```
X_{train\_diabetes}, X_{test\_diabetes}, Y_{train\_diabetes}, Y_{test\_diabetes} = train\_test\_split(X_d, Y_d, Y_d)
         test_size=0.34, random_state=10)
         X_train_glass, X_test_glass, Y_train_glass, Y_test_glass = train_test_split(X_g, Y_g,
         test_size=0.34, random_state=10)
In [117... # Building decision trees
         # one-level
         clf_1_d = tree.DecisionTreeClassifier(criterion = 'entropy', max_depth = 1)
         clf_1_g = tree.DecisionTreeClassifier(criterion = 'entropy', max_depth = 1)
         clf_1_d = clf_1_d.fit(X_train_diabetes, Y_train_diabetes)
         clf_1_g = clf_1_g.fit(X_train_glass, Y_train_glass)
         # multi-level
         clf_m_d = tree.DecisionTreeClassifier(criterion = 'entropy', max_depth = None)
         clf_m_g = tree.DecisionTreeClassifier(criterion = 'entropy', max_depth = None)
         clf_m_d = clf_m_d.fit(X_train_diabetes, Y_train_diabetes)
         clf_m_g = clf_m_g.fit(X_train_glass, Y_train_glass)
In [118... # Accuracy of the predictions
         # one-level
         Yp_1_d = clf_1_d.predict(X_test_diabetes)
         acc_1_d = accuracy_score(Y_test_diabetes, Yp_1_d)
         print("One-level, diabetes accuracy = " , acc_1_d)
         Yp_1_g = clf_1_g.predict(X_test_glass)
         acc_1_g = accuracy_score(Y_test_glass, Yp_1_g)
         print("One-level, glass accuracy = " , acc_1_g)
         # multi-level
         Yp_m_d = clf_m_d.predict(X_test_diabetes)
         acc_m_d = accuracy_score(Y_test_diabetes, Yp_m_d)
         print("Multi-level, diabetes accuracy = " , acc_m_d)
         Yp_m_g = clf_m_g.predict(X_test_glass)
         acc_m_g = accuracy_score(Y_test_glass, Yp_m_g)
         print("Multi-level, glass accuracy = " , acc_m_g)
         One-level, diabetes accuracy = 0.7213740458015268
         One-level, glass accuracy = 0.4246575342465753
         Multi-level, diabetes accuracy = 0.7290076335877863
         Multi-level, glass accuracy = 0.5753424657534246
In [119... # Explain why there is a difference in the accuracy rates. Compare one-level decision trees and multi-level
         # decision trees in terms of explainability.
         # In case of diabetes dataset, multi-level trees do not let us gain significantly more accuracy (the multi-level
         # tree accuracy is ~ 0.0038 more than single-level), while drasticly increasing the complexity of explainability. I am not
         # sure if it is visible in pdf file, but I have plotted the one-level and multi-level decision tree for both diabetes and
         # glass datasets. For diabetes, the decision is made using the second attribute, which is "Plasma glucose concentration a
         # 2 hours in an oral glucose tolerance test". If the value is less than or equal to 143.5, then the instances are
         # classified as negative-tested, otherwise, they are classified as positive-tested. Taking the multi-level tree, it has
         # way too many level and is completely unexplainable. The conclusion here is that one-level decision tree is good enough.
         # With regards to glass dataset, we notice that multi-level decision trees increase the accurcy by 25% (!!). This is a
         # major improvement and we cannot ignore it. As multi-level decision trees are not limited in the maximum number of steps,
         # they are very likely to overfit and get too complex for understanding. Thus, I tried to keep the restriction on max number
         # of levels, but make it larger than 1. Below there are the results:
         for i in range (2,5):
             clf_i_g = tree.DecisionTreeClassifier(criterion = 'entropy', max_depth = i)
             clf_i_g = clf_i_g.fit(X_train_glass, Y_train_glass)
             Yp_i_g = clf_i_g.predict(X_test_glass)
             acc_i_g = accuracy_score(Y_test_glass, Yp_i_g)
             print(i, "- level, glass accuracy = " , acc_i_g)
         # Based on the results, I would pick 3-level decision tree. The accuracy is increase by more than 20% and the complexity
         # stays more or less acceptable.
         # In terms of explainability, multi-level decision tree in this case, same as for diabetes dataset, is ahrdly explainable,
         # as it has way too many levels. One-level tree makes the decision considering the value of the third attribute, which is
         # "Magnesium". The split is made at Magnesium level of 2.56 units.
         2 - level, glass accuracy = 0.5753424657534246
         3 - level, glass accuracy = 0.6301369863013698
         4 - level, glass accuracy = 0.6301369863013698
In [120... tree.plot_tree(clf_m_d)
         tree.plot_tree(clf_1_d)
Out[120]: [Text(0.5, 0.75, 'X[1] \le 143.5 \le 0.928 \le 506 \le [332, 174]'),
           Text(0.25, 0.25, 'entropy = 0.761 \setminus samples = 381 \setminus value = [297, 84]'),
           Text(0.75, 0.25, 'entropy = 0.855 \setminus samples = 125 \setminus value = [35, 90]')
                              X[1] \le 143.5
                             entropy = 0.928
                              samples = 506
                           value = [332, 174]
             entropy = 0.761
                                             entropy = 0.855
                                              samples = 125
              samples = 381
                                             value = [35, 90]
            value = [297, 84]
In [121... tree.plot_tree(clf_m_g)
         tree.plot_tree(clf_1_g)
Out[121]: [Text(0.5, 0.75, 'X[2] <= 2.56\nentropy = 2.166\nsamples = 141\nvalue = [44, 50, 10, 8, 24, 5]'),
           Text(0.25, 0.25, 'entropy = 1.777 \setminus samples = 42 \setminus value = [0, 8, 0, 8, 21, 5]'),
           Text(0.75, 0.25, 'entropy = 1.532 \setminus samples = 99 \setminus value = [44, 42, 10, 0, 3, 0]')]
                                   X[2] \le 2.56
                                  entropy = 2.166
                                  samples = 141
                           value = [44, 50, 10, 8, 24, 5]
                 entropy = 1.777
                                                  entropy = 1.532
                                                   samples = 99
                   samples = 42
                                            value = [44, 42, 10, 0, 3, 0]
             value = [0, 8, 0, 8, 21, 5]
         d. Experiment with multi-level decision trees and error pre-pruning by changing the option min_samples_leaf from 0 to the size of the datasets (use some step). (The option
         min samples leaf determines the min number of training instances in the leaf nodes of the decision trees.) Estimate the accuracy rates of the resulting decision trees using the
         training set and hold-out validation. Plot the accuracy rates based on the training set and hold-out validation for min_samples_leaf from 1 to the size of the datasets with step of 5.
         Identify the regions of underfitting, optimality, and overfitting. Explain how you have identified these regions.
In [122...
         run_num = 10
         # DIABETES
         n = 768
         x_d = [0] * round(n/5)
         y_d = [0] * round(n/5)
         y_d_{trainonly} = [0] * round(n/5)
         for k in range (0, run_num):
             di = 0
             X_train_diabetes, X_test_diabetes, Y_train_diabetes, Y_test_diabetes = train_test_split(X_d, Y_d,
             test_size=0.34, random_state = k)
         \# X_train_diabetes, X_test_diabetes, Y_train_diabetes, Y_test_diabetes = train_test_split(X_d, Y_d,
         # test_size=0.34, random_state = 10)
             for i in range (1, n, 5):
                 # Building decision trees, diabetes
                 clf_d = tree.DecisionTreeClassifier(criterion = 'entropy', min_samples_leaf = i)
                 clf_d = clf_d.fit(X_train_diabetes, Y_train_diabetes)
                 # Accuracy of the predictions on train data, diabetes
                 Yp_d_train = clf_d.predict(X_train_diabetes)
                 acc_d_train = accuracy_score(Y_train_diabetes, Yp_d_train)
                 y_d_trainonly[di] += acc_d_train
                 # Accuracy of the predictions on test data, diabetes
                 Yp_d = clf_d.predict(X_test_diabetes)
                 acc_d = accuracy_score(Y_test_diabetes, Yp_d)
                 # print("i = ", i, "; Diabetes accuracy = " , acc_d)
                 x_d[di] = i
                 y_d[di] += acc_d
                 di+=1
         for k in range (0, len(y_d)):
             y_d[k] /= (run_num)
             y_d_trainonly[k] /= (run_num)
         # GLASS
         m = 214
         x_g = [0] * round(m/5)
         y_g = [0] * round(m/5)
         y_g_{trainonly} = [0] * round(m/5)
         gj = 0
         for k in range (0, run_num):
             X_train_glass, X_test_glass, Y_train_glass, Y_test_glass = train_test_split(X_g, Y_g,
             test_size=0.34, random_state = k)
             for j in range (1, m, 5):
                 # Building decision trees, glass
                 clf_g = tree.DecisionTreeClassifier(criterion = 'entropy', min_samples_leaf = j)
                 clf_g = clf_g.fit(X_train_glass, Y_train_glass)
                 # Accuracy of the predictions on train data, glass
                 Yp_g_train = clf_g.predict(X_train_glass)
                 acc_g_train = accuracy_score(Y_train_glass, Yp_g_train)
                 y_g_trainonly[gj] += acc_g_train
                 # Accuracy of the predictions on test data, glass
                 Yp_g = clf_g.predict(X_test_glass)
                 acc_g = accuracy_score(Y_test_glass, Yp_g)
                 \# print("j = ", j, "; Glass accuracy = " , acc_g)
                 x_g[gj] = j
                 y_g[gj] += acc_g
                 gj+=1
         for k in range (0, len(y_g)):
             y_g[k] /= run_num
             y_g_trainonly[k] /= run_num
In [123... import matplotlib.pyplot as plt
         plt.suptitle('Diabetes')
         plt.plot(x_d, y_d, 'b', label = "On test data")
         plt.plot(x_d, y_d_trainonly, 'g', label = "On train data")
         plt.ylabel('Accuracy')
         plt.xlabel('Number of min_samples_leaf')
         plt.axvline(x = 125, color = 'r', label = "Sweet spot", linestyle = ':')
         leg = plt.legend(loc="upper right")
         plt.show()
         plt.suptitle('Glass')
         plt.plot(x_g, y_g, 'b', label = "On test data")
         plt.plot(x_g, y_g_trainonly, 'g', label = "On train data")
         plt.ylabel('Accuracy')
         plt.xlabel('Number of min_samples_leaf')
         plt.axvline(x = 42, color = 'r', label = "Sweet spot", linestyle = ':')
         leg = plt.legend(loc="upper right")
         plt.show()
                                            Diabetes
            1.00
                                                                     On test data
                                                                     On train data
                                                                     Sweet spot
            0.95
            0.90
            0.85
          Accuracy
            0.80
            0.75
            0.70
            0.65
                          100
                                  200
                                          300
                                                  400
                                                         500
                                                                 600
                                                                         700
                                                                                800
                    0
                                     Number of min_samples_leaf
                                             Glass
                                                                    On test data
            1.0
                                                                    On train data
                                                                    Sweet spot
            0.9
            0.8
          Accuracy
            0.6
            0.5
            0.4
            0.3
                                50
                                             100
                                                            150
                                                                         200
                   0
                                    Number of min_samples_leaf
         Sweet spot is so called optimality, the area where the algorithm neither underfits, nor overfits. On the graoh it is the area where the accuracy on test data and train data are more or
         less the same. Everything before this area underfits, everything after - overfits.
         DIABETES
         Regions of underfitting: min samples leaf < 125, regions of optimality: min samples leaf ~ 125, regions of overfitting: min samples leaf > 125
         GLASS
         Regions of underfitting: min samples leaf < 42, regions of optimality: min samples leaf ~ 42, regions of overfitting: min samples leaf > 42
```

In [113... import pandas as pd

from sklearn import tree

Y\_d = diabetes\_data['class']

In [116... | # Splits the data into training and test

Y\_g = glass\_data['class']

from sklearn.metrics import accuracy\_score

X\_d = diabetes\_data.drop(['class'], axis=1)

X\_g = glass\_data.drop(['class'],axis=1)

from sklearn.model\_selection import train\_test\_split

# X\_d is everuthing but class column and id (I guess)

In [114... diabetes\_data = pd.read\_csv('C:/Users/sophi/Desktop/UM\_bachelor/year\_2/Machine Learning/Lab 1/diabetes.csv')
glass\_data = pd.read\_csv('C:/Users/sophi/Desktop/UM\_bachelor/year\_2/Machine Learning/Lab 1/glass.csv')

c. Train one-level decision trees and multi-level decision trees on the two data sets. Determine the accuracy rates of the resulting classifiers using the training set and hold- out

validation1. Explain why there is a difference in the accuracy rates. Compare one- level decision trees and multi-level decision trees in terms of explainability.

In [115... # Y\_d is the class column, which stores one of the two values: tested\_negative, tested\_positive