DEEP LEARNING FOR ECONOMICS AND FINANCE

ESOMAS, University of Torino, Italy August 25th – 27th, 2025

https://github.com/sischei/SummerSchool_DL_Turin_2025

Simon Scheidegger simon.scheidegger@unil.ch

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A DENSE PROGRAM

Day 1, Monday, August 25th, 2025

Time	Main Topics	Lecturer
08:30 - 09:00	Registration at ESOMAS: Location TBD	
09:00 - 10:30	Welcome, and Introduction to Machine Learning and Deep Learning (part I)	Scheidegger/Trojani
10:30 - 11:00	Coffee Break	
11:00 - 12:30	Introduction to Machine Learning and Deep Learning (part II), Tensorflow and PyTorch	Scheidegger/Trojani
12:30 - 13:30	Lunch Break	
13:30 - 15:00	Introduction to Deep Equilibrium Nets (DEQN)	Scheidegger
15:00 - 15:30	Coffee Break	
15:30 - 17:00	Hands-on: Solving a dynamic model with <u>DEQNs</u>	Scheidegger



A DENSE PROGRAM

Day 2, Tuesday, August 26th, 2025

Time	Main Topics	Lecturer
09:00 - 10:30	Solving heterogenenous agents models with DeepHAM (I)	Yang
10:30 - 11:00	Coffee Break	
11:00 - 12:30	Solving heterogenenous agents models with DeepHAM (II)	Yang
12:30 - 13:30	Lunch Break	
13:30 - 15:00	Hands-on exercises on DeepHAM	Yang
15:00 - 15:30	Coffee Break	
15:30 - 17:00	[Industry Talk <u>DEQNs</u>	Karyampas

A DENSE PROGRAM

Day 3, Wednesday, August 27th, 2025

Time	Main Topics	Lecturer
09:00 - 10:30	Deep Learning for Continuous-time Models	Scheidegger/Yang
10:30 - 11:00	Coffee Break	
11:00 - 12:30	Gaussian Processes for Dynamic Models	Trojani
12:30 - 13:30	Lunch Break	
13:30 - 14:30	Deep Surrogates (I)	Chen
14:30 - 14:45	Short offee Break	
14:45 - 15:45	Deep Surrogates (II)	Chen
15:45 - 16:00	Short offee Break	
16:00 - 17:30	Keynote Presentation	Violante



MOST RECENT INFO AND MATERIALS

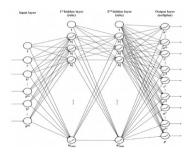
- GITHUB: https://github.com/sischei/SummerSchool_DL_Turin_2025
- Enroll on Nuvolos to get access to the cloud/codes (press the link below)
 - → https://app.nuvolos.cloud/enroll/class/_IQSiRolH94

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INTRO TO MACHINE LEARNING AND DEEP LEARNING

August 25th, 2025

Simon Scheidegger simon.scheidegger@unil.ch



ROAD-MAP OF THIS LECTURE

- Machine Learning Basics
- Intro to Deep Learning
 - The multi-layer perceptron
 - Feed-forward networks
 - Network training SGD
 - Back-propagation
 - Some notes on over-fitting
 - Deep double descent

- Hands-on:
 - Gradient descent
 - A first glance at Keras/Tensorflow



THE RISE OF NEURAL NETWORKS

DEEPMIND BEATS PROS AT STARCRAFT IN ANOTHER TRIUMPH FOR BOTS



A pro gamer and an Al bot duke it out in the strategy game StarCraft, which has becon bed for research on artificial intelligence. Co STARCRAFT

IN LONDON LAST month, a team from Alphabet's UK-ba artificial intelligence research unit DeepMind quietly l new marker in the contest between humans and compa On Thursday it revealed the achievement in a three-ho YouTube stream, in which aliens and robots fought to t death.

NEWS BIOLOGY 21 DECEMBER 2017

AI beats docs in cancer spotting

A new study provides a fresh example of machine learning as an important diagnostic tool. Paul Biegler reports.

THIS MORE POWERFUL VERSION OF ALPHAGO LEARNS ON ITS OWN



FOI NOAH SHELDON FOR WIRED

AT ONE POINT during his historic defeat to AlphaGo last year, world champion Go play abruptly left the room. The bot had played confounded established theories of the box moment that came to epitomize the myster AlphaGo.



Deep Learning Software Speeds Up Drug Discovery

Wed, 01/16/2019 - 8:00am 1 Comment by Kenny Walter, Science Reporter - W@RandDMagazine



The long, arduous process of narrowing down millions of chemical compounds to just a select few that can be further developed into mature drugs, may soon be shortened, thanks to new artificial intelligence (AI) software.

GENERATIVE AI

ChatGPT 5 V

- https://chatgpt.com/
- https://gemini.google.com/app
- https://claude.ai/
- https://grok.com/
- https://www.deepseek.com

draw a bird teaching himself deep learning in the style similar to the one of kandinsky

Bilder erstellt

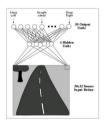




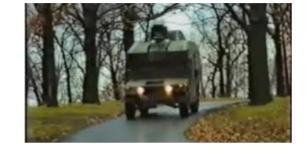
SELF-DRIVING CARS

- Carnegie Mellon University 1990ies
 - ALVINN: Autonomous Land Vehicle In a Neural Network











- Today (e.g., Waymo)
 - https://www.youtube.com/watch?v=LSX3qdy0dFg



APP: COLORING OLD MOVIES

https://deepsense.ai/ai-movie-restoration-scarlett-ohara-hd/







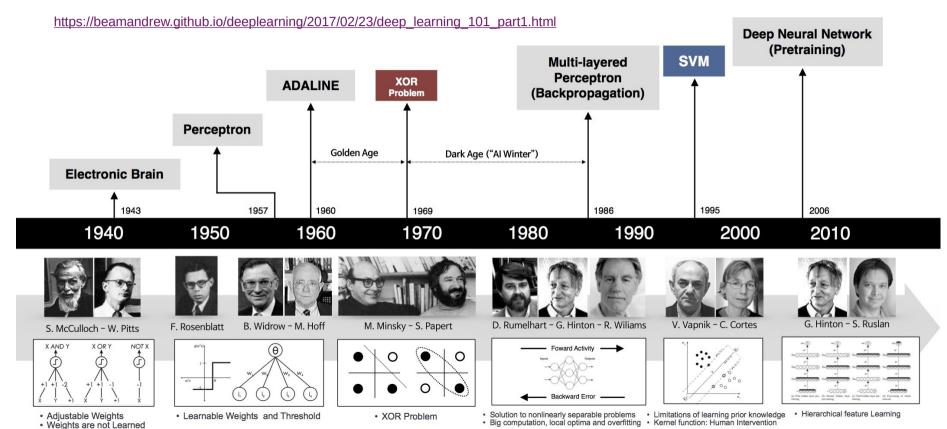
TWO-LEGGED ROBOTS

- https://www.youtube.com/watch?v=tF4DML7FIWk
- https://www.youtube.com/watch?v=-e1_QhJ1EhQ





A TIMELINE OF DEEP LEARNING



^{*}J. Schmidhuber clearly missing on this slide

WHY NOW?

Neural Networks date back decades, so why the resurgence?

(Stochastic Gradient Descent: 1952, Perceptron: 1958, Back-propagation: 1986, Deep Convolutional NN: 1995)

- Big Data
 - Large Datasets
 - Easier Collection and Storage
- Hardware
 - GPUs, TPUs,...
- Software
 - Improved Techniques
 - **Toolboxes**









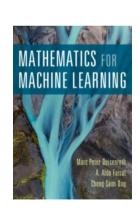
SOME USEFUL MATERIALS

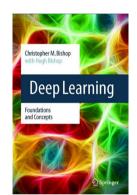
Deep Learning

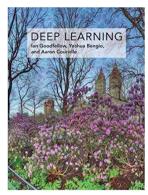
Ian Goodfellow and Yoshua Bengio and Aaron Courville MIT Press 2016 http://www.deeplearningbook.org/

Deep Learning – Foundations and ConceptsC. M Bishop, H. Bishop, Springer 2024
(pdf freely available)

Mathematics for Machine Learning
Deisenroth, A. Aldo Faisal, and Cheng Soon Ong.
Cambridge University Press 2020







→ There is a great community out there (use your browser and Google around...)

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RECAP ON MACHINE LEARNING

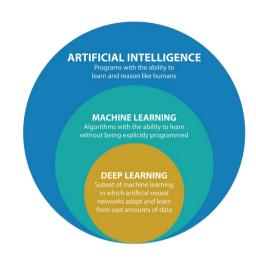


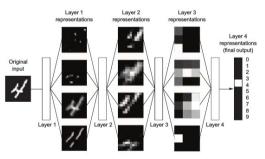
SOME TERMINOLOGY

- Artificial intelligence (AI)
 - Can computers be made to "think"—a question whose ramifications we're still exploring today.
 - A concise definition of the field would be as follows: the effort to automate intellectual tasks normally performed by humans.
- Machine learning (e.g., supervised ML)



Deep Learning as a particular example of an ML technique







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TYPES OF MACHINE LEARNING

Supervised Learning

- assume that training data is available from which they can learn to predict a target feature based on other features (e.g., monthly rent based on area).
 - Classification
 - Regression

Unsupervised Learning

- take a given data-set and aim at gaining insights by identifying patterns, e.g., by grouping similar data points.
- **Reinforcement Learning**

SUPERVISED REGRESSION

Regression aims at predicting a numerical target feature based on one or multiple other (numerical) features.

Example: Price of a used car.

x : car attributes

y : price

• $y = h(x | \theta)$

h (): model

 θ : parameters

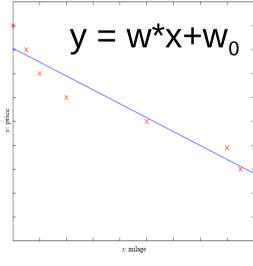


Fig. from Alpaydin (2014)

SUPERVISED CLASSIFICATION

Example 1: Spam Classification

- Decide which emails are Spam and which are not.
- Goal: Use emails seen so far to produce a good prediction
- rule for future data.

Example 2: Credit Scoring

 Differentiating between low-risk and high-risk customers from their income and savings.

• Discriminant: IF income > θ_2 AND savings > θ_2 THEN low-risk ELSE high-risk



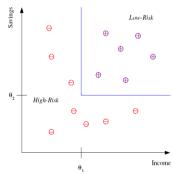


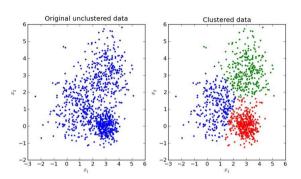
Fig. from Alpaydin (2014)

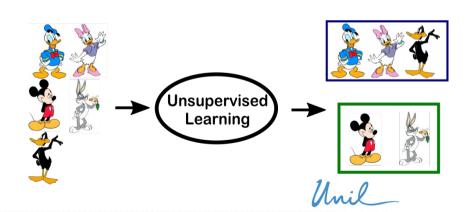
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UNSUPERVISED ML

- No output
- Clustering: Grouping similar instances
- Example applications:
 - Customer segmentation
 - Image compression
 - Bio-informatics: Learning motifs
 - ...

Unsupervised Learning





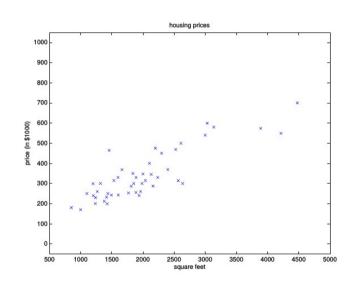
REINFORCEMENT LEARNING

- Learning a policy: A sequence of outputs
- No supervised output but delayed reward
 - Game playing
 - Robot in a maze
 - ...
- See, e.g., https://www.youtube.com/watch?v=V1eYniJ0Rnk&vl=en

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BUILDING AN ML ALGORITHM (I)

Living area ($feet^2$)	Price (1000\$s)
2104	400
1600	330
2400	369
1416	232
3000	540
:	:

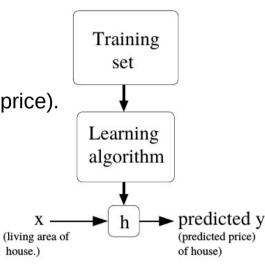


• Given data like this, how can we learn to predict the prices of other houses as a function of the size of their living areas?

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BUILDING AN ML ALGORITHM (II)

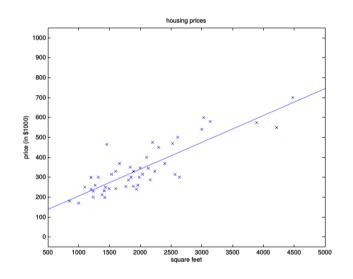
- x(i): "input" variables (living area in this example), also called input features
- y(i): "output" / target variable that we are trying to predict (price).
- Training example: a pair (x(i), y(i)).
- Training set: a list of m training examples {(x(i), y (i)); i = 1, . . . , m}
 - To perform supervised learning, we must decide how we're going to represent functions/hypotheses h in a computer.



BUILDING AN ML ALGORITHM (III)

- Model / Hypothesis: $h_{\theta}(x) = \theta_0 + \theta_1 x_1$
 - θ_i 's: parameters
- Cost Function:

$$J(\theta) = \frac{1}{2} \sum_{i=1}^{m} \left(h_{\theta} \left(x^{(i)} \right) - y^{(i)} \right)^{2}$$



• Minimize $J(\theta)$ in order to obtain the coefficients θ .

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BUILDING AN ML ALGORITHM (IV)

- In General: Machine learning in 3 steps:
 - Choose a **model** $h(x|\theta)$.
 - Define a **cost function** $J(\theta|x)$.
 - Optimization procedure to find θ^* that minimizes $J(\theta)$.
- Computationally, we need:
 - data, linear algebra, statistics tools, and optimization routines.

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DON'T RE-INVENT THE WHEEL

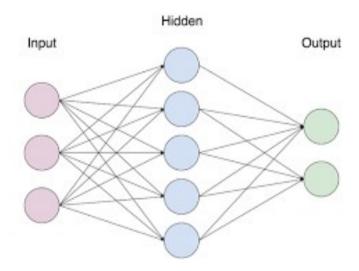
- Plenty of Frameworks out there
 - Keras
 - Tensorflow
 - Pytorch
 - Caffee
 - Scikit-learn

EXAMPLE NOTEBOOK

day1/code/01_BasicML_intro.ipynb

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ARTIFICIAL NEURAL NETWORKS



ARTIFICIAL NEURAL NETWORKS

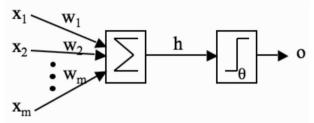
- Artificial Neural networks arise from attempts to model human/animal brains
 - Many models, many claims of biological plausibility.

- We will focus on multi-layer perceptron
 - Mathematical properties rather than plausibility.





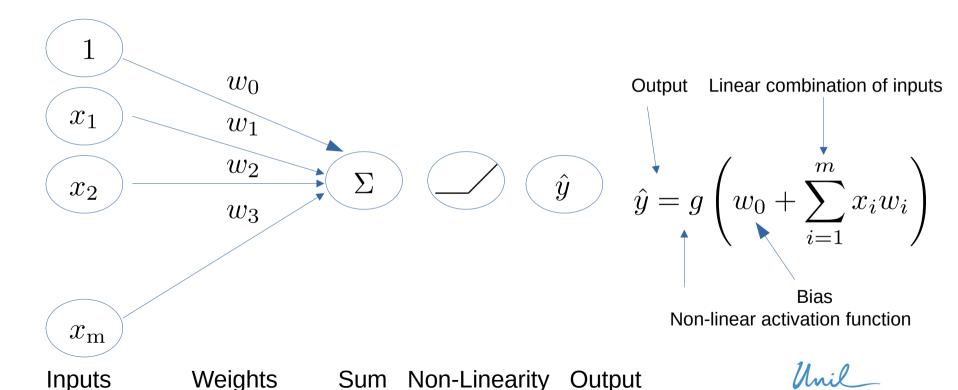
MODEL OF A NEURON (1943)



- A picture of McCulloch and Pitts' (1943) mathematical model of a neuron.
 - 1. a set of weighted inputs w_i that correspond to the synapses.
 - 2. an adder that sums the input signals (equivalent to the membrane of the cell that collects electrical charge).
 - 3. an activation function (initially a threshold function) that decides whether the neuron fires ('spikes') for the current inputs.
- The inputs x_i are multiplied by the weights w_i , and the neurons sum their values.
- If this sum is greater than the threshold θ then the neuron fires; otherwise it does not.

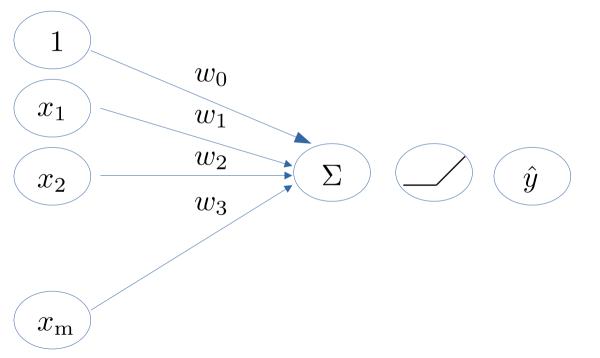
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A SINGLE NEURON: THE PERCEPTRON



Bias term allows you to shift your activation function to the left or the right

THE PERCEPTRON: FORWARD PROPAGATION



$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

$$\hat{y} = g \left(w_0 + \boldsymbol{X}^T \boldsymbol{W} \right)$$

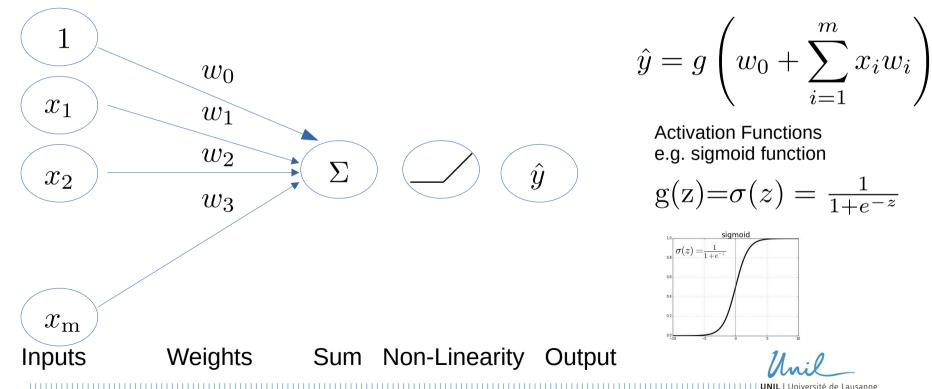
$$\begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix} \text{ and } \boldsymbol{W} = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$$

Inputs Weights Sum Non-Linearity Output

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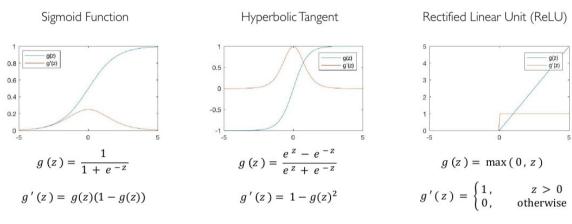
→ Bias term allows you to shift your activation function to the left or the right

THE PERCEPTRON: FORWARD PROPAGATION



→ Bias term allows you to shift your activation function to the left or the right

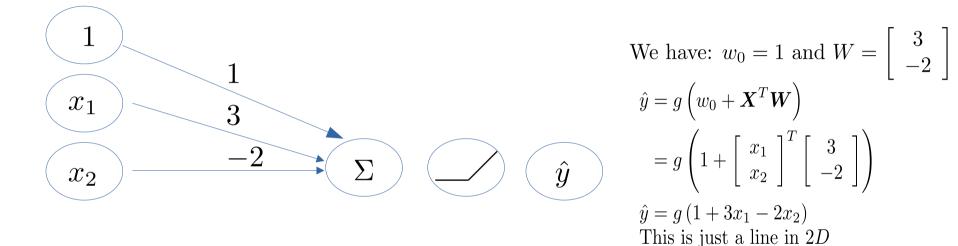
FEW ACTIVATION FUNCTIONS



- Needs to be differentiable for gradient-based learning (later)
 - Very useful in practice.
 - Sigmoid function, e.g., useful for classification (Probability).

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PERCEPTRON – AN EXAMPLE

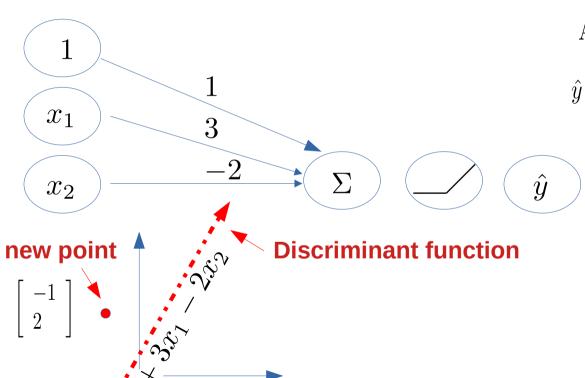


Imagine we have a trained network with weights given.

→ how do we compute the output?

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PERCEPTRON – AN EXAMPLE

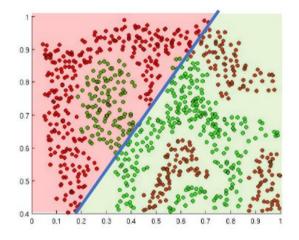


Assume we have input: $X = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$

$$\hat{y} = g(1 + (3*-1) - (2*2))$$
$$= g(-6) \approx 0.002$$

IMPORTANCE OF ACTIVATION FCT.

The purpose of activation functions is to introduce non-linearities into the network.

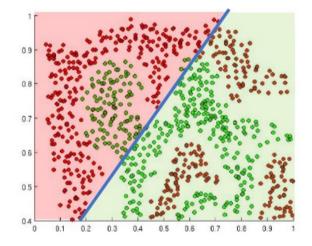


What if we wanted to build a Neural Network to distinguish green versus red points?

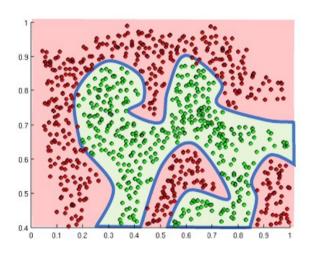
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IMPORTANCE OF ACTIVATION FCT.

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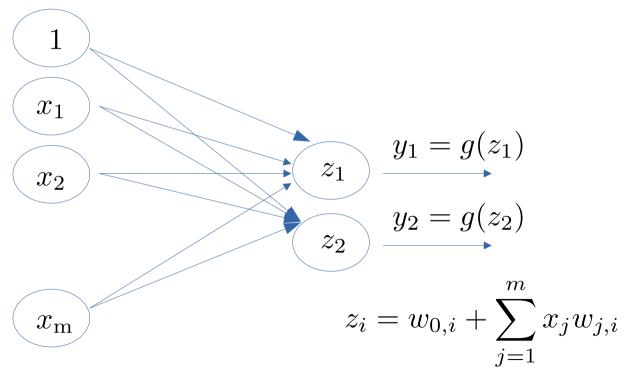
Linear activation functions produce linear decisions no matter the network size.



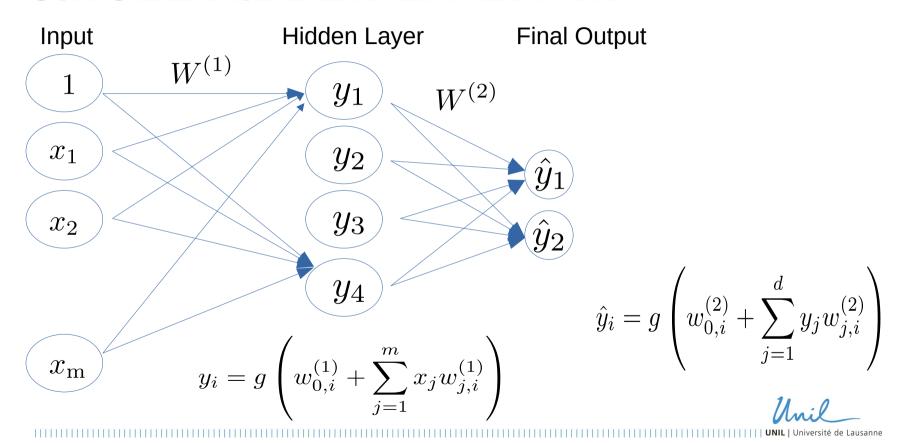
 Non-linearities allow us to approximate arbitrarily complex functions.



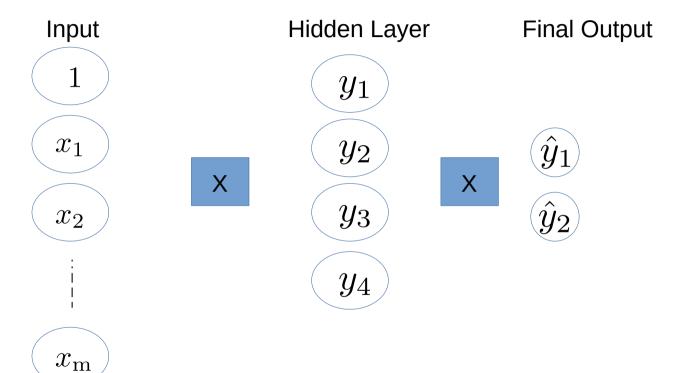
BUILDING A NN WITH PERCEPTRONS: A MULTI-OUTPUT PERCEPTRON



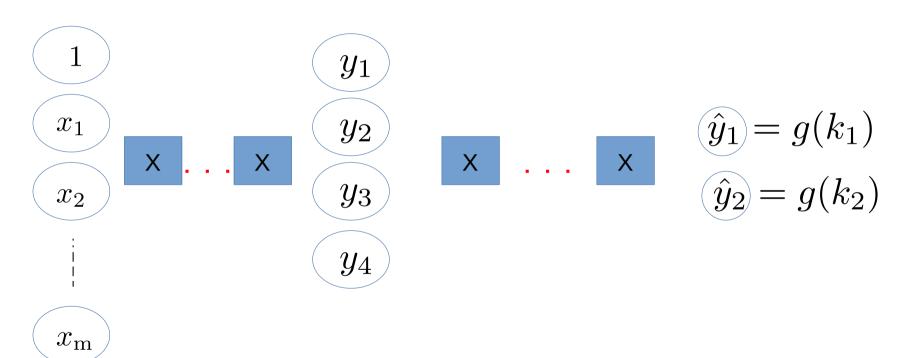
SINGLE HIDDEN LAYER NN



SINGLE HIDDEN LAYER NN



FULLY CONNECTED DEEP NN



EXPRESSIVENESS OF ANN

Boolean functions:

- Every Boolean function can be represented by a network with a single hidden layer.
- Might require exponential (in number of inputs) hidden units.

Continuous functions:

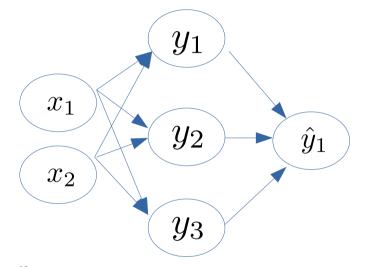
- Every bounded continuous function can be approximated with arbitrarily small error, by network with one hidden layer [Cybenko 1989; Hornik et al. 1989].
- Deep NN are in practice superior to other ML methods in presence of large data sets.

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EMPIRICAL LOSS

The empirical loss measures the total loss over our entire data set.





Prediction: 0.2

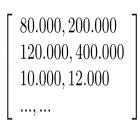
Actual: 1

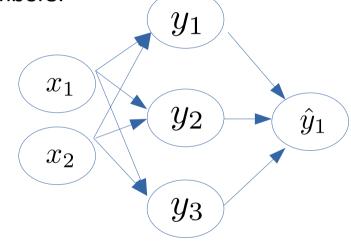
$$J(W) = \frac{1}{n} \sum_{i=1}^{n} \mathcal{J}\left(f\left(x^{(i)}; \boldsymbol{W}\right), \tilde{y}^{(i)}\right)$$
Predicted Actual

MEAN SQUARED ERROR (MSE)

Mean squared error can be used with regression models that output

continuous real numbers.





$$J(W) = \frac{1}{n} \sum_{i=1}^{n} \left(y_{true}^{(i)} - f\left(x^{(i)}; W\right) \right)^{2}$$

Actual Predicted

f(x)	${f y}_{\sf true}$
[450.000]	$\begin{bmatrix} 470.000 \end{bmatrix}$
250.000	220.000
190.000	250.000
[,]	[,]

Loan requested

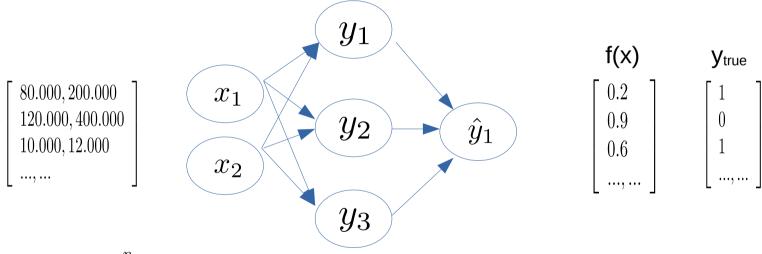
Loan required

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BINARY CROSS ENTROPY LOSS

Our example was a classification problem with output (0 or 1)



$$J(W) = \frac{1}{n} \sum_{i=1}^{n} \underline{y_{true}^{(i)}} \log \left(\underline{f\left(x^{(i)}; W\right)} \right) + \left(1 - \underline{y_{true}^{(i)}}\right) \log \left(1 - \underline{f\left(x^{(i)}; W\right)}\right)$$

Actual

Predicted

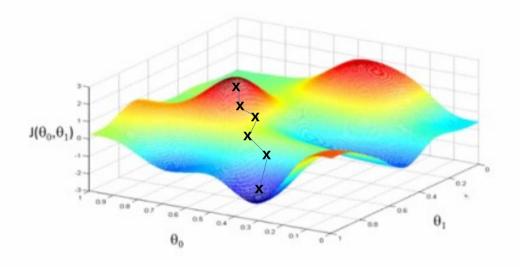
Actual

Predicted

GRADIENT DESCENT IN WEIGHT SPACE

→ We want to find the network weights that achieve the lowest loss!

- $-W^* = \operatorname{argmin} J(W)$
- -Randomly pick an initial (w_0, w_1)
- -Compute gradient
- -Take small steps in the opposite direction of gradient.
- -Repeat until convergence





GRADIENT DESCENT ALGORITHM

Algorithm

- I. Initialize weights randomly $\sim \mathcal{N} \left(0, \sigma^2
 ight)$
- 2. Loop until convergence:
- 3. Compute gradient, $\frac{\partial J(W)}{\partial W}$ Can be computationally expensive
- 4. Update weights, $oldsymbol{W} \leftarrow oldsymbol{W} \eta rac{\partial J(oldsymbol{W})}{\partial W}$
- 5. Return weights



GRADIENT DESCENT ALGORITHM

Algorithm

- I. Initialize weights randomly $\sim \mathcal{N} \left(0, \sigma^2
 ight)$
- 2. Loop until convergence:
- 3. Compute gradient, $\frac{\partial J(W)}{\partial W}$
- 4. Update weights, $oldsymbol{W} \leftarrow oldsymbol{W} \eta \frac{\partial J(oldsymbol{W})}{\partial W}$
- 5. Return weights

Learning rate

All that matters to train a NN.
Computationally expensive!

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STOCHASTIC GRADIENT DESCENT

Algorithm

- I. Initialize weights randomly $\sim \mathcal{N} \left(0, \sigma^2
 ight)$
- 2. Loop until convergence:
- 3. Pick single data point i
- 4. Compute gradient, $\frac{\partial J_i(W)}{\partial W}$ Can be noisy
- 5. Update weights, $m{W} \leftarrow m{W} \eta \frac{\partial J(m{W})}{\partial m{W}}$
- 6. Return weights

STOCHASTIC GRADIENT DESCENT

Algorithm

- I. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Pick batch of B data points
- 4. Compute gradient, $\frac{\partial J(W)}{\partial W} = \frac{1}{B} \sum_{k=1}^{B} \frac{\partial J_k(W)}{\partial W}$ 5. Update weights, $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 6. Return weights

STOCHASTIC GRADIENT DESCENT

Consider the term $\sum_{n=1}^{N} (\nabla L_n(\boldsymbol{\theta}_i))$ in (7.15). We can reduce the amount of computation by taking a sum over a smaller set of L_n . In contrast to batch gradient descent, which uses all L_n for $n=1,\ldots,N$, we randomly choose a subset of L_n for mini-batch gradient descent. In the extreme case, we randomly select only a single L_n to estimate the gradient. The key insight about why taking a subset of data is sensible is to realize that for gradient descent to converge, we only require that the gradient is an unbiased estimate of the true gradient. In fact the term $\sum_{n=1}^{N} (\nabla L_n(\boldsymbol{\theta}_i))$ in (7.15) is an empirical estimate of the expected value (Section 6.4.1) of the gradient. Therefore, any other unbiased empirical estimate of the expected value, for example using any subsample of the data, would suffice for convergence of gradient descent.

*cf. Deisenroth et al. (2021) Mathematics for Machine learning, Sec. 7.1.3.

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MINI-BATCHES WHILE TRAINING

- More accurate estimation of gradient
 - Smoother convergence
 - Allows for larger learning rates
- Mini-batches lead to fast training!
 - Can parallelize computation + achieve significant speed increases on GPU's
- Note: a complete pass over all the patterns in the training set is called an epoch.

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INTERMEZZO – ACTION REQUIRED

Let's look at this notebook on Nuvolos.cloud:



- day1/code/02_GradientDescent_and_StochasticGradientDescent.ipynb
- If you are not familiar with Jupyter Notebooks, look at python_refresher/jupyter_intro.ipynb

LOG INTO NUVOLOS.CLOUD & LAUNCH AN APPLICATION

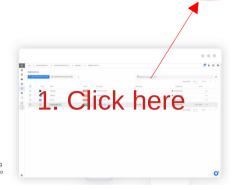


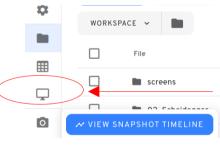
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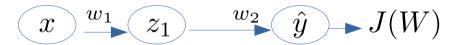


2. Click here



COMPUTING GRADIENTS: ERROR BACKPROPAGATION

How does a small change in one weight (e.g., w₂) affect the final loss J(W)?



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COMPUTING GRADIENTS: ERROR BACKPROPAGATION

- How does a small change in one weight (e.g., w₂) affect the final loss J(W)?
- Chain rule

$$\begin{array}{c|c} x & \xrightarrow{w_1} & z_1 \\ \hline \end{array} \qquad \begin{array}{c} w_2 \\ \hline \end{array} \qquad \begin{array}{c} \hat{y} \\ \hline \end{array} \qquad \begin{array}{c} J(W) \\ \hline \end{array}$$

$$\frac{\partial J(W)}{\partial w_2} = \frac{\partial J(W)}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial w_2}$$

COMPUTING GRADIENTS: ERROR BACKPROPAGATION

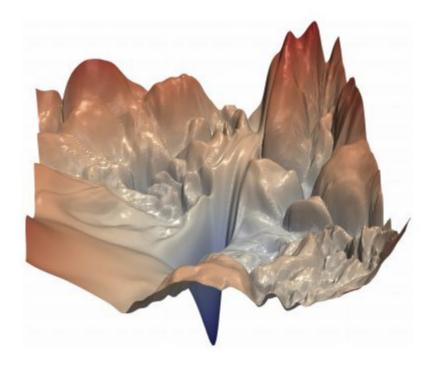
- How does a small change in one weight (e.g., w₂) affect the final loss J(W)?
- Chain rule
- Repeat this for every weight in the network using gradients from later layers

$$\frac{x}{\partial y} = \frac{w_1}{\partial y} \cdot z_1 \qquad \frac{w_2}{\partial y} \cdot \hat{y} \longrightarrow J(W)$$

$$\frac{\partial J(W)}{\partial w_1} = \frac{\partial J(W)}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial w_1} \qquad \frac{\partial J(W)}{\partial w_1} = \frac{\partial J(W)}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

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TRAINING NEURAL NETWORKS





LOSS FUNCTION: CAN BE DIFFICULT TO OPTIMIZE

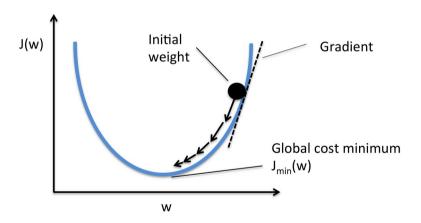
- Remember:
 - Optimization through gradient descent:

$$W \leftarrow W - \eta \frac{\partial J(W)}{\partial W}$$

How can we set the learning rate?

SETTING THE LEARNING RATE

- Small learning rate converges slowly and gets stuck in false local minima
 - Design an adaptive learning rate that "adapts" to the landscape.



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FEW VARIANTS OF SGD

Method	Formula
Learning Rate	$w^{(t+1)} = w^{(t)} - \eta \cdot \nabla \ell(w^{(t)}, z) \qquad = w^{(t)} - \eta \cdot \nabla w^{(t)}$
Adaptive Learning Rate	$w^{(t+1)} = w^{(t)} - \eta_t \cdot \nabla w^{(t)}$
Momentum [Qian 1999]	$w^{(t+1)} = w^{(t)} + \mu \cdot (w^{(t)} - w^{(t-1)}) - \eta \cdot \nabla w^{(t)}$
Nesterov Momentum [Nesterov 1983]	$w^{(t+1)} = w^{(t)} + v_t; \qquad v_{t+1} = \mu \cdot v_t - \eta \cdot \nabla \ell(w^{(t)} - \mu \cdot v_t, z)$
AdaGrad [Duchi et al. 2011]	$w_i^{(t+1)} = w_i^{(t)} - \frac{\eta \cdot \nabla w_i^{(t)}}{\sqrt{A_{i,t}} + \varepsilon}; \qquad A_{i,t} = \sum_{\tau=0}^t \left(\nabla w_i^{(t)} \right)^2$
RMSProp [Hinton 2012]	$w_{i}^{(t+1)} = w_{i}^{(t)} - \frac{\eta \cdot \nabla w_{i}^{(t)}}{\sqrt{A_{i,t}'} + \varepsilon}; \qquad A_{i,t}' = \beta \cdot A_{t-1}' + (1 - \beta) \left(\nabla w_{i}^{(t)} \right)^{2}$
Adam [Kingma and Ba 2015]	$w_i^{(t+1)} = w_i^{(t)} - \frac{\eta \cdot M_{i,t}^{(1)}}{\sqrt{M_{i,t}^{(2)} + \varepsilon}}; \qquad M_{i,t}^{(m)} = \frac{\beta_m \cdot M_{i,t-1}^{(m)} + (1 - \beta_m) \left(\nabla w_i^{(t)}\right)^m}{1 - \beta_m^t}$

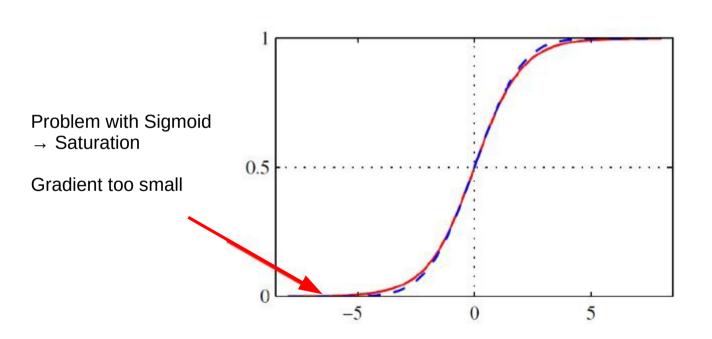
WEIGHT INITIALIZATION

- Before the training process starts: all weights vectors must be initialized with some numbers.
- There are many initializers of which random initialization is one of the most widely known ones (e.g., with a normal distribution).
 - Specifically, one can configure the mean and the standard deviation, and once again seed the distribution to a specific (pseudo-)random number generator.
 - which distribution to use, then?
 - random initialization itself can become problematic under some conditions: you may then face the vanishing gradients and exploding gradients problems.
- What to do against these problems?
 - e.g. Xavier & He initialization (available in Keras)
 - They are different in the way how they manipulate the drawn weights to arrive at approximately 1. By consequence, they are best used with different activation functions.
 - Specifically, He initialization is developed for ReLU based activating networks and by consequence is best used on those. For others, Xavier (or Glorot) initialization generally works best.

VANISHING GRADIENTS

- Deep learning community often deals with two types of problems during training: vanishing gradients (and exploding) gradients.
 - Vanishing gradients
 - the backpropagation algorithm, which chains the gradients together when computing the error backwards, will find really small gradients towards the left side of the network (i.e., farthest from where error computation started).
 - This problem primarily occurs e.g. with the Sigmoid and Tanh activation functions, whose derivatives produce outputs of 0 < x' < 1, except for Tanh which produces x' = 1 at x = 0.
 - Consequently, when using Tanh and Sigmoid, you risk having a suboptimal model that might possibly not converge due to vanishing gradients.
 - ReLU does not have this problem its derivative is 0 when x < 0 and is 1 otherwise.
 - It is computationally faster. Computing this function often by simply maximizing between (0, x) takes substantially fewer resources than computing e.g. the sigmoid and tanh functions. By consequence, ReLU is the de facto standard activation function in the deep learning community today.

VANISHING GRADIENTS



VANISHING GRADIENTS

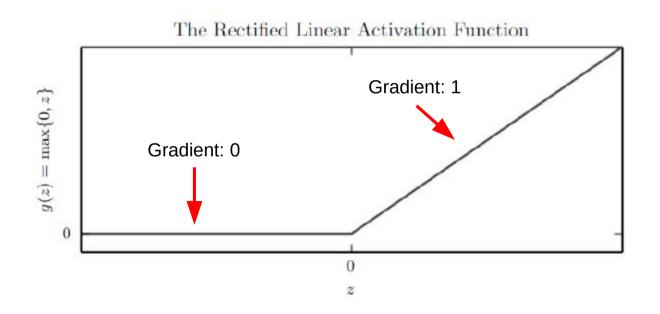
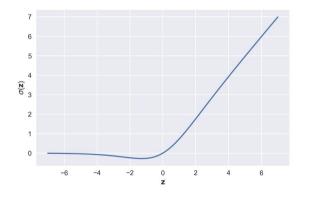


Fig. From Goodfellow et al. (2016)

SWISH ACTIVATION FUNCTION

- Nevertheless, it does not mean that it cannot be improved.
 - Swish activation function.
 - Instead, it does look like the de-facto standard activation function, with one difference: the domain around 0 differs from ReLU.
- Swish is a smooth function. That means that it does not abruptly change direction like ReLU does near x = 0.
 - Swish is non-monotonic. It thus does not remain stable or move in one direction, such as ReLU.
 - It is in fact this property which separates Swish from most other activation functions, which do share this monotonicity.
- In applications Swish could be better than ReLU.

$$f(x) = x * \operatorname{sigmoid}(x)$$
$$= x * (1 + e^{-x})^{-1}$$



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A GEOMETRIC INTERPRETATION

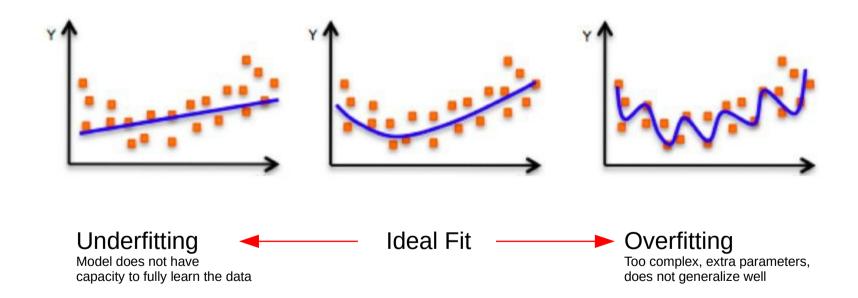
- In 3D, the following mental image may prove useful. Imagine two sheets of colored paper: one red and one blue.
- Put one on top of the other.
- Crumple them together into a small ball. That crumpled paper ball is your input data, and each sheet of paper is a class of data in a classification problem.
- What a neural network (or any other machine-learning model) is meant to do is figure out a **transformation of the paper** ball that would uncrumple it, so as to make the two classes cleanly separable again.
- With deep learning, this would be implemented as a series of simple transformations of the 3D space, such as those you could apply on the paper ball with your fingers, one movement at a time.



Figure 2.9 Uncrumpling a complicated manifold of data

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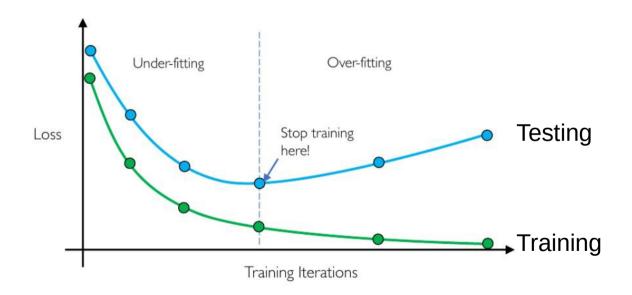
NOTES ON OVERFITTING



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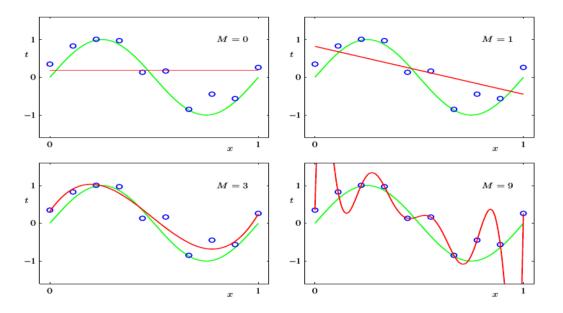
EARLY STOPPING

Stop training before we have a chance to overfit



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NOTES ON OVERFITTING (II)



Polynomial Curve Fitting of polynomials having various orders M, shown as red curves, fitted to the data set shown above.

NOTES ON OVERFITTING (III)

- So far, we have assessed the prediction quality of our model based on the same data that we used for training.
- This is a very bad idea, since we can not accurately measure how well our model works for previously unseen data points (e.g., for cars not in our dataset)
- Our model may over-fit to the training data and loose its ability to make predictions.
 - → Next, we'll see some best practices for evaluating machine learning models

SPLIT THE DATA

- To avoid over-fitting, it is good practice to assess the quality of a model based on test data that must not be used for training the model.
- The key idea is to split the available data (randomly) into <u>training</u>, <u>validation</u>, and <u>test data</u>.

SPLITTING THE DATA

- One common approach to reliably assess the quality of a machine learning model and avoid over-fitting is to randomly split the available data into
 - training data (~70% of the data)
 is used for determining optimal coefficients.
 - validation data (~20% of the data) is used for model selection (e.g., fixing degree of polynomial, selecting a subset of features, etc.)
 - test data (~10% of the data) is used to measure the quality that is reported.

DEEP DOUBLE DESCENT

https://arxiv.org/abs/1912.02292

- The double descent phenomenon occurred so far in practical applications
 - performance first improves, then gets worse, and then improves again with increasing model size, data size, or training time.
 - This effect is often avoided through careful regularization.
 - While this behavior appears to be fairly universal, we don't yet fully understand why it happens, and view further study of this phenomenon as an important research direction.

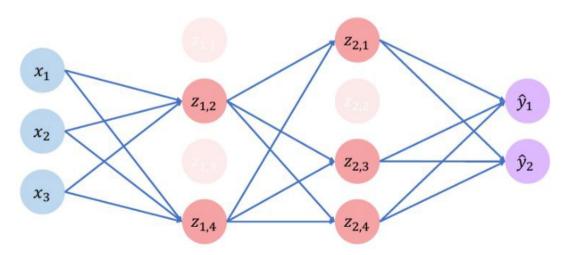


NOTES ON REGULARIZATION

- Regularization is a technique that constrains our optimization problem to discourage complex models.
- We use it to improve generalization of our model on unseen data.

REGULARIZATION IN NN: DROPOUT

- During training, randomly set some activations to 0
 - Typically 'drop' 50 % of activations in layer
 - Forces network to not rely on any node



*REGULARIZATION IN NN: DROPOUT

- It is an efficient way of performing model averaging with neural networks.
- Can be interpreted as some sort of bagging.
- Now, we assume that the model's role is to output a probability distribution. In the case of bagging, each model i produces a probability distribution $p^{(i)}(y \mid x)$.
- The prediction of the ensemble is given by the arithmetic mean of all these distributions: $\frac{1}{k}\sum_{i=1}^k p^{(i)}(y\mid \boldsymbol{x})$
- In the case of dropout, each sub-model defined by mask vector μ defines a probability distribution p(y | x, μ).
- The arithmetic mean over all masks is given by $\sum_{\mu} p(\mu)p(y \mid x, \mu)$ where $p(\mu)$ is the probability distribution that was used to sample μ at training time.

RECIPE FOR USING MLP

Select inputs and outputs for your problem

- Before anything else, you need to think about the problem you are trying to solve, and make sure that you have data for the problem, both input vectors and target outputs.
- At this stage you need to choose what features are suitable for the problem and decide on the output encoding that you will use — standard neurons, or linear nodes.
- These things are often decided for you by the input features and targets that you have available to solve the problem.
- Later on in the learning it can also be useful to re-evaluate the choice by training networks with some input feature missing to see if it improves the results at all.

RECIPE FOR USING MLP (II)

Normalize inputs

 Re-scale the data by subtracting the mean value from each element of the input vector, and divide by the variance (or alternatively, either the maximum or minus the minimum, whichever is greater).

Split the data into training, testing, and validation sets

- You cannot test the learning ability of the network on the same data that you trained it on, since it will generally fit that data very well (often too well, overfitting and modeling the noise in the data as well as the generating function).
- Recall: we generally split the data into three sets, one for training, one for testing, and then a third set for validation, which is testing how well the network is learning during training.

RECIPE FOR USING MLP (III)

Select a network architecture

- You already know how many input nodes there will be, and how many output neurons.
- You need to consider whether you will need a hidden layer at all, and if so how many neurons it should have in it.
- You might want to consider more than one hidden layer.
- The more complex the network, the more data it will need to be trained on, and the longer it will take.
- It might also be more subject to over-fitting.
- The usual method of selecting a network architecture is to try several with different numbers of hidden nodes and see which works best.

RECIPE FOR USING MLP (IV)

Train a network

- The training of the NN consists of applying the MLP algorithm to the training data.
- This is usually run in conjunction with early stopping, where after a few iterations of the algorithm through all of the training data, the generalization ability of the network is tested by using the validation set.
- The NN is very likely to have far too many degrees of freedom for the problem, and so after some amount of learning it will stop modeling the generating function of the data, and start to fit the noise and inaccuracies inherent in the training data. At this stage the error on the validation set will start to increase, and learning should be stopped.

Test the network

Once you have a trained network that you are happy with, it is time to use the test data for the first (and only) time. This will enable you to see how well the network performs on some data that it has not seen before, and will tell you whether this network is likely to be usable for other data, for which you do not have targets.

KERAS & TENSORFLOW BASICS

tensorflow.org



- Keras API: https://www.tensorflow.org/guide/keras/sequential_model
- Fun data sets to play with: https://www.kaggle.com/datasets
- Some "clean" data to play with: https://archive.ics.uci.edu/ml/index.php
- Help for debugging Tensorboard: https://www.tensorflow.org/tensorboard

GOOD NEWS

https://keras.io/keras_core/announcement/



Introducing Keras Core: Keras for TensorFlow, JAX, and PyTorch.

Get started	API docs	Guides	GitHub

We're excited to share with you a new library called **Keras Core**, a preview version of the future of Keras. In Fall 2023, this library will become Keras 3.0. Keras Core is a full rewrite of the Keras codebase that rebases it on top of a **modular backend architecture**. It makes it possible to run Keras workflows on top of arbitrary frameworks — starting with TensorFlow, JAX, and PyTorch.

Keras Core is also a drop-in replacement for tf.keras, with near-full backwards compatibility with tf.keras code when using the TensorFlow backend. In the vast majority of cases you can just start importing it via import keras_core as keras in place of from tensorflow import keras and your existing code will run with no issue — and generally with slightly improved performance, thanks to XLA compilation.

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A GENTLE FIRST EXAMPLE

- Lets look at the notebook: day1/code/03_Gentle_DNN.ipynb.
- This Notebook contains all the basic functionality from a theoretical point of view.
- 2 simple examples, one regression, and one classification.

ACTION REQUIRED

Look at the test functions below*. Pick three of those test functions (from Genz 1987).

- Approximate a 2-dimensional function stated below with Neural Nets based 10, 50, 100, 500 points randomly sampled from [0, 1]². Compute the average and maximum error.
- The errors should be computed by generating 1,000 uniformly distributed random test points from within the computational domain.
- Plot the maximum and average error as a function of the number of sample points.

Repeat the same for 5-dimensional and 10-dimensional functions. Is there anything particular you observe?

oscillatory:
$$f_1(x) = \cos\left(2\pi w_1 + \sum_{i=1}^d c_i x_i\right),$$
 product peak:
$$f_2(x) = \prod_{i=1}^d \left(c_i^{-2} + (x_i - w_i)^2\right),$$
 corner peak:
$$f_3(x) = \left(1 + \sum_{i=1}^d c_i x_i\right)^{-(d+1)},$$
 Gaussian:
$$f_4(x) = \exp\left(-\sum_{i=1}^d c_i^2 \cdot (x_i - w_i)^2\right),$$
 continuous:
$$f_5(x) = \exp\left(-\sum_{i=1}^d c_i \cdot |x_i - w_i|\right),$$
 discontinuous:
$$f_6(x) = \begin{cases} 0, & \text{if } x_1 > w_1 \text{ or } x_2 > w_2, \\ \exp\left(\sum_{i=1}^d c_i x_i\right), & \text{otherwise.} \end{cases}$$

Varying test functions can be obtained by altering the parameters $c=(c_1,\ldots,c_n)$ and $w=(w_1,\ldots,w_n)$. We chose these parameters randomly from [0,1]. Similarly to Barthelmann et al. [2000], we normalized the c_i such that $\sum_{i=1}^d c_i = b_j$, with b_j depending on d, f_j according to

Furthermore, we normalized the w_i such that $\sum_{i=1}^{d} w_i = 1$.

ACTION REQUIRED (II)

- Play with the architecture.
 - Number of hidden layers.
 - activation functions.
 - choice of the stochastic gradient descent algorithm.
 - Monitor the performance with respect to the architecture.



TENSORBOARD

- day1/code/04_Tensorboard.ipynb
- Introduction to Tensorboard (https://www.tensorflow.org/tensorboard)
- Play with it in your spare time

PYTORCH

- day1/code/05_PyTorch_intro.ipynb
- Introduction to PyTorch (https://pytorch.org)
- Play with it in your spare time

QUESTIONS?

