

Section 1

Indirect search of WIMPs using Drell-Yan process

So far, we have argued several ways to search for WIMPs using DM searches and collider experiments. We have seen that, while WIMPs with relatively large $SU(2)_L$ charges such as Wino and the 5-plet fermion are promising for these searches, Higgsino is typically more challenging to probe. Given this situation, another search strategy attracts a lot of attention [1–9] that probes WIMPs via the electroweak precision measurement at colliders. It utilizes a pair production of charged leptons or that of a charged lepton and a neutrino, where WIMPs affect the pair production processes through the vacuum polarizations of the electroweak gauge bosons as shown in Fig. 1. It is an indirect search method in the sense that it does not produce on-shell WIMPs as final states.

There are several virtues in this method such as the robustness against the change of the lifetime and the decay modes of WIMPs and the characteristic dip-like shape of the invariant mass distributions at the value close to twice the WIMP mass as we will see below. We will see that the latter point helps us to distinguish the WIMP effects from backgrounds and systematic errors. However, the obtained reach for Higgsino in the most of the literature is still unsatisfactory since the use of the LHC or lepton colliders gives us only a few events at the position of the dip, which results in the reach much below the thermal Higgsino DM mass $m_\chi \sim 1$ TeV.

Thus, in this section, we pursue this indirect search method further, considering a much higher center-of-mass energy using the future 100 TeV hadron colliders such as FCC-hh [10–

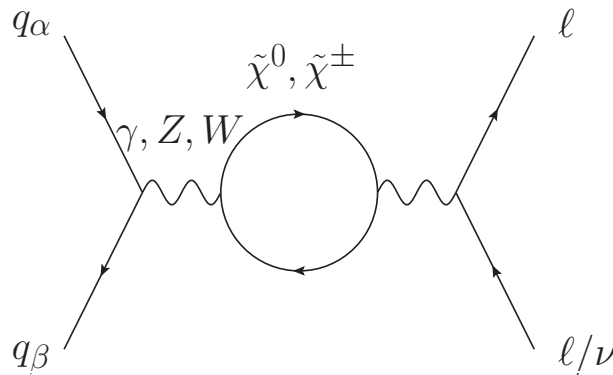


Figure 1: WIMP effect on the Drell-Yan processes considered in this section.

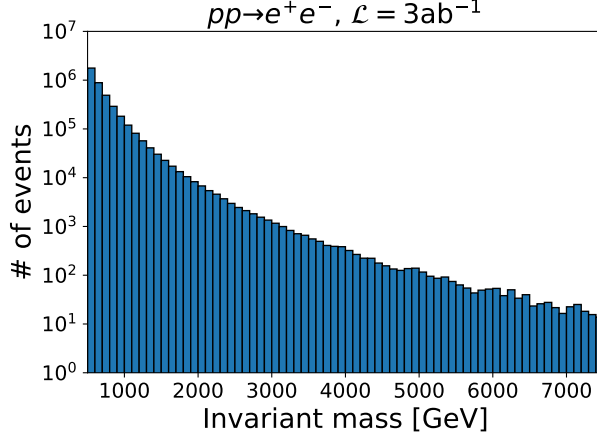


Figure 2: Invariant mass distribution of the pair-produced electrons at a 100 TeV collider with the integrated luminosity $\mathcal{L} = 3 \text{ ab}^{-1}$.

[13] and SppC [14, 15]. We concentrate on the Drell-Yan processes that have two charged leptons or mono-lepton plus a neutrino in the final state since they provide a very clean signal without any hadronic jets at least from the final state particles. In Fig. 2, we show the invariant mass distribution of the pair produced electrons, for example, at a 100 TeV collider with the integrated luminosity $\mathcal{L} = 3 \text{ ab}^{-1}$. In the figure, events are divided into bins with equal width of 100 GeV. Thanks to the large center-of-mass energy, there are more than 10^4 events around the invariant mass of 2 TeV that can be used to probe the $\mathcal{O}(1)\%$ effect of the new physics, which will be turned out to be useful for the 1 TeV Higgsino search.

Below, we will show that the indirect search method provides *a comparable or better experimental reach for Higgsino* compared to the direct production search of WIMPs at future colliders [16–19]. Besides, we demonstrate that the indirect search method can be applied not only to discover WIMPs but also *to investigate their properties, such as charges, masses, and spins*. To this end, it is important to consider both the charged current (CC) process with two-lepton final state and the neutral current (NC) process with mono-lepton final state to break some degeneracy among different WIMP charge assignments; the NC and CC processes depend on different combinations of the $SU(2)_L$ and $U(1)_Y$ charges of WIMP, and hence the inclusion of both processes allows us to extract these charges separately.

This section is based on our works [1, 2].

1.1 WIMP effect on the Drell-Yan processes

We investigate contributions of the WIMPs to the Drell-Yan processes through the vacuum polarization of the electroweak gauge bosons at the loop level. Throughout this section, we

assume that all the other beyond the SM particles are heavy enough so that they do not affect the following discussion. After integrating out the WIMPs, the effective lagrangian is expressed as

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + C_2 g^2 W_{\mu\nu}^a f\left(-\frac{D^2}{m^2}\right) W^{a\mu\nu} + C_1 g'^2 B_{\mu\nu} f\left(-\frac{\partial^2}{m^2}\right) B^{\mu\nu}, \quad (1.1)$$

where \mathcal{L}_{SM} is the SM Lagrangian, D is a covariant derivative, m is the WIMP mass,^{‡1} g and g' are the $SU(2)_L$ and $U(1)_Y$ gauge coupling constants, and $W_{\mu\nu}^a$ and $B_{\mu\nu}$ are the field strength associated with the $SU(2)_L$ and $U(1)_Y$ gauge group, respectively. The function $f(x)$ is defined as^{‡2}

$$f(x) = \begin{cases} \frac{1}{16\pi^2} \int_0^1 dy y(1-y) \ln(1 - y(1-y)x - i0) & \text{(Fermion)}, \\ \frac{1}{16\pi^2} \int_0^1 dy (1-2y)^2 \ln(1 - y(1-y)x - i0) & \text{(Scalar)}, \end{cases} \quad (1.2)$$

where the first (second) line corresponds to a fermionic (scalar) WIMP, respectively. The coefficients C_1 and C_2 for an $SU(2)_L$ n -plet WIMP with hypercharge Y are given by

$$C_1 = \frac{\kappa}{8} n Y^2, \quad (1.3)$$

$$C_2 = \frac{\kappa}{8} I(n), \quad (1.4)$$

where $\kappa = 1, 2, 8, 16$ for a real scalar, a complex scalar, a Weyl or Majorana fermion, and a Dirac fermion, respectively. $I(n)$ is the Dynkin index for the n dimensional representation of $SU(2)_L$ defined in Eq. (??). The coefficients are uniquely determined by the representation of the WIMPs. For example, $(C_1, C_2) = (1, 1)$ for Higgsino, and $(C_1, C_2) = (0, 2)$ for Wino. We emphasize that, contrary to the usual effective field theory, our prescription is equally applied when the typical scale of the gauge boson four-momentum q is larger than the WIMP mass scale m since we do not perform a derivative expansion of f in Eq. (1.1). It is important because, as we see soon, the effect of the WIMPs is maximized when $\sqrt{q^2} \sim m$, where the derivative expansion is not applicable.

At the leading order (LO), we are interested in $u(p) \bar{u}(p') \rightarrow \ell^-(k) \ell^+(k')$ and $d(p) \bar{d}(p') \rightarrow \ell^-(k) \ell^+(k')$ as the NC processes and $u(p) \bar{d}(p') \rightarrow \nu(k) \ell^+(k')$ and $d(p) \bar{u}(p') \rightarrow \ell^-(k) \bar{\nu}(k')$ as the CC processes. Here, u and d collectively denote up-type and down-type quarks,

^{‡1}Here we neglect a small mass splitting among the $SU(2)_L$ multiplet.

^{‡2}If a WIMP interacts only through the electroweak interaction, its decay width is of $O(1)\%$ or less of its mass even if it is unstable. We assume that this is the case, and neglect the small effect on the function $f(x)$ due to the small decay width. Also, $f(x)$ corresponds to the finite part of the WIMP loop contribution after performing the renormalization in the $\overline{\text{MS}}$ scheme.

Fermion f	$v_f^{(\gamma)}$	$a_f^{(\gamma)}$	$v_f^{(Z)}$	$a_f^{(Z)}$	$v_f^{(W)}$	$a_f^{(W)}$
up-type quark	$\frac{2}{3}e$	0	$(\frac{1}{4} - \frac{2}{3}s_W^2)g_Z$	$-\frac{1}{4}g_Z$	$\frac{1}{2\sqrt{2}}g$	$-\frac{1}{2\sqrt{2}}g$
down-type quark	$-\frac{1}{3}e$	0	$(-\frac{1}{4} + \frac{1}{3}s_W^2)g_Z$	$\frac{1}{4}g_Z$	$\frac{1}{2\sqrt{2}}g$	$-\frac{1}{2\sqrt{2}}g$
lepton	$-e$	0	$(-\frac{1}{4} + s_W^2)g_Z$	$\frac{1}{4}g_Z$	$\frac{1}{2\sqrt{2}}g$	$-\frac{1}{2\sqrt{2}}g$

Table 1: Coefficients of the weak interaction defined as $\Gamma_f^{(V)} \equiv v_f^{(V)} + a_f^{(V)}\gamma_5$. Here, $e = g s_W$ and $g_Z = g/c_W$, where $s_W \equiv \sin \theta_W$ and $c_W \equiv \cos \theta_W$ with θ_W being the weak mixing angle.

respectively, and p, p', k , and k' are initial and final state momenta. In the SM, the amplitudes for both the NC and CC processes at the LO are expressed as

$$\mathcal{M}_{\text{SM}} = \sum_V \frac{\left[\bar{v}(p') \gamma^\mu \Gamma_q^{(V)} u(p) \right] \left[\bar{u}(k) \gamma_\mu \Gamma_\ell^{(V)} v(k') \right]}{s' - m_V^2}, \quad (1.5)$$

where $\sqrt{s'}$ is the invariant mass of the final state leptons, which is denoted as $m_{\ell\ell}$ for the NC processes and $m_{\ell\nu}$ for the CC processes. The relevant gauge bosons are $V = \gamma, Z$ for the NC processes and $V = W^\pm$ for the CC processes, with m_V being the corresponding gauge boson mass. In addition,

$$\Gamma_f^{(V)} \equiv v_f^{(V)} + a_f^{(V)}\gamma_5, \quad (1.6)$$

with $v_f^{(V)}$ and $a_f^{(V)}$ given in Tab. 1. The WIMP contribution is given by

$$\mathcal{M}_{\text{WIMP}} = \sum_{V, V'} C_{VV'} s' f \left(\frac{s'}{m^2} \right) \frac{\left[\bar{v}(p') \gamma^\mu \Gamma_q^{(V)} u(p) \right] \left[\bar{u}(k) \gamma_\mu \Gamma_\ell^{(V')} v(k') \right]}{(s' - m_V^2)(s' - m_{V'}^2)}, \quad (1.7)$$

where $C_{\gamma\gamma} = 4(C_1 g'^2 c_W^2 + C_2 g^2 s_W^2)$, $C_{\gamma Z} = C_{Z\gamma} = 4(C_2 g^2 - C_1 g'^2) s_W c_W$, $C_{ZZ} = 4(C_1 g'^2 s_W^2 + C_2 g^2 c_W^2)$, and $C_{WW} = 4C_2 g^2$. Again $V, V' = \gamma, Z$ for the NC processes and $V, V' = W^\pm$ for the CC processes.

We use $d\Pi_{\text{LIPS}}$ for a Lorentz invariant phase space factor for the two particles final state. Then, using Eqs. (1.5) and (1.7), we define

$$\frac{d\sigma_{\text{SM}}}{d\sqrt{s'}} = \sum_{\alpha, \beta} \frac{dL_{\alpha\beta}}{d\sqrt{s'}} \int d\Pi_{\text{LIPS}} |\mathcal{M}_{\text{SM}}(q_\alpha q_\beta \rightarrow \ell\ell/\ell\nu)|^2, \quad (1.8)$$

$$\frac{d\sigma_{\text{WIMP}}}{d\sqrt{s'}} = \sum_{\alpha, \beta} \frac{dL_{\alpha\beta}}{d\sqrt{s'}} \int d\Pi_{\text{LIPS}} 2\Re[\mathcal{M}_{\text{SM}} \mathcal{M}_{\text{WIMP}}^* (q_\alpha q_\beta \rightarrow \ell\ell/\ell\nu)], \quad (1.9)$$

where we take the average and summation over spins. Here, $dL_{\alpha\beta}/d\sqrt{s'}$ is the so-called luminosity function for a fixed $\sqrt{s'}$:

$$\frac{dL_{\alpha\beta}}{d\sqrt{s'}} \equiv \frac{1}{s} \int_0^1 dx_1 dx_2 f_\alpha(x_1) f_\beta(x_2) \delta\left(\frac{s'}{s} - x_1 x_2\right), \quad (1.10)$$

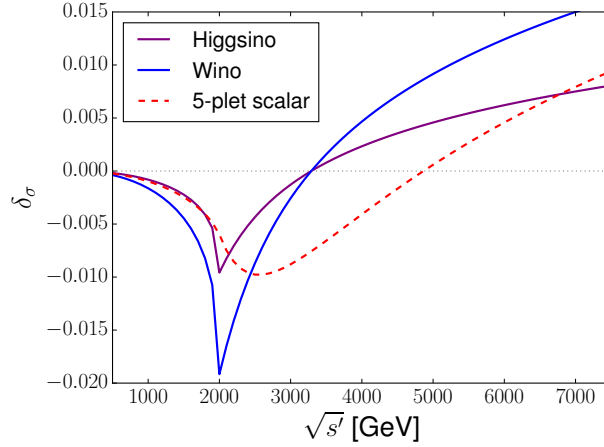


Figure 3: δ_σ for the CC processes as a function of $\sqrt{s'} = m_{\ell\nu}$. The purple, blue, and red lines correspond to Higgsino, Wino, and 5-plet real scalar, respectively.

where α and β denote species of initial partons, $\sqrt{s} = 100$ TeV, and $f_a(x)$ is the PDF used in Sec. ???. Eq. (1.8) represents the SM cross section, while Eq. (1.9) the WIMP contribution to the cross section. For the statistical treatment in the next section, we introduce a parameter μ that parametrizes the strength of the WIMP effect, and express the cross section with μ as

$$\frac{d\tilde{\sigma}}{d\sqrt{s'}} = \frac{d\sigma_{\text{SM}}}{d\sqrt{s'}} + \mu \frac{d\sigma_{\text{WIMP}}}{d\sqrt{s'}}. \quad (1.11)$$

Obviously, $\mu = 0$ corresponds to the pure SM, while $\mu = 1$ corresponds to the SM+WIMP model. Hereafter, we use

$$\delta_\sigma(\sqrt{s'}) \equiv \frac{d\sigma_{\text{WIMP}}/d\sqrt{s'}}{d\sigma_{\text{SM}}/d\sqrt{s'}}, \quad (1.12)$$

to denote the correction from the WIMP. Note that this ratio remains unchanged even if we take into account the next-to-leading order (NLO) QCD effect because the EWIMPs affect the cross sections only through the vacuum polarization.^{‡3}

In Fig. 3, we plot δ_σ for the CC processes as a function of $\sqrt{s'}$. The purple, blue, and red lines correspond to Higgsino, Wino, and 5-plet scalar, respectively. There is a dip around $\sqrt{s'} = 2m$ for all the cases of the WIMPs which originates from the loop function f in Eq. (1.2). The WIMP contributions to the NC processes show a similar dip structure that again comes from f . This dip is crucial not only for the discovery of the WIMP signal (see

^{‡3}When the NLO QCD effect is included, one of the initial partons can be gluon with the real emission of one jet in the final state. However, we can easily see that $\delta_\sigma^{ug} = \delta_\sigma^{uu}$ and so on.

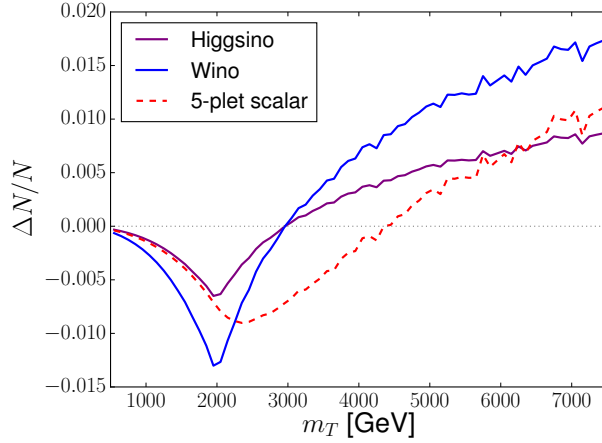


Figure 4: The WIMP effect on the ratio of the number of events $\Delta N/N$ as a function of m_T . The line colors are the same as Fig. 3.

Sec. 1.2.3) but also for the determination of the properties of the WIMPs (see Sec. 1.2.4). In particular, the WIMP mass can be extracted from the dip position, while the WIMP charges (n and Y) can be determined from the depth of the dip.

For the NC processes, the momenta of two final state charged leptons are measurable and we can use the invariant mass distribution of the number of events for the study of the WIMPs. For the CC processes, on the contrary, we cannot measure the momentum of the neutrino in real experiments, and hence we instead use the missing transverse momentum \not{p}_T . We use the transverse mass defined as

$$m_T^2 \equiv 2p_{T,\ell}\not{p}_T(1 - \cos \phi), \quad (1.13)$$

where $p_{T,\ell}$ denotes the transverse momentum of the charged lepton and ϕ is the difference between the azimuth angles of $p_{T,\ell}$ and \not{p}_T . The important property of m_T is that the distribution of m_T peaks at $m_T = m_{\ell\nu}$ (see Appendix. ?? for more detailed description of the quantity m_T). Because of this property, the characteristic shape of δ_σ remains in the m_T distribution in the CC events. To see this, we plot in Fig. 4 the WIMP effect on the number of events as a function of m_T . Here, the vertical axis is the ratio of the WIMP correction to the number of events ΔN to the number of events in the SM N for each bin with the bin width of 100 GeV.^{‡4} We find that the dip structure remains in the m_T distribution, though the depth of the dip is smaller compared to the $m_{\ell\nu}$ distribution.

^{‡4}Just for an illustrative purpose, we generate events corresponding to the integrated luminosity $\mathcal{L} = 1 \text{ ab}^{-1}$ for this figure, which is not the same luminosity as we use in the next section (see Sec. 1.2.1 for details of the event generation).

1.2 Analysis

1.2.1 Event generation

Now we discuss how well we can extract information about WIMPs from the invariant mass and transverse mass distributions for the processes of our concern at future 100 TeV pp collider experiments. We take into account the effects of the next-to-leading order QCD corrections in the events as well as detector effects through Monte-Carlo simulations.

In our analysis, we first generate the SM event sets for the NC processes $pp \rightarrow e^-e^+/\mu^-\mu^+$ and for the CC processes $pp \rightarrow e^\pm\nu_e/\mu^\pm\nu_\mu$. We use `MadGraph5_aMC@NLO` (v2.6.3.2) [20, 21] for the event generation with the successive use of `Pythia8` [22] for the parton shower and the hadronization and `Delphes` (v3.4.1) [23] with the card `FCChh.tcl` for the detector simulation. We use `NNPDF2.3QED` with $\alpha_s(M_Z) = 0.118$ [24] as a canonical set of PDFs. For the renormalization and factorization scales, we use the default values of `MadGraph5_aMC@NLO`, i.e., the central m_T^2 scale after k_T -clustering of the event (which we denote by Q). We take into account the NLO QCD effect by the `[QCD]` option of `MadGraph5_aMC@NLO` since it enhances the cross section roughly by a factor of 2 compared to the LO calculation.^{‡5} The events are binned by the characteristic mass m_{char} for each process: we use the lepton invariant mass $m_{\text{char}} = m_{\ell\ell}$ for the NC processes, and the transverse mass $m_{\text{char}} = m_T$ for the CC processes, respectively. In both cases, we generated events with the characteristic mass within the range of $500 \text{ GeV} < m_{\text{char}} < 7.5 \text{ TeV}$ and divide them into 70 bins with the equal width of 100 GeV.

As for the event selection by a trigger, we may have to impose some cut on the lepton transverse momentum p_T . As we will see, we concentrate on events with high p_T charged lepton(s) with which we expect the event may be triggered. For the NC processes, we use events with at least two high p_T leptons. For our analysis, we use events with $m_{\ell\ell} > 500 \text{ GeV}$; we assume that such events are triggered by using two energetic charged leptons so that we do not impose extra kinematical requirements. On the contrary, the CC events are characterized only by a lepton and a missing transverse momentum. For such events, we require that the p_T of the charged lepton should be larger than 500 GeV.^{‡6} For the CC events, the cut reduces the number of events in particular for the bins with the low transverse mass $m_T \sim 500 \text{ GeV}$, and thus affects the sensitivity of the CC processes to relatively light WIMPs. We will come back to this point later.

^{‡5}This large enhancement implies that the next-to-next-to-leading order QCD effect may also have a non-negligible effect on the cross section, and its calculation remains as a future task. However, due to its smooth dependence on $\sqrt{s'}$, it may not much affect the detection reach of the EWIMPs. See Sec. 1.2.2 for the details.

^{‡6}In the ATLAS analysis of the mono-lepton signal during the 2015 (2016) data taking period [25], they use the event selection condition $p_T > 24$ (60) GeV for leptons that satisfy the *medium* identification criteria. In the CMS analysis during the period on 2016 [26], they use the condition $p_T > 130$ (53) GeV for an electron (a muon).

The WIMP effect is incorporated by rescaling the SM event by δ_σ defined in Eq. (1.12). With the parameter μ defined in Eq. (1.11), the number of events corresponding to the SM+WIMP hypothesis in i -th bin, characterized by $m_{i,\min} < m_{\text{char}} < m_{i,\max}$, is

$$x_{f,i}(\mu) = \sum_{m_{i,\min} < m_{\text{char}} < m_{i,\max}} \left[1 + \mu \delta_\sigma(\sqrt{s'}) \right], \quad (1.1)$$

where the sum runs over all the events of the final state f whose characteristic mass m_{char} (after taking into account the detector effects) falls into the bin. Note that the true value of $\sqrt{s'}$ should be used for each event for the computation of δ_σ : we extract it from the hard process information.^{‡7}

1.2.2 Statistical treatment

We now explain the statistical method we will adopt in our analysis. Throughout this section, we rely on the so-called profile likelihood method, which is described in detail in Appendix ???. We collectively denote our theoretical model as $\mathbf{x}_f(\mu) = \{x_{f,i}(\mu)\}$, where $x_{f,i}(\mu)$ is given by Eq. (1.1). We denote the experimental data set as $\tilde{\mathbf{x}}_f$ that in principle is completely unrelated to our theoretical model $\mathbf{x}_f(\mu)$. Since we do not have an actual experimental data set for 100 TeV colliders for now, however, we take $\tilde{\mathbf{x}}_f = \mathbf{x}_f(\mu = 1)$ (for some fixed values of the WIMP mass and charges) throughout our analysis, assuming that the WIMP does exist. In particular, this choice tests the SM-only hypothesis if we take our theoretical model as $\mathbf{x}_f(\mu = 0)$.

If the expectation values of $x_{f,i}(\mu)$ are precisely known, the sensitivity to WIMPs can be studied only with statistical errors. In reality, however, the computation of $x_{f,i}(\mu)$ suffers various sources of uncertainties, which results in systematic errors in our theoretical model. The sources include errors in the integrated luminosity, the beam energy, choices of the renormalization and the factorization scales, choices of PDF, the pile-up effect, higher order corrections to the cross section, and so on. In order to deal with these uncertainties, we introduce sets of free parameters $\boldsymbol{\theta}_f = \{\theta_{f,\alpha}\}$ (i.e. nuisance parameters) which absorb (smooth) uncertainties of the number of events, and modify our theoretical model as

$$\tilde{x}_{f,i}(\boldsymbol{\theta}_f, \mu) \equiv x_{f,i}(\mu) f_{\text{sys},i}(\boldsymbol{\theta}_f), \quad (1.2)$$

where $f_{\text{sys},i}(\boldsymbol{\theta}_f)$ is a function that satisfies $f_{\text{sys},i}(\mathbf{0}) = 1$. We expect that, if the function $f_{\text{sys},i}$ is properly chosen, the true distribution of the number of events in the SM is given by $\tilde{\mathbf{x}}_f(\boldsymbol{\theta}_f, 0) = \{\tilde{x}_{f,i}(0) f_{\text{sys},i}(\boldsymbol{\theta}_f)\}$ for some value of $\boldsymbol{\theta}_f$. In our analysis, we adopt the five

^{‡7}The p_T cut for the CC process does not affect this estimation since the WIMP does not modify the angular distribution of the final lepton and neutrino for the CC process.

parameters fitting function given by [27]

$$f_{\text{sys},i}(\boldsymbol{\theta}_f) = e^{\theta_{f,1}}(1 - p_i)^{\theta_{f,2}} p_i^{(\theta_{f,3} + \theta_{f,4} \ln p_i + \theta_{f,5} \ln^2 p_i)}, \quad (1.3)$$

where $p_i = 2m_i/\sqrt{s}$ with m_i being the central value of the lepton invariant mass (transverse mass) of the i -th bin for the NC (CC) processes. As we will see, the major effects of systematic errors can be absorbed into $\boldsymbol{\theta}_f$ with this fitting function.

To test the SM-only hypothesis, we define the following test statistic [28]:

$$q_0 \equiv -2 \sum_{f=\ell\ell, \ell\nu} \ln \frac{L(\tilde{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, \mu = 0)}{L(\tilde{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, \hat{\mu})}. \quad (1.4)$$

Here, $\hat{\boldsymbol{\theta}}_f$ and $\{\hat{\boldsymbol{\theta}}_f, \hat{\mu}\}$ are determined so that $\prod_f L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, \mu = 0)$ and $\prod_f L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, \mu)$ are maximized, respectively. The likelihood function is defined as

$$L(\tilde{\mathbf{x}}_f; \boldsymbol{\theta}_f, \mu) \equiv L_{\boldsymbol{\theta}_f}(\tilde{\mathbf{x}}_f; \mu) L'(\boldsymbol{\theta}_f; \boldsymbol{\sigma}_f), \quad (1.5)$$

where

$$L_{\boldsymbol{\theta}_f}(\tilde{\mathbf{x}}_f; \mu) \equiv \prod_i \exp \left[-\frac{(\tilde{x}_{f,i} - \tilde{x}_{f,i}(\boldsymbol{\theta}_f, \mu))^2}{2\tilde{x}_{f,i}(\boldsymbol{\theta}_f, \mu)} \right], \quad (1.6)$$

$$L'(\boldsymbol{\theta}_f; \boldsymbol{\sigma}_f) \equiv \prod_{\alpha} \exp \left[-\frac{\theta_{f,\alpha}^2}{2\sigma_{f,\alpha}^2} \right]. \quad (1.7)$$

The product in Eq. (1.6) runs over all the bins, while the product in Eq. (1.7) runs over all the free parameters we introduced. For each $\theta_{f,\alpha}$, we define the “standard deviation” $\sigma_{f,\alpha}$, which parametrizes the possible size of $\theta_{f,\alpha}$ within the SM with the systematic errors.^{b8} If the systematic errors are negligible compared with the statistical error, we can take $\boldsymbol{\sigma}_f \rightarrow \mathbf{0}$, while the analysis with $\boldsymbol{\sigma}_f \rightarrow \infty$ assumes no knowledge of systematic errors and gives a conservative result. We identify $\sqrt{q_0} = 5$ (1.96) as the detection reach at the 5σ (95 % C.L.) level, since q_0 asymptotically obeys a chi-square distribution with the degree of freedom one.

In order to determine $\boldsymbol{\sigma}_f$, we consider the following sources of the systematic errors:

- Luminosity ($\pm 5\%$ uncertainty is assumed),
- Renormalization scale ($2Q$ and $Q/2$, instead of Q),
- Factorization scale ($2Q$ and $Q/2$, instead of Q),

^{b8}Here we assume the Gaussian form for the nuisance parameter distribution. The dependence of the results on the choice of the distribution will be discussed later in Sec. 1.2.3.

- PDF choice (We use 101 variants of NNPDF2.3QED with $\alpha_s(M_Z) = 0.118$ [24] provided by LHAPDF6 [29] with IDs ranging from 244600 to 244700).

The values of σ_f are determined as follows. Let \mathbf{y}_f be the set of number of events in the SM for the final state f with the canonical choices of the parameters, and \mathbf{y}'_f be that with one of the sources of the systematic errors being varied. We minimize the chi-square function defined as

$$\chi_f^2 \equiv \sum_i \frac{(y'_{f,i} - \tilde{y}_{f,i}(\boldsymbol{\theta}_f))^2}{\tilde{y}_{f,i}(\boldsymbol{\theta}_f)}, \quad (1.8)$$

where

$$\tilde{y}_{f,i}(\boldsymbol{\theta}_f) \equiv y_{f,i} f_{\text{sys},i}(\boldsymbol{\theta}_f), \quad (1.9)$$

for each final state f , and determine the best-fit values of $\boldsymbol{\theta}_f$ for each set of \mathbf{y}'_f . We repeat this process for different sets of \mathbf{y}'_f , and σ_f are determined from the distributions of the best-fit values of $\boldsymbol{\theta}_f$. For example, let us denote the best-fit values for the fit associated with the luminosity errors $\pm 5\%$ as $\boldsymbol{\theta}_f^\pm$. We estimate σ_f associated with these errors, denoted here as $\sigma_f^{\text{lumi.}}$, as

$$\sigma_{f,\alpha}^{\text{lumi.}} = \sqrt{\frac{(\theta_{f,\alpha}^+)^2 + (\theta_{f,\alpha}^-)^2}{N}}, \quad (1.10)$$

where N denotes the number of fitting procedures we have performed: $N = 2$ for this case. We estimate σ_f associated with the other sources of the errors, denoted as $\sigma_f^{\text{ren.}}$, $\sigma_f^{\text{fac.}}$, and σ_f^{PDF} , in a similar manner. Finally, the total values of σ_f are obtained by combining all the sources together as^{‡9}

$$\sigma_{f,\alpha} = \sqrt{(\sigma_{f,\alpha}^{\text{lumi.}})^2 + (\sigma_{f,\alpha}^{\text{ren.}})^2 + (\sigma_{f,\alpha}^{\text{fac.}})^2 + (\sigma_{f,\alpha}^{\text{PDF}})^2}. \quad (1.11)$$

In Tables 2 and 3, we show the values of σ_{ee} and $\sigma_{e\nu_e}$ associated with each source of the systematic errors, respectively. These values can be interpreted as the possible size of the fit parameters within the SM, which is caused by the systematic uncertainties. As explained in Eq. (1.11), we combine these values in each column to obtain σ_f . In Table 4, we summarize the result of the combination for all the final states. The values of σ_f are independent of the final state lepton flavors since the energy scale of our concern is much higher than the lepton masses. However, we use different sets of fit parameters $\boldsymbol{\theta}_{ee}$ and $\boldsymbol{\theta}_{\mu\mu}$ for the NC processes

^{‡9}There may be some correlations between the distribution of nuisance parameters $\boldsymbol{\theta}_f$. In this section, we treat each of them as obeying to an independent Gaussian distribution for simplicity.

Sources of systematic errors	$\sigma_{ee,1}$	$\sigma_{ee,2}$	$\sigma_{ee,3}$	$\sigma_{ee,4}$	$\sigma_{ee,5}$
Luminosity: $\pm 5\%$ ($\sigma_{ee}^{\text{lumi.}}$)	0.05	0	0	0	0
Renormalization scale: $2Q, Q/2$ ($\sigma_{ee}^{\text{ren.}}$)	0.4	0.6	0.3	0.05	0.004
Factorization scale: $2Q, Q/2$ ($\sigma_{ee}^{\text{fac.}}$)	0.3	0.5	0.2	0.06	0.004
PDF choice (σ_{ee}^{PDF})	0.4	0.7	0.3	0.06	0.004

Table 2: Values of σ_{ee} for each source of systematic errors. The result is the same for the $\mu\mu$ final state.

Sources of systematic errors	$\sigma_{e\nu_e,1}$	$\sigma_{e\nu_e,2}$	$\sigma_{e\nu_e,3}$	$\sigma_{e\nu_e,4}$	$\sigma_{e\nu_e,5}$
Luminosity: $\pm 5\%$ ($\sigma_{e\nu_e}^{\text{lumi.}}$)	0.05	0	0	0	0
Renormalization scale: $2Q, Q/2$ ($\sigma_{e\nu_e}^{\text{ren.}}$)	0.3	0.4	0.2	0.04	0.003
Factorization scale: $2Q, Q/2$ ($\sigma_{e\nu_e}^{\text{fac.}}$)	1.0	1.6	0.6	0.1	0.01
PDF choice ($\sigma_{e\nu_e}^{\text{PDF}}$)	0.6	0.9	0.4	0.08	0.006

Table 3: Best fit values of fit parameters for several sources of systematic errors for the $e\nu_e$ final state. The result is the same for the $\mu\nu_\mu$ final state.

and $\theta_{e\nu_e}$ and $\theta_{\mu\nu_\mu}$ for the CC processes because of the different detector response to electrons and muons.

Several comments on other possible sources of systematic errors are in order. As for the beam energy error, we could not generate events at NLO due to the lack of sufficient computational power. Instead, we checked at LO that the corresponding values of σ (assuming that the uncertainty of the beam energy is 1%) are small enough, and hence we simply ignored it. Two of the remaining sources are the pile-up effect and the underlying event, but they may be thought of as negligible since we are focusing on the very clean signal of two energetic leptons. Another one is the effect of higher order corrections to the cross section and that of background processes which are not considered in our analysis. It is in principle possible to estimate their effects through the simulation and improve the analysis but here we just leave it as a future task. Related to this, we note here that a smooth change of the number of events in general, possibly including the uncertainty listed above, could be absorbed by a minimization procedure using some fitting function like in Eq. (1.3). On the other hand, as we will discuss below, the WIMP signal can not be fully absorbed by the fit because of the sharp bend we mentioned before.

We have also neglected the systematic errors from the detector effect. The main errors are expected to come from the lepton identification, in which some of the leptons in any process are overlooked or identified incorrectly, resulting in the mis-reconstruction of the

Final state f	$\sigma_{f,1}$	$\sigma_{f,2}$	$\sigma_{f,3}$	$\sigma_{f,4}$	$\sigma_{f,5}$
ee	0.7	1.0	0.4	0.09	0.008
$\mu\mu$	0.7	1.0	0.4	0.09	0.008
$e\nu_e$	1.2	1.9	0.7	0.2	0.01
$\mu\nu_\mu$	1.2	1.9	0.7	0.2	0.01

Table 4: Summary of standard deviations σ_f for each final state.

event topology. Again, it is expected that the small and smooth modification of the number of events may be absorbed into the choice of nuisance parameters, if the corresponding values of σ_f are properly taken into account in addition to the values in Tables 2 and 3. What is dangerous is the possible jerky modification that mimics the WIMP signal, which may be induced by the detector setup, the complicated detector response to leptons, and so on. Such unwanted fake signals may be avoided by checking the consistency between the electron and muon channels. This is because there should be the same size signals at the same lepton invariant mass in both channels for the WIMP signal, while the detector response to electrons and muons is different and such a coincidence is not expected in general. It may also be helpful to look for similar fake signals in different processes associated with several leptons. In this section, we just assume that these systematic errors from the detector effect are well controlled once the real experiment will start and focus on the theoretical uncertainties listed in tables.

1.2.3 Detection reach

Now we show the detection reach of WIMPs at future 100 TeV colliders. In Fig. 5, we plot the value of $\sqrt{q_0}$ as a function of the WIMP mass, with the integrated luminosity $\mathcal{L} = 30 \text{ ab}^{-1}$. As representative scenarios, we show the cases for Higgsino (the left figure) and Wino (the right figure). In both figures, the green and blue dashed lines are the result obtained only from the NC processes and the CC processes, respectively. We find that the CC processes are more sensitive to the effect of the WIMPs than the NC processes because of the larger cross section. This result is consistent with Refs. [8, 9]. The sensitivity of the CC processes is weakened for $m \lesssim 700 \text{ GeV}$ because of the lepton p_T cut we have applied.^{‡10} The combined results of the NC and CC processes are shown by the red solid lines. By combining the two types of processes, the 5σ discovery reaches (95 % C.L. bounds) for Higgsino and Wino

^{‡10}We note here that the sensitivity of the CC processes depends on the lepton p_T cut. For example, adopting the tighter cut, lepton- $p_T > 1 \text{ TeV}$, the CC processes have almost no sensitivity to WIMPs with $m < 1 \text{ TeV}$. Thus, in particular for the purpose of the Higgsino search, it is important to realize the lepton p_T cut as low as $\sim 500 \text{ GeV}$.

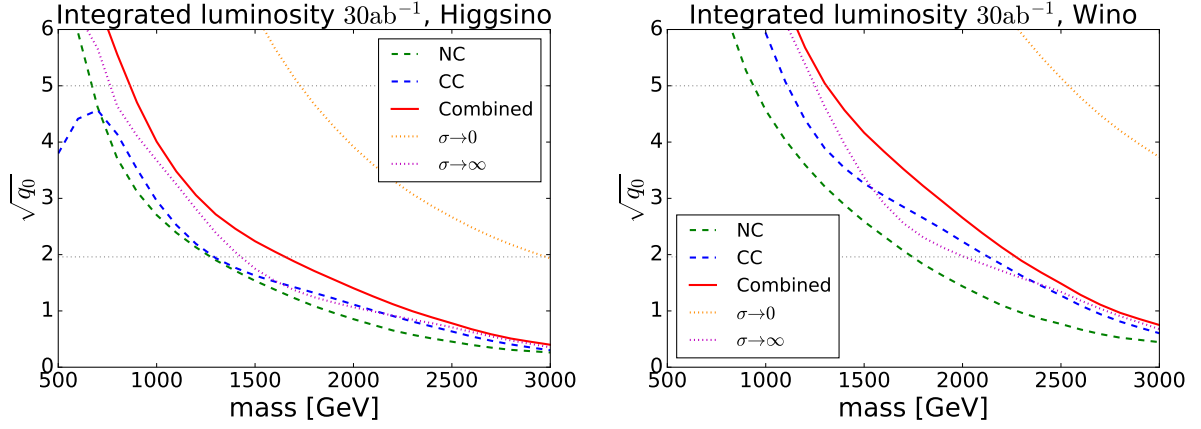


Figure 5: $\sqrt{q_0}$ as a function of the WIMP mass. **Left:** The figure for Higgsino. The green and blue dashed lines represent the result from the NC processes and the CC processes, respectively, while the red solid lines correspond to that from the combined analysis. The orange and purple lines denote the results from the combined analysis with the optimistic $\sigma_f \rightarrow 0$ limit and those with conservative $\sigma_f \rightarrow \infty$ limit, respectively. **Right:** The same for Wino. (♣ Also show a figure for MDM! ♣)

are 850 GeV (1.7 TeV) and 1.3 TeV (2.3 TeV), respectively. We find that the combination of the NC and CC processes improves the sensitivity of the WIMP mass. Furthermore, if we understand all the systematic uncertainties quite well and effectively take the $\sigma_f \rightarrow 0$ limit in the combined result, the detection reach will be pushed up significantly as shown by the orange dotted lines: 1.1 TeV Higgsino signal at well above 5σ level and a 4σ hint of the 2.9 TeV Wino. These lines should be compared with the combined results and also with those obtained from the conservative analysis with $\sigma_f \rightarrow \infty$ shown by the purple dotted lines, assuming no knowledge about sources of systematic errors. The plot shows us that it is essential to reduce the systematic uncertainties for the detection of WIMPs through the NC and CC processes.

We also show the detection reach of the MDM scenario in Fig. ???. The 5σ reaches are ??? TeV and ??? TeV for 5-plet fermion and 7-plet scalar, while the 95 % reaches are ??? TeV and ??? TeV. They are lowered to ??? TeV and ??? TeV (5σ) and ??? TeV and ??? TeV (95 % C.L.) when the systematic errors are included. If we assume the vanilla thermal freeze-out scenario, the mass should be 10 TeV for 5-plet fermion and 25 TeV for 7-plet scalar [30]. Thus, our method probes only a part of the allowed mass range for these multiplets. (♣ Fill the values, and 5-plet scalar, maybe? ♣)

Next, we plot in Fig. 6 the contribution of each bin to the value of q_0 to take a closer look at the significance of the dip structure, focusing on the NC processes as an example.

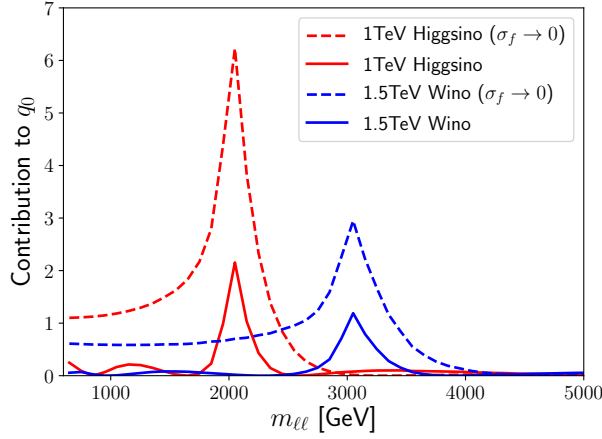


Figure 6: Plot of the contribution of each bin to the value of q_0 for the NC processes. The red (blue) lines correspond to the 1 TeV Higgsino (1.5 TeV Wino). The solid and dotted lines correspond to the results with the fitting procedure and those without it (*i.e.*, the $\sigma_f \rightarrow 0$ limit), respectively.

The red (blue) lines correspond to the 1 TeV Higgsino (1.5 TeV Wino), while the solid and dotted lines correspond to the results with the fitting procedure and those without it (*i.e.*, the $\sigma_f \rightarrow 0$ limit), respectively. We can see that the most contributions come from the bins around the peak at $m_{\ell\ell} = 2m$. This feature is clearer for the fitting based approach, where all the smooth parts of the correction are absorbed into the fit parameters, thus there is almost no contribution to q_0 from the bins other than $m_{\ell\ell} \sim 2m$. Note also that, for the $\sigma_f \rightarrow 0$ analysis, there are more contributions from the bins with lower $m_{\ell\ell}$ than those with higher $m_{\ell\ell}$, though sometimes the WIMP effect on the cross section is much larger in the latter bins. This is just because of the difference of number of events in each bin, that is $\mathcal{O}(10^7)$ for $500 \text{ GeV} < m_{\ell\ell} < 600 \text{ GeV}$, while $\mathcal{O}(10^3)$ for $4900 \text{ GeV} < m_{\ell\ell} < 5000 \text{ GeV}$ in our set up, for instance. The similar behavior can be expected also for the CC processes.

So far, we have adopted the assumption that the distribution of the nuisance parameters is the Gaussian form and that the fitting function Eq. (1.3) is sufficient for treating systematic errors. In order to discuss the dependence of the results on these assumptions, we have repeated the same analysis using another distribution or fitting function. In the former case, we have adopted the top-hat distribution: the likelihood function for the nuisance parameters L' is given by

$$L'(\theta_f; \sigma_f) \equiv \prod_{\alpha} \Theta \left(\sqrt{3} \sigma_{f,\alpha} - |\theta_{f,\alpha}| \right), \quad (1.12)$$

where Θ is the Heaviside step function. This corresponds to the top-hat distribution of $\theta_{f,\alpha}$ with the variance $\sigma_{f,\alpha}^2$ for each α . As for an example of another fitting function, we have

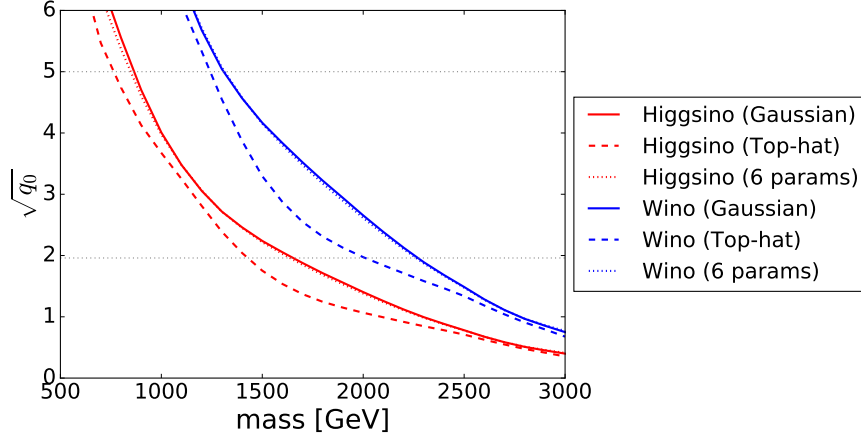


Figure 7: $\sqrt{q_0}$ as a function of the WIMP mass using both the NC and CC processes. The convention for the line colors is the same as Fig. 5. The line styles denote the result same as Fig. 5 (solid), that with the top-hat distribution (dashed), and that with the six parameters fitting function (dotted).

adopted a simple one parameter extension of Eq. (1.3)

$$f_{\text{sys},i}(\theta_f) = e^{\theta_{f,1}}(1 - p_i)^{\theta_{f,2}} p_i^{(\theta_{f,3} + \theta_{f,4} \ln p_i + \theta_{f,5} \ln^2 p_i + \theta_{f,6} \ln^3 p_i)}, \quad (1.13)$$

which consists of six parameters. The variances of the nuisance parameters are estimated in the same way as Sec. 1.2.2, but now with the six parameters.

In Fig. 7, we show the corresponding results for Higgsino and Wino as an example. The convention for the line colors is the same as Fig. 5, while the line styles denote different procedures: the dashed and dotted lines correspond to the result with the top-hat distribution and that with the six parameters fitting function, respectively, while solid lines are the same as Fig. 5. From the figure, we can see that the choice of the distribution may slightly affect the result, while the addition of a nuisance parameter as Eq. (1.13) causes almost no effect. The size of the effect of the choice of the distribution for the current estimation of errors σ_f is about 100 GeV (200 GeV) for the 5σ (95 % C.L.) bounds. We expect that such uncertainties due to the procedure to include the systematic errors will be reduced once the data from the real experiment (and hence better understanding of the systematic errors) will become available.

1.2.4 Determination of WIMP properties

In this subsection, we show that it is possible to determine the properties of the WIMPs from the NC and CC processes, thanks to the fact that we can study the $m_{\ell\ell}$ and m_T distribution in great detail for these processes. Some information about the mass, charge, and spin of

the WIMPs can be extracted because the corrections to these distributions from the WIMPs are completely determined by these WIMP properties. Firstly, we can extract the WIMP mass from the position of the dip-like structure in the correction since it corresponds to roughly twice the WIMP mass as we have shown in Sec. 1.1. Secondly, the overall size of the correction gives us information about the $SU(2)_L$ and $U(1)_Y$ charges. The CC processes depend only on the $SU(2)_L$ charge, while the NC processes depend both on the $SU(2)_L$ and $U(1)_Y$ charges. Consequently, we can obtain information about the gauge charges of the WIMPs from the NC and CC processes.

We now demonstrate the mass and charge determination of fermionic WIMPs. This is equivalent to the determination of the parameter set (m, C_1, C_2) . We generate the data assuming the SM + WIMP model ($\mu = 1$) with some specific values of m, n, Y , and κ , with which we obtain (m, C_1, C_2) . We fix $\mu = 1$ for our theoretical model as well, and hence the theoretical predictions of the number of events also depend on these three parameters, $\mathbf{x}_f = \mathbf{x}_f(m, C_1, C_2)$. We define the likelihood function $L(\check{\mathbf{x}}_f; \boldsymbol{\theta}_f, m, C_1, C_2)$ in the same form as Eqs. (1.2) and (1.5) with the theoretical prediction \mathbf{x}_f now understood as a function of (m, C_1, C_2) , not of μ .^{‡11} The test statistic is defined as

$$q(m, C_1, C_2) \equiv -2 \sum_f \ln \frac{L(\check{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, m, C_1, C_2)}{L(\check{\mathbf{x}}_f; \hat{\boldsymbol{\theta}}_f, \hat{m}, \hat{C}_1, \hat{C}_2)}, \quad (1.14)$$

where the parameters $(\{\hat{\boldsymbol{\theta}}_f\}, \hat{m}, \hat{C}_1, \hat{C}_2)$ maximize $\prod_f L(\check{\mathbf{x}}_f; \boldsymbol{\theta}_f, m, C_1, C_2)$, while $\hat{\boldsymbol{\theta}}_f$ maximize $L(\check{\mathbf{x}}_f; \boldsymbol{\theta}_f, m, C_1, C_2)$ for fixed values of (m, C_1, C_2) . It follows the chi-squared distribution with three degrees of freedom in the limit of a large number of events [31]. The test statistic defined in this way examines the compatibility of a given WIMP model (i.e. a parameter set (m, C_1, C_2)) with the observed signal.

Once a deviation from the SM prediction is observed in a real experiment, we may determine (m, C_1, C_2) using the above test statistic q . In the following, we show the expected accuracy of the determination of (m, C_1, C_2) for the case where there exists 1.1 TeV Higgsino.^{‡12}

In Fig. 8, we show the contours of 1σ (dotted) and 2σ (solid) constraints, which correspond to the values $\sqrt{q} = 1.9$ and $\sqrt{q} = 2.8$, respectively, in the C_1 vs. C_2 plane for $m = 1.1$ TeV. The blue, green, and red lines denote the result obtained from the NC processes, the CC processes, and the combined analysis, respectively. The models in the gray region are in more than 2σ tension with the observation. We also show several star markers

^{‡11}As shown in Eqs. (1.3) and (1.4), C_1 and C_2 are positive quantities (and C_2 is discrete). In the figures, however, we extend the C_1 and C_2 axes down to negative regions just for presentation purposes.

^{‡12}The expected significance is 3.5σ for 1.1 TeV Higgsino in our estimation. Even though it is slightly below the 5σ discovery, we take 1.1 TeV Higgsino as an example because it is a candidate of the thermal relic DM.

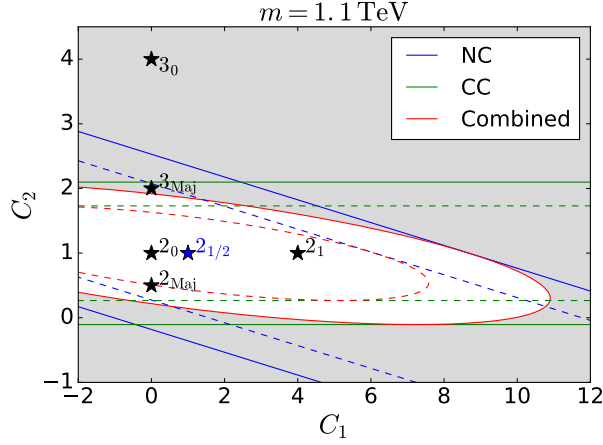


Figure 8: Contour of \sqrt{q} in the C_1 vs. C_2 plane with $m = 1.1$ TeV, where we assume 1.1 TeV Higgsino signal. The dotted and solid lines denote 1σ and 2σ contours, respectively, and the gray region corresponds to the parameter space that is in tension with the observation at more than 2σ level. The blue, green, and red lines correspond to the result from the NC processes, the CC processes, and the combined analysis, respectively. Each star marker annotated as “ n_Y ” represents a point corresponding to a $SU(2)_L$ n -plet Dirac fermion with hypercharge Y , while that with “ n_{Maj} ” corresponds to an $SU(2)_L$ n -plet Majorana fermion.

that correspond to the single $SU(2)_L$ multiplet contributions: the markers with “ n_Y ” represent an $SU(2)_L$ n -plet Dirac fermion with hypercharge Y , while those with “ n_{Maj} ” an $SU(2)_L$ n -plet Majorana fermion. Both the NC and CC constraints are represented as straight bands in the C_1 vs. C_2 plane since each process depends on a specific linear combination of C_1 and C_2 . In particular, the CC constraint is independent of C_1 , or Y . In this sense, the NC and CC processes are complementary to each other, and thus we can separately constrain C_1 and C_2 only after combining these two results. For instance, we can exclude a single fermionic $SU(2)_L$ multiplet with $n \neq 2$ at more than 2σ level, although each process by itself cannot exclude the possibility of 3_{Maj} . We can also constrain the hypercharge, yet it is not uniquely determined. In addition to the Higgsino, the WIMP as an $SU(2)_L$ doublet Dirac fermion with $|Y|^2 \lesssim 2$ or an $SU(2)_L$ doublet Majorana fermion with $|Y|^2 \lesssim 5$ is still allowed.

In Fig. 9, we show the contour plots of \sqrt{q} in the C_1 vs. m plane with $C_2 = 1$ (left) and those in the C_2 vs. m plane with $C_1 = 1$ (right). The star marker in each panel shows the true values of parameters $(C_1, m) = (1, 1.1 \text{ TeV})$ (left) and $(C_2, m) = (1, 1.1 \text{ TeV})$ (right). Again, by combining the NC and CC results, we can significantly improve the determination of WIMP properties, making 1σ and 2σ contours closed circles in the planes of our concern. In particular, as red lines show, the combined analysis allows us to determine the observed WIMP mass at the level of $\mathcal{O}(10)\%$.

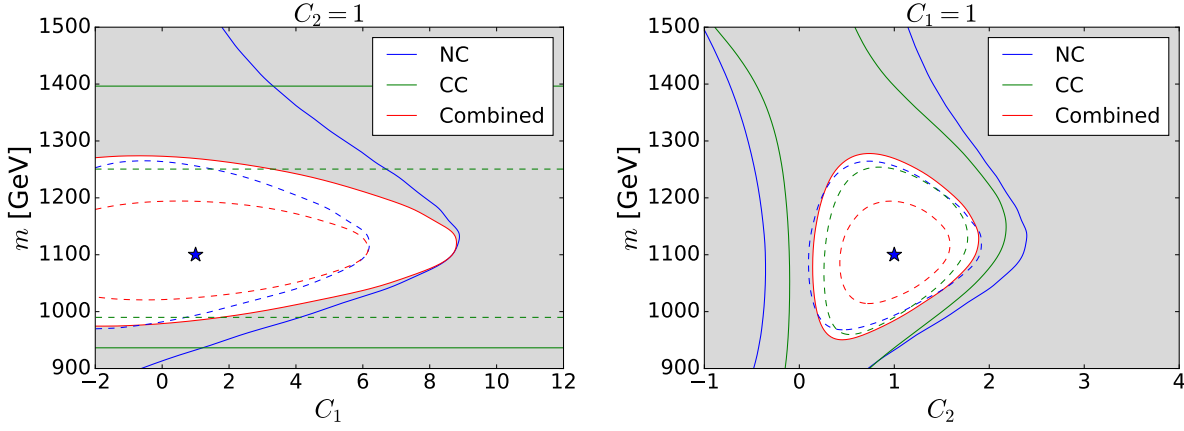


Figure 9: **Left:** Contour of \sqrt{q} in the C_1 vs. m plane with $C_2 = 1$, where we assume the 1.1 TeV Higgsino signal. The colors and styles of lines and the meaning of the gray region are the same as Fig. 8. The star maker corresponds to the true Higgsino property $(C_1, m) = (1, 1.1 \text{ TeV})$. **Right:** Contour of \sqrt{q} in the C_2 vs. m plane for $C_1 = 1$, where we assume the 1.1 TeV Higgsino signal. The star maker corresponds to the true Higgsino property $(C_2, m) = (1, 1.1 \text{ TeV})$.

Finally, we comment on the possibility of discriminating between fermionic and scalar WIMPs, whose difference comes from the loop function $f(x)$ (see Eq. (1.2)). Here we repeat the same analysis explained above, assuming the 1.1 TeV Higgsino signal for example, but use the scalar loop function to evaluate the theoretical predictions $\mathbf{x}_f(m, C_1, C_2)$. In Figs. 10 and 11, we show the results in the C_1 vs. C_2 plane and the C_1 (or C_2) vs. m plane, respectively, where one of the three parameters is fixed to its best fit value. It is seen that, in the case of the 1.1 TeV Higgsino signal, it is hard to distinguish between the bosonic and fermionic WIMPs only with our method. However, if a part of the WIMP properties (in particular its mass) is determined from another approach, our method may allow us to determine its spin correctly.

We also stress here that, with some favorable assumption about the observed signal, we may obtain some hint about its spin. For example, if we assume that the observed signal composes a fraction of the dark matter in our Universe, the choice of the WIMP charges is significantly constrained. Note from Fig. 10 that the only choices of WIMP charges that allow the WIMP multiplet to contain an electrically neutral component are $(n, |Y|) = (3, 0), (3, 1), (4, 1/2), (4, 3/2)$, and $(5, 0)_{\text{real}}$. The last column of the table 5 shows proper choices of WIMP masses in order for their thermal relic abundances become comparable with the dark matter abundance in the current Universe. All of those values are somewhat larger than the central value of the mass of the observed signal, which means that the scalar

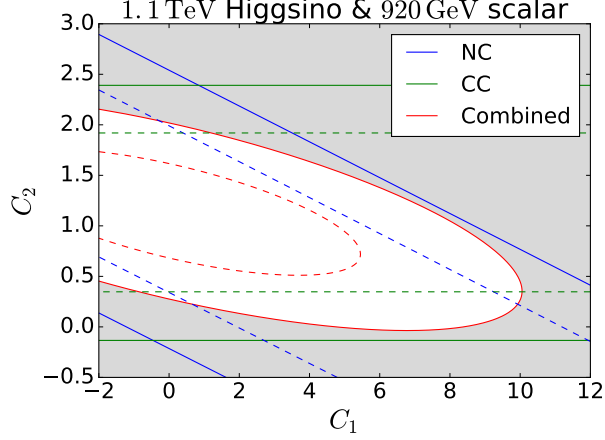


Figure 10: Contour of \sqrt{q} in the C_1 vs. C_2 plane for the 1.1 TeV Higgsino signal, tested with the scalar WIMP assumption. The plane is defined as the scalar mass of 920 GeV. The colors and styles of lines and the meaning of the gray region are the same as Fig. 8.

(n, Y)	C_1	C_2	$m_{\text{DM}}[\text{TeV}]$
$(3, 0)_{\text{real}}$	0	0.25	2.5 [32]
$(3, 0)$	0	0.5	1.55 [33]
$(3, 1)$	0.75	0.5	1.6 [32]
$(4, \frac{1}{2})$	0.25	1.25	2.4 [32]
$(4, \frac{3}{2})$	2.25	1.25	2.9 [32]
$(5, 0)_{\text{real}}$	0	1.25	9.4 [32]

Table 5: The scalar WIMPs that are compatible with the result in Fig. 10. The observed DM energy density is explained by the thermal relic of the WIMP with m_{DM} shown in the fourth column.

interpretation of the signal cannot explain the whole of the dark matter relic abundance without introducing some non-thermal production mechanism.

1.3 Conclusion

In this section, we have discussed the indirect search of WIMPs at future 100 TeV hadron colliders based on the precision measurement of the production processes of a charged lepton pair and that of a charged lepton and a neutrino. In particular, we have demonstrated that not only we can discover the WIMPs, but also we can determine their properties such as their masses, $SU(2)_L$ and $U(1)_Y$ charges, and spins via the processes of our concern. It is based

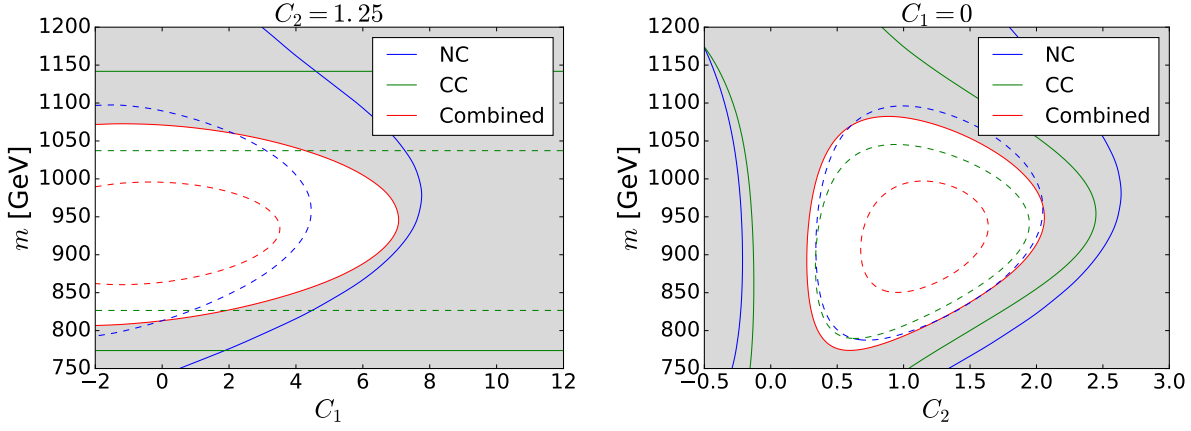


Figure 11: **Left:** Contour of \sqrt{q} in the C_1 vs. m plane with $C_2 = 1.25$ for the 1.1 TeV Higgsino signal, tested with the scalar WIMP assumption. The colors and styles of lines and the meaning of the gray region are the same as Fig. 8. **Right:** Contour of \sqrt{q} in the C_2 vs. m plane with $C_1 = 0$ for the 1.1 TeV Higgsino signal, tested with the scalar WIMP assumption.

on two facts: the high energy lepton production channel enables us to study its momentum distribution in great detail, and the WIMP correction shows characteristic features, including a dip-like structure as the final state invariant mass being twice the WIMP mass. The latter feature also helps us to distinguish the WIMP signals from backgrounds and systematic errors, as they are not expected to show a dip-like structure. In order to fully exploit the differences between the distributions the WIMP signals and systematic errors, we have adopted the profile likelihood method as our statistical treatment.

First, we have shown in Fig. 5 the detection reach of WIMPs from the NC processes (mediated by photon or Z -boson), the CC processes (mediated by W -boson), and the combination of these two results. We have seen that the addition of the CC processes improves the detection reach from the previous analysis [1]. From the combined analysis, the bounds at the 5σ (95% C.L.) level for Higgsino and Wino are 850 GeV (1.7 TeV) and 1.3 TeV (2.3 TeV), respectively. We have also shown the 95 % C.L. reach for 5-plet fermion and 7-plet scalar: ??? TeV and ??? TeV for the optimistic analysis and ??? TeV and ??? TeV for the analysis with a fitting procedure. (**♣ Fill the values ♣**) This result, in particular that for short lifetime Higgsino, indicates the importance of our method for the WIMP search.

Next, we have considered the determination of the mass and $SU(2)_L$ and $U(1)_Y$ charges of the observed WIMP. By combining the NC and the CC events, the position and the height of the dip in the WIMP effect on the cross section gives us enough information for determining all the three parameters. In Figs. 8 and 9, we have shown the plots of the test

statistics that test the validity of several choices of parameters. As a result, the $SU(2)_L$ charge of the observed signal is correctly identified under the assumption of a single WIMP multiplet, and the $U(1)_Y$ charge and mass are also determined precisely. In order for the determination of the WIMP spin, we have plotted the contours of the test statistics that test the validity of the scalar WIMP models with some fixed values of masses and charges. The results are shown in Figs. 10 and 11, which reveals that the spin is not completely determined by solely using our method. Use of another approach to determine the WIMP properties, or of some assumption like that the observed signal corresponds to the dark matter in our Universe, may help us to obtain further information regarding the WIMP spin.

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