denote from top to bottom the contours of  $m_h = 131, 128, 125, 122, 119$  GeV for the minimal (maximal) stop mixing. Gray shade corresponds to the region where the central value of the observation  $m_h = 125.10$  GeV can be explained. From the figure, we can see that the discovery of the Higgs with  $m_h = 125.10$  GeV may indicate a somewhat heavy SUSY breaking scale  $M_S \gtrsim 10$  TeV for the case with a small stop mixing or a small  $\tan \beta$ . Combined with the fact that there is still no sign of the superpartners at the collider experiment, this motivates us to consider a heavy SUSY scenario.

### Light Higgsino and its relation to the naturalness

When we consider a heavy SUSY model concerning the Higgs mass, there is another problem called the little hierarchy problem. This mentions the hierarchy between the electroweak scale and the heavy SUSY breaking scale and an accompanying fine-tuning. Although the degree of the required fine-tuning is several orders of magnitude smaller than that for the large hierarchy between the electroweak and Planck scales, it will be more acceptable if some mechanism relieves the fine-tuning. The required fine-tuning can be clearly expressed in the equation

$$\frac{1}{2}m_Z^2 = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan \beta^2 - 1} - \mu^2, \quad (2.14)$$

where the right-handed side is the MSSM prediction for the  $Z$ -boson mass assuming the successful electroweak symmetry breaking. If some of the MSSM parameters  $m_{H_d}$ ,  $m_{H_u}$ ,  $\mu$  are much larger than  $m_Z$ , there should be some amount of fine-tuning to satisfy the equation.

There is a measure of the fine-tuning in this sense, proposed in [74, 75]:

$$\Delta_{a_i} \equiv \frac{a_i}{m_Z^2} \frac{\partial m_Z^2}{\partial a_i}, \quad (2.15)$$

---

<sup>5</sup>Eq. (2.12) shows that  $\delta\lambda < 0$  for  $\tilde{X}_t > 12$ , resulting in the prediction of a lighter Higgs mass than the minimal stop mixing case. However, the parameter space with  $\tilde{X}_t \gtrsim 6$  is severely constrained by the requirement of the stability of the electroweak vacuum (**♣ Citation ♣**) and is not considered here.



where  $a_i$  is an MSSM model parameter. In order for the model to be “natural”, we require  $|\Delta_{a_i}| < \Delta$  for any  $a_i$  with a typical choice of  $\Delta \sim \mathcal{O}(10-100)$ . Since  $m_Z$  is sensitive to the Higgsino mass  $\mu$ , this gives an upper bound on the “natural” choice of the Higgsino mass

$$\mu^2 < \frac{m_Z^2}{2} \Delta, \quad (2.16)$$

predicting the (sub-)TeV scale Higgsino. As we will see in Sec. (♣ ???? ♣), the light Higgsino is also fascinating as a dark matter candidate.

Even when the SUSY breaking scale is much higher than the electroweak scale, it is not strange for Higgsino to be around the electroweak scale since it is protected by an R-symmetry and a Peccei Quinn symmetry. (♣ Definition? ♣) The symmetry protection is also important for a solution to the so-called “ $\mu$ -problem” [76], where the large hierarchy between the SUSY preserving parameter  $\mu$  and the cut-off scale of the MSSM such as  $M_{\text{Pl}}$  is discussed. When we consider the low energy effective field theory in which SUSY is broken and all the squarks and sleptons are decoupled, a unique linear combination of the R-symmetry and the Peccei Quinn symmetry is enhanced only if both gauginos and Higgsinos are massless. This fact leads to the framework of the split SUSY [10], in which there is a hierarchy between the masses of Higgsinos/gauginos and the other SUSY particles. In this framework, the phenomenology is determined by the ordering and hierarchy of Higgsino and gaugino masses. In particular, the collider phenomenology of Higgsino will be summarized in Sec. 4 for the case when gauginos are heavier than Higgsino.

Finally, the naturalness requirement discussed above also imposes an upper bound on other parameters, in particular, on  $m_{H_u}^2$  for  $\tan^2 \beta \gg 1$ . The small value of  $m_{H_u}^2$  can be realized by the focus point mechanism [77–79], where the choice of the SM parameters in our universe, in particular that of  $y_t$ , allows  $m_{H_u}^2$  at the low energy scale to be insensitive to its boundary condition at the high energy scale.

### Light Wino in the anomaly mediated SUSY breaking model

Among many heavy SUSY models, the anomaly mediated SUSY breaking [13, 14] and the pure gravity mediation scenario based on it [80–82] is of particular interest since it naturally predicts the existence of WIMPs (in particular Winos denoted as  $\tilde{W}$ ) in the TeV range. In this scenario, the SUSY breaking effect is directly mediated to the quark and lepton supermultiplets, and they obtain masses comparable to the scale of the SUSY breaking, which is roughly equal to the gravitino mass  $m_{3/2}$ . Higgsino is also considered to be heavy contrary to the model described above. In fact, it is easy to realize the hidden sector dynamics that generates the  $\mu$ -term of  $\mathcal{O}(m_{3/2})$ . On the other hand, the superpartners of gauge bosons, gauginos, feel the SUSY breaking effect only through a one-loop diagram, which is related to the conformal anomaly. As a result, gaugino mass parameters in Eq. (2.7) are one-loop

suppressed compared with other mass parameters and given by

$$M_i(M_S) = - \frac{\beta_i}{2g_i^2} \Big|_{M_S} m_{3/2}, \quad (2.17)$$

where  $i = 1, 2, 3$  is a gauge index and  $\beta_i$  denote the beta functions of gauge coupling constants. ( $\clubsuit$   $M_S$ ?  $M_{\text{GUT}}$ ?  $\clubsuit$ ) At the one-loop level, this gives

$$M_1(M_S) = \frac{11g_1^2(M_S)}{16\pi^2} m_{3/2}, \quad (2.18)$$

$$M_2(M_S) = \frac{g_2^2(M_S)}{16\pi^2} m_{3/2}, \quad (2.19)$$

$$M_3(M_S) = -\frac{3g_3^2(M_S)}{16\pi^2} m_{3/2}. \quad (2.20)$$

Since Higgsinos are assumed to have a mass comparable to  $m_{3/2} \sim M_S$ , they decouple from the effective theory below the scale  $M_S$ . To take account of the correction to the gaugino masses from the Higgs-Higgsino loop, one has to include the threshold correction at  $M_S$

$$\Delta M_1 = \frac{g_1^2(M_S)}{16\pi^2} L, \quad \Delta M_2 = \frac{g_2^2(M_S)}{16\pi^2} L, \quad (2.21)$$

with

$$L \equiv \mu \sin 2\beta \frac{m_A^2}{|\mu|^2 - m_A^2} \ln \frac{|\mu|^2}{m_A^2}, \quad (2.22)$$

where  $m_A$  is the mass of the heavy CP-odd Higgs.

Below  $M_S$ , gaugino mass parameters further run towards the gaugino mass scale  $M_{\tilde{G}}$ , where the physical gaugino masses are determined. Note that the Bino and Wino masses are well approximated by  $|M_1(M_{\tilde{G}})|$  and  $|M_2(M_{\tilde{G}})|$ , while the gluino pole mass  $m_{\tilde{g}}$  includes a sizable effect from the threshold correction as [10]

$$m_{\tilde{g}} = |M_3(M_{\tilde{G}})| \left[ 1 + \frac{g_3^2}{16\pi^2} \left( 12 + 9 \ln \frac{M_{\tilde{G}}^2}{|M_3|^2} \right) \right]. \quad (2.23)$$

The gaugino scale is often defined through  $M_3(M_{\tilde{G}}) = M_{\tilde{G}}$  to make the logarithmic term in Eq. (2.23) vanish.

In Fig. 3, we show the dependence of gaugino masses on  $m_{3/2}$  and  $L$ . In the left panel, we take  $\tan \beta = 2.5$  and  $L = 0$ , and the  $m_{3/2}$  dependence is shown. Blue, green, and red lines denote the masses of Bino, Wino, and gluino, respectively. We can see that, throughout the parameter region used here, Wino becomes the lightest gaugino and becomes the LSP

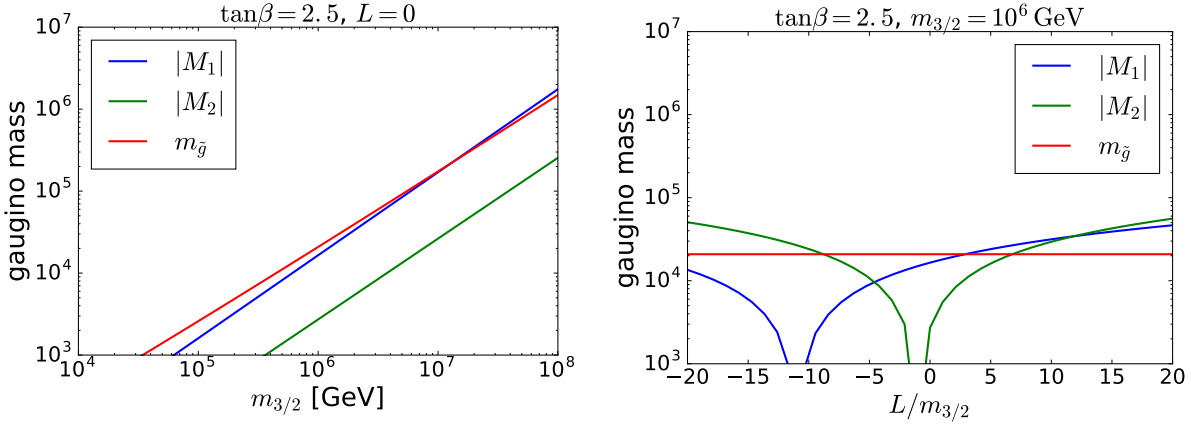


Figure 3: Gaugino masses as a function of  $m_{3/2}$  with a fixed value of  $L = 0$  (left) and that of  $L/m_{3/2}$  with a fixed value of  $m_{3/2} = 10^6$  GeV (right). Blue, green, and red lines denote the masses of Bino, Wino, and gluino, respectively.  $\tan\beta = 2.5$  is used in both figures.

that can be a dark matter candidate. In this choice of parameters,  $m_{3/2} = 10^6$  GeV roughly corresponds to the observed value of the Higgs mass  $m_h \sim 125$  GeV, which at the same time realizes the  $\mathcal{O}(1)$  TeV mass for Wino. As we will see in Sec. ??, (**♣ Caution!! ♣**) the Wino dark matter in this mass range is well-motivated since it gives us a collect relic abundance of the dark matter.

In the right panel of Fig. 3, we also show the  $L$  dependence of gaugino masses for  $\tan\beta = 2.5$  and  $m_{3/2} = 10^6$  GeV. For simplicity, we neglect the relative phase of  $m_{3/2}$  and  $L$  and only consider the relative sign of them. It can be seen that the hierarchy between gaugino masses is changed when a large value of  $|L|$  is considered. However, we can safely say that when the threshold correction is sufficiently small,  $|L| \lesssim \mathcal{O}(m_{3/2})$ , Wino remains to be the LSP. Besides, the dependence of  $m_h$  on  $L$  is negligibly small and  $m_h$  changes only  $\mathcal{O}(0.1)$  GeV within the parameter choice of the right panel.

## 2.2 Minimal dark matter model

The MDM [83–85] is another example model that contains a WIMP DM candidate. This model attempts to explain the existence of stable DM by extending the SM as simply as possible. More specifically, we just assume the same gauge groups as the SM and add only one  $SU(2)_L$   $n$ -plet with  $U(1)_Y$  hypercharge  $Y$  in the model.<sup>46</sup>  $Y$  is chosen such that one

<sup>46</sup>This new particle, even if it is a fermion, does not contribute to the  $SU(2)_L^2 U(1)_Y$ ,  $U(1)_Y^3$ , nor  $U(1)_Y \text{ grav}^2$  anomalies when  $Y = 0$ . When  $Y \neq 0$ , we always consider a vector-like pair of Weyl fermions, similar to the Higgsinos  $\tilde{H}_u$  and  $\tilde{H}_d$ , which as a whole consists of a Dirac fermion and cancels the contributions to the gauge anomalies.

component of the multiplet, after the electroweak symmetry breaking, has vanishing  $U(1)_{\text{EM}}$  charge, and thus can be a DM candidate. This condition leaves only  $n$  discrete choices of  $Y$  for an  $SU(2)_L$   $n$ -plet.

In the  $SU(2)_L$  limit, masses of all the components in the multiplet are the same. Since  $SU(2)_L$  symmetry is spontaneously broken, the mass difference among them is generated at the one-loop level and a heavy component can decay into a lighter component. For the multiplet to explain the DM in the current universe, the  $U(1)_{\text{EM}}$  neutral component should have the lowest mass. We will return to this point and check that this is the case in Sec. (♣ ??? ♣), related to the collider search for MDMs using the disappearing track signal.

In some sense, WIMPs contained in the MSSM can also be viewed as an example of the MDM (if we assume all the other superpartners are decoupled). In fact, if we choose the set of  $SU(2)_L$  and  $U(1)_Y$  charges as  $(n, Y) = (2, \pm 1/2)$  and  $(3, 0)$ , they correspond to the Higgsino and Wino, respectively. However, for these choices, the stability of the  $U(1)_{\text{EM}}$  neutral component is not automatically ensured, and some extra symmetry (in this case the R-parity) is needed for the DM to survive until now. The important point of the new framework MDM is that, when we use large  $n \geq 5$ , there are examples of multiplets that automatically contain a sufficiently long-lived DM candidate.

The stability of such multiplets can be understood through a simple group theoretical argument. To write down the effective operator that describes the decay of a  $n$ -plet field to SM particles, we have to make a  $n$ -plet representation out of several SM fields. However, since the largest  $SU(2)_L$  representation in the SM is doublet, we need at least  $n - 1$  SM fields in the operator. The operator made out of this large number of fields should be suppressed by a power of the cutoff scale  $\Lambda$ , at least by  $\Lambda^{4-n}$  ( $\Lambda^{3-n}$ ) for a scalar (fermion) MDM, and results in a small decay rate. Since the well-motivated DM mass is of  $\mathcal{O}(\text{TeV})$  as we will see in Sec. (♣ ?? ♣), the resulting lifetime of the DM candidate is estimated as  $\tau \sim \Lambda^{-2p}(\text{TeV})^{2p-1}$  for an operator with a suppression factor  $\Lambda^{-p}$ . By demanding  $\tau$  to be larger than the age of the universe under the assumption for the cut off scale  $\Lambda < M_{\text{pl}}$ , we can conclude that the operator of the DM decay should have a dimension larger than five. Then, we recast this condition to that for  $n$  and obtain

$$n \geq \begin{cases} 6 & \text{for scalar MDM,} \\ 5 & \text{for fermion MDM.} \end{cases} \quad (2.1)$$

On the other hand, since we consider large  $SU(2)_L$  multiplets, the RGE running of the  $SU(2)_L$  gauge structure constant  $\alpha_2$  above the MDM mass is drastically modified. At the one-loop level, we have (see for example [86])

$$\alpha_2^{-1}(Q) = \alpha_2^{-1}(M_{\text{MDM}}) - \frac{b_2}{2\pi} \ln \frac{Q}{M_{\text{MDM}}}, \quad (2.2)$$

$$b_2 \equiv -\frac{19}{6} + c \frac{n^3 - n}{18}, \quad (2.3)$$

with  $c = 1$  ( $1/4$ ) for a Majorana/Weyl fermion (real scalar). Note that the first and second term of Eq. (2.3) represent the contributions from SM particles and the MDM, respectively. Then, assuming the perturbativity of the  $SU(2)_L$  gauge coupling up to  $M_{\text{pl}}$ , this relationship puts an upper bound on the choice of  $n$ . According to the strong dependence on  $n$  of  $b_2$ , a strong bound is obtained,

$$n \leq \begin{cases} 8 & \text{real scalar MDM,} \\ 5 & \text{Majorana fermion MDM.} \end{cases} \quad (2.4)$$

In Table 4, we summarize the properties of MDMs for several different choices of  $(n, Y)$ . Throughout the table, the checkmark represents a suitable property as a DM candidate. In the first three columns, we show the quantum numbers of our choice, namely the set of  $(n, y)$  and spin. In the next column, we show the condition for the DM stability, namely, whether all the DM decay operators have dimensions larger than five or not. The checkmarks correspond to the automatically stable DM candidates. The next column shows if the DM direct detection experiment has already excluded these DM candidates or not. Since the non-zero value of  $Y$  usually leads to the large cross section as will be discussed in Sec. (♣ ??? ♣), only  $Y = 0$  candidates are associated with checkmarks. However, note that these properties may be changed due to a small modification to the model, such as the imposition of an extra symmetry or the mixing between other new physics particles. The final column shows examples of the viable DM candidates analyzed in the literature.

From the table, we can see that there are two fascinating targets, a 5-plet fermion and a 7-plet scalar both of which have  $Y = 0$ . Among them, we neglect the latter possibility because it has been pointed out [88, 89] that a dimension five operator combined with a loop consisted of the TeV scale 7-plet scalar induces a sizable decay rate for the  $U(1)_{\text{EM}}$  neutral component. Instead, we will take a 5-plet scalar with  $Y = 0$  just as a working example, assuming that its stability is ensured by some other mechanism.

### 2.3 Mass splitting among an $SU(2)_L$ multiplet

As a final remark in this section, we consider an important property of  $SU(2)_L$  multiplets after the spontaneous breakdown of the electroweak symmetry: the mass splitting among the components of a multiplet. This mass splitting, which we will call  $\Delta m_\chi$ , is typically much smaller compared with the WIMP mass  $m_\chi$ , but its value is phenomenologically important as we will see in later sections.

First, we start with the tree-level propagation of heavy particles, such as the SUSY particles other than the LSP, or other unknown particles. After integrating out all the

$SU(2)_L$	Quntum numbers		DM stability	Not excluded by direct detection	Examples
	$U(1)_Y$	Spin			
2	1/2	Scalar			
2	1/2	Fermion			Higgsino
3	0	Scalar		✓	[87]
3	0	Fermion		✓	Wino
3	1	Scalar/Fermion			[87]
4	1/2	Scalar/Fermion			[87]
4	3/2	Scalar/Fermion			[87]
5	0	Scalar		✓	[87]
5	0	Fermion	✓	✓	[83–85]
5	1	Scalar			
5	1	Fermion	✓		
5	2	Scalar			
5	2	Fermion	✓		
6	1/2, 3/2, 5/2	Scalar	✓		
7	0	Scalar	✓	✓	[83–85]
7	1, 2, 3	Scalar	✓		

Table 4: Table of the MDM properties. In the first three columns, we show the quantum numbers of our choice. In the next two columns, DM stability (the checkmark means ”stable”) and its status under the DM direct detection experiment (the checkmark means it is still alive) are shown. The last column is devoted to the examples in the literature.

heavy particles other than the SM particles or the light WIMP, we may obtain operators of the form of  $\mathcal{O} = M_{ij}\chi_i\chi_j$ , where  $\chi$  denotes the WIMP and  $i$  is the  $SU(2)_L$  index. This operator causes the mass splitting only when  $M_{ij}$  transforms non-trivially under the  $SU(2)_L$  symmetry. Then, we can explicitly construct the lowest dimensional operator among those relevant for the mass splitting. For Higgsino,

$$\mathcal{O} = \frac{1}{\Lambda}(\bar{\chi}H^*)(H\chi), \quad (2.1)$$

where  $\chi = (\tilde{H}_u, -i\sigma_2\tilde{H}_d^*)^t$ ,  $\Phi$  is the SM Higgs doublet with  $Y = 1/2$ ,  $\Lambda$  is the cut-off scale of the effective theory, *i.e.*, the typical mass scale of the relevant heavy particles, and the parenthesis denotes the  $SU(2)_L$  invariant product of fundamental representations. Similarly, for Wino, [90]

$$\mathcal{O} = \frac{1}{\Lambda^3}(H^\dagger\sigma^a H)(H^\dagger\sigma^b H)\tilde{W}^a\tilde{W}^b, \quad (2.2)$$

is the lowest dimensional operator that causes the mass splitting. A simple implication of this observation is that, for multiplets with large  $n$ , there are suppression factors that keep the tree-level mass splitting small. For Wino, the suppression is of  $\mathcal{O}(M_W^4/\Lambda^3)$ , which yields a splitting smaller than 10 MeV for heavy particles with a few TeV masses. For fermionic MDMs with  $n \gtrsim 5$ , a similarly small mass splitting at the tree-level is expected.<sup>‡7</sup> This is the main reason why the loop correction plays a more important role in the mass splitting of Wino and MDMs.

The situation is different for Higgsino because of the much less drastic suppression factor of  $\mathcal{O}(M_W^2/\Lambda)$ , which generates  $\mathcal{O}(100)$  MeV mass splitting for  $\Lambda \lesssim 10$  TeV.<sup>‡8</sup> In fact, in models like the split SUSY, the mixing between Higgsino and heavier gauginos can generate the large mass splitting among the Higgsino components. As a result, neutral components that originally forms a Dirac fermion splits into two Majorana fermions with mass difference  $\Delta m_0$ , and the charged components also become heavier than the lighter neutral component by  $\Delta m_+^{(\text{tree})}$ . According to [91], their approximate expressions are given by

$$\Delta m_0 \simeq \frac{M_W^2}{g_2^2} \left( \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2} \right), \quad (2.3)$$

$$\Delta m_+^{(\text{tree})} \simeq \frac{M_W^2}{2g_2^2} \left[ \left( \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2} \right) + \text{sgn}(\mu) \sin 2\beta \left( \frac{g_1^2}{M_1} - \frac{g_2^2}{M_2} \right) \right], \quad (2.4)$$

<sup>‡7</sup>For scalar MDMs, there is another renormalizable operator that generates a mass splitting

$$\mathcal{O} = -\lambda_H (\chi^* \sigma^a \chi) (H^\dagger \sigma^a H).$$

Here, we just assume that  $\lambda_H$  is sufficiently small and the discussion below is not affected by the above term.

<sup>‡8</sup>For the order estimation of the mass splitting, we have taken account of the size of the coupling constants omitted in Eq. (2.1), using the rough estimation  $g_1^2 \sim g_2^2 \sim \mathcal{O}(10^{-1})$ .

assuming the CP invariance for simplicity. Note that the results agree with the previous order estimation with  $\Lambda \sim M_1, M_2$ .

Next, we consider the loop correction to the WIMP masses. When the loop is composed of heavy particles, the effective operator that causes the mass splitting again becomes the same as above, which is now associated with a small loop factor. Thus, the largest contribution comes from the gauge boson – WIMP loop. For the charged components of Higgsino, the one-loop result is known: [91]

$$\Delta m_+^{(\text{rad})} \simeq \frac{1}{2} \alpha_2 M_Z \sin^2 \theta_W \left( 1 - \frac{3M_Z}{2\pi m_\chi} \right) \sim 355 \text{ MeV} \left( 1 - \frac{3M_Z}{2\pi m_\chi} \right), \quad (2.5)$$

with  $\theta_W$  being the Weinberg angle, which gives  $\Delta m_+^{(\text{rad})} \simeq 341 \text{ MeV}$  for  $m_\chi = 1.1 \text{ TeV}$  and may be comparable to  $\Delta m_+^{(\text{tree})}$ . On the other hand, for Wino, we have the two-loop result [92]

$$\frac{\Delta m}{\text{MeV}} = -413.315 + 305.383 \left( \log \frac{m_\chi}{\text{GeV}} \right) - 60.8831 \left( \log \frac{m_\chi}{\text{GeV}} \right)^2 \quad (2.6)$$

$$+ 5.41948 \left( \log \frac{m_\chi}{\text{GeV}} \right)^3 - 0.181509 \left( \log \frac{m_\chi}{\text{GeV}} \right)^4, \quad (2.7)$$

which exhibits  $\Delta m \simeq 165 \text{ MeV}$  for  $m_\chi = 2.9 \text{ TeV}$ . For the MDM, there are neutral, singly charged, doubly charged, and so on, components. Among them, the neutral and singly charged components have the smallest mass difference of  $\Delta m \simeq 166 \text{ MeV}$  [83], which is the most important value for the phenomenology.

## 2.4 Summary

In Table 5, we summarize the properties of WIMPs discussed in this thesis. In the first block named “Quantum numbers”, we show the  $SU(2)_L$  electroweak charge,  $U(1)_Y$  hypercharge, and spin nature. In the second block named “Masses”, two types of masses are shown.  $m_\chi$  is the required masses to explain the DM relic abundance without non-thermal production (see Sec. (♣ ??? ♣) for the detail).  $\Delta m_\chi$  is the mass difference between the electromagnetically neutral and (singly) charged components of the multiplet discussed in the previous section. Values are taken from [84, 87, 93–96].



WIMP DM candidate	Quantum numbers			Masses	
	$SU(2)_L$	$U(1)_Y$	Spin	$m_\chi/\text{TeV}$	$\Delta m_\chi/\text{MeV}$
Higgsino	2	1/2	Dirac fermion	1.1	341
Wino	3	0	Majorana fermion	2.9	166
5-plet scalar	5	0	real scalar	9.4	166
5-plet fermion	5	0	Majorana fermion	10	166

Table 5: Table of properties of WIMPs discussed in this thesis. In the “Quantum numbers” block, the  $SU(2)_L$  and  $U(1)_Y$  charges and spin nature are shown. In the “Masses” block, the proper mass of the thermally produced DM  $m_\chi$  and mass difference between the neutral and charged components of the multiplet  $\Delta m_\chi$  are shown. See Sec. (♣ ??? ♣) for the descriptions and implications of  $m_\chi$  and Sec. 2.3 for those of  $\Delta m_\chi$ .

## Section 3

# WIMP as a dark matter

In this section, we review the properties of WIMPs as DM. It is revealed, when we take a close look at the relic abundance of WIMP DM in Sec. 3.1, that a WIMP with the TeV scale mass is a good DM candidate, which is sometimes called *WIMP miracle* and is a strong motivation to consider WIMPs. In Sec. 3.2 and 3.3, we will consider two different ways to search for the WIMP DM, called the indirect and direct detection. Finally, Sec. 3.4 is devoted to the summary and concluding remarks of this section.

### 3.1 WIMP DM relic abundance

One of the most important evidences of the beyond SM is the existence of DM [97]. DM is an unknown object that occupies a non-negligible ratio of the total energy of our universe, but has not yet been directly observed because of its weak interaction with the SM particles.<sup>‡9</sup> In spite of its invisibility, the existence of DM is confirmed by several astrophysical observations such as the mass measurement using the gravitational lensing effect caused by galaxies and clusters [98, 99], the flatness of galactic rotation curves further the optical radius [100, 101], the measurement of the power spectrum of the cosmic microwave background (CMB), and so on. In particular, the observation of CMB allows us the precise determination of various cosmological parameters [102, 103] including the density of the non-relativistic matter and baryon, which is currently determined as [104]

$$\Omega_m h^2 = 0.1430 \pm 0.0011, \quad (3.1)$$

$$\Omega_b h^2 = 0.02237 \pm 0.00015, \quad (3.2)$$

where  $h \sim \mathcal{O}(1)$  is the Hubble constant in units of  $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . The difference between  $\Omega_m h^2$  and  $\Omega_b h^2$  implies the existence of DM and its abundance  $\Omega_\chi h^2 \simeq 0.12$ .

In cosmology, DM production mechanisms that try to explain the DM abundance are divided into two main categories: thermal and non-thermal production. The former assumes the equilibrium between the DM and the thermal bath in the early universe. As the universe expands, the interaction rate that maintains the thermal equilibrium becomes smaller and the DM decouples from the thermal bath at some time, which is the so-called *freezeout*. As we will see below, the resulting abundance of the DM in this scenario is mainly controlled by the temperature of the thermal bath  $T_f$  when the freezeout occurs. On the other hand,

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<sup>‡9</sup>At worst DM interacts with the SM particles through the gravity, which is considerably weaker than all the other known interactions. (♣ Mention to Ema paper?? ♣)

non-thermal production assumes the DM production by some processes irrespective of the thermal bath such as decay of a heavy particle. Since the thermal production scenario can be realized in relatively simple setup and WIMPs are well motivated in connection with this kind of scenario, we focus on it.

We assume the stable DM particle  $\chi$  with mass  $m_\chi$  can pair annihilate into SM particles with some cross section  $\sigma$ . When DM is in thermal equilibrium with the thermal bath of temperature  $T$ , DM velocity obeys the corresponding Boltzmann distribution. Let  $v$  be the relative velocity of annihilating DM particles and  $\langle\sigma v\rangle$  be the thermal average of the product of  $\sigma$  and  $v$ . By using this quantity, we can write down the Boltzmann equation for the DM number density  $n_\chi$  as

$$\frac{d(n_\chi a^3)}{dt} = -a^3 \langle\sigma v\rangle (n_\chi^2 - n_{\text{eq}}^2), \quad (3.3)$$

where  $t$  and  $a$  are the time coordinate and the scale factor, respectively, of the Friedmann Robertson Walker metric

$$ds^2 = -dt^2 + a(t)^2 d\mathbf{x}^2, \quad (3.4)$$

while  $n_{\text{eq}}$  denotes the number density of DM in equilibrium. When DMs are non-relativistic, its temperature dependence is given by  $n_{\text{eq}} \propto T^{3/2} \exp(-m_\chi/T)$ . The first term of the right handed-side of Eq. (3.3) represents the annihilation rate of DM pairs that should be proportional to  $n_\chi^2$ , while the second term describes the DM creation through the inverse process. As desired, the number density does not change in time if  $n_\chi = n_{\text{eq}}$ . Recalling the total entropy conservation in a comoving volume  $sa^3 = (\text{const})$ , it turns out to be convenient to define the ratio  $Y \equiv n_\chi/s$ . In fact, this modification cancels the effect of the expansion of the universe  $\dot{a} \equiv da/dt > 0$  from Eq. (3.3), leading to a simpler equation

$$\frac{dY}{dt} = -s \langle\sigma v\rangle (Y^2 - Y_{\text{eq}}^2), \quad (3.5)$$

with  $Y_{\text{eq}} \equiv n_{\text{eq}}/s$ .

Here we assume that the freezeout occurs when the relativistic radiation dominates the total energy of the universe, which will be verified to be correct later. In this case, we can derive  $a \propto T^{-1}$  from the entropy conservation with  $s \propto T^3$ . For the numerical calculation, we define a dimensionless parameter  $x \equiv m_\chi/T$ . Then we can rewrite Eq. (3.5) as

$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = -\frac{\Gamma}{H} \left( \frac{Y^2}{Y_{\text{eq}}^2} - 1 \right), \quad (3.6)$$

where  $\Gamma$  denotes the DM interaction rate defined as

$$\Gamma \equiv n_{\text{eq}} \langle\sigma v\rangle. \quad (3.7)$$

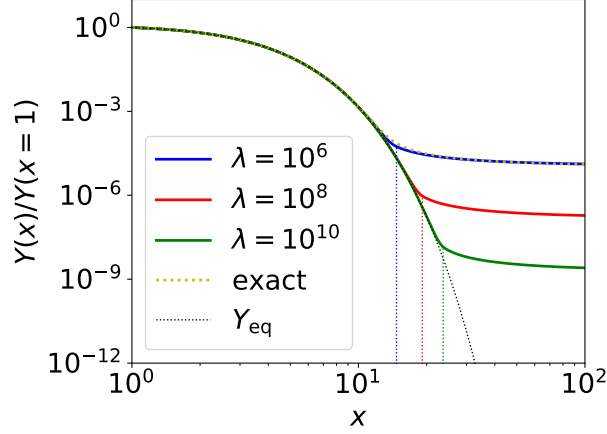


Figure 4: Plot of  $Y(x)/Y(x=1)$  with  $Y(x)$  being a solution of the evolution equation Eq. (3.6). The yellow dotted line is a solution for  $\lambda \equiv \Gamma/H|_{x=1} = 10^6$ , while the black dotted line denotes  $Y_{\text{eq}}(x)/Y_{\text{eq}}(x=1)$ . The solid lines are the approximation to the solutions described in the text. The blue, red, and green colors correspond to  $\lambda = 10^8$ ,  $10^{10}$ , and  $10^{12}$ , respectively. The vertical dotted lines denote the freezeout temperature  $x_f$ .

Finally,  $\langle\sigma v\rangle$  is known to be expanded as [105]

$$\langle\sigma v\rangle = \langle\sigma v\rangle_s + \langle\sigma v\rangle_p x^{-1} + \dots, \quad (3.8)$$

corresponding to the  $s$ -wave,  $p$ -wave, and so on, contributions to the cross section. When  $x \gg 1$ , the term with the highest power of  $x$  dominates the cross section. When the  $x^{-p}$  term dominates ( $p \geq 0$ ), temperature dependence of the interaction rate is  $\Gamma \propto x^{-3/2-p}e^{-x}$ , while the Hubble parameter only reduces as  $H \propto \rho^{1/2} \propto x^{-2}$ . As a result, at some point  $\Gamma$  becomes smaller than  $H$  and  $Y$  freezes out as Eq. (3.6) indicates. Hereafter, we focus on the case of the  $s$ -wave domination with  $\langle\sigma v\rangle_s \neq 0$  for simplicity. **(♣ What is the difference for  $p$ -wave and so on? ♣)** In Fig. 4, we show the solution of Eq. (3.6) for  $\lambda \equiv \Gamma/H|_{x=1} = 10^6$  by the yellow dotted line. In the calculation, we use the boundary condition  $Y(x=1) = Y_{\text{eq}}(x=1)$  and plot the normalized value  $Y(x)/Y(x=1)$ . We also plot the function  $Y_{\text{eq}}(x)/Y_{\text{eq}}(x=1)$  by the black dotted line.

Unfortunately, it is computationally hard to solve Eq. (3.6) for larger values of  $\lambda$  because of the almost complete cancellation between two terms of the right handed side for small  $x \sim \mathcal{O}(1)$  and its amplification caused by large  $\lambda$ . We adopt instead to use an approximation that is the same with the one adopted in the public code **MicrOMEGAs** [106, 107]. For the small  $x$  region, temperature is still high enough to maintain the equilibrium  $Y \simeq Y_{\text{eq}}$ , which means that  $d\Delta Y/dx \ll dY_{\text{eq}}/dx$  with  $\Delta Y \equiv Y - Y_{\text{eq}}$ . From this approximation we obtain a

formula

$$\Delta Y \simeq -\frac{x}{2\lambda} \frac{dY_{\text{eq}}}{dx}. \quad (3.9)$$

Then we define the time  $x_f$ , or equivalently the so-called freezeout temperature  $T_f$ , when the approximation becomes invalid through the equation

$$\Delta Y(x_f) = 2.5Y_{\text{eq}}(x_f). \quad (3.10)$$

After the freezeout  $x > x_f$ , the annihilation of the DM pairs rapidly slows down and the DM abundance far exceeds its equilibrium value:  $Y \gg Y_{\text{eq}}$ . Then we can neglect the second term of the right hand of Eq. (3.6) and obtain the analytical solution

$$Y(x) \simeq -\frac{x}{c_1 x + \lambda/Y_{\text{eq}}(x=1)}, \quad (3.11)$$

where  $c_1$  is a integration constant. In Fig. 4, we show results obtained with these two approximations Eqs. (3.9) and (3.11) for  $\lambda = 10^6$  (blue),  $10^8$  (red), and  $10^{10}$  (green). In particular, the blue and the yellow lines almost completely overlaps with each other, which proves the validity of the approximations. The vertical dotted lines in the figure show the freezeout temperature. It can be seen from the figure that  $x = x_f$  does correspond to the time when  $Y$  starts to deviate from  $Y_{\text{eq}}$ . Note also that as  $\lambda \propto \langle\sigma v\rangle$  becomes larger, the freezeout time becomes later and the late time relic abundance becomes smaller.

When the DM properties (*i.e.*, the mass  $m_\chi$  and the annihilation cross section  $\langle\sigma v\rangle$ ) are given, corresponding relic abundance can be calculated using above procedure. In particular,  $m_\chi$  determines the normalization of the figure, namely  $Y_{\text{eq}}(x=1) = Y_{\text{eq}}(T=m_\chi)$ , and  $\langle\sigma v\rangle$  determines the freezeout temperature through the combination of Eq. (3.7). Assuming the absence of non-thermal effect, only some good combination of these two values should explain the current relic abundance of the DM. From the numerical calculation, we obtain an order estimation formula

$$\Omega_\chi h^2 \sim \frac{3 \times 10^{-27} \text{ cm}^3/\text{s}}{\langle\sigma v\rangle_0} \sim 0.1 \left( \frac{0.01}{\alpha} \right)^2 \left( \frac{m_\chi}{300 \text{ GeV}} \right)^2, \quad (3.12)$$

where the rough estimation  $\langle\sigma v\rangle \sim \alpha^2/m_\chi^2$  is used in the last equation with  $\alpha$  being the fine structure constant for the DM-SM coupling. What is fascinating in Eq. (3.12) is that an object can be a DM candidate if it has mass comparable to the electroweak scale and coupling constant comparable to the electroweak coupling constant. This is the so-called *WIMP miracle*, which support the hypothesis of the WIMP as a candidate of the DM. Such TeV-scale WIMPs are theoretically well-motivated in connection with problems of the SM such as the naturalness problem as reviewed in Sec. 2.

**(♣ Virial velocity, mass density of DM, velocity of sun etc ♣)**

## 3.2 WIMP DM search : indirect detection

(♣ Briefly review later ♣)

## 3.3 WIMP DM search : direct detection

There are also many experiments aimed for the direct detection of the DM.<sup>‡10</sup> Here, we again assume some interaction between the DM and SM particles and look for a recoil of a target SM particle due to the collision with the DM in the laboratory. In the case of WIMPs of our concern, any particle with non-zero electroweak charge can be a target particle, which interacts with WIMPs through the  $t$ -channel electroweak gauge boson exchange. In the traditional setup such as the XENON1T experiment [17], a nucleus (of xenon in this case) and an electron are the frequently used target particles. (♣ Cite electron scattering ♣).

## 3.4 Summary

(♣ To search for WIMPs that do not compose a sizable fraction of the DM, we have to rely on the collider search. ♣)

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<sup>‡10</sup>For the recent review of the direct detection experiments, see for example [108].

## Section 4

# Direct collider search of WIMPs

In this section, we review the production of TeV-scale WIMPs and search for their signals using the collider experiment. In particular, we will summarize the current bounds for WIMPs obtained at the large hadron collider (LHC) and prospects at the future planned 100 TeV colliders such as the hadron option of the future circular collider (FCC-hh) [109] and the super proton-proton collider (SPPC) [44, 45]. In Sec. 4.1, we discuss the dominant production processes of WIMPs at a hadron collider. In Sec. 4.2 – 4.4, we review three different methods for the signal identification, the disappearing track, soft-lepton, and mono-jet search, and summarize the current and future bounds. (♣ Correct? ♣)

### 4.1 WIMP production

There are two relevant processes both of which significantly contribute to the production cross section of WIMPs considered here. The pair production via electroweak interaction is a universal process that can be considered for any particle with a non-zero electroweak charge. The decay of colored particles may also be efficient particularly for the MSSM. In this subsection, we will review these two in order.

#### Pair production via electroweak interaction

Since all the WIMPs of our interest possess non-zero  $SU(2)_L$  and  $U(1)_Y$  charges, they can be directly produced via electroweak interaction at the hadron collider as shown in Fig. 5.<sup>‡11</sup>

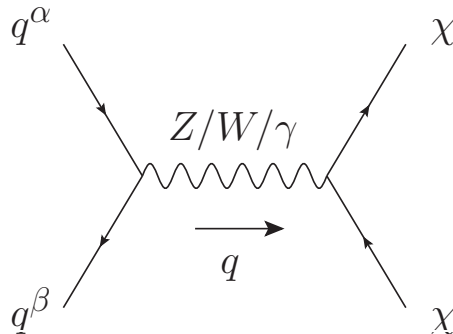


Figure 5: WIMP pair production process at the hadron collider.

<sup>‡11</sup>All the Feynman diagrams in this thesis are drawn with the public code `JaxoDraw-2.1` [110], which is a graphical user interface that allows users to draw Feynman diagrams intuitively and export them in the

In the figure,  $q^\alpha$  and  $q^\beta$  denote the partons (namely, one of quarks or gluons) of the incident protons relevant for the process, while  $\chi$  denotes the WIMP and  $q$  is the momentum transfer. Assuming the WIMP to be a  $SU(2)_L$   $n$ -plet with  $U(1)_Y$  charge  $Y$  and the mass  $m_\chi$ , this process is well described by the effective lagrangian<sup>‡12</sup>

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + (D^\mu \chi)^\dagger (D_\mu \chi) - m_\chi^2 \chi^\dagger \chi \quad (\text{complex scalar}), \quad (4.1)$$

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \bar{\chi}(i\not{D} - m_\chi)\chi \quad (\text{Dirac fermion}), \quad (4.2)$$

with  $\mathcal{L}_{\text{SM}}$  being the SM lagrangian, while the covariant derivative is given by

$$D_\mu \equiv \partial_\mu - ig_2 \not{W}^a T_n^a - ig_1 Y \not{B}, \quad (4.3)$$

where  $T_n^a$  ( $a = 1, 2, 3$ ) are  $n$ -dimensional representation matrices of  $SU(2)_L$ . Note that when  $\chi$  is a real scalar (Majorana fermion) with  $Y = 0$ , the terms with  $\chi$  in Eq. (4.1) (Eq. (4.2)) should be divided by two.

For the calculation, we neglect the effect of the electroweak symmetry breaking, which is valid because we are interested in the high-energy collision with the parton-level center-of-mass (CM) energy  $\sqrt{s'} \equiv \sqrt{q^2} \gtrsim \text{TeV}$ . Then, we consider the process in the CM frame and estimate the parton-level differential cross section as

$$\left. \frac{d\sigma_{\alpha\beta}}{d\sqrt{s'}d\Omega} \right|_{\text{CM}} = \frac{C_{\alpha\beta}}{8s'} \left( 1 - \frac{4m_\chi^2}{s'} \right)^{3/2} \sin^2 \theta_{\text{CM}} \quad (\text{complex scalar}) \quad (4.4)$$

$$\left. \frac{d\sigma_{\alpha\beta}}{d\sqrt{s'}d\Omega} \right|_{\text{CM}} = \frac{C_{\alpha\beta}}{4s'} \sqrt{1 - \frac{4m_\chi^2}{s'}} \left[ 1 + \frac{4m_\chi^2}{s'} + \left( 1 - \frac{4m_\chi^2}{s'} \right) \cos^2 \theta_{\text{CM}} \right] \quad (\text{Dirac fermion}), \quad (4.5)$$

where  $\theta_{\text{CM}}$  is the angle between the momentum of the initial parton  $q^\alpha$  and that of a final state WIMP. These expressions are valid only when the center of mass energy exceeds the production threshold,  $\sqrt{s'} > 2m_\chi$ . Note also that these expressions represent inclusive cross sections, *i.e.*, the total cross section for the production of any component of the WIMP multiplet  $\chi$ . The coefficient  $C_{\alpha\beta}$  consists of contributions from  $U(1)_Y$  and  $SU(2)_L$  gauge bosons,<sup>‡13</sup>

$$C_{\alpha\beta} = c_{1\alpha\beta} Y^2 \alpha_1^2 + c_{2\alpha\beta} I(n) \alpha_2^2, \quad (4.6)$$

---

**eps** format with the help of the (modification of) **axodraw** style file for L<sup>A</sup>T<sub>E</sub>X [111]. Under the environment of macOS Mojave, it apparently fails to start, but one can still execute it by looking inside the application and start the Java executable file **jaxodraw-2.1-0.jar** directly. We would like to thank the authors for providing the best tools to write the thesis with.

<sup>‡12</sup>In this subsection, we neglect the small mass splitting among different components in the multiplet  $\chi$  described in Sec. 2.3. This approximation is valid since the mass splitting is by far smaller than  $m_\chi$  and has only a tiny effect on the production process.

<sup>‡13</sup>There is no contribution from the interference term between  $U(1)_Y$  and  $SU(2)_L$  contributions, since it is proportional to  $\text{Tr}(T_n^a) = 0$ .



with  $I(n)$  being the Dynkin index for the  $n$ -dimensional representation given by

$$I(n) \equiv \frac{n^3 - n}{12}, \quad (4.7)$$

which is normalized so that  $I(2) = 1/2$ . The explicit form of  $c_{1\alpha\beta}$  and  $c_{2\alpha\beta}$ , which are sizes of the couplings between partons of our choice and gauge bosons, can be expressed using the  $U(1)_Y$  charge  $Y_\alpha$  for the parton  $q^\alpha$  and the reducible 13-dimensional representation matrices of  $SU(2)_L$  in the parton basis  $T_{\alpha\beta}^a$  as

$$c_{1\alpha\beta} = Y_\alpha^2 \delta_{\alpha\beta}, \quad (4.8)$$

$$c_{2\alpha\beta} = \sum_a |T_{\alpha\beta}^a|^2. \quad (4.9)$$

Recalling that  $\alpha_1 < \alpha_2$  and that we often consider the WIMPs with large  $n$  and moderate  $Y$ , the WIMP production cross section grows as  $n^3$  for larger multiplets according to the group theoretical factor (4.7).

In reality, the initial state of the hadron collider is not the individual partons but two protons. To obtain the cross section for the two-proton initial state, we rely on the parton distribution function (PDF), which expresses the fraction of the partons with some given momentum in each accelerated proton. Let  $f_\alpha(x)$  ( $0 < x < 1$ ) be the PDF for a given parton  $q^\alpha$  inside a proton with momentum  $p^\mu$ .  $f_\alpha(x)$  can be interpreted as a probability distribution to find the parton  $q^\alpha$  with momentum  $xp^\mu$ , so we have a relationship

$$\sum_\alpha \int_0^1 dx x f_\alpha(x) = 1, \quad (4.10)$$

associated with the total momentum conservation, and

$$\int_0^1 dx [f_d(x) - f_{\bar{d}}(x)] = 1, \quad (4.11)$$

$$\int_0^1 dx [f_u(x) - f_{\bar{u}}(x)] = 2, \quad (4.12)$$

from the composition of the proton. (**♣ Reference ♣**) Using the PDF, the cross section of the process of interest at the hadron collider is evaluated as

$$\frac{d\sigma}{d\sqrt{s'}d\Omega} = \sum_{\alpha,\beta} \int_0^1 dx_1 dx_2 f_\alpha(x_1) f_\beta(x_2) \delta(s' - sx_1x_2) \left. \frac{d\sigma_{\alpha\beta}}{d\Omega} \right|_{\text{lab}}, \quad (4.13)$$

where  $\sqrt{s}$  is the CM energy of the proton-proton collision. Note that  $d\sigma_{\alpha\beta}/d\Omega|_{\text{lab}}$  in the integrand is a function of  $x_1$  and  $x_2$ , which is obtained by applying the appropriate Lorentz transformation to  $d\sigma_{\alpha\beta}/d\Omega|_{\text{CM}}$ .

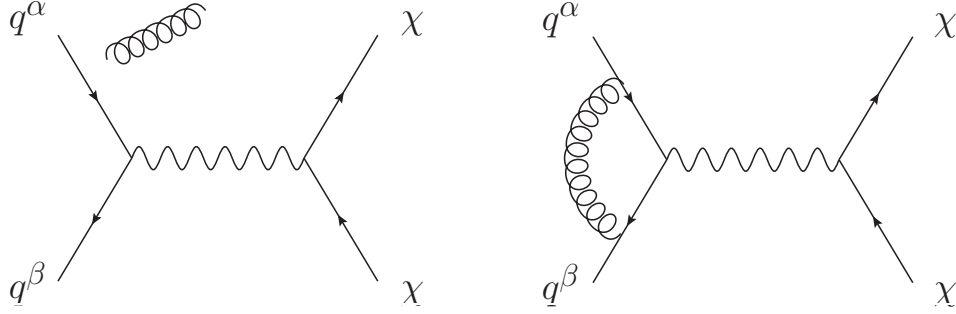


Figure 6: Example of NLO QCD contributions to the WIMP pair production process.

**(♣ Comment on factorization scale? ♣)**

Hadron colliders have several more features related to the strong interaction of quantum chromodynamics (QCD). Firstly, the next-to-leading order (NLO) QCD contribution to each process is not necessarily negligible. For the WIMP pair production, the real and virtual emission of a gluon shown in the left and right panels of Fig. 6, respectively, give the NLO QCD contributions, which will also be taken into account from now on. In particular, when the large transverse momentum is important for the phenomenology of our concern, such as the case in Sec. 4.2, the real emission of a gluon with sizable transverse momentum significantly modifies the calculation. Also, an additional real emission may be required to trigger the event, in particular when the other products are invisible for detectors like in Sec. 4.4. Secondly, all the colored particles in the initial, intermediate, and final states should be accompanied by numbers of soft emissions of gluons, which is the phenomena so-called the parton shower. In practice, there is a difficulty caused by the partial overlap of the gluon phase space between the one-gluon emission cross section calculated as an NLO QCD effect and the same calculated as the parton shower. To avoid the overlap, we often perform the matching procedure, in which we set some merging energy scale by hand and include the contribution to the cross section with gluon energy above (below) the scale only from the NLO QCD (parton shower) calculation. Finally, the colored particles in the final states should eventually be confined, which is called the hadronization, and observed as some energetic and collimated sprays of hadrons, which as a whole is called a jet.

In the following, we perform the numerical calculation, taking account of all the above complexities. For this purpose, we make use of the Monte Carlo generator **MadGraph5 aMC@NLO** (v2.6.3.2) [112, 113] with the successive use of **Pythia8** [114] for the parton shower, hadronization, and matching and **Delphes** (v3.4.1) [115] for the detector simulation, including the definition of jets as observed objects. We use the so-called MLM-style matching [116] with the merging scale of 67.5 GeV and **NNPDF2.3QED** with  $\alpha_3(M_Z) = 0.118$  [117] as a canonical set of PDFs.

In Table 6, we list the production cross sections of various WIMPs via a weak gauge

WIMP name	Higgsino	Wino	5-plet Majorana fermion	5-plet real scalar
$\sigma_{\text{LO}}$ [fb]	15	52	(♣ ??? ♣)	(♣ ??? ♣)
$\sigma_{\text{NLO}}$ [fb]	17	60	(♣ ??? ♣)	(♣ ??? ♣)
$K$ -factor	1.15	1.15		

Table 6: Table of pair production cross sections of several types of WIMPs. The CM energy  $\sqrt{s} = 100$  TeV is assumed and WIMP masses are set to be 1 TeV.

Wino mass [TeV]	1.0	1.5	2.0	2.9
$\sigma_{\text{LO}}$ [fb]	52	12	4.0	0.86
$\sigma_{\text{NLO}}$ [fb]	60	15	4.7	1.0
$K$ -factor	1.15	1.20	1.19	1.21

Table 7: Table of pair production cross sections of Wino with several choice of masses. The CM energy  $\sqrt{s} = 100$  TeV is assumed.

boson exchange at a  $\sqrt{s} = 100$  TeV hadron collider. As for the WIMP mass, we use the common value  $m = 1$  TeV to compare the cross sections among a different choice of quantum numbers.  $\sigma_{\text{LO}}$  and  $\sigma_{\text{NLO}}$  denote the production cross sections without and with the NLO QCD correction, respectively, while the last line is the so-called  $K$ -factor defined as  $K = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$ . From the table, by paying attention to the factor two difference in degrees of freedom between the Dirac (Higgsino) and Majorana (Wino and 5-plet) fermions, we can roughly see the dependence of the cross section on the  $SU(2)_L$  charge  $\sigma \propto n^3$ .

### (♣ Cross section to neutral Higgsino seems missing ♣)

In Table 7, we also show the mass dependence of the Wino pair production cross section. For heavier mass, a wider range of  $\sqrt{s'}$  is below the production threshold  $2m_\chi$  or accompanied with a small suppression factor  $(1 - 4m_\chi^2/s')^{1/2}$  as shown in Eq. (4.5), and the cross section becomes significantly smaller. However, values in the tables still denote that plenty of well-motivated WIMP DM candidates, such as 1 TeV Higgsino and 2.9 TeV Wino, are produced at, for example, the  $30 \text{ ab}^{-1}$  option of the FCC-hh.

In Fig. 7, we show the  $\sqrt{s'}$  distribution for the pair production process at a  $\sqrt{s} = 100$  TeV collider. Left and right figures correspond to the production of  $m_\chi = 1$  TeV Higgsino at the integrated luminosity  $\mathcal{L} = 3 \text{ ab}^{-1}$  and of  $m_\chi = 3$  TeV Wino at  $\mathcal{L} = 30 \text{ ab}^{-1}$ , respectively. At around  $\sqrt{s'} \sim 2m_\chi$ , we clearly see the production threshold and the suppression effect  $\sigma \propto (1 - 4m_\chi^2/s')^{1/2}$ . On the other hand, when  $\sqrt{s'}$  becomes much larger than  $2m_\chi$ , we can see the correct behavior of the cross section, which decreases as  $\sigma \propto (\sqrt{s'})^{-3}$  as Eq. (4.5) indicates. Note that these properties are universal among several processes, including one of the contributions to the gluino pair production process through the  $s$ -channel gluon exchange

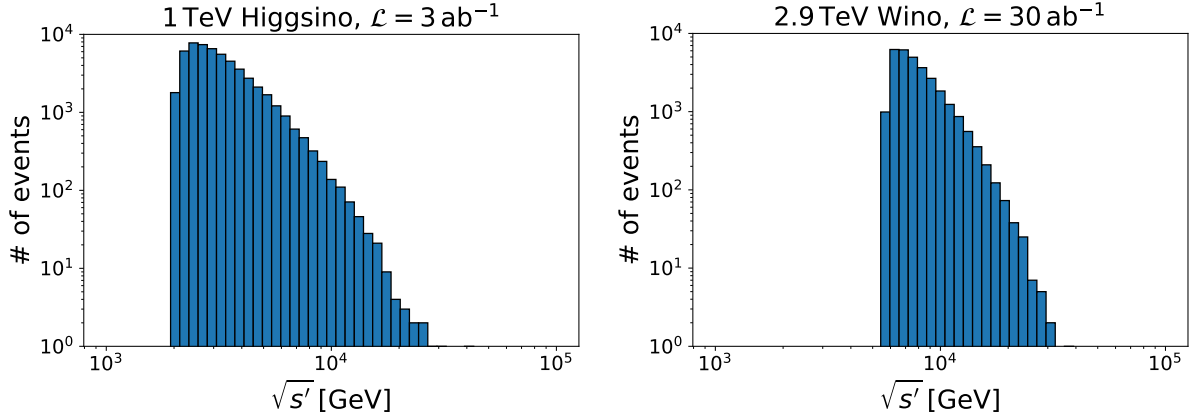


Figure 7: Histogram of the  $\sqrt{s'}$  distribution for  $\sqrt{s} = 100$  TeV. *Left:* Production of 1 TeV Higgsino at  $\mathcal{L} = 3 \text{ ab}^{-1}$ . *Right:* Production of 2.9 TeV Wino at  $\mathcal{L} = 30 \text{ ab}^{-1}$ .

gluino mass [TeV]	6.0	7.0	8.0
$\sigma(pp \rightarrow \tilde{g}\tilde{g})$ [fb]	7.9	2.7	1.0

Table 8: Gluino pair production cross section at  $\sqrt{s} = 100$  TeV taken from [118].

discussed in the next subsection, and the lepton pair production via an electroweak gauge boson that is the main topics of Sec. 5.

**(♣ Histogram of angular dependence ♣)**

**(♣ Comment on the lack of one-loop process in the simulation and IR divergence ♣)**

## Decay of colored particles

In hadron colliders, particles with color charges have far more chance to be produced than non-colored particles. When we consider the split SUSY or the anomaly mediation model reviewed in Sec. 2.1, gluino tends to be relatively light, whose decay produces WIMPs. Without fine-tuning of Higgsino and gaugino masses, gluino lifetime is sufficiently short and only its decay products are observed by the detectors. Since all the SUSY particles finally decay into the LSP as described in Sec. 2.1, the gluino production cross section can effectively be counted as the production cross section of WIMPs in these models.

Keeping the R-parity conservation in our mind, the dominant process accompanied by gluinos in these models is the gluino pair production. In Table 8, we summarize the gluino pair production cross section for various gluino masses at  $\sqrt{s} = 100$  TeV, taken from [118]. The values in the table show that the gluino pair production process, depending on masses

of gluino and WIMP, may give a much larger cross section for the WIMP production than the purely electroweak processes described above. We will mainly focus on, however, the electroweak pair production process below, in case gluino is out of the reach at 100 TeV colliders.

## 4.2 Disappearing track search

In the last section, we have checked the possibility that a large number of WIMPs are produced at hadron colliders. On the other hand, the detection of produced WIMPs is not a straight-forward task, because there are huge background events with many charged and/or colored particles. To reduce the background events and obtain the best possible reach for WIMPs, we consider several methods using typical properties for the WIMP signals, one of which is the disappearing track signal described here.

As mentioned in Sec. 2.3, the spontaneous breaking of the electroweak symmetry leads to the mass splitting among an  $SU(2)_L$  multiplet, leaving the neutral component as the lightest one. As a result, the charged components of a multiplet, if produced, eventually decay into the neutral component. However, the mass splitting is so small in many cases that the typical flight length of the charged components is comparable to the detector size. Such long-lived charged particles, which travel for a few cm and then decay into an invisible counterpart, can be detected as charged tracks disappearing in the middle. They are very characteristic signals and can be used as the most efficient discriminator between the SM background and the WIMP signals. In this section, we will study what we have summarized above in more detail.

### Lifetime of charged components

The small mass splitting among a WIMP multiplet allows the heavier charged component to decay into the neutral component and SM particles via an off-shell  $W$  boson. Depending on the size of the relevant mass difference  $\Delta m$ , several channels contribute to the decay [119]. For tiny  $\Delta m < m_\pi$  with  $m_\pi$  being the charged pion mass,  $\chi^\pm \rightarrow \ell^\pm \nu_\ell \chi^0$  ( $\ell = e, \mu$ ) are the unique decay modes. Once  $\Delta m$  exceeds  $m_\pi$ , the mode  $\chi^\pm \rightarrow \pi^\pm \chi^0$  opens up and becomes the dominant one. After  $\Delta m \gtrsim 1$  GeV, final states with two and three pions start to give a sizable contribution, and the total decay rate asymptotes to that for  $\chi^\pm \rightarrow q' \bar{q} \chi^0$ . For a larger mass splitting, the mode  $\chi^\pm \rightarrow \tau^\pm \nu_\tau \chi^0$  may also be allowed. As a whole, these decay modes determine the lifetime of a charged component of a WIMP, which is typically long enough to be probed by experiments thanks to the small mass difference.

Let  $\tau$  be the lifetime of the (singly) charged component of a WIMP, defined using the total decay rate  $\Gamma$  as  $\tau \equiv 1/\Gamma$ . Taking into account that a WIMP, if produced at colliders with sufficiently high energy, has a velocity comparable to the speed of light  $c$ ,  $c\tau$  expresses a rough

estimation of its flight length inside detectors. For Higgsino with  $m_\pi < \Delta m \lesssim 1 \text{ GeV}$ ,<sup>‡14</sup> we can estimate [119, 120]

$$c\tau \simeq 0.7 \text{ cm} \left[ \left( \frac{\Delta m_+}{340 \text{ MeV}} \right)^3 \sqrt{1 - \frac{m_\pi^2}{\Delta m_+^2}} \right]^{-1}, \quad (4.1)$$

where  $\Delta m_+ \equiv \Delta m_+^{\text{tree}} + \Delta m_+^{\text{rad}}$  with using Eqs. (2.4) and (2.5). Since the mass difference for Wino is a factor two smaller than Higgsino, we obtain a much longer flight length

$$c\tau \simeq 3.1 \text{ cm} \left[ \left( \frac{\Delta m}{165 \text{ MeV}} \right)^3 \sqrt{1 - \frac{m_\pi^2}{\Delta m^2}} \right]^{-1}, \quad (4.2)$$

which gives  $c\tau \simeq 5.8 \text{ cm}$  for  $\Delta m = 165 \text{ MeV}$ . The same calculation applies to the fermionic MDMs with  $n \geq 5$  and  $\Delta m = 166 \text{ MeV}$ , resulting in somewhat shorter flight length that scales as  $c\tau \sim 44 \text{ cm}/(n^2 - 1)$  [83] due to the stronger interaction with  $W$  bosons.

**(♣ Scalar MDM ♣)**

### Disappearing track signal

Once a long-lived charged component of WIMP is produced, it is detected by the trackers installed in the innermost part of the detectors for the case of ATLAS and CMS collaborations at the LHC. For example, in the ATLAS setup, several tracking detectors are equipped cylindrically around the beamline from the radius  $r = 3 \text{ cm}$  to  $108 \text{ cm}$ . The pixel detector spans the radius from  $3 \text{ cm}$  to  $12 \text{ cm}$ , the strip semiconductor tracker (SCT) from  $30 \text{ cm}$  to  $52 \text{ cm}$ , and the transition radiation tracker from  $56 \text{ cm}$  to  $108 \text{ cm}$ . In particular, the pixel detector is the most important for our discussion, which is composed of four layers, with the innermost one being the recently equipped so-called the insertable B-layer [121–123]. To detect the charged track signal of a long-lived WIMP with the typical flight length of  $\mathcal{O}(1) \text{ cm}$ , they require the hit at every layer of the pixel detector and apply the SCT veto to search for the track signal disappearing in between  $12 \text{ cm} < r < 30 \text{ cm}$ . As for the fake events within the SM, the SCT veto denies the possibility for a stable SM particle to mimic the signal. However, there are two important sources of the fake track generated by hadrons/electrons and the so-called pile-up.

The first possibility with hadrons/electrons is a physical background caused by the interaction of hadrons with detector material or by the hard photon emission of electrons. After these interactions, the orbit of a hadron/electron is bent and, if this secondary interaction occurs in between  $12 \text{ cm} < r < 30 \text{ cm}$ , two tracks in the pixel detector and the SCT are not

<sup>‡14</sup>We are not interested in Higgsino with  $\Delta m \gtrsim 1 \text{ GeV}$  here since the corresponding flight length will be much shorter than  $\mathcal{O}(1) \text{ cm}$ , which is the scale of the detectors.

identified with each other. As a result, the first track in the pixel detector seems to disappear in the middle, which mimics the true WIMP signals. In the LHC, this type of background dominates and generates  $\mathcal{O}(10\text{--}100)$  fake events for  $\sqrt{s} = 13\text{ TeV}$ ,  $\mathcal{L} = 36.1\text{ fb}^{-1}$  (see Fig. 7 of [31]).

On the other hand, for future hadron colliders, the second possibility of the fake track from the pile-up may be more important. In hadron colliders, a bunch of protons is accelerated at the same time and two bunches “collide” with each other with some given frequency. Since there are many protons inside a bunch, typically more than one collisions of two protons occur for each bunch crossing. The average number of collisions per bunch crossing is often denoted as  $\langle\mu\rangle$  and the values of  $\langle\mu\rangle \sim 20, 80$ , and  $200$  are expected for LHC Run-2, Run-3, and HL-LHC. With this large number of collisions, there are a lot of collision products detected almost at the same time, which makes the signal significantly messy. Then, among a huge number of hits on tracking detectors, several of them occasionally form a straight line in position and time, which is sometimes called the fake track. Since this track is only a fake, it can easily pass the SCT veto and mimic the disappearing track signal of WIMPs. In the real experiment, the rate for fake track reduces as we require more hits on trackers. See the results reviewed below for a concrete estimation of the fake track rate at the FCC-hh.

From now on, we estimate how many events are expected at the FCC-hh. Recalling that the detectors are installed in a cylindrical geometry, the transverse distance  $d_T$  of the charged WIMP flight measured from the beamline plays an important role. We can estimate the probability for  $d_T$  to be larger than  $d$  as

$$P(d_T > d) = \exp\left(-\frac{d}{\beta\gamma c\tau \sin\theta}\right), \quad (4.3)$$

where  $\beta$  is the WIMP velocity,  $\gamma \equiv (1 - \beta^2)^{-1/2}$ , and  $\theta$  is the angle between the WIMP momentum and the beamline. One of the implications of the above expression is that WIMPs with large transverse momentum have a larger possibility to reach outer layers of the pixel detector. This enlarges the importance of considering the NLO (and higher-order) QCD processes with real emissions for the pair production. Due to the hard emission of the gluon, the produced pair of WIMPs recoil in the opposite direction, and WIMPs tend to have larger transverse momentum than the case without gluon emission. It can be directly checked that, for  $\sqrt{s} = 100\text{ TeV}$ , even the two-gluon emission process possesses non-negligible contribution to the simulation of the disappearing track search for WIMPs.

In Fig. 8, we show the distribution of  $P(d_T > 15\text{ cm})$ , which is motivated by the FCC-hh detector setup assumed below, for the 2.9 TeV Wino,  $\sqrt{s} = 100\text{ TeV}$ , and  $\mathcal{L} = 30\text{ ab}^{-1}$ . Here, we only consider the WIMP pair production process with up to one gluon emission as an example. Note that  $\tau \simeq 5.8\text{ cm}$  and  $\exp(-15\text{ cm}/\tau) \sim 7.5 \times 10^{-2}$  for this setup. We can see that the effect of the large Lorentz boost  $\beta\gamma \gg 1$  pushes the probability to  $P \gtrsim \mathcal{O}(10^{-1})$  for

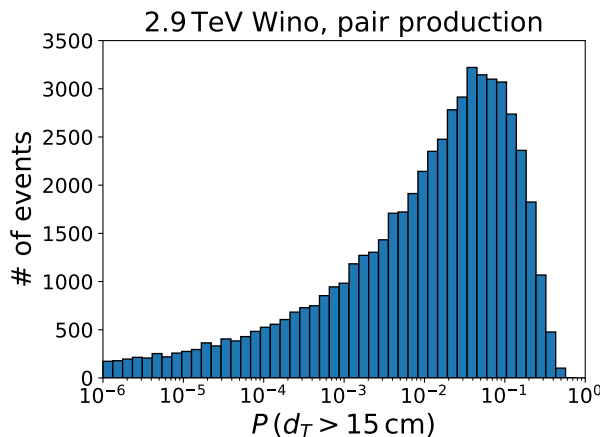


Figure 8: Distribution of the survival probability  $P(d_T > 15 \text{ cm})$  for 2.9 TeV Wino. The pair production process at  $\sqrt{s} = 100 \text{ TeV}$  and  $\mathcal{L} = 30 \text{ ab}^{-1}$  is assumed.

some Winos, while the angular distribution of Winos makes a wide tail of the distribution at  $P \lesssim \mathcal{O}(10^{-2})$  when  $\sin \theta \sim 0$ . By summing the shown probabilities for all produced Winos, we can obtain the expectation value  $N_{15}$  for the number of Winos with  $d_T > 15 \text{ cm}$ . We find  $N_{15} \sim 2400$ ,<sup>†15</sup> to which a lot of Winos with  $P \gtrsim \mathcal{O}(10^{-1})$  significantly contribute. Thus, we infer that we can detect the Wino signal if we can suppress the number of background events to  $\lesssim \mathcal{O}(10^5)$ . In the next subsection, we will see that this may be the case for the FCC-hh and the parameter space for the Wino DM candidate can fully be covered.

In Fig. 9, we show the distribution of the Wino velocity  $\beta$  for the same process. The blue histogram shows the distribution of all Winos, while the orange one shows that of Winos with  $d_T > 15 \text{ cm}$ , picked up randomly according to the survival probability Eq. (4.3). As already seen in Fig. 7, the center of mass energy of the two-Wino system distributes from a few to  $\mathcal{O}(10) \text{ TeV}$ , and many Winos are highly boosted with  $\beta \sim 1$ . Since a charged Wino tends to survive for a longer distance when it is more accelerated, some of the boosted Winos  $\beta \gtrsim 0.6$  satisfy the requirement  $d_T > 15 \text{ cm}$ .

### Current constraints and future prospects

So far, the disappearing track search is performed by both ATLAS [31] and CMS [33] collaborations. Below, we will focus particularly on the ATLAS collaboration and discuss current constraints.

<sup>†15</sup>In the real analysis, it may also be important to put a cut on the missing transverse energy  $\cancel{E}_T$  to further reduce the number of background. If we require  $\cancel{E}_T > 1 \text{ TeV}$  as [118], we expect smaller number of Winos  $N_{15} \sim 600$ .



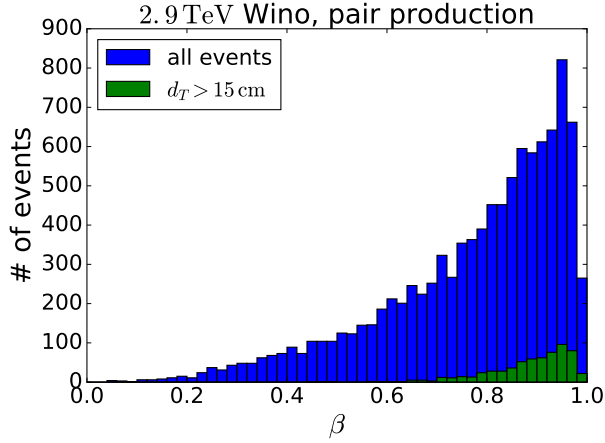


Figure 9: Distribution of the Wino velocity  $\beta$  for 2.9 TeV Wino. The pair production process at  $\sqrt{s} = 100$  TeV and  $\mathcal{L} = 30 \text{ ab}^{-1}$  is assumed.

WIMP	pure Higgsino	Wino	5-plet fermion
Upper bound on $m_\chi$	120 GeV	460 GeV	260 GeV

Table 9: Current upper bound for WIMP masses obtained from the disappearing track search shown in Fig. 10.

In Fig. 10, we show the result of the disappearing track search taken from [31]. As for the production process, only the pair production via an electroweak gauge boson is considered. The yellow band shows the current constraint on the WIMP mass and lifetime plane and the left part of the band is already excluded. The sensitivity becomes weak when we consider  $\tau \gtrsim 1 \text{ ns}$  or  $c\tau \gtrsim 30 \text{ cm}$  due to the requirement of the SCT veto. In the figure, the lifetime of Wino as a function of its mass is also shown by the black dot-dashed line. It can be seen that the current constraint on Wino mass is  $m_\chi \lesssim 460 \text{ GeV}$ .

Using the lifetime evaluated in the previous subsection, we summarize the current status for several WIMPs in Table 9, which exhibits upper limits of  $\mathcal{O}(100) \text{ GeV}$ . However, note that the bound for the Higgsino listed in the table neglects the mixing between Higgsino and gauginos. Actually,  $\Delta m_+$  and thus  $\tau$  are sensitive to the mixing, and an order estimation shows that the mixing lowers the lifetime to be  $\tau \lesssim 0.01 \text{ ns}$  and spoils the bound for Higgsino when  $M_1, M_2 \lesssim 100 \text{ TeV}$  without any non-trivial cancellation in Eq. (2.4).

The analysis of the disappearing track search at future hadron colliders is performed in [48, 124]. Since the detector setup for future colliders such as the FCC-hh is undetermined yet, in [124], the authors assume several setups and compare the result. In each setup, five layers of the pixel detector are installed and the fifth layer position (which we call  $r_5$ )

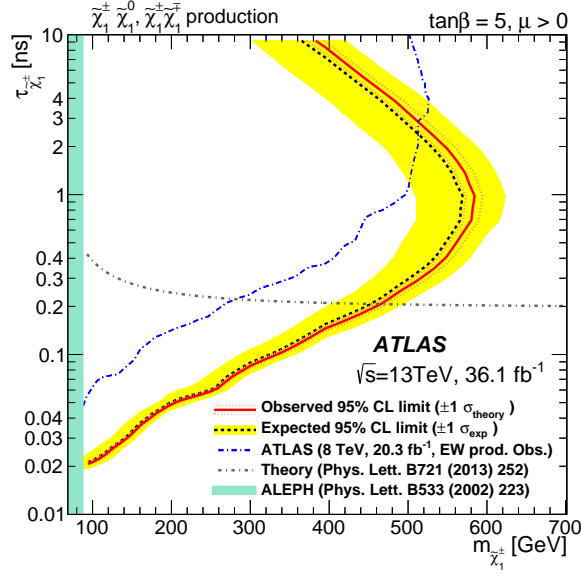


Figure 10: Current status of the disappearing track search using the pair production process via an electroweak gauge boson. The figure is taken from [31].

Detector setup	pure Higgsino	Wino
$r_5 = 15$ cm	0.9–1.2 TeV	> 4.0 TeV
$r_5 = 27$ cm	< 0.7 TeV	2.9–4.0 TeV

Table 10: Prospects of  $5\sigma$  discovery reach at FCC-hh with  $\mathcal{L} = 30 \text{ ab}^{-1}$  using the pair production process via an electroweak gauge boson. The results are based on [124].

ranges from 15 cm to 27 cm.<sup>h16</sup> For the background reduction, hits to all of the five layers are required. By varying the average number of  $pp$  interactions per bunch crossing from  $\langle\mu\rangle = 200$  to 500, the fake background rate is estimated to range from  $10^{-7}$  to  $10^{-5}$ .

In Table 10, we summarize the obtained  $5\sigma$  discovery reach for pure Higgsino and Wino for two detector setups with the integrated luminosity  $\mathcal{L} = 30 \text{ ab}^{-1}$ , again using the pair production process via an electroweak gauge boson. The uncertainty of the reach corresponds to the variation of  $\langle\mu\rangle = 200$ –500 and the uncertainty in soft QCD processes. Recalling the discussion in Sec. (♣ ??? ♣), Table 10 shows that the FCC-hh can cover the whole region of the parameter space consistent with Wino DM  $m_\chi \lesssim 2.9 \text{ TeV}$ . On the other hand, there is a sensitivity up to the mass of the thermal Higgsino DM  $m_\chi \sim 1.1 \text{ TeV}$  only when we adopt

<sup>h16</sup>For simplicity of the discussion, we just assume that the detectors outside the pixel detector are far apart from the beamline so that all the WIMPs decay before reaching them. Then, we can estimate the discovery reach by counting the number of WIMP signals that reach the fifth layer of the pixel detector.

the most optimistic assumption, *i.e.*, the pure Higgsino with small  $\Delta m_+$  searched for with  $r_5 = 15$  cm. Thus, it is an important task to consider another way of search for Higgsino, in particular, a way that is unaffected by the mass splitting  $\Delta m_+$ . The authors do not give any comment on the MDM search, but we can give some very rough estimates of the reach from Table 10. For example, considering the 5-plet fermion with  $c\tau \sim 1.8$  cm, the size of the significance of the signal should be in between that for Higgsino and Wino assuming the same production cross section, while the cross section scales as  $n^3$  as a function of the  $SU(2)_L$  charge as we have seen so far. Thus, the reach for the 5-plet fermion should be a few TeV, which covers a non-negligible fraction of the parameter space viable as a DM candidate. (

### 4.3 Soft lepton search

(clubsuit If possible clubsuit)

### 4.4 Mono-jet search

(clubsuit For Higgsino search, cite clubsuit) [35].

## Section 5

# Indirect search of WIMPs using Drell-Yan process

### (♣ Histogram of lepton invariant mass? ♣)

So far, we have argued several ways to search for WIMPs using DM searches and collider experiments. We have seen that, while WIMPs with relatively large  $SU(2)_L$  charges such as Wino and the 5-plet fermion are promising for these searches, Higgsino is typically more challenging to probe. Given this situation, another search strategy attracts a lot of attention [1, 2, 36–40, 125, 126] that probes WIMPs via the electroweak precision measurement at colliders. It utilizes a pair production of charged leptons or that of a charged lepton and a neutrino, where WIMPs affect the pair production processes through the vacuum polarizations of the electroweak gauge bosons as shown in Fig. 11. It is an indirect search method in the sense that it does not produce on-shell WIMPs as final states. A virtue of this method is that it is robust against the change of the lifetime and the decay modes of WIMPs and whether a WIMP constitutes a sizable portion of the DM or not. Another important point is that, due to WIMPs, the invariant mass distributions of the final state particles show sharp dip-like behavior at the invariant mass close to twice the WIMP mass. It helps us to distinguish the WIMP effects from backgrounds and systematic errors.

In this section, we pursue this indirect search method further. In particular, we study the prospect of the indirect search method at future 100 TeV hadron colliders such as FCC-hh [41–43, 109] and SppC [44, 45]. We concentrate on the Drell-Yan processes that have

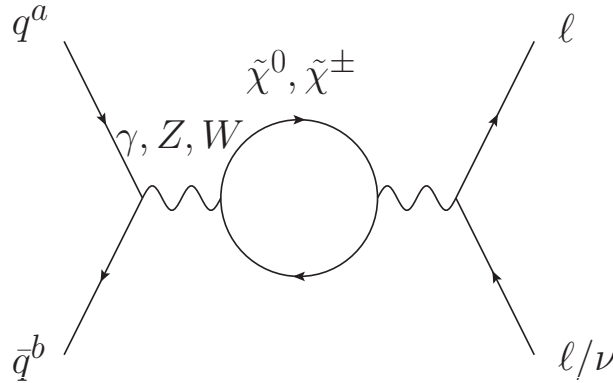


Figure 11: WIMP effect on the Drell-Yan processes considered in this section. (♣ Correct the figure to  $q_\alpha q_\beta \rightarrow \dots$ . ♣)

two charged leptons or mono-lepton plus a neutrino in the final state since they provide a very clean signal without any hadronic jets at least from the final state particles. We will show that it provides *a comparable or better experimental reach for Higgsino* compared to the direct production search of WIMPs at future colliders [46–49]. Besides, we demonstrate that the indirect search method can be applied not only to discover WIMPs but also *to investigate their properties, such as charges, masses, and spins*. To this end, it is important to consider both the charged current (CC) process with two-lepton final state and the neutral current (NC) process with mono-lepton final state to break some degeneracy among different WIMP charge assignments; the NC and CC processes depend on different combinations of the  $SU(2)_L$  and  $U(1)_Y$  charges of WIMP, and hence the inclusion of both processes allows us to extract these charges separately.

This section is based on our works [1, 2].

## 5.1 WIMP effect on the Drell-Yan processes

We investigate contributions of the WIMPs to the Drell-Yan processes through the vacuum polarization of the electroweak gauge bosons at the loop level. Throughout this section, we assume that all the other beyond the SM particles are heavy enough so that they do not affect the following discussion. After integrating out the WIMPs, the effective lagrangian is expressed as

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + C_2 g^2 W_{\mu\nu}^a f \left( -\frac{D^2}{m^2} \right) W^{a\mu\nu} + C_1 g'^2 B_{\mu\nu} f \left( -\frac{\partial^2}{m^2} \right) B^{\mu\nu}, \quad (5.1)$$

where  $\mathcal{L}_{\text{SM}}$  is the SM Lagrangian,  $D$  is a covariant derivative,  $m$  is the WIMP mass,<sup>‡17</sup>  $g$  and  $g'$  are the  $SU(2)_L$  and  $U(1)_Y$  gauge coupling constants, and  $W_{\mu\nu}^a$  and  $B_{\mu\nu}$  are the field strength associated with the  $SU(2)_L$  and  $U(1)_Y$  gauge group, respectively. The function  $f(x)$  is defined as<sup>‡18</sup>

$$f(x) = \begin{cases} \frac{1}{16\pi^2} \int_0^1 dy y(1-y) \ln(1 - y(1-y)x - i0) & \text{(Fermion),} \\ \frac{1}{16\pi^2} \int_0^1 dy (1-2y)^2 \ln(1 - y(1-y)x - i0) & \text{(Scalar),} \end{cases} \quad (5.2)$$

<sup>‡17</sup>Here we neglect a small mass splitting among the  $SU(2)_L$  multiplet.

<sup>‡18</sup>If a WIMP interacts only through the electroweak interaction, its decay width is of  $O(1)\%$  or less of its mass even if it is unstable. We assume that this is the case, and neglect the small effect on the function  $f(x)$  due to the small decay width. Also,  $f(x)$  corresponds to the finite part of the WIMP loop contribution after performing the renormalization in the  $\overline{\text{MS}}$  scheme.

Fermion $f$	$v_f^{(\gamma)}$	$a_f^{(\gamma)}$	$v_f^{(Z)}$	$a_f^{(Z)}$	$v_f^{(W)}$	$a_f^{(W)}$
up-type quark	$\frac{2}{3}e$	0	$(\frac{1}{4} - \frac{2}{3}s_W^2)g_Z$	$-\frac{1}{4}g_Z$	$\frac{1}{2\sqrt{2}}g$	$-\frac{1}{2\sqrt{2}}g$
down-type quark	$-\frac{1}{3}e$	0	$(-\frac{1}{4} + \frac{1}{3}s_W^2)g_Z$	$\frac{1}{4}g_Z$	$\frac{1}{2\sqrt{2}}g$	$-\frac{1}{2\sqrt{2}}g$
lepton	$-e$	0	$(-\frac{1}{4} + s_W^2)g_Z$	$\frac{1}{4}g_Z$	$\frac{1}{2\sqrt{2}}g$	$-\frac{1}{2\sqrt{2}}g$

Table 11: Coefficients of the weak interaction defined as  $\Gamma_f^{(V)} \equiv v_f^{(V)} + a_f^{(V)}\gamma_5$ . Here,  $e = g_{SW}$  and  $g_Z = g/c_W$ , where  $s_W \equiv \sin \theta_W$  and  $c_W \equiv \cos \theta_W$  with  $\theta_W$  being the weak mixing angle.

where the first (second) line corresponds to a fermionic (scalar) WIMP, respectively. The coefficients  $C_1$  and  $C_2$  for an  $SU(2)_L$   $n$ -plet WIMP with hypercharge  $Y$  are given by

$$C_1 = \frac{\kappa}{8}nY^2, \quad (5.3)$$

$$C_2 = \frac{\kappa}{8}I(n), \quad (5.4)$$

where  $\kappa = 1, 2, 8, 16$  for a real scalar, a complex scalar, a Weyl or Majorana fermion, and a Dirac fermion, respectively.  $I(n)$  is the Dynkin index for the  $n$  dimensional representation of  $SU(2)_L$  defined in Eq. (??). The coefficients are uniquely determined by the representation of the WIMPs. For example,  $(C_1, C_2) = (1, 1)$  for Higgsino, and  $(C_1, C_2) = (0, 2)$  for Wino. We emphasize that, contrary to the usual effective field theory, our prescription is equally applied when the typical scale of the gauge boson four-momentum  $q$  is larger than the WIMP mass scale  $m$  since we do not perform a derivative expansion of  $f$  in Eq. (5.1). It is important because, as we see soon, the effect of the WIMPs is maximized when  $\sqrt{q^2} \sim m$ , where the derivative expansion is not applicable.

At the leading order (LO), we are interested in  $u(p) \bar{u}(p') \rightarrow \ell^-(k) \ell^+(k')$  and  $d(p) \bar{d}(p') \rightarrow \ell^-(k) \ell^+(k')$  as the NC processes and  $u(p) \bar{d}(p') \rightarrow \nu(k) \ell^+(k')$  and  $d(p) \bar{u}(p') \rightarrow \ell^-(k) \bar{\nu}(k')$  as the CC processes. Here,  $u$  and  $d$  collectively denote up-type and down-type quarks, respectively, and  $p, p', k$ , and  $k'$  are initial and final state momenta. In the SM, the amplitudes for both the NC and CC processes at the LO are expressed as

$$\mathcal{M}_{\text{SM}} = \sum_V \frac{\left[ \bar{v}(p') \gamma^\mu \Gamma_q^{(V)} u(p) \right] \left[ \bar{u}(k) \gamma_\mu \Gamma_\ell^{(V)} v(k') \right]}{s' - m_V^2}, \quad (5.5)$$

where  $\sqrt{s'}$  is the invariant mass of the final state leptons, which is denoted as  $m_{\ell\ell}$  for the NC processes and  $m_{\ell\nu}$  for the CC processes. The relevant gauge bosons are  $V = \gamma, Z$  for the NC processes and  $V = W^\pm$  for the CC processes, with  $m_V$  being the corresponding gauge boson mass. In addition,

$$\Gamma_f^{(V)} \equiv v_f^{(V)} + a_f^{(V)}\gamma_5, \quad (5.6)$$

with  $v_f^{(V)}$  and  $a_f^{(V)}$  given in Tab. 11. The WIMP contribution is given by

$$\mathcal{M}_{\text{WIMP}} = \sum_{V, V'} C_{VV'} s' f\left(\frac{s'}{m^2}\right) \frac{\left[\bar{v}(p') \gamma^\mu \Gamma_q^{(V)} u(p)\right] \left[\bar{u}(k) \gamma_\mu \Gamma_\ell^{(V')} v(k')\right]}{(s' - m_V^2)(s' - m_{V'}^2)}, \quad (5.7)$$

where  $C_{\gamma\gamma} = 4(C_1 g'^2 c_W^2 + C_2 g^2 s_W^2)$ ,  $C_{\gamma Z} = C_{Z\gamma} = 4(C_2 g^2 - C_1 g'^2) s_W c_W$ ,  $C_{ZZ} = 4(C_1 g'^2 s_W^2 + C_2 g^2 c_W^2)$ , and  $C_{WW} = 4C_2 g^2$ . Again  $V, V' = \gamma, Z$  for the NC processes and  $V, V' = W^\pm$  for the CC processes.

We use  $d\Pi_{\text{LIPS}}$  for a Lorentz invariant phase space factor for the two particles final state. Then, using Eqs. (5.5) and (5.7), we define

$$\frac{d\sigma_{\text{SM}}}{d\sqrt{s'}} = \sum_{\alpha, \beta} \frac{dL_{\alpha\beta}}{d\sqrt{s'}} \int d\Pi_{\text{LIPS}} |\mathcal{M}_{\text{SM}}(q_\alpha q_\beta \rightarrow \ell\ell/\ell\nu)|^2, \quad (5.8)$$

$$\frac{d\sigma_{\text{WIMP}}}{d\sqrt{s'}} = \sum_{\alpha, \beta} \frac{dL_{\alpha\beta}}{d\sqrt{s'}} \int d\Pi_{\text{LIPS}} 2\Re[\mathcal{M}_{\text{SM}} \mathcal{M}_{\text{WIMP}}^*(q_\alpha q_\beta \rightarrow \ell\ell/\ell\nu)], \quad (5.9)$$

where we take the average and summation over spins. Here,  $dL_{\alpha\beta}/d\sqrt{s'}$  is the so-called luminosity function for a fixed  $\sqrt{s'}$ :

$$\frac{dL_{\alpha\beta}}{d\sqrt{s'}} \equiv \frac{1}{s} \int_0^1 dx_1 dx_2 f_\alpha(x_1) f_\beta(x_2) \delta\left(\frac{s'}{s} - x_1 x_2\right), \quad (5.10)$$

where  $\alpha$  and  $\beta$  denote species of initial partons,  $\sqrt{s} = 100$  TeV, and  $f_a(x)$  is the PDF used in Sec. 4.1. Eq. (5.8) represents the SM cross section, while Eq. (5.9) the WIMP contribution to the cross section. For the statistical treatment in the next section, we introduce a parameter  $\mu$  that parametrizes the strength of the WIMP effect, and express the cross section with  $\mu$  as

$$\frac{d\tilde{\sigma}}{d\sqrt{s'}} = \frac{d\sigma_{\text{SM}}}{d\sqrt{s'}} + \mu \frac{d\sigma_{\text{WIMP}}}{d\sqrt{s'}}. \quad (5.11)$$

Obviously,  $\mu = 0$  corresponds to the pure SM, while  $\mu = 1$  corresponds to the SM+WIMP model. Hereafter, we use

$$\delta_\sigma(\sqrt{s'}) \equiv \frac{d\sigma_{\text{WIMP}}/d\sqrt{s'}}{d\sigma_{\text{SM}}/d\sqrt{s'}}, \quad (5.12)$$

to denote the correction from the WIMP. Note that this ratio remains unchanged even if we take into account the next-to-leading order (NLO) QCD effect because the EWIMPs affect the cross sections only through the vacuum polarization.<sup>†19</sup>

<sup>†19</sup>When the NLO QCD effect is included, one of the initial partons can be gluon with the real emission of one jet in the final state. However, we can easily see that  $\delta_\sigma^{ug} = \delta_\sigma^{uu}$  and so on.

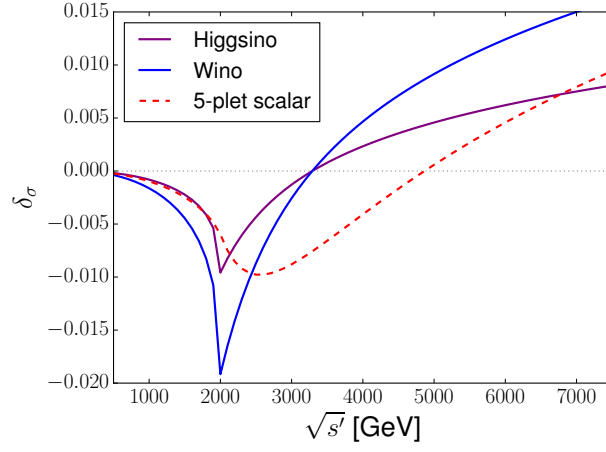


Figure 12:  $\delta_\sigma$  for the CC processes as a function of  $\sqrt{s'} = m_{\ell\nu}$ . The purple, blue, and red lines correspond to Higgsino, Wino, and 5-plet real scalar, respectively.

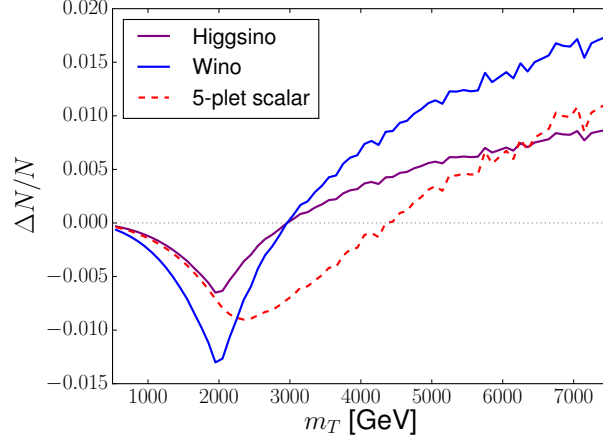


Figure 13: The WIMP effect on the ratio of the number of events  $\Delta N/N$  as a function of  $m_T$ . The line colors are the same as Fig. 12.

In Fig. 12, we plot  $\delta_\sigma$  for the CC processes as a function of  $\sqrt{s'}$ . The purple, blue, and red lines correspond to Higgsino, Wino, and 5-plet scalar, respectively. There is a dip around  $\sqrt{s'} = 2m$  for all the cases of the WIMPs which originates from the loop function  $f$  in Eq. (5.2). The WIMP contributions to the NC processes show a similar dip structure that again comes from  $f$ . This dip is crucial not only for the discovery of the WIMP signal (see Sec. 5.2.3) but also for the determination of the properties of the WIMPs (see Sec. 5.2.4). In particular, the WIMP mass can be extracted from the dip position, while the WIMP charges ( $n$  and  $Y$ ) can be determined from the depth of the dip.



For the NC processes, the momenta of two final state charged leptons are measurable and we can use the invariant mass distribution of the number of events for the study of the WIMPs. For the CC processes, on the contrary, we cannot measure the momentum of the neutrino in real experiments, and hence we instead use the missing transverse momentum  $\cancel{p}_T$ . We use the transverse mass defined as

$$m_T^2 \equiv 2p_{T,\ell}\cancel{p}_T(1 - \cos\phi), \quad (5.13)$$

where  $p_{T,\ell}$  denotes the transverse momentum of the charged lepton and  $\phi$  is the difference between the azimuth angles of  $p_{T,\ell}$  and  $\cancel{p}_T$ . The important property of  $m_T$  is that the distribution of  $m_T$  peaks at  $m_T = m_{\ell\nu}$  (see Appendix. C for more detailed description of the quantity  $m_T$ ). Because of this property, the characteristic shape of  $\delta_\sigma$  remains in the  $m_T$  distribution in the CC events. To see this, we plot in Fig. 13 the WIMP effect on the number of events as a function of  $m_T$ . Here, the vertical axis is the ratio of the WIMP correction to the number of events  $\Delta N$  to the number of events in the SM  $N$  for each bin with the bin width of 100 GeV.<sup>‡20</sup> We find that the dip structure remains in the  $m_T$  distribution, though the depth of the dip is smaller compared to the  $m_{\ell\nu}$  distribution.

## 5.2 Analysis

(♣ Some comment on lepton mis-tagging? ♣)

### 5.2.1 Event generation

Now we discuss how well we can extract information about WIMPs from the invariant mass and transverse mass distributions for the processes of our concern at future 100 TeV  $pp$  collider experiments. We take into account the effects of the next-to-leading order QCD corrections in the events as well as detector effects through Monte-Carlo simulations.

In our analysis, we first generate the SM event sets for the NC processes  $pp \rightarrow e^-e^+/\mu^-\mu^+$  and for the CC processes  $pp \rightarrow e^\pm\nu_e/\mu^\pm\nu_\mu$ . We use `MadGraph5_aMC@NLO` (v2.6.3.2) [112, 113] for the event generation with the successive use of `Pythia8` [114] for the parton shower and the hadronization and `Delphes` (v3.4.1) [115] with the card `FCChh.tcl` for the detector simulation. We use `NNPDF2.3QED` with  $\alpha_s(M_Z) = 0.118$  [117] as a canonical set of PDFs. For the renormalization and factorization scales, we use the default values of `MadGraph5_aMC@NLO`, i.e., the central  $m_T^2$  scale after  $k_T$ -clustering of the event (which we denote by  $Q$ ). We take into account the NLO QCD effect by the [QCD] option of `MadGraph5_aMC@NLO` since

<sup>‡20</sup>Just for an illustrative purpose, we generate events corresponding to the integrated luminosity  $\mathcal{L} = 1 \text{ ab}^{-1}$  for this figure, which is not the same luminosity as we use in the next section (see Sec. 5.2.1 for details of the event generation).

it enhances the cross section roughly by a factor of 2 compared to the LO calculation.<sup>‡21</sup> The events are binned by the characteristic mass  $m_{\text{char}}$  for each process: we use the lepton invariant mass  $m_{\text{char}} = m_{\ell\ell}$  for the NC processes, and the transverse mass  $m_{\text{char}} = m_T$  for the CC processes, respectively. In both cases, we generated events with the characteristic mass within the range of  $500 \text{ GeV} < m_{\text{char}} < 7.5 \text{ TeV}$  and divide them into 70 bins with the equal width of 100 GeV.

As for the event selection by a trigger, we may have to impose some cut on the lepton transverse momentum  $p_T$ . As we will see, we concentrate on events with high  $p_T$  charged lepton(s) with which we expect the event may be triggered. For the NC processes, we use events with at least two high  $p_T$  leptons. For our analysis, we use events with  $m_{\ell\ell} > 500 \text{ GeV}$ ; we assume that such events are triggered by using two energetic charged leptons so that we do not impose extra kinematical requirements. On the contrary, the CC events are characterized only by a lepton and a missing transverse momentum. For such events, we require that the  $p_T$  of the charged lepton should be larger than 500 GeV.<sup>‡22</sup> For the CC events, the cut reduces the number of events in particular for the bins with the low transverse mass  $m_T \sim 500 \text{ GeV}$ , and thus affects the sensitivity of the CC processes to relatively light WIMPs. We will come back to this point later.

The WIMP effect is incorporated by rescaling the SM event by  $\delta_\sigma$  defined in Eq. (5.12). With the parameter  $\mu$  defined in Eq. (5.11), the number of events corresponding to the SM+WIMP hypothesis in  $i$ -th bin, characterized by  $m_{i,\min} < m_{\text{char}} < m_{i,\max}$ , is

$$x_{f,i}(\mu) = \sum_{m_{i,\min} < m_{\text{char}} < m_{i,\max}} \left[ 1 + \mu \delta_\sigma(\sqrt{s'}) \right], \quad (5.1)$$

where the sum runs over all the events of the final state  $f$  whose characteristic mass  $m_{\text{char}}$  (after taking into account the detector effects) falls into the bin. Note that the true value of  $\sqrt{s'}$  should be used for each event for the computation of  $\delta_\sigma$ : we extract it from the hard process information.<sup>‡23</sup>

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<sup>‡21</sup>This large enhancement implies that the next-to-next-to-leading order QCD effect may also have a non-negligible effect on the cross section, and its calculation remains as a future task. However, due to its smooth dependence on  $\sqrt{s'}$ , it may not much affect the detection reach of the EWIMPs. See Sec. 5.2.2 for the details.

<sup>‡22</sup>In the ATLAS analysis of the mono-lepton signal during the 2015 (2016) data taking period [127], they use the event selection condition  $p_T > 24$  (60) GeV for leptons that satisfy the *medium* identification criteria. In the CMS analysis during the period on 2016 [128], they use the condition  $p_T > 130$ (53) GeV for an electron (a muon).

<sup>‡23</sup>The  $p_T$  cut for the CC process does not affect this estimation since the WIMP does not modify the angular distribution of the final lepton and neutrino for the CC process.

### 5.2.2 Statistical treatment

We now explain the statistical method we will adopt in our analysis. Throughout this section, we rely on the so-called profile likelihood method, which is described in detail in Appendix D. We collectively denote our theoretical model as  $\mathbf{x}_f(\mu) = \{x_{f,i}(\mu)\}$ , where  $x_{f,i}(\mu)$  is given by Eq. (5.1). We denote the experimental data set as  $\tilde{\mathbf{x}}_f$  that in principle is completely unrelated to our theoretical model  $\mathbf{x}_f(\mu)$ . Since we do not have an actual experimental data set for 100 TeV colliders for now, however, we take  $\tilde{\mathbf{x}}_f = \mathbf{x}_f(\mu = 1)$  (for some fixed values of the WIMP mass and charges) throughout our analysis, assuming that the WIMP does exist. In particular, this choice tests the SM-only hypothesis if we take our theoretical model as  $\mathbf{x}_f(\mu = 0)$ .

If the expectation values of  $x_{f,i}(\mu)$  are precisely known, the sensitivity to WIMPs can be studied only with statistical errors. In reality, however, the computation of  $x_{f,i}(\mu)$  suffers various sources of uncertainties, which results in systematic errors in our theoretical model. The sources include errors in the integrated luminosity, the beam energy, choices of the renormalization and the factorization scales, choices of PDF, the pile-up effect, higher order corrections to the cross section, and so on. In order to deal with these uncertainties, we introduce sets of free parameters  $\boldsymbol{\theta}_f = \{\theta_{f,\alpha}\}$  (i.e. nuisance parameters) which absorb (smooth) uncertainties of the number of events, and modify our theoretical model as

$$\tilde{x}_{f,i}(\boldsymbol{\theta}_f, \mu) \equiv x_{f,i}(\mu) f_{\text{sys},i}(\boldsymbol{\theta}_f), \quad (5.2)$$

where  $f_{\text{sys},i}(\boldsymbol{\theta}_f)$  is a function that satisfies  $f_{\text{sys},i}(\mathbf{0}) = 1$ . We expect that, if the function  $f_{\text{sys},i}$  is properly chosen, the true distribution of the number of events in the SM is given by  $\tilde{\mathbf{x}}_f(\boldsymbol{\theta}_f, 0) = \{\tilde{x}_{f,i}(0) f_{\text{sys},i}(\boldsymbol{\theta}_f)\}$  for some value of  $\boldsymbol{\theta}_f$ . In our analysis, we adopt the five parameters fitting function given by [129]

$$f_{\text{sys},i}(\boldsymbol{\theta}_f) = e^{\theta_{f,1}} (1 - p_i)^{\theta_{f,2}} p_i^{(\theta_{f,3} + \theta_{f,4} \ln p_i + \theta_{f,5} \ln^2 p_i)}, \quad (5.3)$$

where  $p_i = 2m_i/\sqrt{s}$  with  $m_i$  being the central value of the lepton invariant mass (transverse mass) of the  $i$ -th bin for the NC (CC) processes. As we will see, the major effects of systematic errors can be absorbed into  $\boldsymbol{\theta}_f$  with this fitting function.

To test the SM-only hypothesis, we define the following test statistic [130]:

$$q_0 \equiv -2 \sum_{f=\ell\ell, \ell\nu} \ln \frac{L(\tilde{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, \mu = 0)}{L(\tilde{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, \hat{\mu})}. \quad (5.4)$$

Here,  $\hat{\boldsymbol{\theta}}_f$  and  $\{\hat{\boldsymbol{\theta}}_f, \hat{\mu}\}$  are determined so that  $\prod_f L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, \mu = 0)$  and  $\prod_f L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, \mu)$  are maximized, respectively. The likelihood function is defined as

$$L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, \mu) \equiv L_{\boldsymbol{\theta}_f}(\tilde{\mathbf{x}}_f; \mu) L'(\boldsymbol{\theta}_f; \boldsymbol{\sigma}_f), \quad (5.5)$$

where

$$L_{\theta_f}(\tilde{\mathbf{x}}_f; \mu) \equiv \prod_i \exp \left[ -\frac{(\tilde{x}_{f,i} - \tilde{x}_{f,i}(\theta_f, \mu))^2}{2\tilde{x}_{f,i}(\theta_f, \mu)} \right], \quad (5.6)$$

$$L'(\theta_f; \sigma_f) \equiv \prod_{\alpha} \exp \left[ -\frac{\theta_{f,\alpha}^2}{2\sigma_{f,\alpha}^2} \right]. \quad (5.7)$$

The product in Eq. (5.6) runs over all the bins, while the product in Eq. (5.7) runs over all the free parameters we introduced. For each  $\theta_{f,\alpha}$ , we define the “standard deviation”  $\sigma_{f,\alpha}$ , which parametrizes the possible size of  $\theta_{f,\alpha}$  within the SM with the systematic errors.<sup>‡24</sup> If the systematic errors are negligible compared with the statistical error, we can take  $\sigma_f \rightarrow \mathbf{0}$ , while the analysis with  $\sigma_f \rightarrow \infty$  assumes no knowledge of systematic errors and gives a conservative result. We identify  $\sqrt{q_0} = 5$  (1.96) as the detection reach at the  $5\sigma$  (95 % C.L.) level, since  $q_0$  asymptotically obeys a chi-square distribution with the degree of freedom one.

In order to determine  $\sigma_f$ , we consider the following sources of the systematic errors:

- Luminosity ( $\pm 5\%$  uncertainty is assumed),
- Renormalization scale ( $2Q$  and  $Q/2$ , instead of  $Q$ ),
- Factorization scale ( $2Q$  and  $Q/2$ , instead of  $Q$ ),
- PDF choice (We use 101 variants of NNPDF2.3QED with  $\alpha_s(M_Z) = 0.118$  [117] provided by LHAPDF6 [131] with IDs ranging from 244600 to 244700).

The values of  $\sigma_f$  are determined as follows. Let  $\mathbf{y}_f$  be the set of number of events in the SM for the final state  $f$  with the canonical choices of the parameters, and  $\mathbf{y}'_f$  be that with one of the sources of the systematic errors being varied. We minimize the chi-square function defined as

$$\chi_f^2 \equiv \sum_i \frac{(y'_{f,i} - \tilde{y}_{f,i}(\theta_f))^2}{\tilde{y}_{f,i}(\theta_f)}, \quad (5.8)$$

where

$$\tilde{y}_{f,i}(\theta_f) \equiv y_{f,i} f_{\text{sys},i}(\theta_f), \quad (5.9)$$

for each final state  $f$ , and determine the best-fit values of  $\theta_f$  for each set of  $\mathbf{y}'_f$ . We repeat this process for different sets of  $\mathbf{y}'_f$ , and  $\sigma_f$  are determined from the distributions of the best-fit values of  $\theta_f$ . For example, let us denote the best-fit values for the fit associated with

<sup>‡24</sup>Here we assume the Gaussian form for the nuisance parameter distribution. The dependence of the results on the choice of the distribution will be discussed later in Sec. 5.2.3.

Sources of systematic errors	$\sigma_{ee,1}$	$\sigma_{ee,2}$	$\sigma_{ee,3}$	$\sigma_{ee,4}$	$\sigma_{ee,5}$
Luminosity: $\pm 5\%$ ( $\sigma_{ee}^{\text{lumi.}}$ )	0.05	0	0	0	0
Renormalization scale: $2Q, Q/2$ ( $\sigma_{ee}^{\text{ren.}}$ )	0.4	0.6	0.3	0.05	0.004
Factorization scale: $2Q, Q/2$ ( $\sigma_{ee}^{\text{fac.}}$ )	0.3	0.5	0.2	0.06	0.004
PDF choice ( $\sigma_{ee}^{\text{PDF}}$ )	0.4	0.7	0.3	0.06	0.004

Table 12: Values of  $\sigma_{ee}$  for each source of systematic errors. The result is the same for the  $\mu\mu$  final state.

Sources of systematic errors	$\sigma_{e\nu_e,1}$	$\sigma_{e\nu_e,2}$	$\sigma_{e\nu_e,3}$	$\sigma_{e\nu_e,4}$	$\sigma_{e\nu_e,5}$
Luminosity: $\pm 5\%$ ( $\sigma_{e\nu_e}^{\text{lumi.}}$ )	0.05	0	0	0	0
Renormalization scale: $2Q, Q/2$ ( $\sigma_{e\nu_e}^{\text{ren.}}$ )	0.3	0.4	0.2	0.04	0.003
Factorization scale: $2Q, Q/2$ ( $\sigma_{e\nu_e}^{\text{fac.}}$ )	1.0	1.6	0.6	0.1	0.01
PDF choice ( $\sigma_{e\nu_e}^{\text{PDF}}$ )	0.6	0.9	0.4	0.08	0.006

Table 13: Best fit values of fit parameters for several sources of systematic errors for the  $e\nu_e$  final state. The result is the same for the  $\mu\nu_\mu$  final state.

the luminosity errors  $\pm 5\%$  as  $\theta_f^\pm$ . We estimate  $\sigma_f$  associated with these errors, denoted here as  $\sigma_f^{\text{lumi.}}$ , as

$$\sigma_{f,\alpha}^{\text{lumi.}} = \sqrt{\frac{(\theta_{f,\alpha}^+)^2 + (\theta_{f,\alpha}^-)^2}{N}}, \quad (5.10)$$

where  $N$  denotes the number of fitting procedures we have performed:  $N = 2$  for this case. We estimate  $\sigma_f$  associated with the other sources of the errors, denoted as  $\sigma_f^{\text{ren.}}$ ,  $\sigma_f^{\text{fac.}}$ , and  $\sigma_f^{\text{PDF}}$ , in a similar manner. Finally, the total values of  $\sigma_f$  are obtained by combining all the sources together as<sup>‡25</sup>

$$\sigma_{f,\alpha} = \sqrt{(\sigma_{f,\alpha}^{\text{lumi.}})^2 + (\sigma_{f,\alpha}^{\text{ren.}})^2 + (\sigma_{f,\alpha}^{\text{fac.}})^2 + (\sigma_{f,\alpha}^{\text{PDF}})^2}. \quad (5.11)$$

In Tables 12 and 13, we show the values of  $\sigma_{ee}$  and  $\sigma_{e\nu_e}$  associated with each source of the systematic errors, respectively. These values can be interpreted as the possible size of the fit parameters within the SM, which is caused by the systematic uncertainties. As explained in Eq. (5.11), we combine these values in each column to obtain  $\sigma_f$ . In Table 14, we summarize the result of the combination for all the final states. The values of  $\sigma_f$  are

<sup>‡25</sup>There may be some correlations between the distribution of nuisance parameters  $\theta_f$ . In this section, we treat each of them as obeying to an independent Gaussian distribution for simplicity.

Final state $f$	$\sigma_{f,1}$	$\sigma_{f,2}$	$\sigma_{f,3}$	$\sigma_{f,4}$	$\sigma_{f,5}$
$ee$	0.7	1.0	0.4	0.09	0.008
$\mu\mu$	0.7	1.0	0.4	0.09	0.008
$e\nu_e$	1.2	1.9	0.7	0.2	0.01
$\mu\nu_\mu$	1.2	1.9	0.7	0.2	0.01

Table 14: Summary of standard deviations  $\sigma_f$  for each final state.

independent of the final state lepton flavors since the energy scale of our concern is much higher than the lepton masses. However, we use different sets of fit parameters  $\theta_{ee}$  and  $\theta_{\mu\mu}$  for the NC processes and  $\theta_{e\nu_e}$  and  $\theta_{\mu\nu_\mu}$  for the CC processes because of the different detector response to electrons and muons.

Several comments on other possible sources of systematic errors are in order. As for the beam energy error, we could not generate events at NLO due to the lack of sufficient computational power. Instead, we checked at LO that the corresponding values of  $\sigma$  (assuming that the uncertainty of the beam energy is 1%) are small enough, and hence we simply ignored it. Two of the remaining sources are the pile-up effect and the underlying event, but they may be thought of as negligible since we are focusing on the very clean signal of two energetic leptons. Another one is the effect of higher order corrections to the cross section and that of background processes which are not considered in our analysis. It is in principle possible to estimate their effects through the simulation and improve the analysis but here we just leave it as a future task. Related to this, we note here that a smooth change of the number of events in general, possibly including the uncertainty listed above, could be absorbed by a minimization procedure using some fitting function like in Eq. (5.3). On the other hand, as we will discuss below, the WIMP signal can not be fully absorbed by the fit because of the sharp bend we mentioned before.

We have also neglected the systematic errors from the detector effect. The main errors are expected to come from the lepton identification, in which some of the leptons in any process are overlooked or identified incorrectly, resulting in the mis-reconstruction of the event topology. Again, it is expected that the small and smooth modification of the number of events may be absorbed into the choice of nuisance parameters, if the corresponding values of  $\sigma_f$  are properly taken into account in addition to the values in Tables 12 and 13. What is dangerous is the possible jerky modification that mimics the WIMP signal, which may be induced by the detector setup, the complicated detector response to leptons, and so on. Such unwanted fake signals may be avoided by checking the consistency between the electron and muon channels. This is because there should be the same size signals at the same lepton invariant mass in both channels for the WIMP signal, while the detector response to electrons

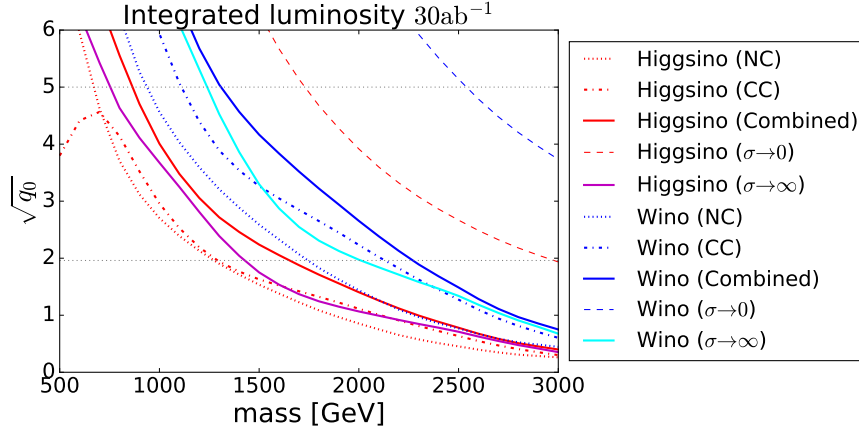


Figure 14:  $\sqrt{q_0}$  as a function of the WIMP mass. Red and blue lines correspond to the Higgsino and Wino, respectively, while line styles represent the result from the NC processes, the CC processes, the combined analysis, and the combined analysis with the optimistic  $\sigma_f \rightarrow 0$  limit. The purple and cyan lines correspond to the results from the conservative analysis with  $\sigma_f \rightarrow \infty$  for the Higgsino and Wino, respectively. (♣ Also show a figure for MDM! ♣)

and muons is different and such a coincidence is not expected in general. It may also be helpful to look for similar fake signals in different processes associated with several leptons. In this section, we just assume that these systematic errors from the detector effect are well controlled once the real experiment will start and focus on the theoretical uncertainties listed in tables.

### 5.2.3 Detection reach

Now we show the detection reach of WIMPs at future 100 TeV colliders. In Fig. 14, we plot the value of  $\sqrt{q_0}$  as a function of the WIMP mass, with the integrated luminosity  $\mathcal{L} = 30 \text{ ab}^{-1}$ . As representative scenarios, we show the cases for Higgsino (the red lines) and Wino (the blue lines). The dotted and dash-dotted lines are the result obtained only from the NC processes and the CC processes, respectively. We find that the CC processes are more sensitive to the effect of the WIMPs than the NC processes because of the larger cross section. This result is consistent with Refs. [125, 126]. The sensitivity of the CC processes is weakened for  $m \lesssim 700 \text{ GeV}$  because of the lepton  $p_T$  cut we have applied.<sup>‡26</sup> The combined

<sup>‡26</sup>We note here that the sensitivity of the CC processes depends on the lepton  $p_T$  cut. For example, adopting the tighter cut, lepton- $p_T > 1 \text{ TeV}$ , the CC processes have almost no sensitivity to WIMPs with  $m < 1 \text{ TeV}$ . Thus, in particular for the purpose of the Higgsino search, it is important to realize the lepton  $p_T$  cut as low as  $\sim 500 \text{ GeV}$ .

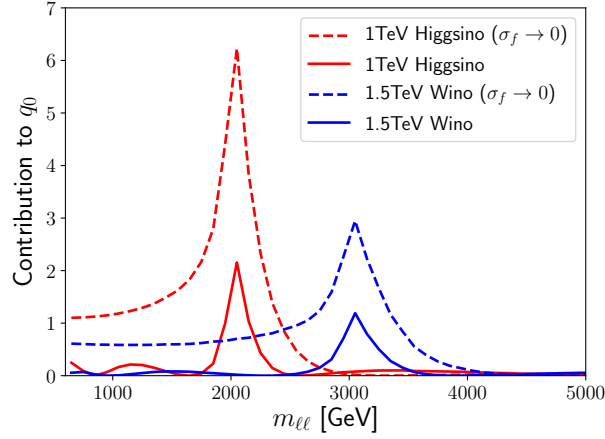


Figure 15: Plot of the contribution of each bin to the value of  $q_0$  for the NC processes. The red (blue) lines correspond to the 1 TeV Higgsino (1.5 TeV Wino). The solid and dotted lines correspond to the results with the fitting procedure and those without it (*i.e.*, the  $\sigma_f \rightarrow 0$  limit), respectively.

results of the NC and CC processes are shown by the solid lines. By combining the two types of processes, the  $5\sigma$  discovery reaches (95 % C.L. bounds) for Higgsino and Wino are 850 GeV (1.7 TeV) and 1.3 TeV (2.3 TeV), respectively. We find that the combination of the NC and CC processes improves the sensitivity of the WIMP mass. Furthermore, if we understand all the systematic uncertainties quite well and effectively take the  $\sigma_f \rightarrow 0$  limit in the combined result, the detection reach will be pushed up significantly as shown by the dashed lines: 1.1 TeV Higgsino signal at well above  $5\sigma$  level and a  $4\sigma$  hint of the 2.9 TeV Wino. These lines should be compared with the combined results and also with those obtained from the conservative analysis with  $\sigma_f \rightarrow \infty$ , assuming no knowledge about sources of systematic errors. The plot shows us that it is essential to reduce the systematic uncertainties for the detection of WIMPs through the NC and CC processes.

We also show the detection reach of the MDM scenario in Fig. ???. The  $5\sigma$  reaches are ??? TeV and ??? TeV for 5-plet fermion and 7-plet scalar, while the 95 % reaches are ??? TeV and ??? TeV. They are lowered to ??? TeV and ??? TeV ( $5\sigma$ ) and ??? TeV and ??? TeV (95 % C.L.) when the systematic errors are included. If we assume the vanilla thermal freeze-out scenario, the mass should be 10 TeV for 5-plet fermion and 25 TeV for 7-plet scalar [84]. Thus, our method probes only a part of the allowed mass range for these multiplets. (♣ **Fill the values, and 5-plet scalar, maybe? ♣**)

Next, we plot in Fig. 15 the contribution of each bin to the value of  $q_0$  to take a closer look at the significance of the dip structure, focusing on the NC processes as an example. The red (blue) lines correspond to the 1 TeV Higgsino (1.5 TeV Wino), while the solid and



dotted lines correspond to the results with the fitting procedure and those without it (*i.e.*, the  $\sigma_f \rightarrow 0$  limit), respectively. We can see that the most contributions come from the bins around the peak at  $m_{\ell\ell} = 2m$ . This feature is clearer for the fitting based approach, where all the smooth parts of the correction are absorbed into the fit parameters, thus there is almost no contribution to  $q_0$  from the bins other than  $m_{\ell\ell} \sim 2m$ . Note also that, for the  $\sigma_f \rightarrow 0$  analysis, there are more contributions from the bins with lower  $m_{\ell\ell}$  than those with higher  $m_{\ell\ell}$ , though sometimes the WIMP effect on the cross section is much larger in the latter bins. This is just because of the difference of number of events in each bin, that is  $\mathcal{O}(10^7)$  for  $500 \text{ GeV} < m_{\ell\ell} < 600 \text{ GeV}$ , while  $\mathcal{O}(10^3)$  for  $4900 \text{ GeV} < m_{\ell\ell} < 5000 \text{ GeV}$  in our set up, for instance. The similar behavior can be expected also for the CC processes.

So far, we have adopted the assumption that the distribution of the nuisance parameters is the Gaussian form and that the fitting function Eq. (5.3) is sufficient for treating systematic errors. In order to discuss the dependence of the results on these assumptions, we have repeated the same analysis using another distribution or fitting function. In the former case, we have adopted the top-hat distribution: the likelihood function for the nuisance parameters  $L'$  is given by

$$L'(\theta_f; \sigma_f) \equiv \prod_{\alpha} \Theta \left( \sqrt{3} \sigma_{f,\alpha} - |\theta_{f,\alpha}| \right), \quad (5.12)$$

where  $\Theta$  is the Heaviside step function. This corresponds to the top-hat distribution of  $\theta_{f,\alpha}$  with the variance  $\sigma_{f,\alpha}^2$  for each  $\alpha$ . As for an example of another fitting function, we have adopted a simple one parameter extension of Eq. (5.3)

$$f_{\text{sys},i}(\theta_f) = e^{\theta_{f,1}} (1 - p_i)^{\theta_{f,2}} p_i^{(\theta_{f,3} + \theta_{f,4} \ln p_i + \theta_{f,5} \ln^2 p_i + \theta_{f,6} \ln^3 p_i)}, \quad (5.13)$$

which consists of six parameters. The variances of the nuisance parameters are estimated in the same way as Sec. 5.2.2, but now with the six parameters.

In Fig. 16, we show the corresponding results for Higgsino and Wino as an example. The convention for the line colors is the same as Fig. 14, while the line styles denote different procedures: the dashed and dotted lines correspond to the result with the top-hat distribution and that with the six parameters fitting function, respectively, while solid lines are the same as Fig. 14. From the figure, we can see that the choice of the distribution may slightly affect the result, while the addition of a nuisance parameter as Eq. (5.13) causes almost no effect. The size of the effect of the choice of the distribution for the current estimation of errors  $\sigma_f$  is about 100 GeV (200 GeV) for the  $5\sigma$  (95 % C.L.) bounds. We expect that such uncertainties due to the procedure to include the systematic errors will be reduced once the data from the real experiment (and hence better understanding of the systematic errors) will become available.

(♣ Comment on bound state effect somewhere ♣)

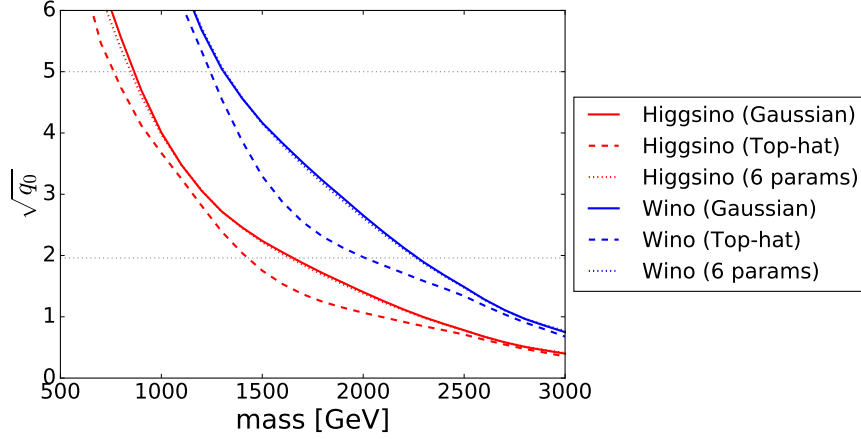


Figure 16:  $\sqrt{q_0}$  as a function of the WIMP mass using both the NC and CC processes. The convention for the line colors is the same as Fig. 14. The line styles denote the result same as Fig. 14 (solid), that with the top-hat distribution (dashed), and that with the six parameters fitting function (dotted).

#### 5.2.4 Determination of WIMP properties

In this subsection, we show that it is possible to determine the properties of the WIMPs from the NC and CC processes, thanks to the fact that we can study the  $m_{\ell\ell}$  and  $m_T$  distribution in great detail for these processes. Some information about the mass, charge, and spin of the WIMPs can be extracted because the corrections to these distributions from the WIMPs are completely determined by these WIMP properties. Firstly, we can extract the WIMP mass from the position of the dip-like structure in the correction since it corresponds to roughly twice the WIMP mass as we have shown in Sec. 5.1. Secondly, the overall size of the correction gives us information about the  $SU(2)_L$  and  $U(1)_Y$  charges. The CC processes depend only on the  $SU(2)_L$  charge, while the NC processes depend both on the  $SU(2)_L$  and  $U(1)_Y$  charges. Consequently, we can obtain information about the gauge charges of the WIMPs from the NC and CC processes.

We now demonstrate the mass and charge determination of fermionic WIMPs. This is equivalent to the determination of the parameter set  $(m, C_1, C_2)$ . We generate the data assuming the SM + WIMP model ( $\mu = 1$ ) with some specific values of  $m, n, Y$ , and  $\kappa$ , with which we obtain  $(m, C_1, C_2)$ . We fix  $\mu = 1$  for our theoretical model as well, and hence the theoretical predictions of the number of events also depend on these three parameters,  $\mathbf{x}_f = \mathbf{x}_f(m, C_1, C_2)$ . We define the likelihood function  $L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, m, C_1, C_2)$  in the same form as Eqs. (5.2) and (5.5) with the theoretical prediction  $\mathbf{x}_f$  now understood as a function of

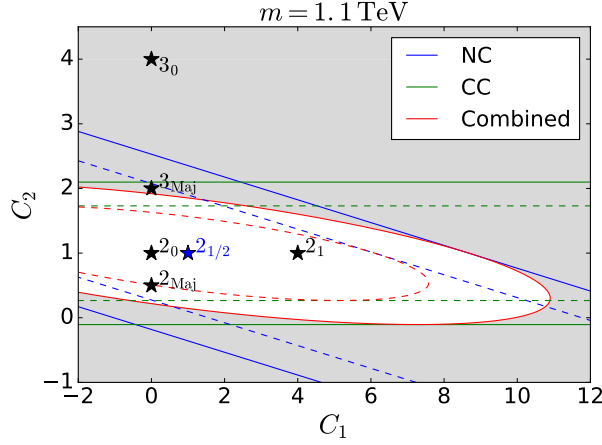


Figure 17: Contour of  $\sqrt{q}$  in the  $C_1$  vs.  $C_2$  plane with  $m = 1.1$  TeV, where we assume 1.1 TeV Higgsino signal. The dotted and solid lines denote  $1\sigma$  and  $2\sigma$  contours, respectively, and the gray region corresponds to the parameter space that is in tension with the observation at more than  $2\sigma$  level. The blue, green, and red lines correspond to the result from the NC processes, the CC processes, and the combined analysis, respectively. Each star marker annotated as “ $n_Y$ ” represents a point corresponding to a  $SU(2)_L$   $n$ -plet Dirac fermion with hypercharge  $Y$ , while that with “ $n_{\text{Maj}}$ ” corresponds to an  $SU(2)_L$   $n$ -plet Majorana fermion.

$(m, C_1, C_2)$ , not of  $\mu$ .<sup>‡27</sup> The test statistic is defined as

$$q(m, C_1, C_2) \equiv -2 \sum_f \ln \frac{L(\tilde{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, m, C_1, C_2)}{L(\tilde{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, \hat{m}, \hat{C}_1, \hat{C}_2)}, \quad (5.14)$$

where the parameters  $(\{\hat{\boldsymbol{\theta}}_f\}, \hat{m}, \hat{C}_1, \hat{C}_2)$  maximize  $\prod_f L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, m, C_1, C_2)$ , while  $\hat{\boldsymbol{\theta}}_f$  maximize  $L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, m, C_1, C_2)$  for fixed values of  $(m, C_1, C_2)$ . It follows the chi-squared distribution with three degrees of freedom in the limit of a large number of events [53]. The test statistic defined in this way examines the compatibility of a given WIMP model (i.e. a parameter set  $(m, C_1, C_2)$ ) with the observed signal.

Once a deviation from the SM prediction is observed in a real experiment, we may determine  $(m, C_1, C_2)$  using the above test statistic  $q$ . In the following, we show the expected accuracy of the determination of  $(m, C_1, C_2)$  for the case where there exists 1.1 TeV Higgsino.<sup>‡28</sup>

<sup>‡27</sup>As shown in Eqs. (5.3) and (5.4),  $C_1$  and  $C_2$  are positive quantities (and  $C_2$  is discrete). In the figures, however, we extend the  $C_1$  and  $C_2$  axes down to negative regions just for presentation purposes.

<sup>‡28</sup>The expected significance is  $3.5\sigma$  for 1.1 TeV Higgsino in our estimation. Even though it is slightly below the  $5\sigma$  discovery, we take 1.1 TeV Higgsino as an example because it is a candidate of the thermal relic DM.

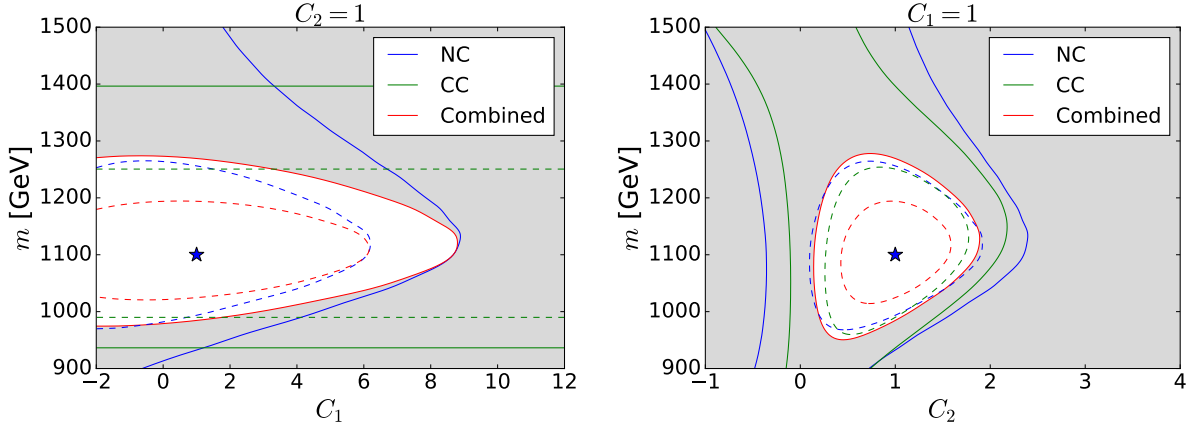


Figure 18: **Left:** Contour of  $\sqrt{q}$  in the  $C_1$  vs.  $m$  plane with  $C_2 = 1$ , where we assume the 1.1 TeV Higgsino signal. The colors and styles of lines and the meaning of the gray region are the same as Fig. 17. The star marker corresponds to the true Higgsino property  $(C_1, m) = (1, 1.1 \text{ TeV})$ . **Right:** Contour of  $\sqrt{q}$  in the  $C_2$  vs.  $m$  plane for  $C_1 = 1$ , where we assume the 1.1 TeV Higgsino signal. The star marker corresponds to the true Higgsino property  $(C_2, m) = (1, 1.1 \text{ TeV})$ .

In Fig. 17, we show the contours of  $1\sigma$  (dotted) and  $2\sigma$  (solid) constraints, which correspond to the values  $\sqrt{q} = 1.9$  and  $\sqrt{q} = 2.8$ , respectively, in the  $C_1$  vs.  $C_2$  plane for  $m = 1.1 \text{ TeV}$ . The blue, green, and red lines denote the result obtained from the NC processes, the CC processes, and the combined analysis, respectively. The models in the gray region are in more than  $2\sigma$  tension with the observation. We also show several star markers that correspond to the single  $SU(2)_L$  multiplet contributions: the markers with “ $n_Y$ ” represent an  $SU(2)_L$   $n$ -plet Dirac fermion with hypercharge  $Y$ , while those with “ $n_{\text{Maj}}$ ” an  $SU(2)_L$   $n$ -plet Majorana fermion. Both the NC and CC constraints are represented as straight bands in the  $C_1$  vs.  $C_2$  plane since each process depends on a specific linear combination of  $C_1$  and  $C_2$ . In particular, the CC constraint is independent of  $C_1$ , or  $Y$ . In this sense, the NC and CC processes are complementary to each other, and thus we can separately constrain  $C_1$  and  $C_2$  only after combining these two results. For instance, we can exclude a single fermionic  $SU(2)_L$  multiplet with  $n \neq 2$  at more than  $2\sigma$  level, although each process by itself cannot exclude the possibility of  $3_{\text{Maj}}$ . We can also constrain the hypercharge, yet it is not uniquely determined. In addition to the Higgsino, the WIMP as an  $SU(2)_L$  doublet Dirac fermion with  $|Y|^2 \lesssim 2$  or an  $SU(2)_L$  doublet Majorana fermion with  $|Y|^2 \lesssim 5$  is still allowed.

In Fig. 18, we show the contour plots of  $\sqrt{q}$  in the  $C_1$  vs.  $m$  plane with  $C_2 = 1$  (left) and those in the  $C_2$  vs.  $m$  plane with  $C_1 = 1$  (right). The star marker in each panel shows the true values of parameters  $(C_1, m) = (1, 1.1 \text{ TeV})$  (left) and  $(C_2, m) = (1, 1.1 \text{ TeV})$  (right).

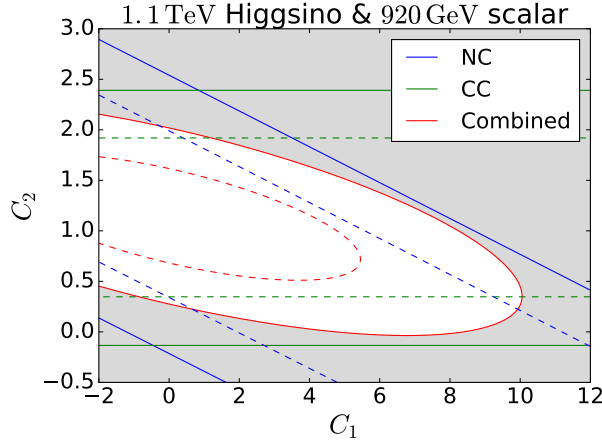


Figure 19: Contour of  $\sqrt{q}$  in the  $C_1$  vs.  $C_2$  plane for the 1.1 TeV Higgsino signal, tested with the scalar WIMP assumption. The plane is defined as the scalar mass of 920 GeV. The colors and styles of lines and the meaning of the gray region are the same as Fig. 17.

Again, by combining the NC and CC results, we can significantly improve the determination of WIMP properties, making  $1\sigma$  and  $2\sigma$  contours closed circles in the planes of our concern. In particular, as red lines show, the combined analysis allows us to determine the observed WIMP mass at the level of  $\mathcal{O}(10)\%$ .

Finally, we comment on the possibility of discriminating between fermionic and scalar WIMPs, whose difference comes from the loop function  $f(x)$  (see Eq. (5.2)). Here we repeat the same analysis explained above, assuming the 1.1 TeV Higgsino signal for example, but use the scalar loop function to evaluate the theoretical predictions  $\mathbf{x}_f(m, C_1, C_2)$ . In Figs. 19 and 20, we show the results in the  $C_1$  vs.  $C_2$  plane and the  $C_1$  (or  $C_2$ ) vs.  $m$  plane, respectively, where one of the three parameters is fixed to its best fit value. It is seen that, in the case of the 1.1 TeV Higgsino signal, it is hard to distinguish between the bosonic and fermionic WIMPs only with our method. However, if a part of the WIMP properties (in particular its mass) is determined from another approach, our method may allow us to determine its spin correctly.

We also stress here that, with some favorable assumption about the observed signal, we may obtain some hint about its spin. For example, if we assume that the observed signal composes a fraction of the dark matter in our Universe, the choice of the WIMP charges is significantly constrained. Note from Fig. 19 that the only choices of WIMP charges that allow the WIMP multiplet to contain an electrically neutral component are  $(n, |Y|) = (3, 0), (3, 1), (4, 1/2), (4, 3/2)$ , and  $(5, 0)_{\text{real}}$ . The last column of the table 15 shows proper choices of WIMP masses in order for their thermal relic abundances become comparable with the dark matter abundance in the current Universe. All of those values are somewhat

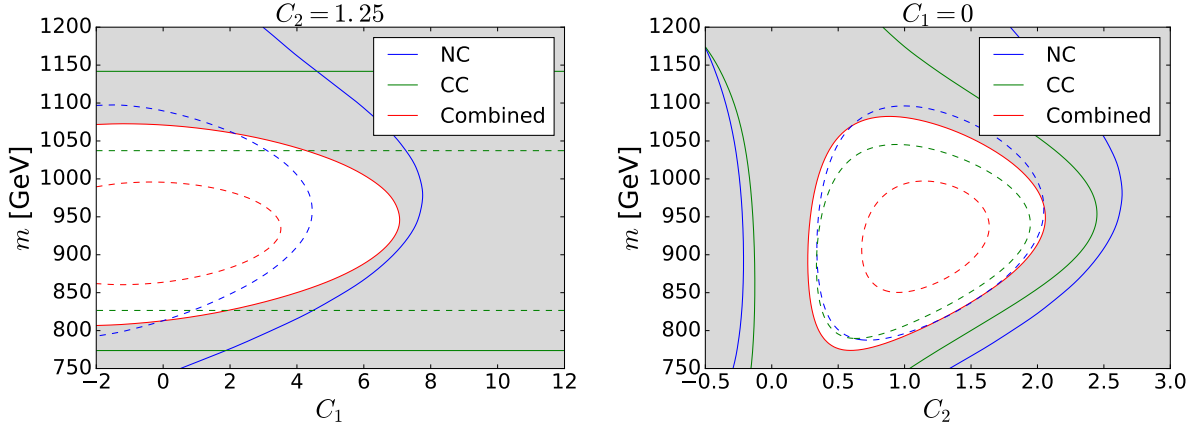


Figure 20: **Left:** Contour of  $\sqrt{q}$  in the  $C_1$  vs.  $m$  plane with  $C_2 = 1.25$  for the 1.1 TeV Higgsino signal, tested with the scalar WIMP assumption. The colors and styles of lines and the meaning of the gray region are the same as Fig. 17. **Right:** Contour of  $\sqrt{q}$  in the  $C_2$  vs.  $m$  plane with  $C_1 = 0$  for the 1.1 TeV Higgsino signal, tested with the scalar WIMP assumption.

$(n, Y)$	$C_1$	$C_2$	$m_{\text{DM}}[\text{TeV}]$
$(3, 0)_{\text{real}}$	0	0.25	2.5 [87]
$(3, 0)$	0	0.5	1.55 [89]
$(3, 1)$	0.75	0.5	1.6 [87]
$(4, \frac{1}{2})$	0.25	1.25	2.4 [87]
$(4, \frac{3}{2})$	2.25	1.25	2.9 [87]
$(5, 0)_{\text{real}}$	0	1.25	9.4 [87]

Table 15: The scalar WIMPs that are compatible with the result in Fig. 19. The observed DM energy density is explained by the thermal relic of the WIMP with  $m_{\text{DM}}$  shown in the fourth column.

larger than the central value of the mass of the observed signal, which means that the scalar interpretation of the signal cannot explain the whole of the dark matter relic abundance without introducing some non-thermal production mechanism.

### 5.3 Conclusion

In this section, we have discussed the indirect search of WIMPs at future 100 TeV hadron colliders based on the precision measurement of the production processes of a charged lepton

pair and that of a charged lepton and a neutrino. In particular, we have demonstrated that not only we can discover the WIMPs, but also we can determine their properties such as their masses,  $SU(2)_L$  and  $U(1)_Y$  charges, and spins via the processes of our concern. It is based on two facts: the high energy lepton production channel enables us to study its momentum distribution in great detail, and the WIMP correction shows characteristic features, including a dip-like structure as the final state invariant mass being twice the WIMP mass. The latter feature also helps us to distinguish the WIMP signals from backgrounds and systematic errors, as they are not expected to show a dip-like structure. In order to fully exploit the differences between the distributions the WIMP signals and systematic errors, we have adopted the profile likelihood method as our statistical treatment.

First, we have shown in Fig. 14 the detection reach of WIMPs from the NC processes (mediated by photon or  $Z$ -boson), the CC processes (mediated by  $W$ -boson), and the combination of these two results. We have seen that the addition of the CC processes improves the detection reach from the previous analysis [1]. From the combined analysis, the bounds at the  $5\sigma$  (95% C.L.) level for Higgsino and Wino are 850 GeV (1.7 TeV) and 1.3 TeV (2.3 TeV), respectively. We have also shown the 95 % C.L. reach for 5-plet fermion and 7-plet scalar: ??? TeV and ??? TeV for the optimistic analysis and ??? TeV and ??? TeV for the analysis with a fitting procedure. (**♣ Fill the values ♣**) This result, in particular that for short lifetime Higgsino, indicates the importance of our method for the WIMP search.

Next, we have considered the determination of the mass and  $SU(2)_L$  and  $U(1)_Y$  charges of the observed WIMP. By combining the NC and the CC events, the position and the height of the dip in the WIMP effect on the cross section gives us enough information for determining all the three parameters. In Figs. 17 and 18, we have shown the plots of the test statistics that test the validity of several choices of parameters. As a result, the  $SU(2)_L$  charge of the observed signal is correctly identified under the assumption of a single WIMP multiplet, and the  $U(1)_Y$  charge and mass are also determined precisely. In order for the determination of the WIMP spin, we have plotted the contours of the test statistics that test the validity of the scalar WIMP models with some fixed values of masses and charges. The results are shown in Figs. 19 and 20, which reveals that the spin is not completely determined by solely using our method. Use of another approach to determine the WIMP properties, or of some assumption like that the observed signal corresponds to the dark matter in our Universe, may help us to obtain further information regarding the WIMP spin.

## Section 6

## Conclusion

(♣ To be written ♣)



## Section A

# Conventions and notations

In this appendix, we summarize the conventions and notations used throughout the thesis. Firstly, we use the natural units with

$$c = \hbar = k_B = 1, \quad (\text{A.1})$$

where  $c$ ,  $\hbar$ , and  $k_B$  are the speed of light, the reduced Planck constant, and the Boltzmann constant, respectively.

Our convention of the four-dimensional Lorentzian metric is  $g^{\mu\nu} = \text{diag}(1, -1, -1, -1)$ . We sometimes use the Pauli matrices defined as

$$\sigma_1 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \sigma_2 = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \quad \sigma_3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, \quad (\text{A.2})$$

with  $i$  being the imaginary unit. The slash on any character denotes the so-called Feynmann slash, defined as  $\not{p} \equiv p^\mu \gamma_\mu$  with four-by-four gamma matrices given by

$$\gamma^0 = \begin{pmatrix} \mathbf{0} & \mathbf{1} \\ \mathbf{1} & \mathbf{0} \end{pmatrix}, \quad \gamma^i = \begin{pmatrix} \mathbf{0} & \sigma_i \\ -\sigma_i & \mathbf{0} \end{pmatrix}, \quad (\text{A.3})$$

The unique exception of this rule is  $\not{E}_T$ , which is used to denote the missing transverse momentum in hadron collider experiments.

We use the notation  $g_1$ ,  $g_2$ , and  $g_3$  for the gauge coupling constant of the SM  $U(1)_Y$ ,  $SU(2)_L$ , and  $SU(3)_c$  gauge group. We use the so-called grand unified theory normalization of  $g_1$ ; the corresponding charge assignment is different from the conventional assignment of  $U(1)_Y$  (with, *e.g.*, charge  $-1/2$  for the left-handed leptons) by a factor of  $\sqrt{3/5}$ .

## Section B

# Review of supersymmetry

**(♣ More later ♣)**

In this appendix, we briefly review the  $\mathcal{N} = 1$  supersymmetry, which is an essential element of the MSSM explained in Sec. ???. Our argument is based on [56, 132].

The  $\mathcal{N} = 1$  supersymmetry is

First example is the MSSM, extension of the SM with the so-called  $\mathcal{N} = 1$  supersymmetry (SUSY) [56, 132] that relates a bosonic particle and a fermionic particle. The supersymmetry transformations for a complex scalar  $\phi$  and its “superpartner” Weyl fermion  $\psi$  are defined as

$$\delta\phi = (\epsilon\psi), \quad \delta\phi^* = (\epsilon^\dagger\psi^\dagger), \quad (\text{B.1})$$

$$\delta\psi = -i(\sigma^\mu\epsilon^\dagger)\partial_\mu\phi, \quad \delta\psi^\dagger = i(\epsilon\sigma^\mu)\partial_\mu\phi^*, \quad (\text{B.2})$$

where  $\sigma^\mu \equiv (\mathbf{1}, \boldsymbol{\sigma})$  with  $\boldsymbol{\sigma}$  being Pauli matrices, while  $\epsilon$  is an anti-commuting Weyl fermionic object that parameterizes the SUSY transformation. The summation over the spinor indices is assumed inside each parenthesis. These transformations, if denoted by operators  $\epsilon Q$  and  $\epsilon^\dagger Q^\dagger$ , are known to form a closed algebra

$$[Q, Q^\dagger] = 2i\sigma^\mu\partial_\mu, \quad (\text{B.3})$$

$$[Q, Q] = [Q^\dagger, Q^\dagger] = 0, \quad (\text{B.4})$$

when fields are on-shell.<sup>‡29</sup>

**(♣ chiral and vector superfield ♣)**

**(♣  $m_f = m_S$  for each multiplet ♣)**

**(♣ F-term and D-term potential ♣)**

---

<sup>‡29</sup>In order for the algebra to be closed off-shell, one can introduce a new scalar field  $F$  without a kinetic term that is often called as an *auxiliary* field.  $F$  works as a Lagrange multiplier whose equation of motion

**(♣ What? ♣)**

## Section C

### Properties of the transverse mass

In this appendix, we summarize the properties of the transverse mass, which is used for the analysis of the mono-lepton final state in Sec. 5. The transverse mass is a useful quantity when there is a unique invisible particle (which we will call  $I$ ) such as a neutrino in the final state. As already mentioned in Sec. 5.1, the transverse mass  $m_T$  is defined event by event using the measured value of the missing transverse momentum  $\cancel{E}_T$  as

$$m_T^2 \equiv 2p_T \cancel{E}_T (1 - \cos \phi), \quad (\text{C.1})$$

where  $p_T$  denotes the transverse momentum of a (visible) final state particle (which will call  $P$ ) and  $\phi$  is the difference between the azimuth angles of  $p_T$  and  $\cancel{E}_T$ . It is important that we can infer the invariant mass of particles  $P$  and  $I$  with  $m_T$ , if both  $P$  and  $I$  are (approximately) massless.

Let  $p_P$  and  $p_I$  be the four momenta of  $P$  and  $I$ , respectively. When there is only one invisible particle in the event, the transverse part of  $p_I$  is roughly identified with  $\cancel{E}_T$ . Hereafter, we assume the exact equality among them just for simplicity, which corresponds to neglect the detector errors, transverse momentum of initial partons, soft emissions that is invisible for detectors, and so on. Then, we can write the components of four momenta as

$$p_P = (E_P, p_T \cos \phi_P, p_T \sin \phi_P, p_{Pz}), \quad (\text{C.2})$$

$$p_I = (E_I, \cancel{E}_T \cos \phi_I, \cancel{E}_T \sin \phi_I, p_{Iz}), \quad (\text{C.3})$$

with  $\phi \equiv \phi_P - \phi_I$ . Note that massless conditions are satisfied, namely  $E_P^2 = p_T^2 + p_{Pz}^2$  and  $E_I^2 = \cancel{E}_T^2 + p_{Iz}^2$ . We can derive a relation between  $m_T$  and  $m_{PI} \equiv \sqrt{(p_P + p_I)^2}$

$$m_T \leq m_{PI}, \quad (\text{C.4})$$

where the equation holds when

$$p_{Pz} \cancel{E}_T - p_T p_{Iz} = 0. \quad (\text{C.5})$$

When the above equation roughly holds,  $m_{PI} - m_T$  grows proportional to the quadratic of the left-handed side of Eq. (C.5).

It is more intuitive to understand the situation in the center of mass system (CMS), focusing on the pair production process of particles  $P$  and  $I$ . In this case, the transverse momentum of the event is simply given by

$$m_T^{(\text{CMS})} = m_{PI} \sin \theta^{(\text{CMS})}, \quad (\text{C.6})$$

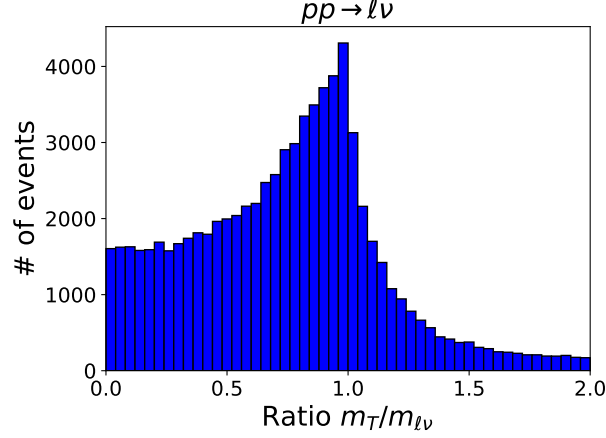


Figure 21: Distribution of  $m_T/m_{\ell\nu}$  for the pair production process of  $P = \ell$  and  $I = \nu$ . Figure for  $\sqrt{s} = 100$  TeV and  $\mathcal{L} = 1 \text{ ab}^{-1}$ .

where  $\theta^{(\text{CMS})}$  is the angle between the momentum of  $P$  and the beam line in the CMS. Although the definition of  $m_T$  is not Lorentz invariant and generally  $m_T^{(\text{CMS})} \neq m_T$ , the former gives a good approximation of the latter when the two-particle system is not highly boosted. Let us simply assume  $m_T = m_T^{(\text{CMS})}$  and consider the repeated production of  $P$  and  $I$  with fixed  $m_{PI}$ . When we postulate the uniform distribution of the production cross section against  $\cos\theta^{(\text{CMS})}$  for simplicity, the distribution of the transverse mass  $f(m_T)$  calculated according to Eq. (C.6) possesses a sharp peak at  $m_T = m_{PI}$ , described by

$$f(m_T) = \frac{m_T}{m_{PI}} \cos^{-1} \left[ \arcsin \left( \frac{m_T}{m_{PI}} \right) \right]. \quad (\text{C.7})$$

This peak, often called as the Jacobian peak, enables us to estimate  $m_{PI}$  from  $m_T$ .

In Fig. 21, we show the distribution of the ratio  $m_T/m_{\ell\nu}$  for the pair production process of  $P = \ell$  and  $I = \nu$ . We use the setup of  $\sqrt{s} = 100$  TeV and  $\mathcal{L} = 1 \text{ ab}^{-1}$ . To evaluate the missing transverse momentum  $\cancel{E}_T$  for each event, we have performed the detector simulation using **Delphes** similar to the analysis in Sec. 5. We can clearly see the peak at  $m_T/m_{\ell\nu} = 1$ , though it is somewhat smeared compared with that expected in the CMS due to the effect of the Lorentz boost and the non-trivial angular dependence of the production cross section. Besides, the small tail of the distribution for  $m_T > m_{\ell\nu}$  can be understood by the effects we have neglected so far, such as the detector errors.

## Section D

### Profile likelihood method

In this appendix, we briefly review the the profile likelihood method used in Sec. 5.2.2. In particular, we describe the motivation and justification to consider this method.

First of all, the experimental outcome of our concern can be expressed as a set of random variables  $\mathbf{x} \equiv \{x_1, \dots, x_n\}$ , with  $n$  being the number of observables. The distribution of these variables is due to both the intrinsic physical randomness (*i.e.*, the statistical fluctuation) and the uncertainty in detector responses such as the efficiency, momentum reconstruction, and so on. We assume  $\mathbf{x}$  obey some probability distribution function and express it as  $f(\mathbf{x}; \boldsymbol{\theta})$ , where  $\boldsymbol{\theta} = \{\theta_1, \dots, \theta_m\}$  parametrize (in many cases unknown) uncertainties listed above. When we repeat  $N$  experiments and obtained  $N$  sets of observables expressed as  $\mathbf{x}^a$  ( $a = 1, \dots, N$ ), we define the likelihood function  $L$  as

$$L = \prod_{a=1}^N f(\mathbf{x}^a; \boldsymbol{\theta}). \quad (\text{D.1})$$

Since  $L$  should take a relatively larger value if the assumed distribution  $f$  approximates the reality very well, we may perform the maximization of  $L$  against the choice of  $\boldsymbol{\theta}$  to obtain the correct probability distribution. Such maximization procedure can be performed analytically only for several simple distribution functions. Thus, in many cases, we need a numerical calculation of the maximization procedure, which can be performed with the MINUIT package [133].

In our analysis in Sec. 5, the data is given in the form of the histogram. In this case,  $x_i$  ( $i = 1, \dots, n$ ) denotes the observed number of events in each bin labeled by  $i$ , with  $n$  being the number of bins. The product of the probability distribution function for each bin gives  $f$ , which is equivalent to  $L$  in this case, expressed as

$$L(\mathbf{x}; \boldsymbol{\theta}) \equiv f(\mathbf{x}; \boldsymbol{\theta}) = \exp \left[ -\frac{(x_i - \mu_i(\boldsymbol{\theta}))^2}{2x_i} \right], \quad (\text{D.2})$$

with  $\mu_i(\boldsymbol{\theta})$  being the average number of events of the bin  $i$  calculated using the parameters  $\boldsymbol{\theta}$ . Note that  $x_i \gg 1$  is assumed for each bin and the central limit theorem is used to replace the Poisson to the Gaussian distribution. Then, it is clear that the maximization of  $L$  is equivalent to the minimization of  $\chi^2$  defined as

$$\chi^2 \equiv -2 \ln L(\mathbf{x}; \boldsymbol{\theta}) = \sum_{i=1}^n \frac{(x_i - \mu_i(\boldsymbol{\theta}))^2}{x_i}, \quad (\text{D.3})$$

which is the so-called Neyman's  $\chi^2$  variable.  $\chi^2$  obeys the chi-square distribution when the distribution of  $x_i$  is well approximated by the Gaussian, and can be easily used to find the optimized choice of parameters  $\boldsymbol{\theta}$  and their errors.

Similarly, one can apply the likelihood maximization to the test of the model. Let  $\boldsymbol{\theta}_{\text{true}}$  and  $\boldsymbol{\theta}_{\text{test}}$  be the model in the reality and that we want to test, respectively. For example, in the new physics search, the former corresponds to the new physics model, while the latter to the SM. Then we can define the test-statistic

$$q(\boldsymbol{\theta}_{\text{test}}) = -2 \ln \frac{L(\mathbf{x}; \boldsymbol{\theta}_{\text{test}})}{L(\mathbf{x}; \boldsymbol{\theta}_{\text{true}})}, \quad (\text{D.4})$$

which plays a role of the so-called  $\Delta\chi^2$  variable according to the discussion above. Again  $q$  may obey a chi-square distribution with some degrees of freedom, and can be used to obtain sensitivities to the new physics, *i.e.*, the 95 % C.L. exclusion and the  $5\sigma$  discovery. Note that the denominator of the test static can also be expressed as  $L(\mathbf{x}; \hat{\boldsymbol{\theta}})$ , where the hat denotes the values of  $\boldsymbol{\theta}$  that maximize the function  $L$ .

However, the situation may be more complicated since some of the parameters  $\boldsymbol{\theta}$  are not directly related to the model parameters, but express the background yield, detector effects, systematic errors, and so on, which should be determined from experimental data. Such additional parameters are often called nuisance parameters. To treat nuisance parameters, it is convenient to rely on the profile likelihood method [130].

For this purpose, we divide the parameters into two categories: the model parameter of our interest  $\boldsymbol{\mu}$  and nuisance parameters  $\boldsymbol{\theta}$ . Similarly to the discussion without the nuisance parameters, let  $\boldsymbol{\mu}$  be the model in we want to test. The test static is defined as

$$q(\boldsymbol{\mu}) = -2 \ln \frac{L(\mathbf{x}; \boldsymbol{\mu}, \hat{\hat{\boldsymbol{\theta}}}(\boldsymbol{\mu}))}{L(\mathbf{x}; \hat{\boldsymbol{\mu}}, \hat{\boldsymbol{\theta}})}, \quad (\text{D.5})$$

where the meaning of the hat is the same as above, while  $\hat{\hat{\boldsymbol{\theta}}}(\boldsymbol{\mu})$  denotes the values that maximize  $L$  with fixed values of  $\boldsymbol{\mu}$ . The motivation for this choice is given by the Wilk's theorem [134], which proves that  $q(\boldsymbol{\mu})$  asymptotically obeys the chi-square distribution whose degrees of freedom equal to the number of model parameters  $\boldsymbol{\mu}$ . Note that this the statement is highly non-trivial, since the individual term  $-2 \ln L$  *does not* obey chi-square distributions in this case. Thanks to the theorem, we can perform the same analysis under the existence of nuisance parameters and, in particular, absorb the effects of systematic errors into the choice of parameters  $\boldsymbol{\theta}$ .

**(♣ Comment on distribution of nuisance parameters? ♣)**

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