

LAB 03

04/08/25

Problema 2: 25%

Utilice el Lema de Arden para encontrar la expresión regular del siguiente autómata. Deje todo su procedimiento



$$q_0 = \epsilon$$

$$q_1 = \epsilon + q_0 \epsilon$$

$$q_2 = \epsilon + q_1 0 \rightarrow \epsilon + (\epsilon + q_0 \epsilon) 0$$

$$q_3 = \epsilon + q_0 \epsilon$$

$$q_4 = \epsilon + q_3 \epsilon \rightarrow \epsilon + (\epsilon + q_0 \epsilon) \epsilon$$

$$q_5 = q_2 \epsilon + q_4 \epsilon$$

$$= \epsilon(q_2 + q_4) \rightarrow \epsilon[\epsilon + (\epsilon + q_0 \epsilon) 0 + \epsilon + (\epsilon + q_0 \epsilon) \epsilon]$$

$$\epsilon[\epsilon + (\epsilon + q_0 \epsilon)(0 + \epsilon)]$$

$$\cancel{\epsilon} + \cancel{\epsilon}(\epsilon + q_0 \epsilon)(0 + \epsilon) = (\epsilon + q_0)(0 + \epsilon)$$

$$q_5 = (\epsilon + q_0)(0 + \epsilon)$$

$$q_6 = q_5 \epsilon = (\epsilon + q_0)(0 + \epsilon)$$

$$q_7 = q_6 \epsilon = (\epsilon + q_0)(0 + \epsilon)$$

$$q_8 = \epsilon + q_7 1 = (\epsilon + q_0)(0 + \epsilon) 1 + \epsilon$$

$$q_9 = q_6 \epsilon = (\epsilon + q_0)(0 + \epsilon)$$

$$q_{10} = q_9 \epsilon = (\epsilon + q_0)(0 + \epsilon)$$

$$q_{11} = q_8 \epsilon + q_{10} \epsilon = (\epsilon + q_0)(0 + \epsilon) 1 + (\epsilon + q_0)(0 + \epsilon) + \epsilon$$

$$q_{11} = (\epsilon + q_0)(0 + \epsilon)(1 + \epsilon)$$

$$q_{12} = q_5 \epsilon = (\epsilon + q_0)(0 + \epsilon)$$

$$q_{13} = "$$

$$q_{14} = q_{13} \epsilon + q_{11} \epsilon = (\epsilon + q_0)(0 + \epsilon) + (\epsilon + q_0)(0 + \epsilon)(1 + \epsilon)$$

$$= (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1 + \epsilon)$$

$$q_{14} = (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1)$$

$$q_{15} = q_{14} \epsilon + q_{10} \epsilon = (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) + q_{10} \epsilon$$

$$q_{16} = \epsilon + q_{15} 0 = [(\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) + q_{10}] 0 + \epsilon$$

$$= (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) 0 + q_{10} 0 + \epsilon \rightarrow q_{16} = [\epsilon + (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) 0] 0^*$$

$$q_{17} = \epsilon + q_{14} \epsilon + (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) 0 + q_{10} 0$$

$$= \epsilon + (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) + (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) 0 + q_{10} 0$$

$$= (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1)[\epsilon + 0] + q_{10}$$

$$q_{17} = (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1)(\epsilon + 0) + [\epsilon + (\epsilon + q_0)(0 + \epsilon)(\epsilon + 1) 0] 0^*$$