



Evaluating State-of-the-Art #SAT Solvers on Industrial Configuration Spaces

Chico Sundermann¹, Tobias Heß¹, Michael Nieke², Paul M. Bittner¹, Jeffrey M. Young⁴, Thomas Thüm¹, Ina Schaefer^{2,3}
SE'24 | 27.02.2024



universität
ulm

2)



3)

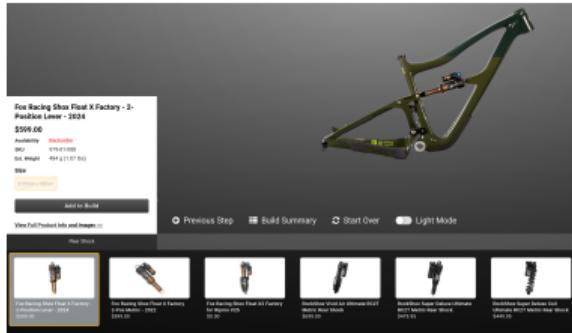


4)

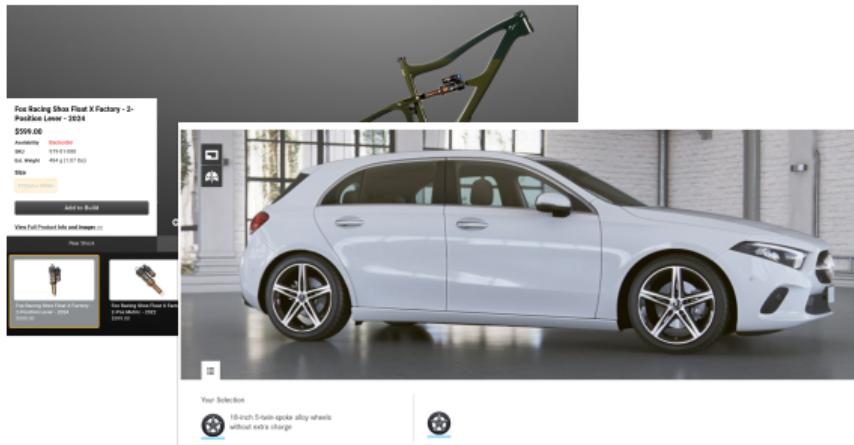


Oregon State
University

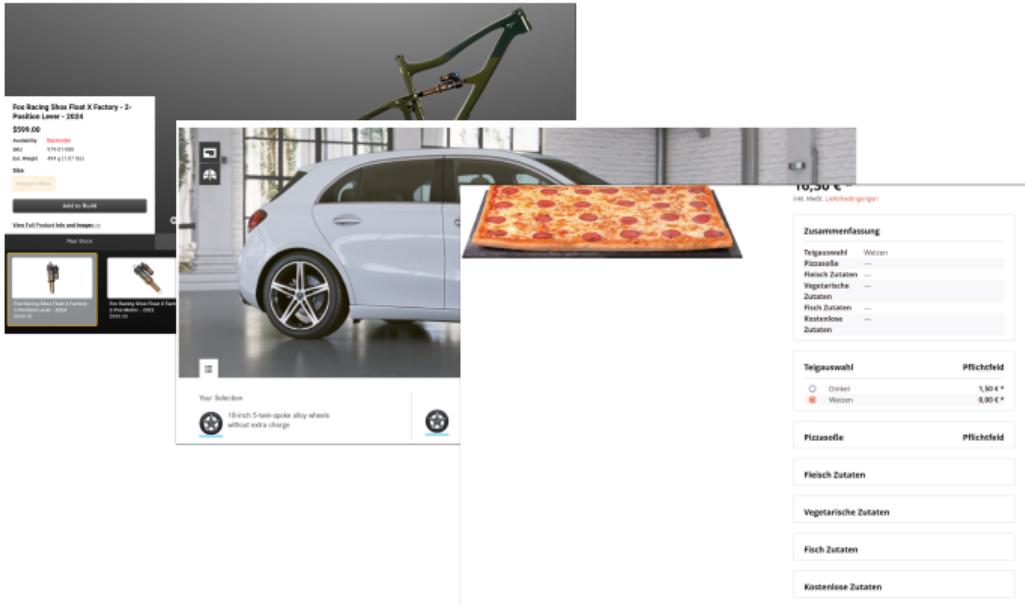
Configurable Systems



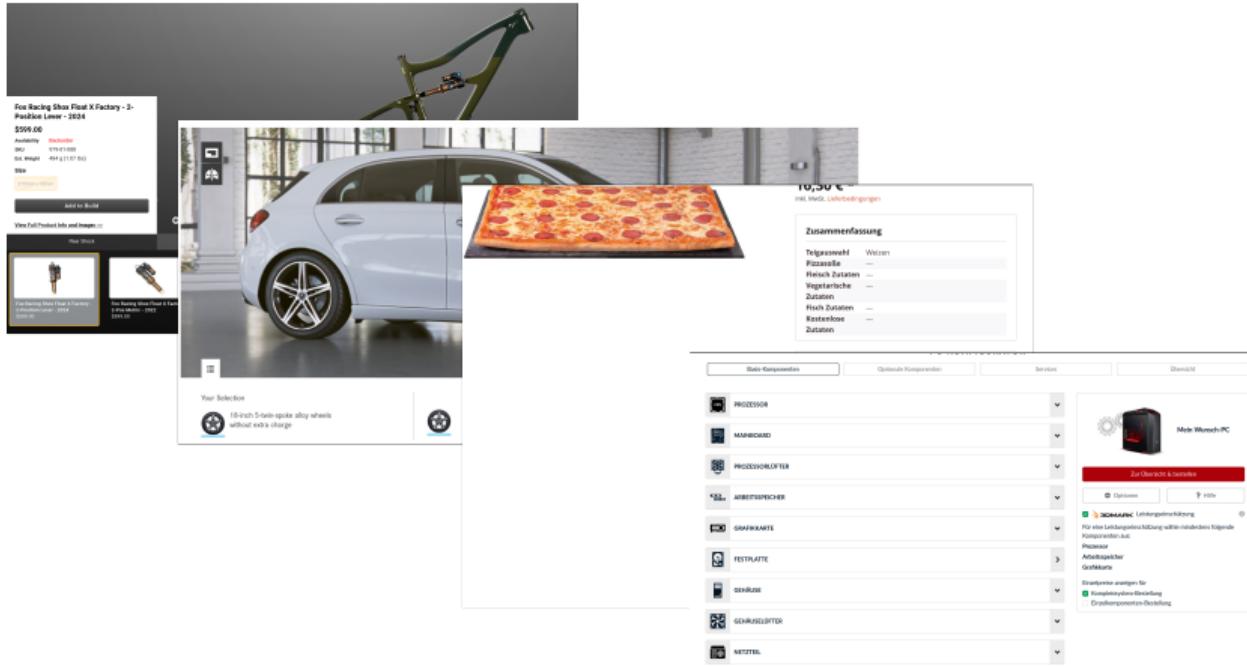
Configurable Systems



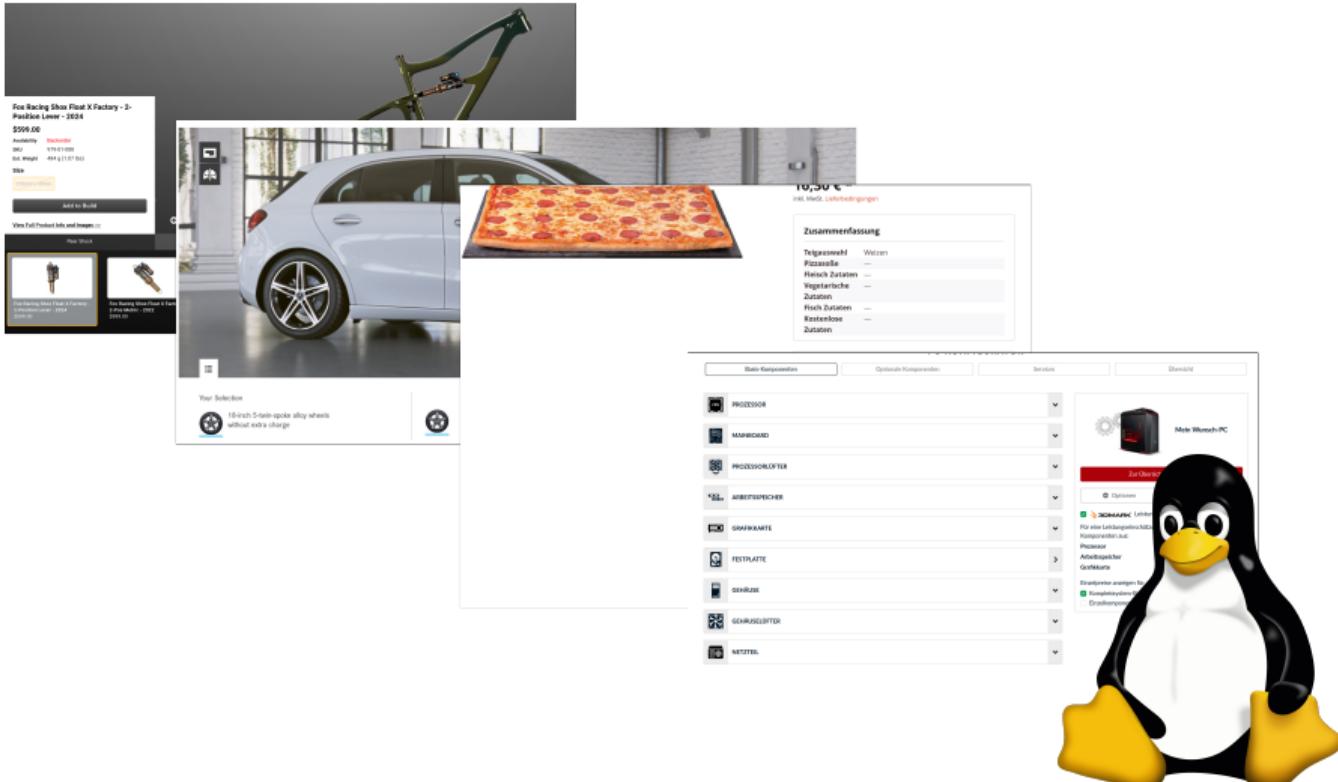
Configurable Systems



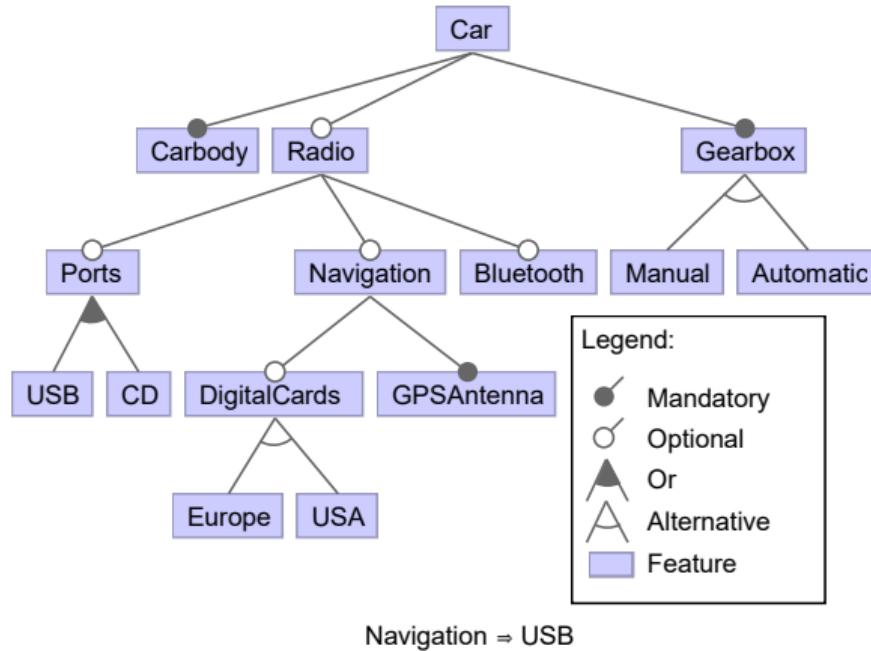
Configurable Systems



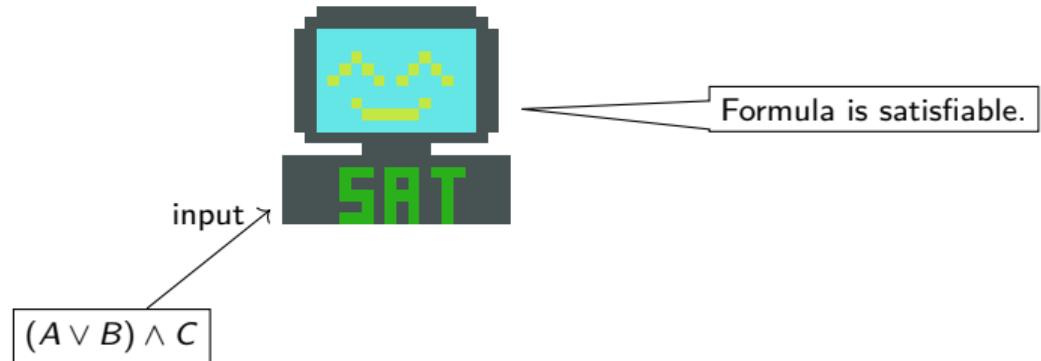
Configurable Systems



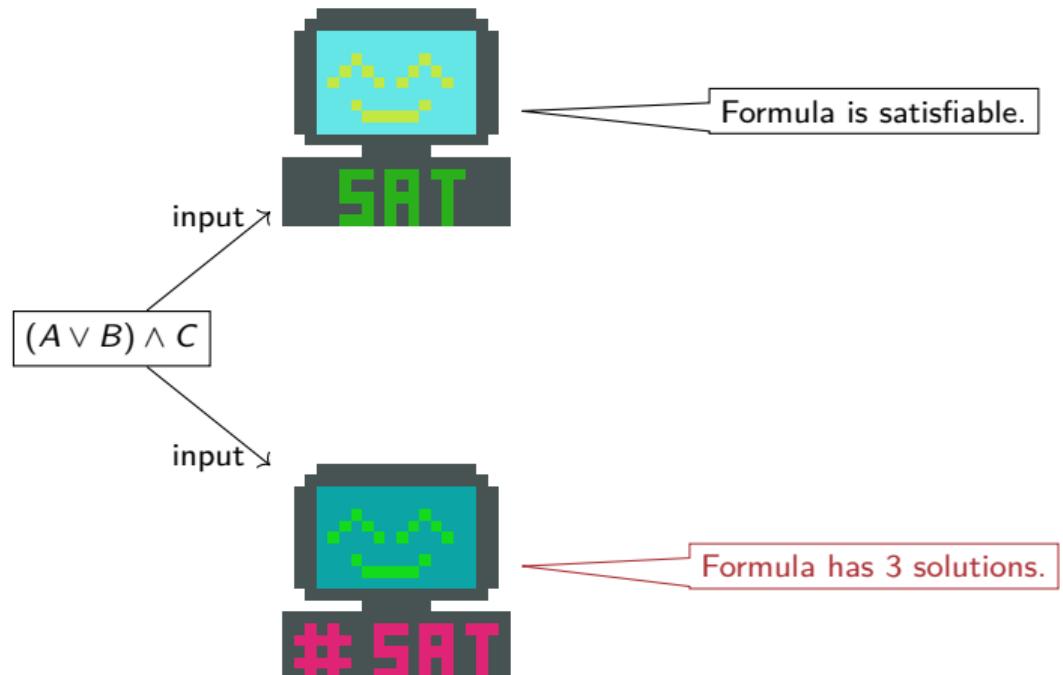
Feature Models



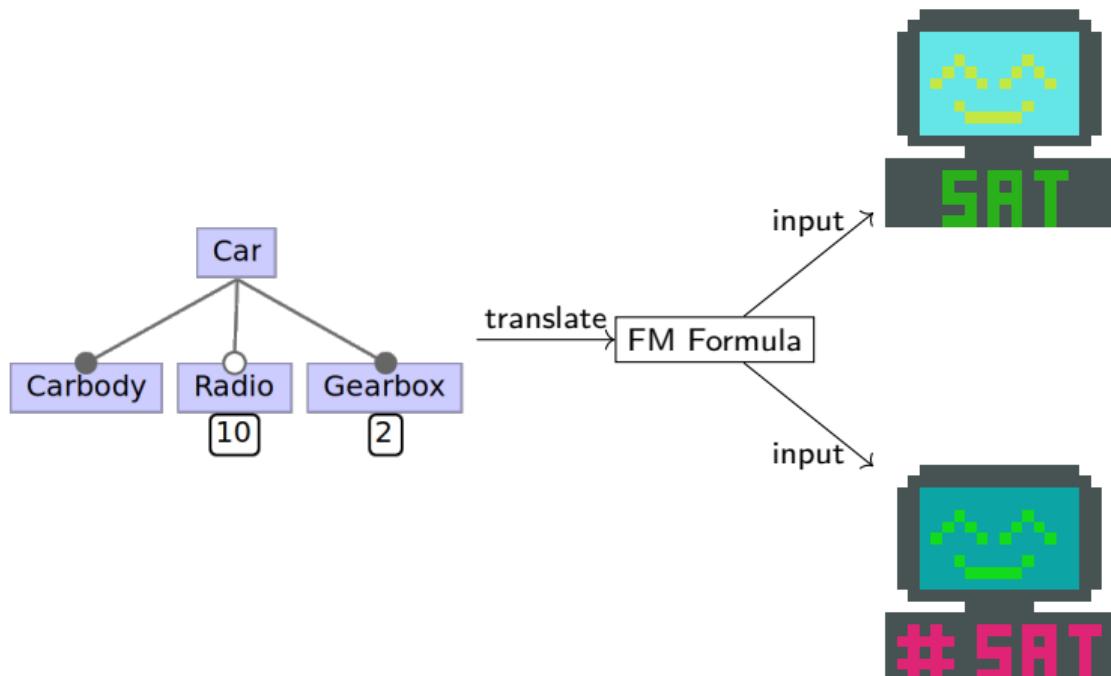
What is SAT?



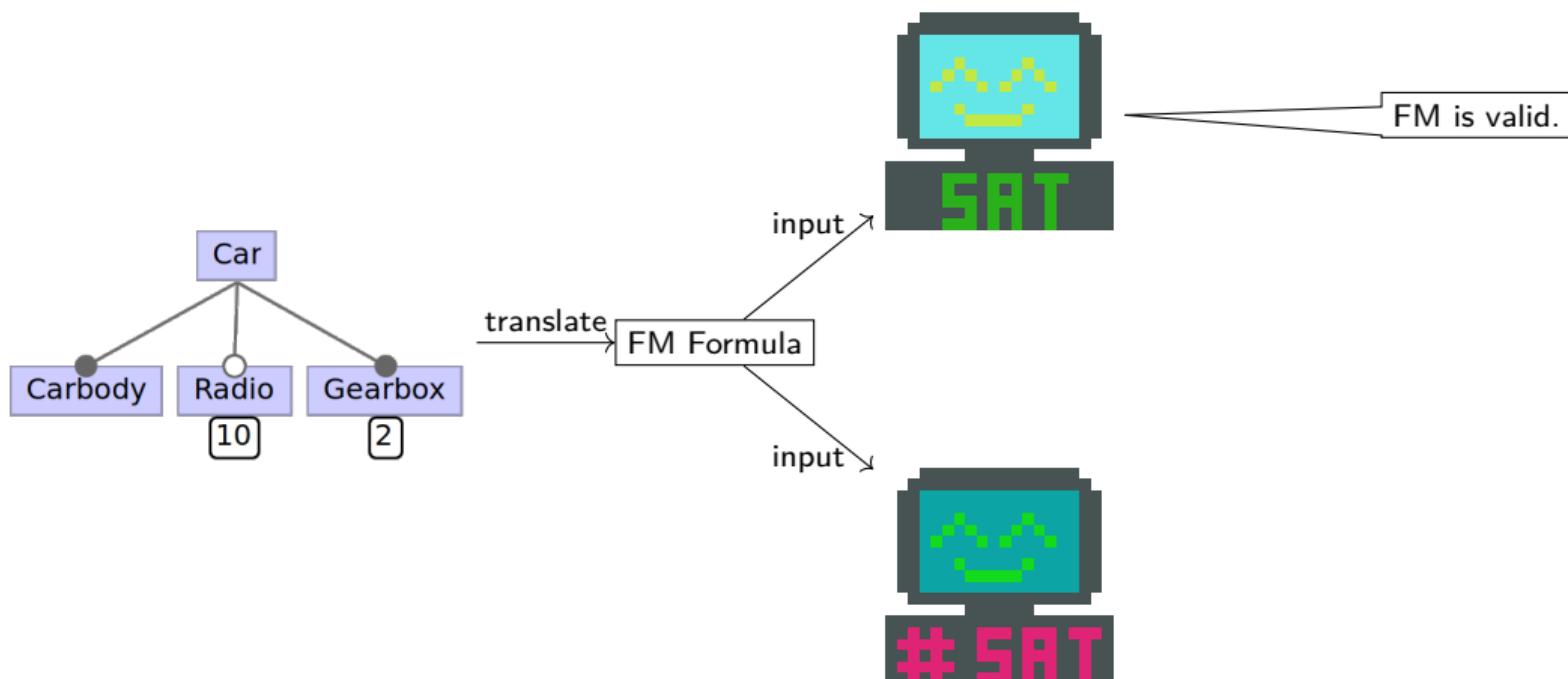
What is #SAT?



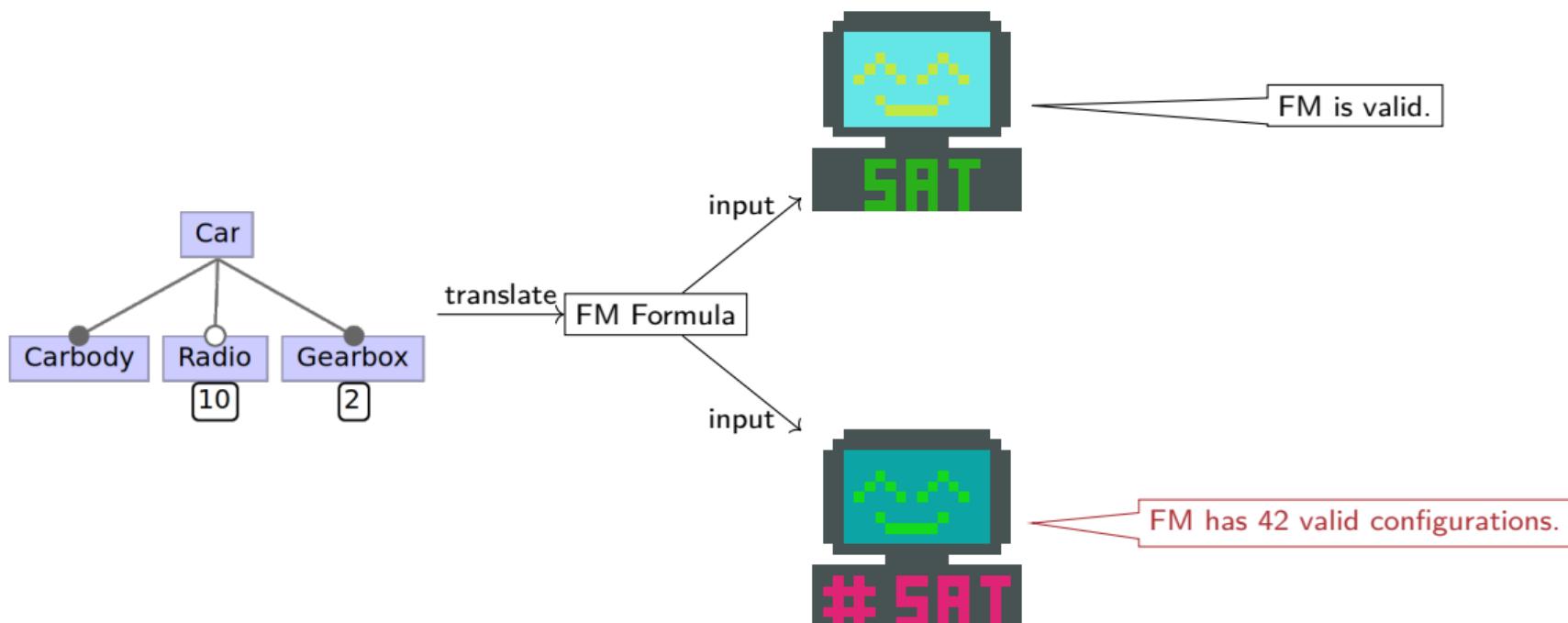
What is #SAT?



What is #SAT?



What is #SAT?



Variability Factor

Homogeneity

Uniform Random Sampling

Applications of #SAT Solvers on Feature Models

Chico Sundermann
University of Ulm, Germany

Tobias Heß
University of Ulm, Germany

Michael Nieke
TU Braunschweig, Germany

Thomas Thüm
University of Ulm, Germany

Paul Maximilian Bittner
University of Ulm, Germany

Ina Schaefer
TU Braunschweig, Germany

Configuration Relevance

Feature Prioritization

Rating Errors

CTC Restrictiveness

Variability Reduction

Optimize Configuring

Subset Variability

Variability Factor

Void Feature Moddel

Degree of Orthogonality

Cost Savings

Maintainability Prediction

Configuration Relevance

Rating Errors

Variability Reduction

Subset Variability

Homogeneity

Payoff Threshold

Degree of Reuse

Core, Dead & False-Optional

Atomic Set Candidates

Feature Prioritization

CTC Restrictiveness

Optimize Configuring

Uniform Random Sampling

Atomic Sets

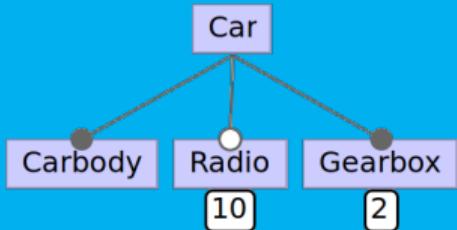
Rate Interactions

Configuration Derivation

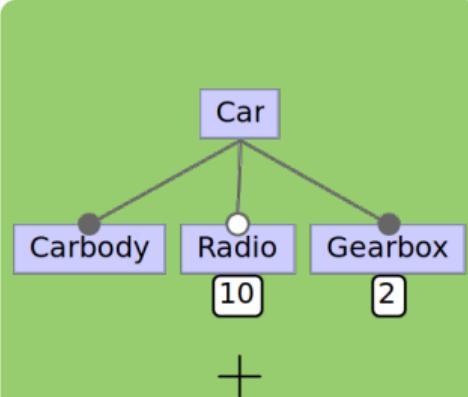
Variability Factor
Void Feature Model
Degree of Orthogonality
Cost Savings
Maintainability Prediction
Configuration Relevance
Rating Errors
Variability Reduction
Subset Variability

Homogeneity
Payoff Threshold
Degree of Reuse
Core, Dead & False-Optional
Atomic Set Candidates
Feature Prioritization
CTC Restrictiveness
Optimize Configuring

Uniform Random Sampling
Atomic Sets
Rate Interactions
Configuration Derivation



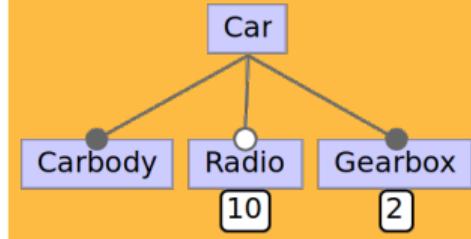
Cardinality of
Feature Models



+

Radio

Cardinality of
Features

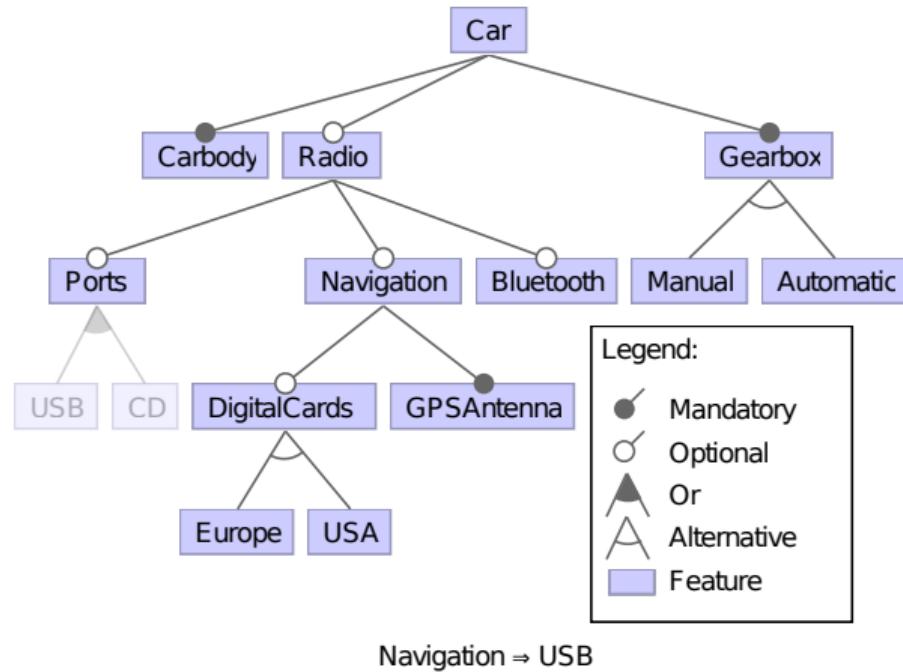


+

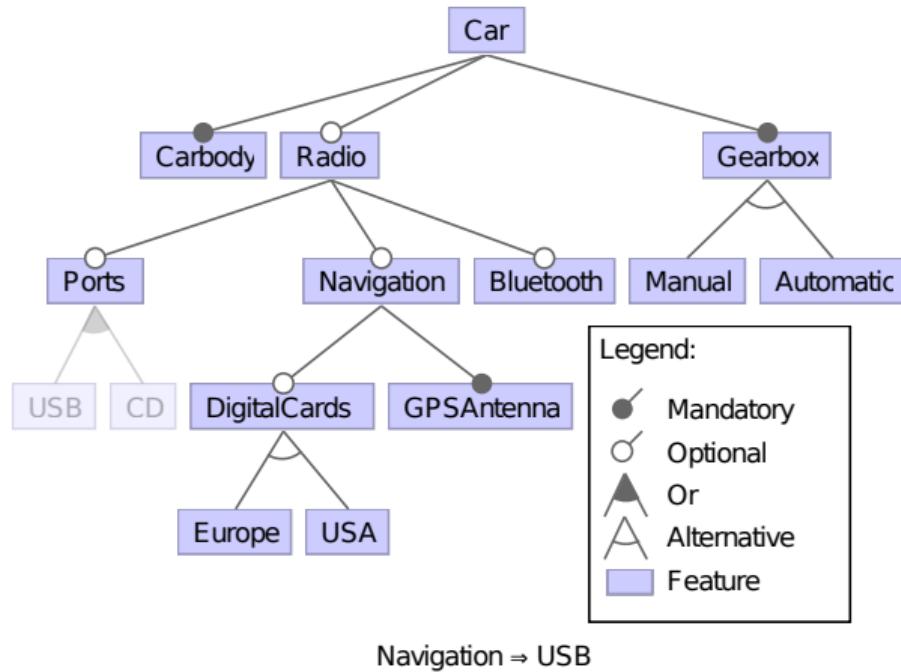


Cardinality of
Partial Configurations

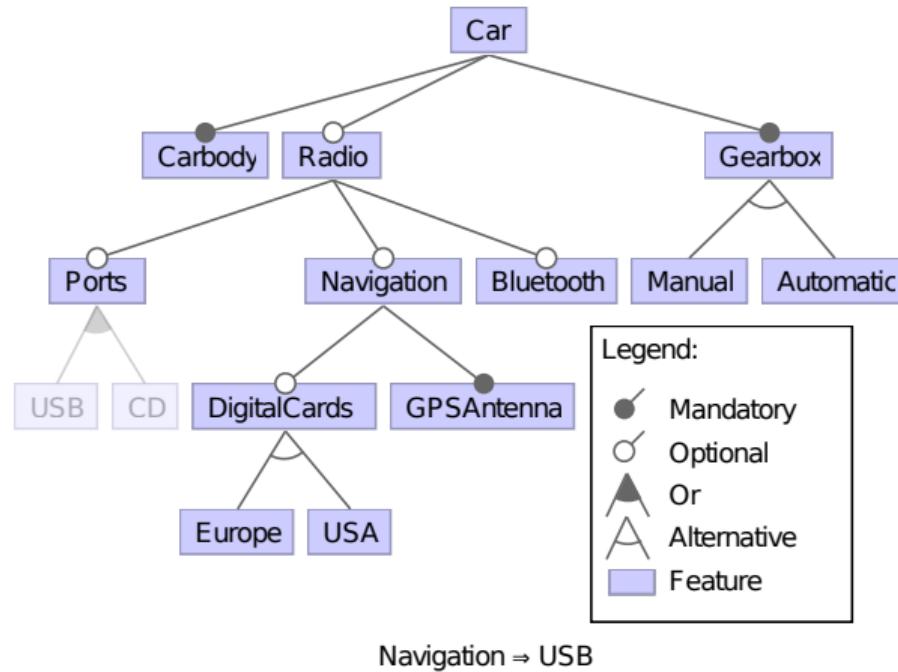
Feature Prioritization



Feature Prioritization



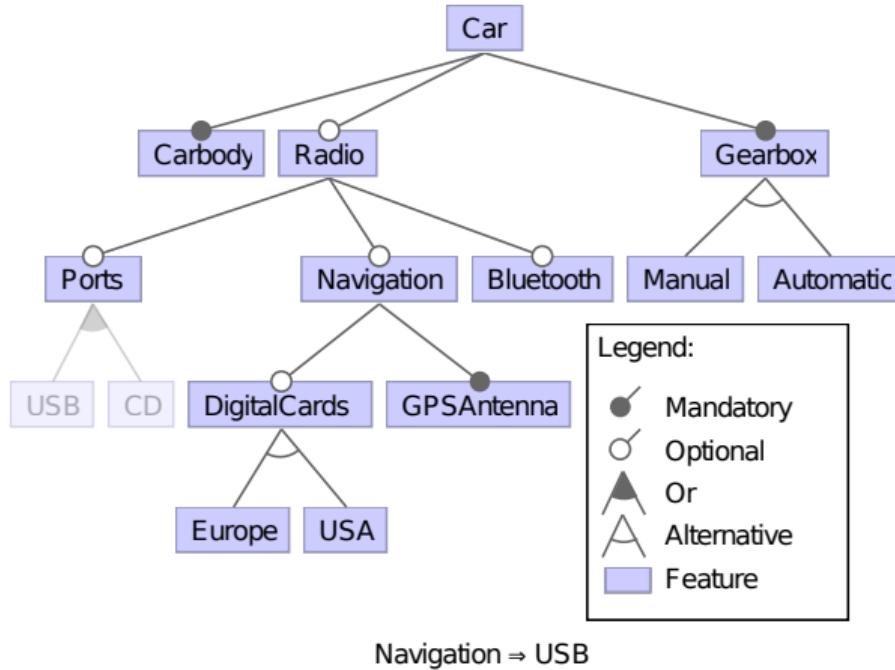
Which feature to develop first?



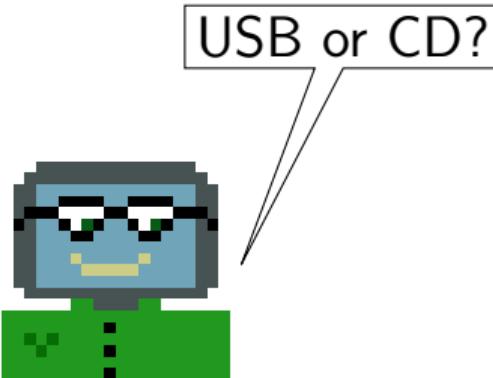
Feature Prioritization

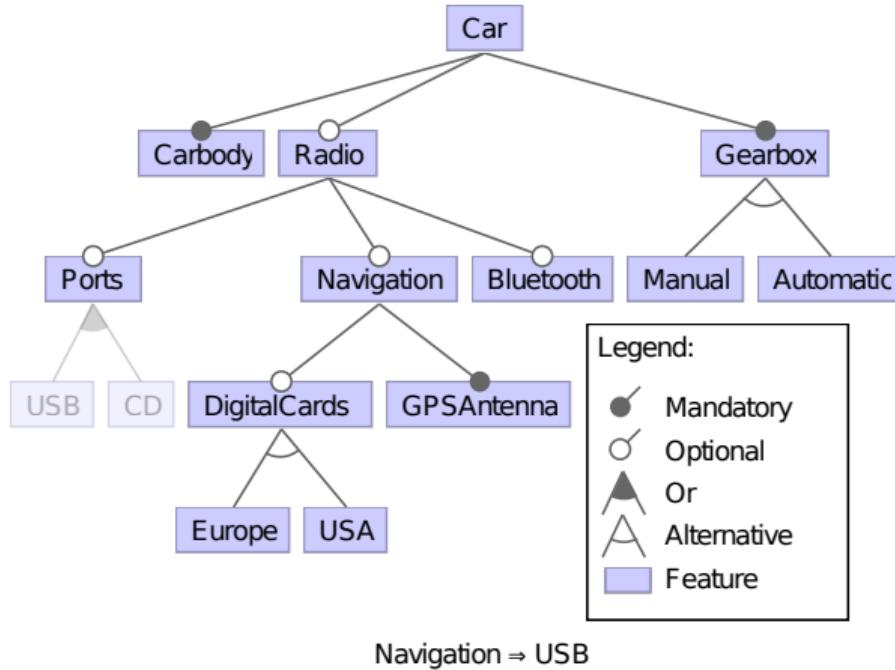
Which feature to develop first?

Prioritize based on cardinality



Feature Prioritization

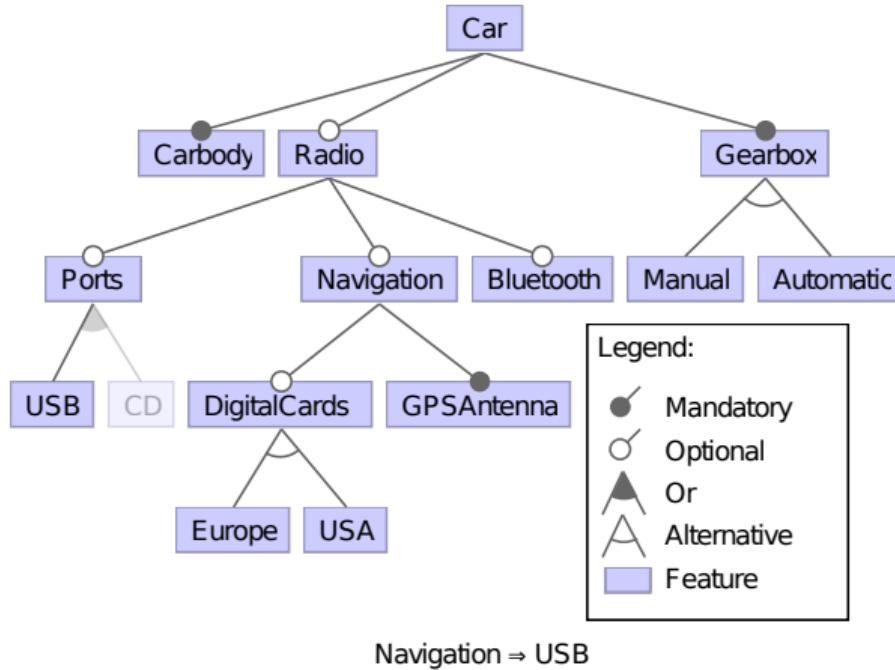




Feature Prioritization

#USB: 32
#CD: 20





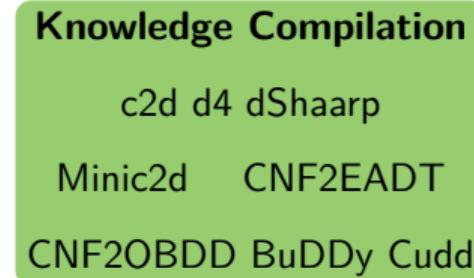
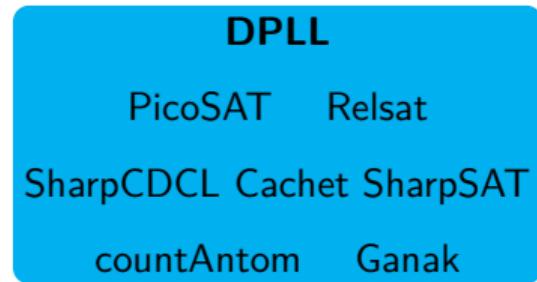
Feature Prioritization

Prioritize USB
 $\#USB > \#CD$



Experiment Design

- 17 Solvers (15 exact, 2 approximate)
 - ▶ 7 DPLL Solvers (Single query)
 - ▶ 8 Knowledge Compilers (3 d-DNNF, 3 BDD, 2 other)



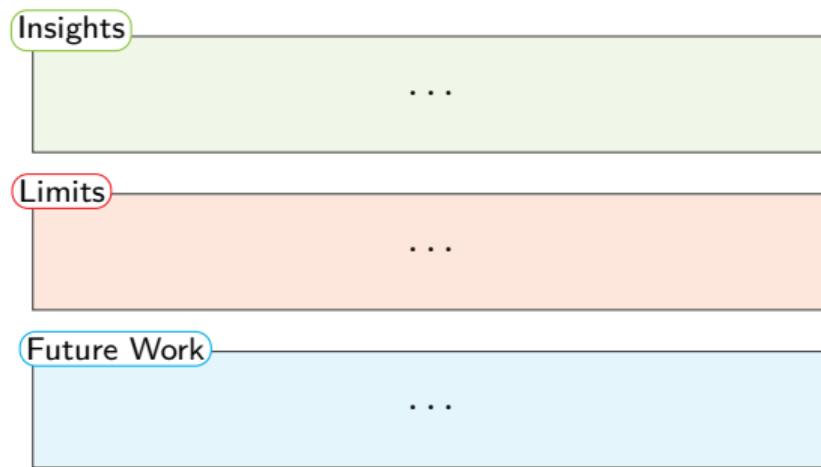
Experiment Design

- 17 Solvers (15 exact, 2 approximate)
 - ▶ 7 DPLL Solvers (Single query)
 - ▶ 8 Knowledge Compilers (3 d-DNNF, 3 BDD, 2 other)
- 15 Subject Systems
 - ▶ 6 Evolutions
 - ▶ 373 Feature Models

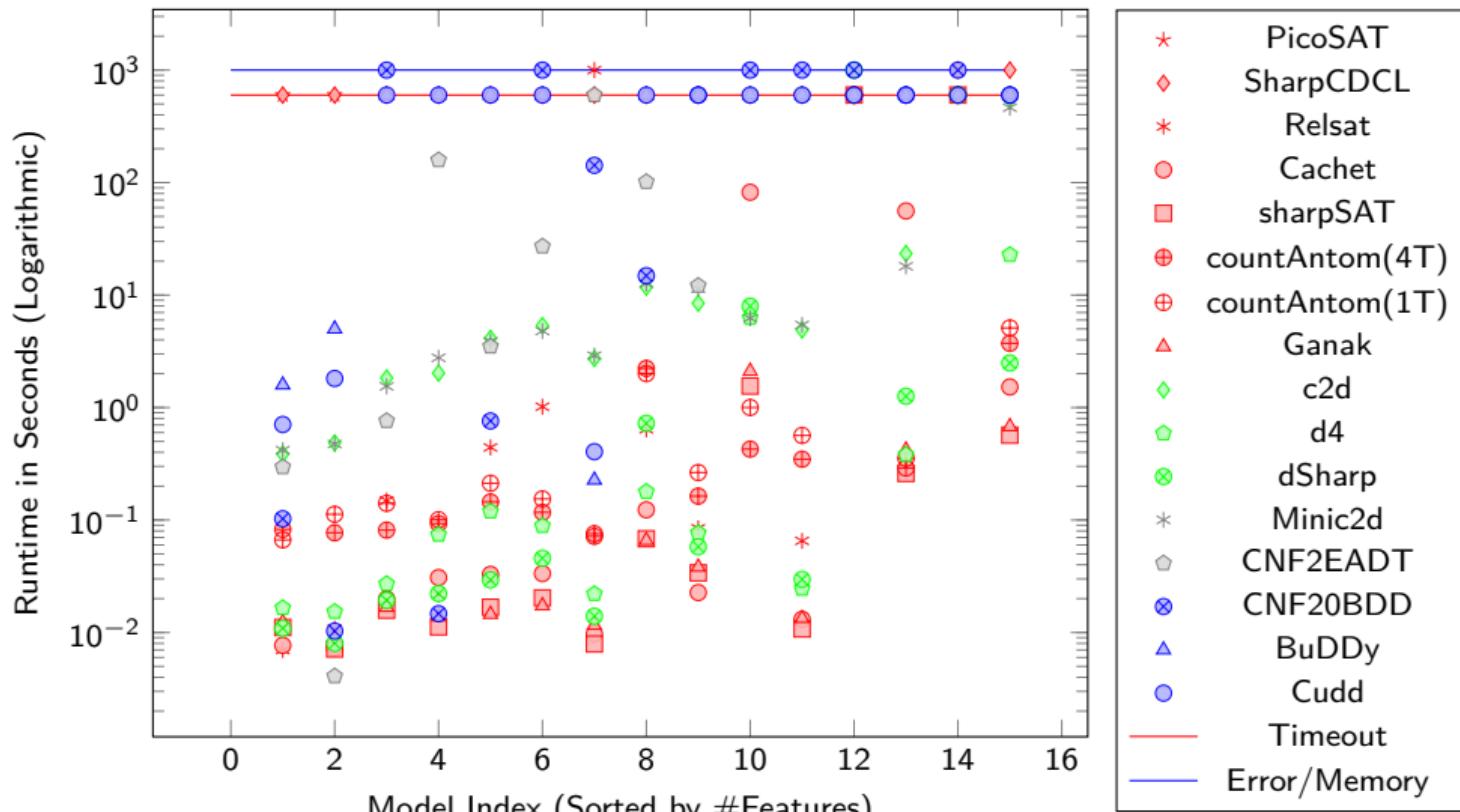
Systems	#Vers.	#Feat.	#Const.
BerkeleyDB	1	76	20
axTLS	1	96	14
uClibc	1	313	56
uClinux-base	1	380	3,455
Automotive04	50	127–531	0–623
Automotive03	5	149–588	0–1,184
BusyBox	37	439–631	463–691
FinancialServices	10	557–771	1,001–1,148
Embtoolkit	1	1,179	323
CDL	116	1,178–1,408	816–956
uClinux-dist.	1	1,580	197
Automotive05	136	246–1,663	0–11,632
Automotive01	1	2,513	2,833
Linux	1	6,467	3,545
Automotive02	4	14,010–18,616	666–1,369

Experiment Design

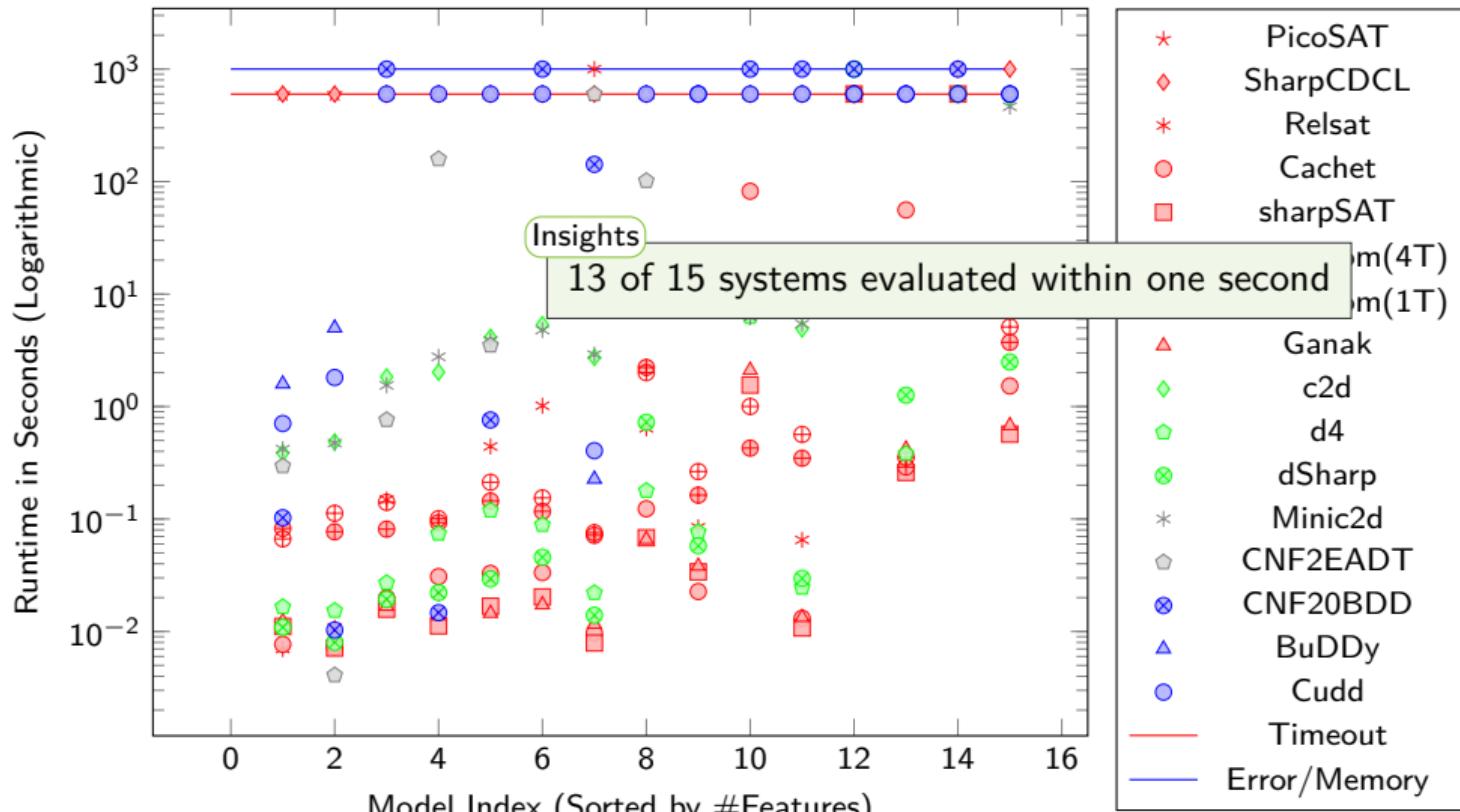
- 17 Solvers (15 exact, 2 approximate)
 - ▶ 7 DPLL Solvers (Single query)
 - ▶ 8 Knowledge Compilers (3 d-DNNF, 3 BDD, 2 other)
- 15 Subject Systems
 - ▶ 6 Evolutions
 - ▶ 373 Feature Models
- Objectives
 - ▶ Scalability #SAT solvers
 - ▶ Recommendations: Solvers/Techniques
 - ▶ Future work



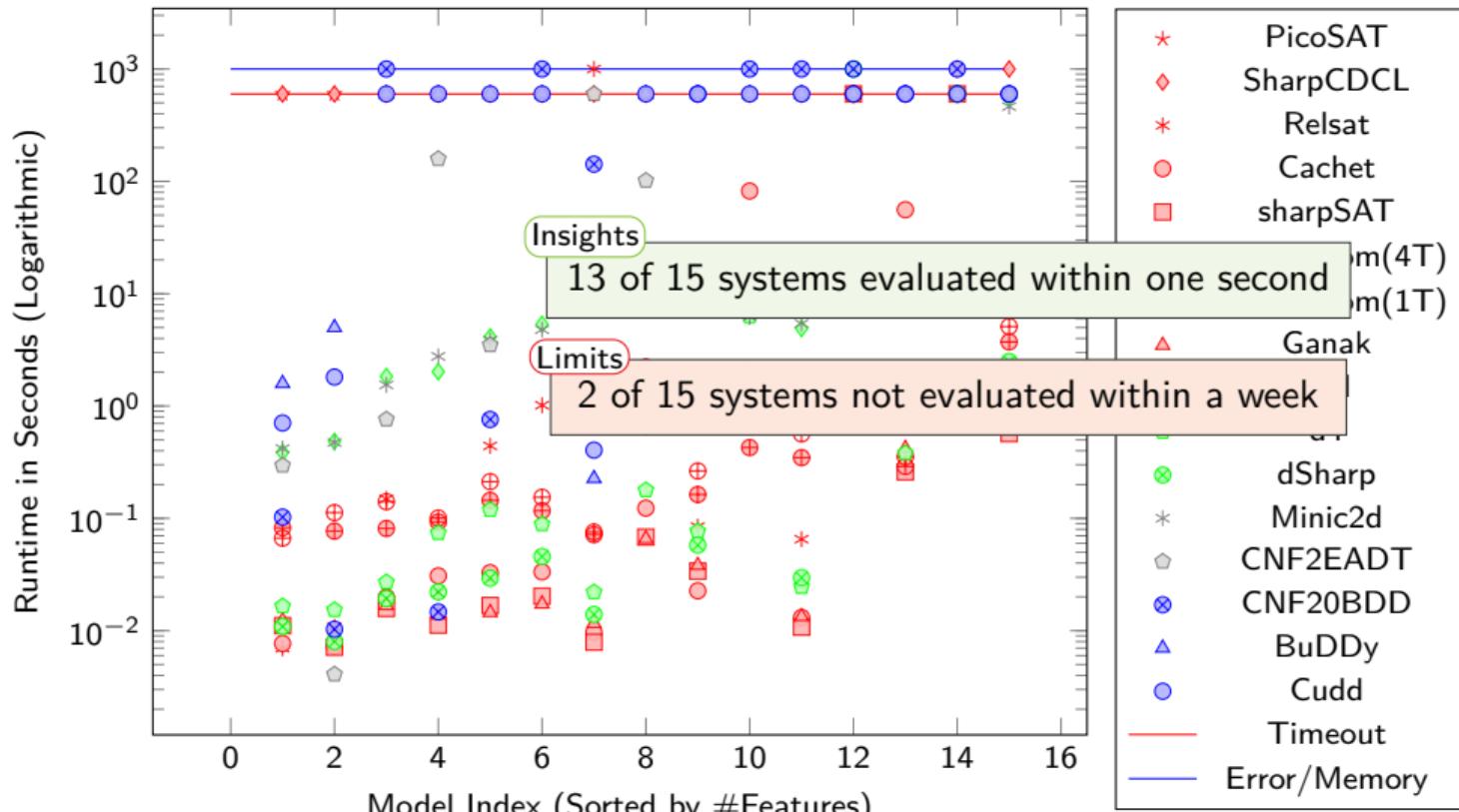
Scalability #SAT



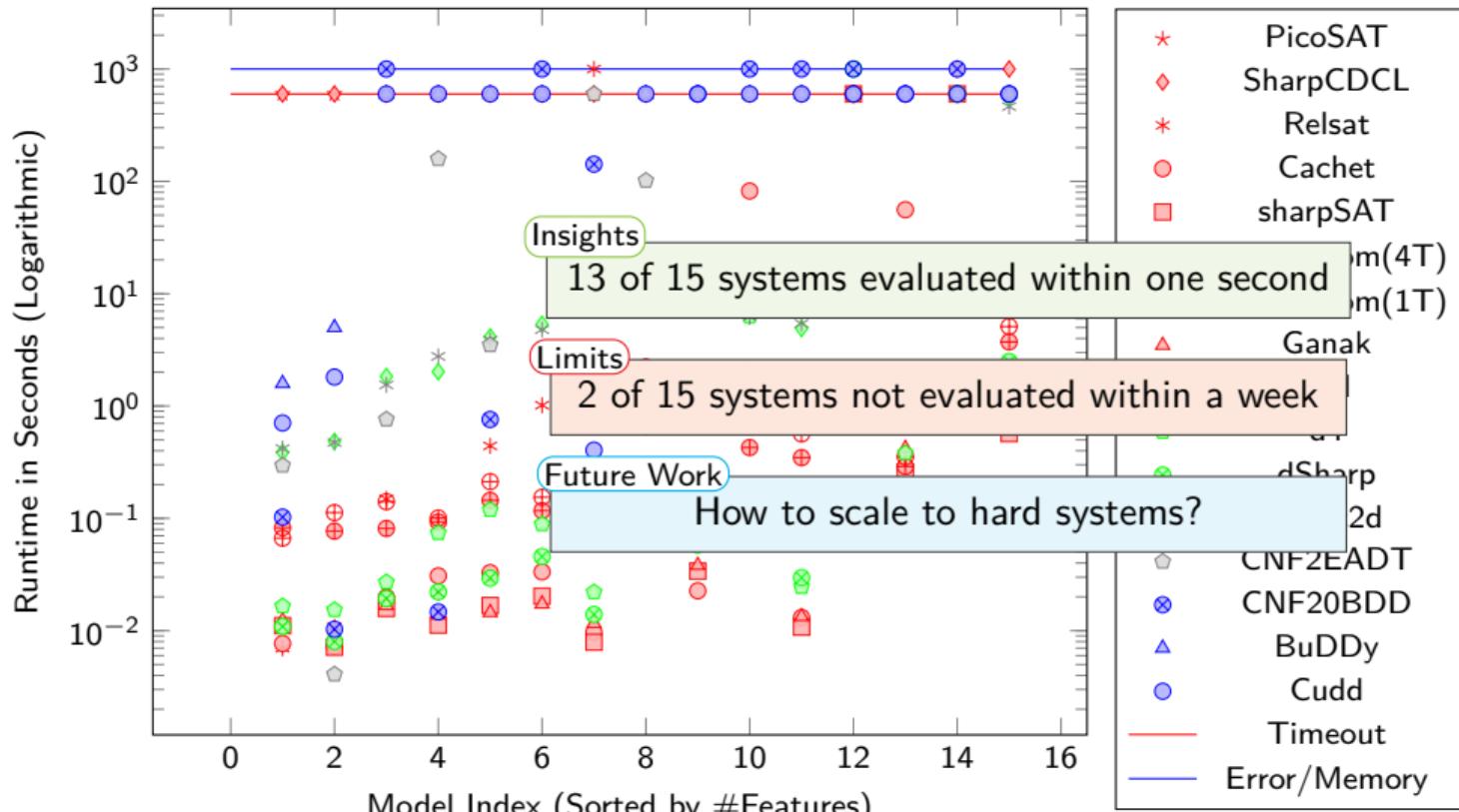
Scalability #SAT



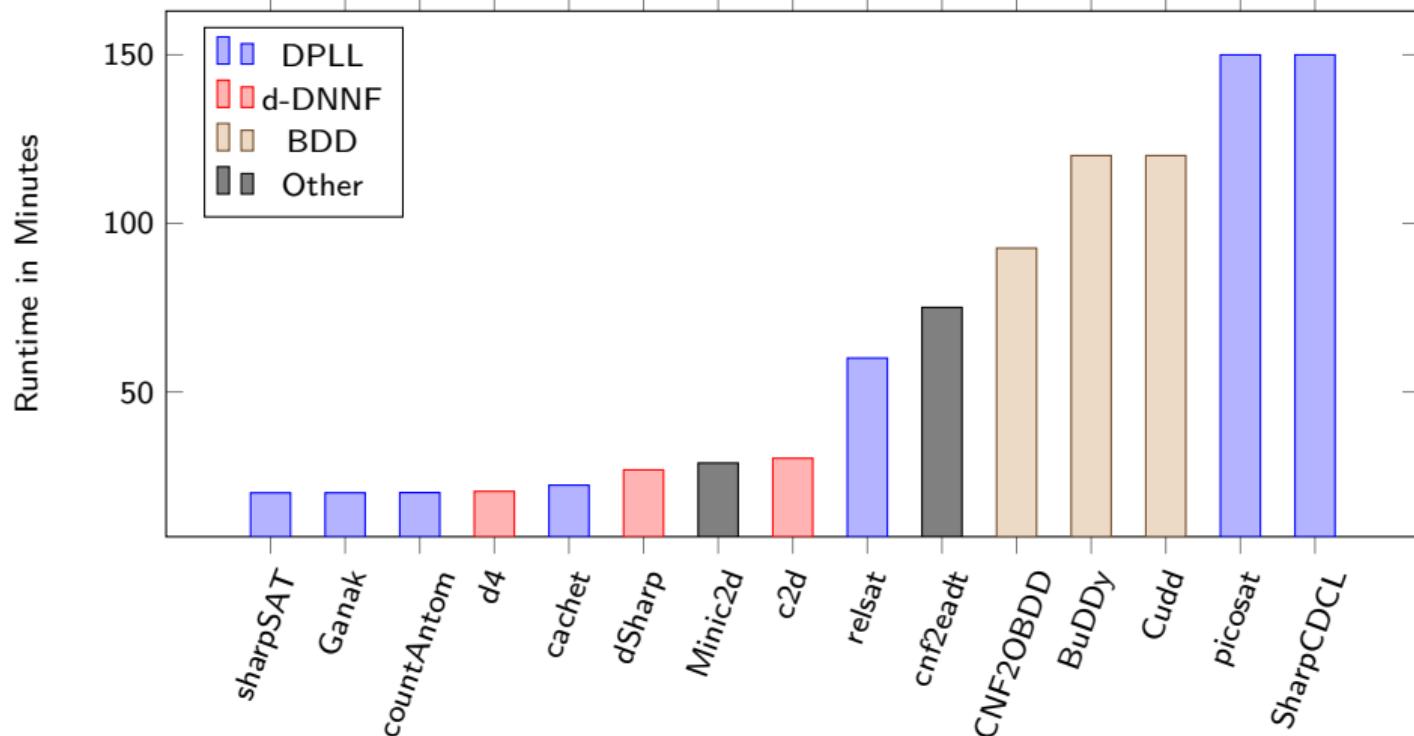
Scalability #SAT



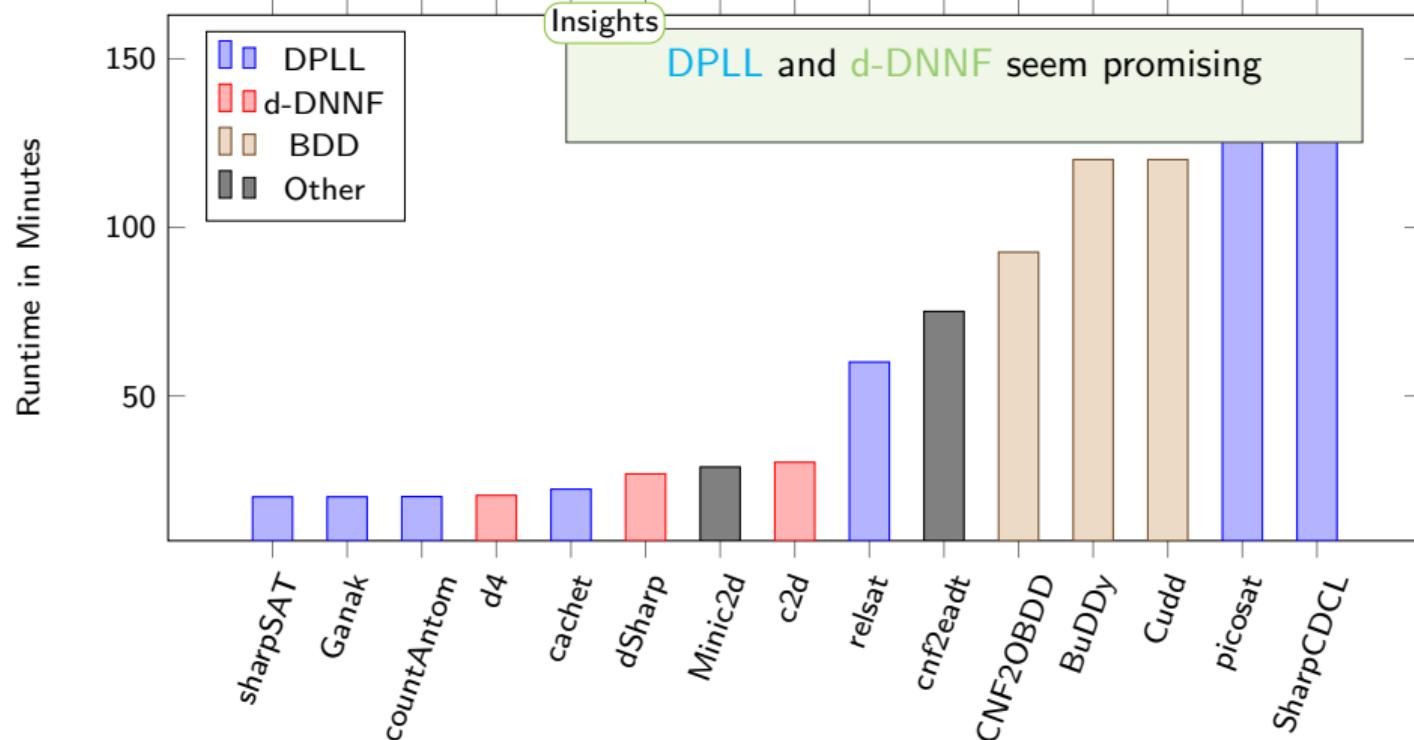
Scalability #SAT



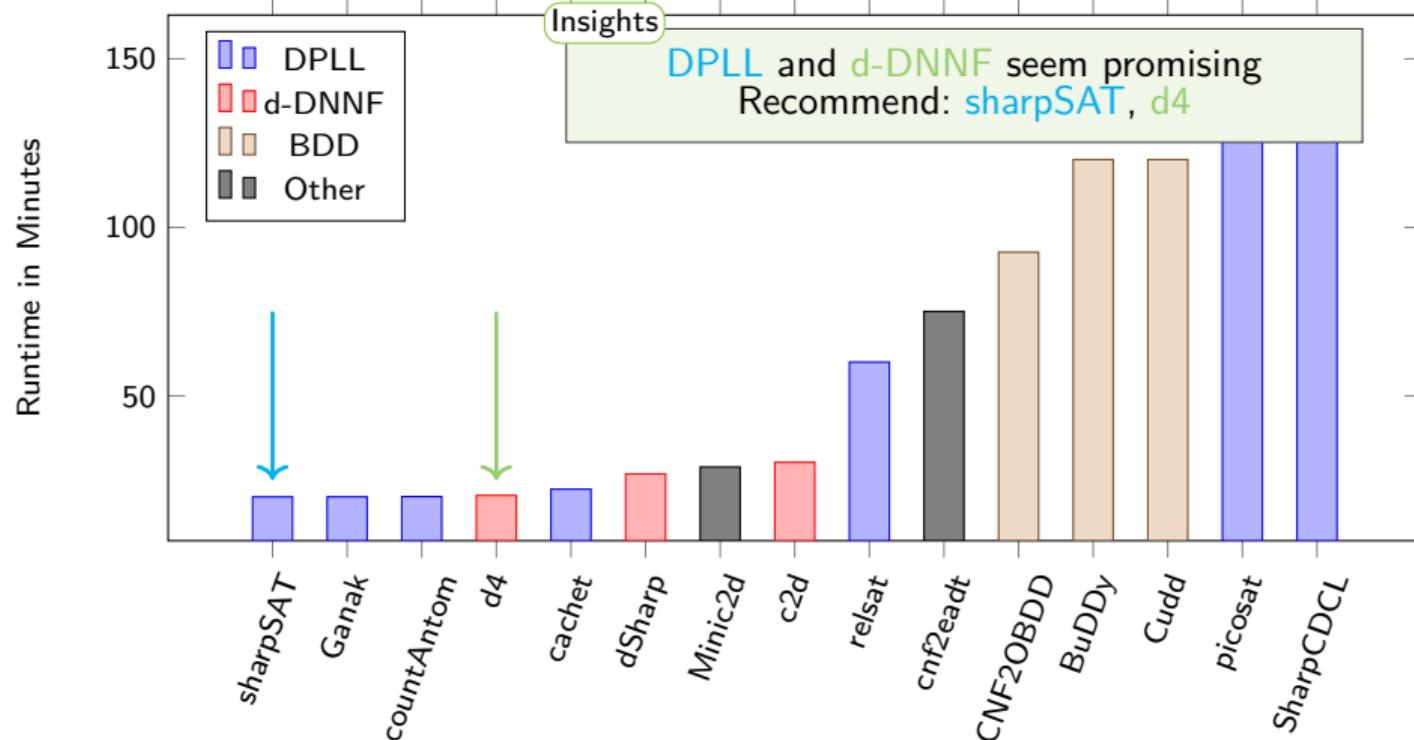
Performance Solvers



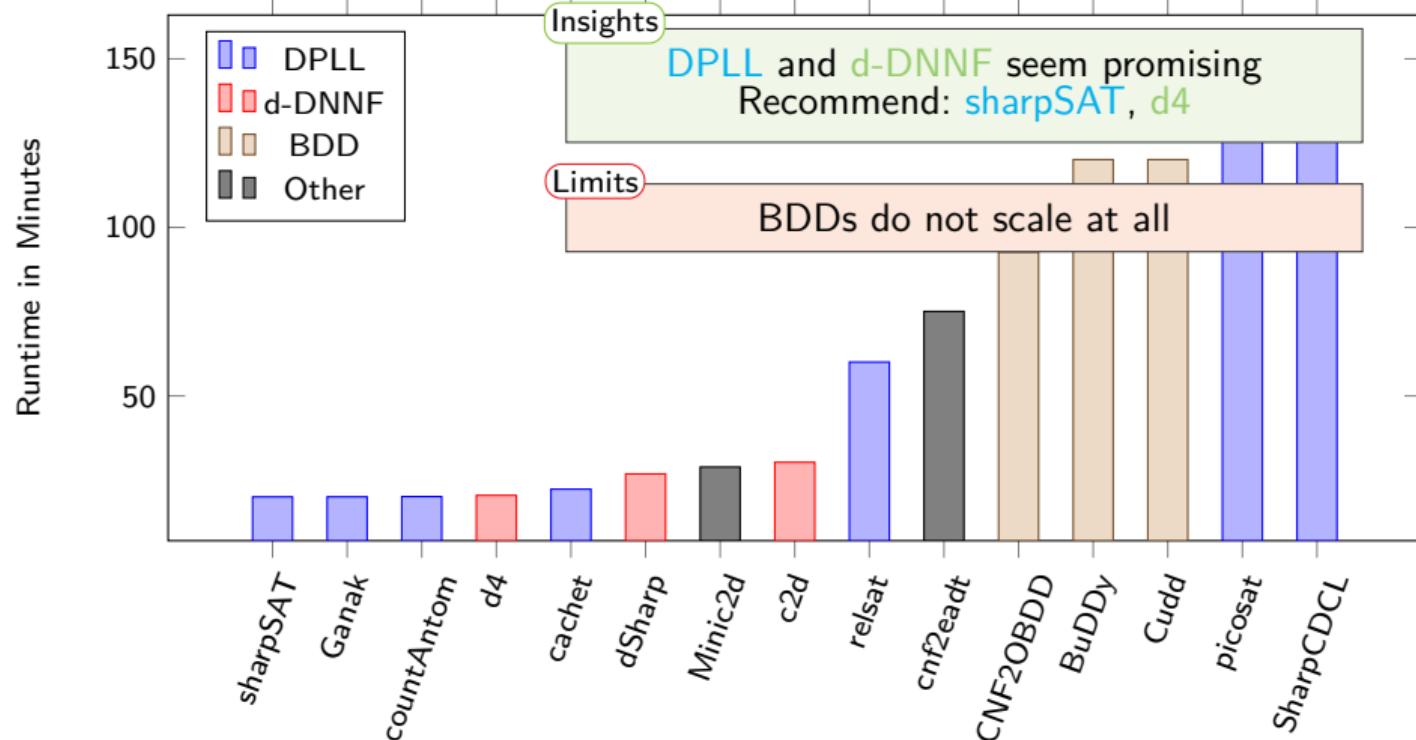
Performance Solvers



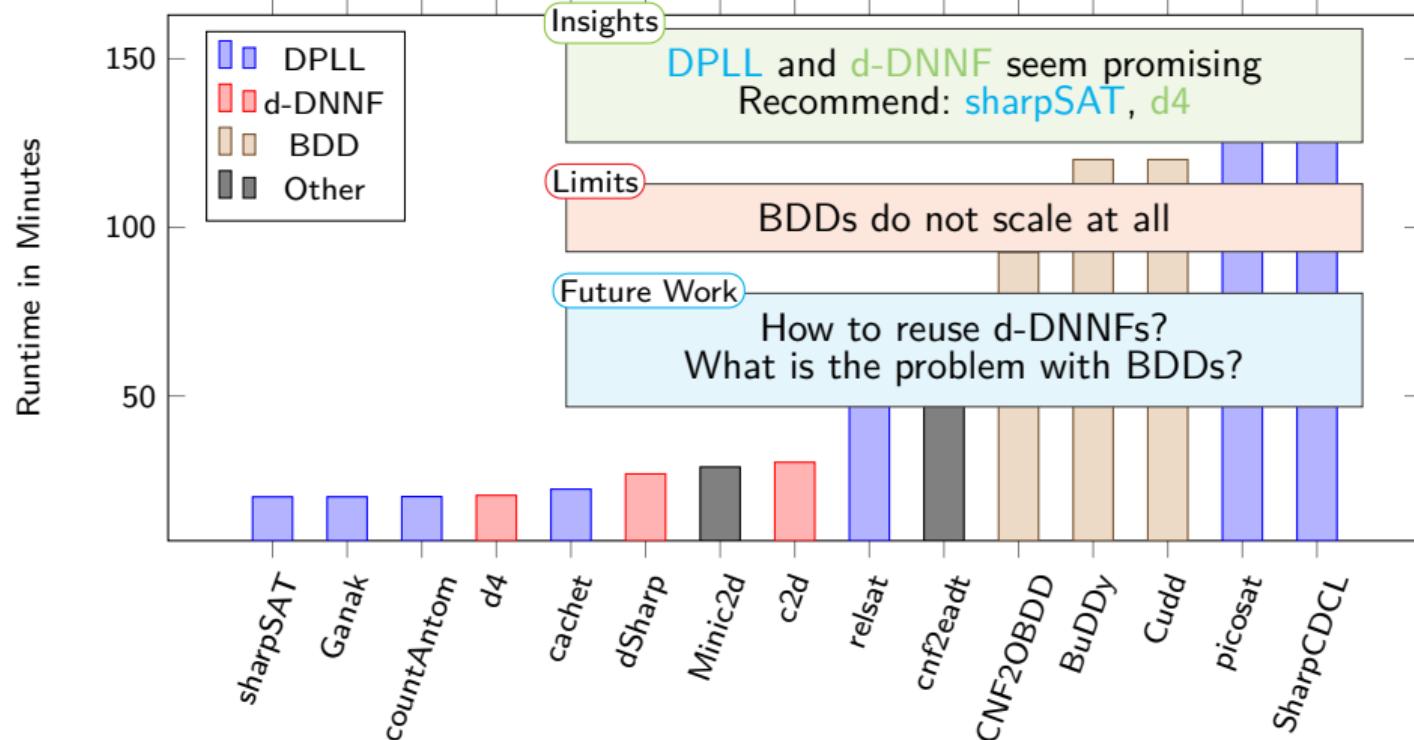
Performance Solvers



Performance Solvers



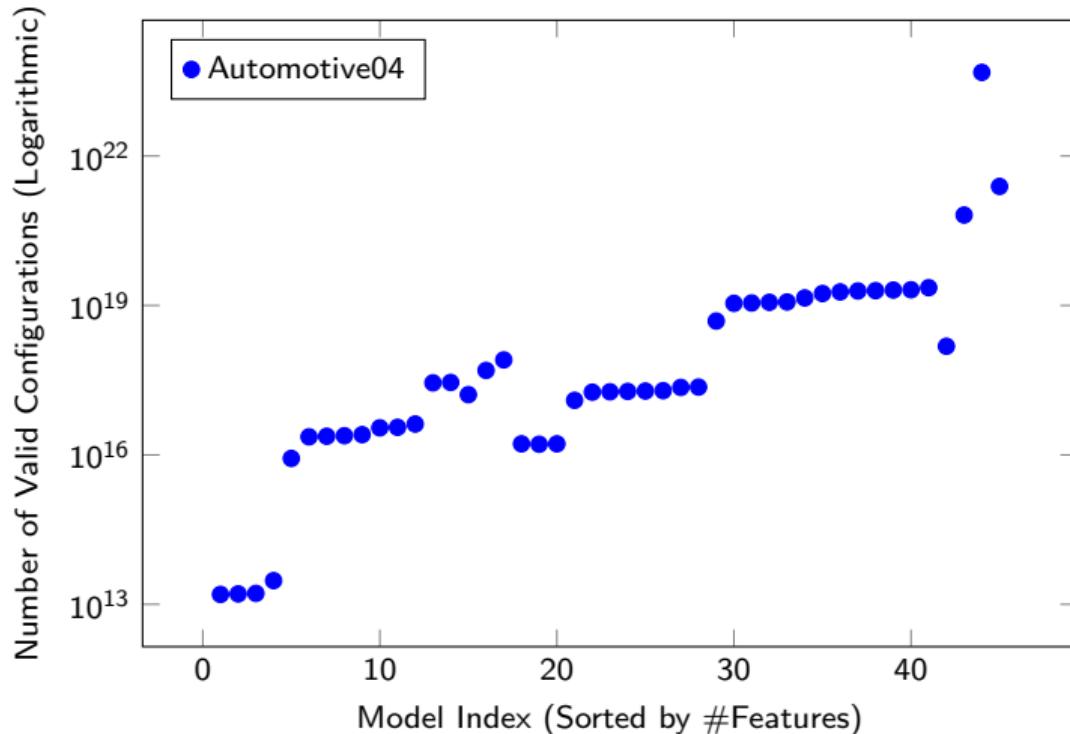
Performance Solvers



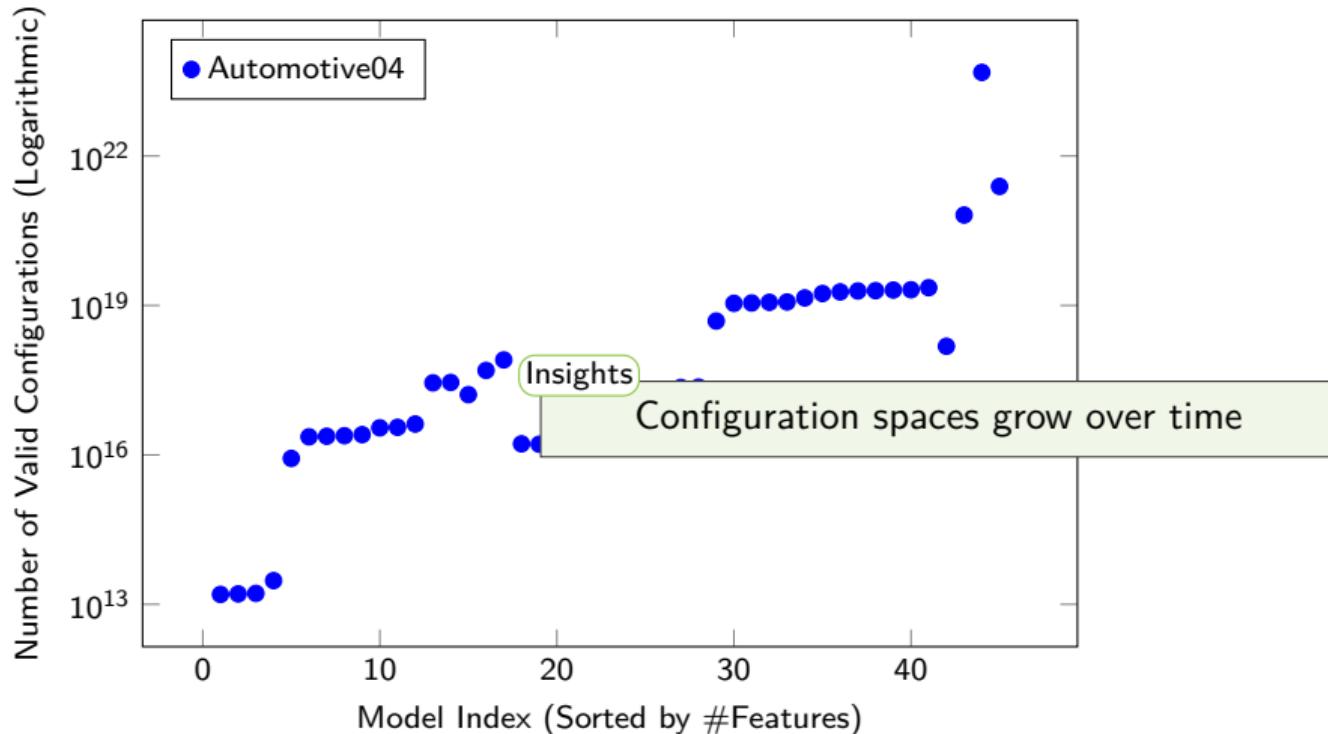
How many configurations do we have in practice?

Subject Systems	Features	Number of Valid Configurations
BerkeleyDB	76	$4.1 \cdot 10^9$
axTLS	96	$8.3 \cdot 10^{11}$
uClibc	313	$1.7 \cdot 10^{40}$
uClinux-base	380	$2.6 \cdot 10^{22}$
Automotive04	531	$2.5 \cdot 10^{21}$
Automotive03	588	$2.5 \cdot 10^{31}$
BusyBox	631	$2.1 \cdot 10^{201}$
FinancialServices	771	$9.7 \cdot 10^{13}$
Embt toolkit	1,179	$5.1 \cdot 10^{96}$
CDL (116 Models)	1,178–1,408	$2.6 \cdot 10^{118} – 3.0 \cdot 10^{136}$
uClinux-distribution	1,580	$4.1 \cdot 10^{409}$
Automotive05	1,663	unknown
Automotive01	2,513	$5.4 \cdot 10^{217}$
Linux	6,467	unknown
Automotive02	18,616	$1.7 \cdot 10^{1534}$

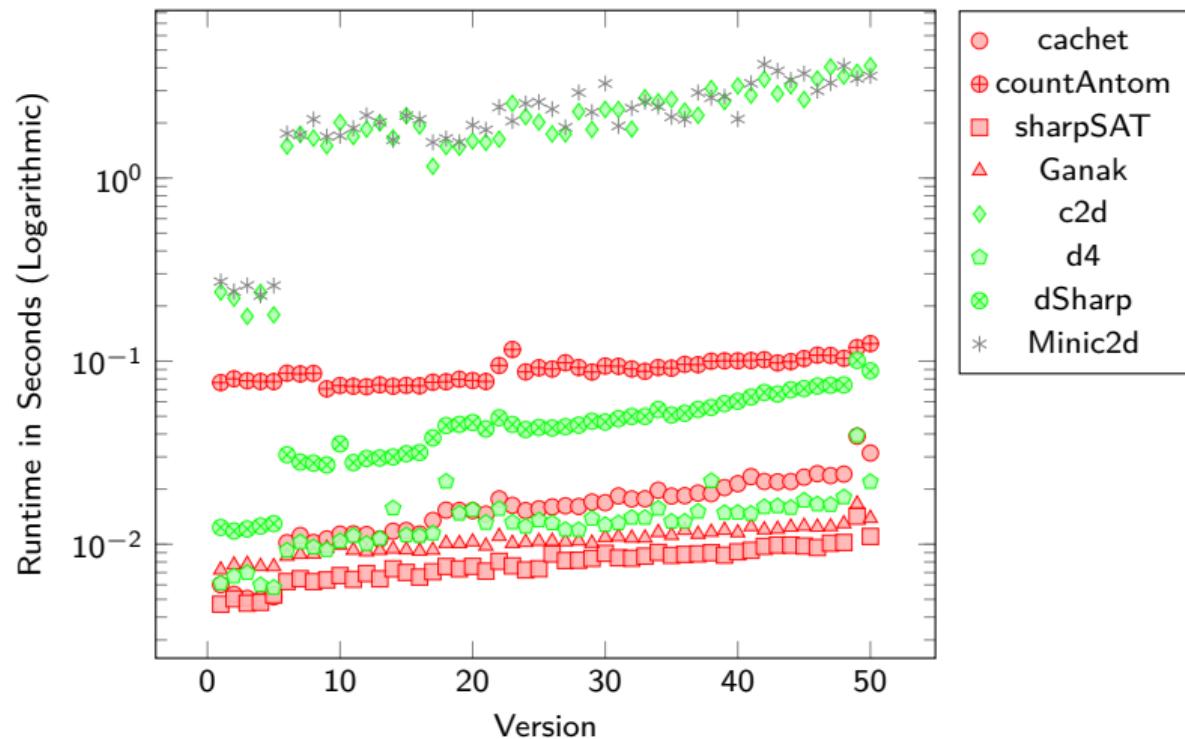
Evolution: Sizes



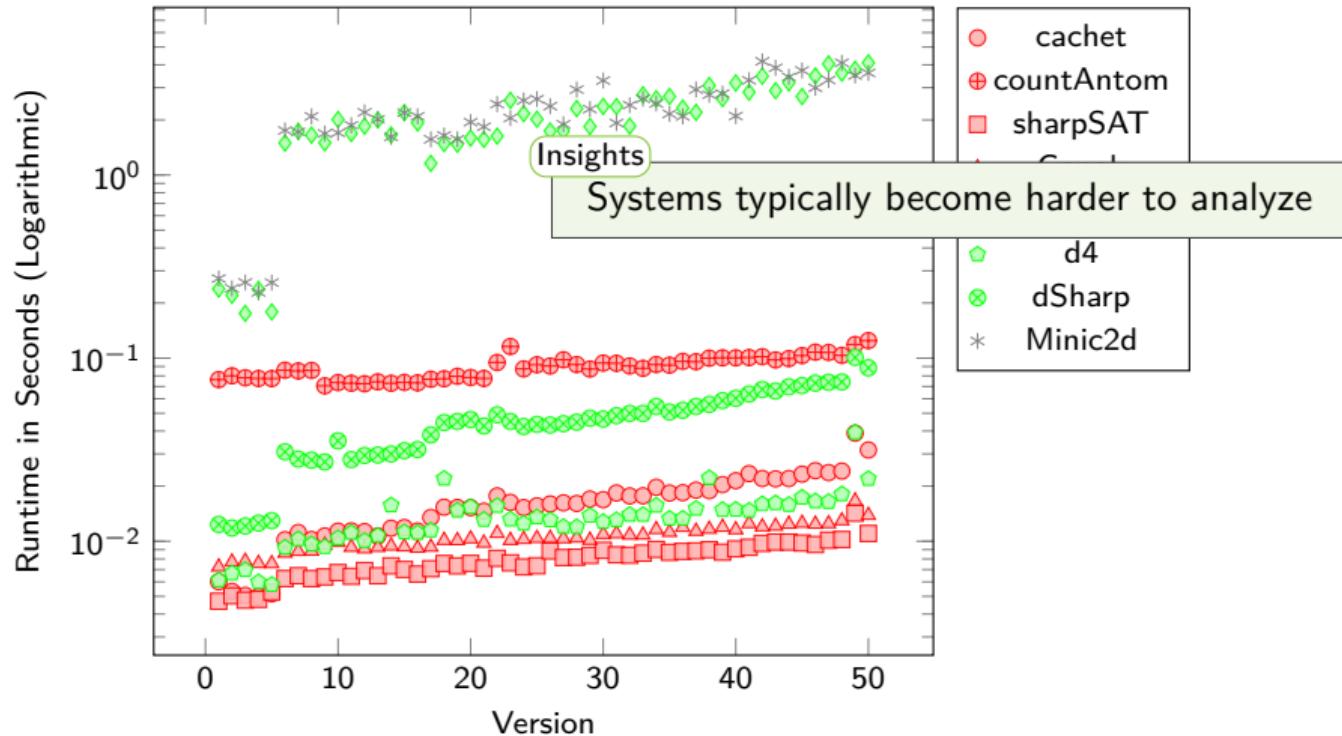
Evolution: Sizes



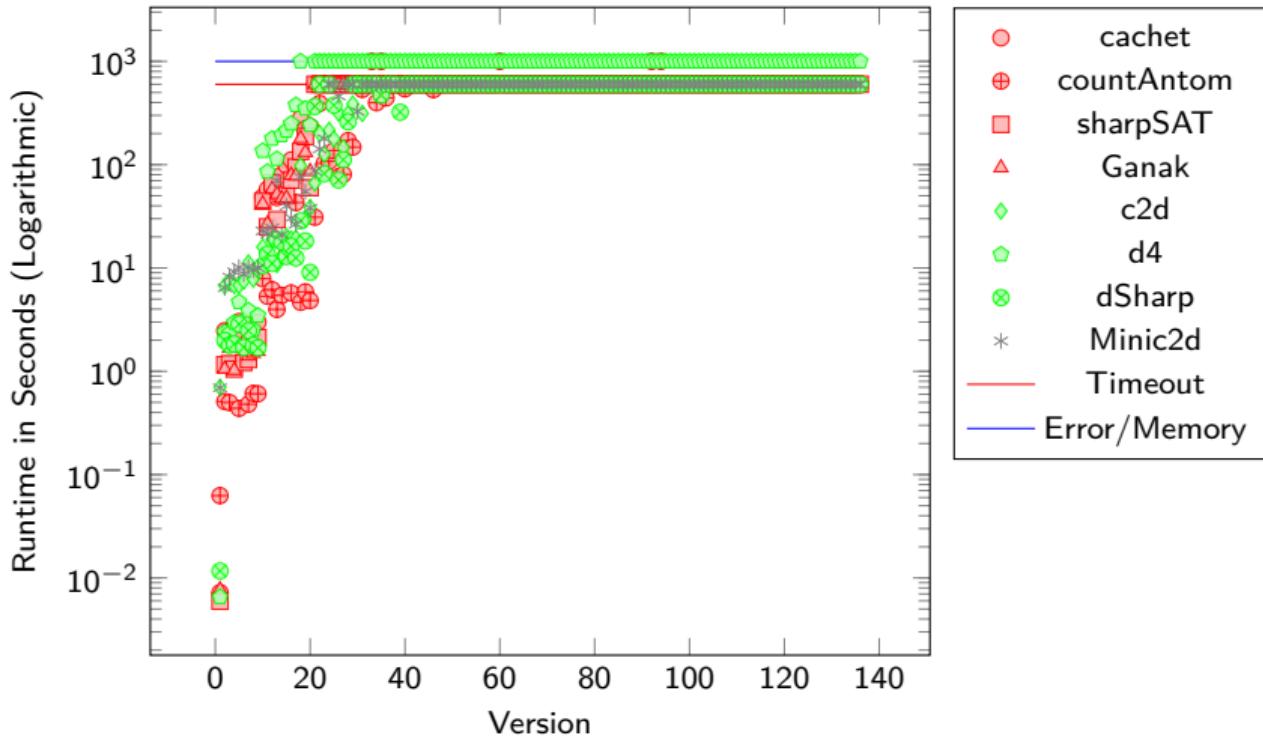
Evolution: Performance



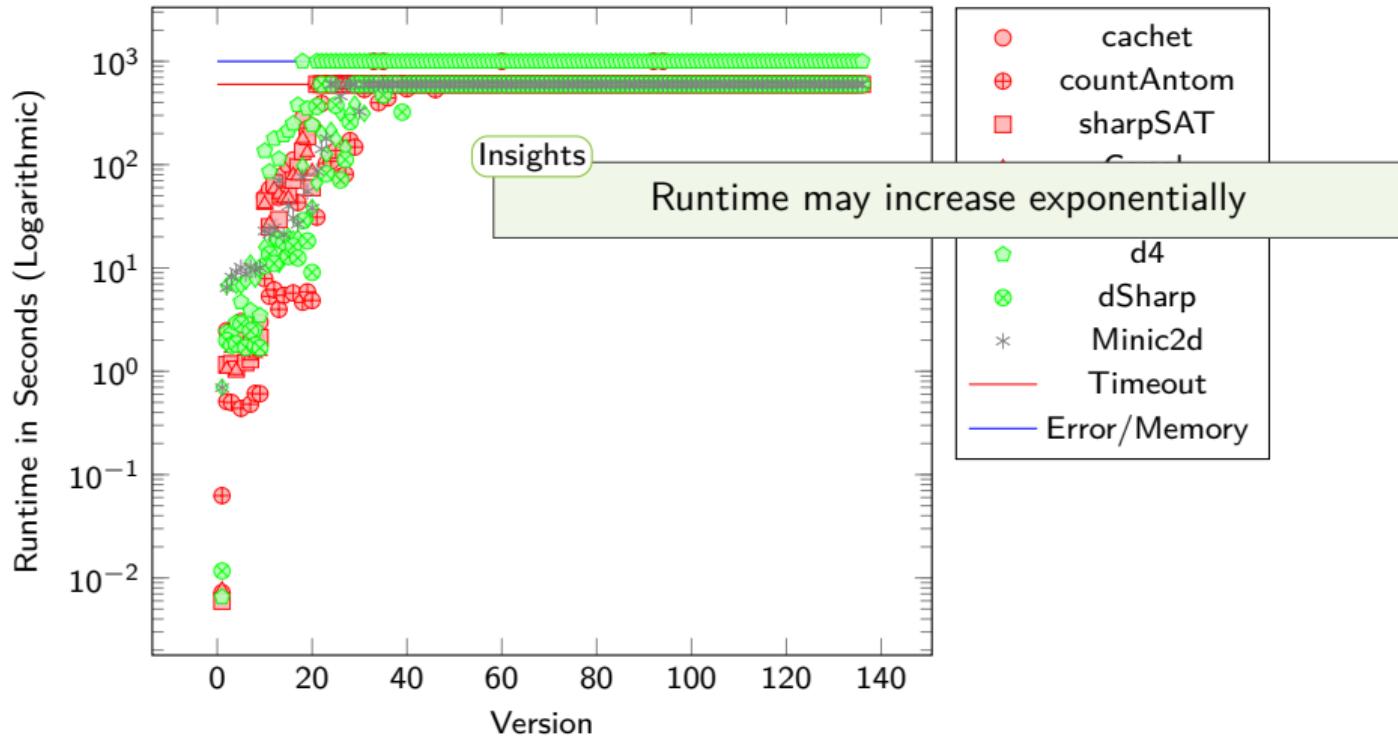
Evolution: Performance



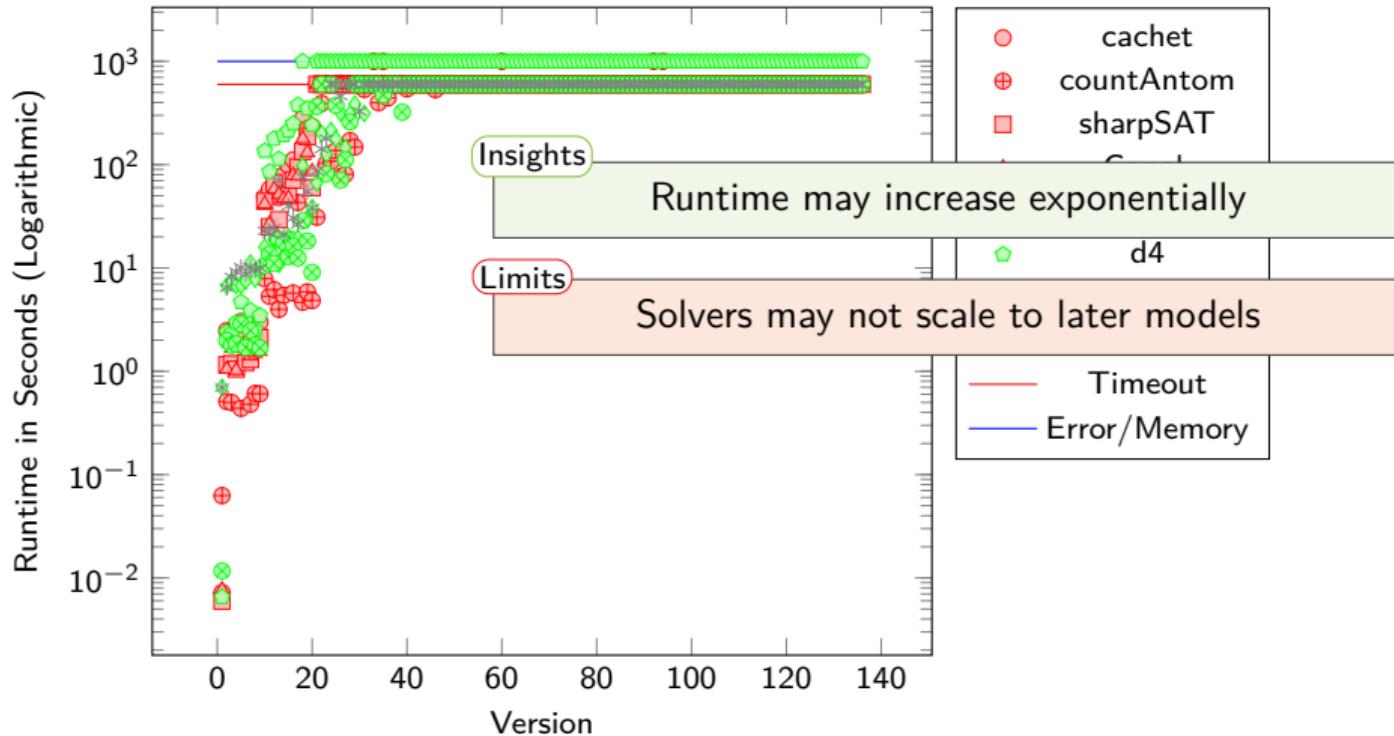
Evolution: Performance



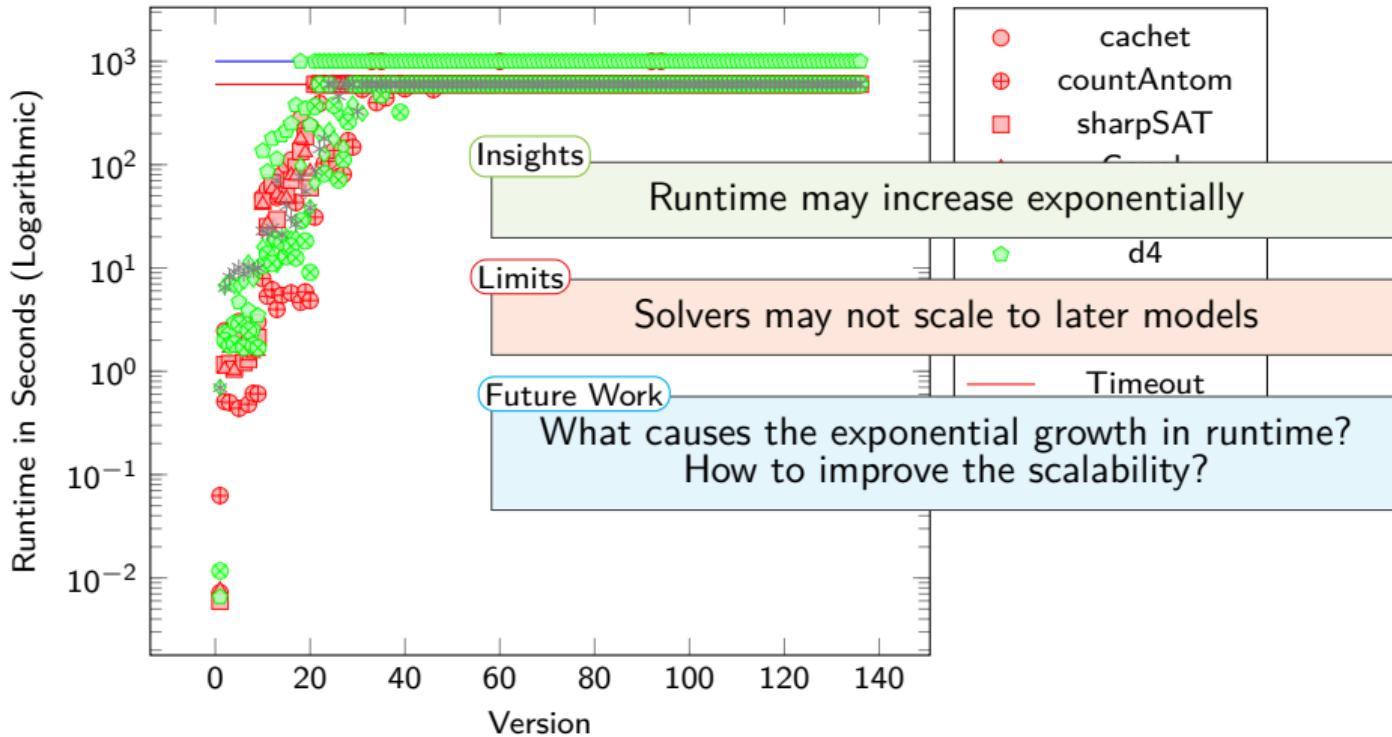
Evolution: Performance



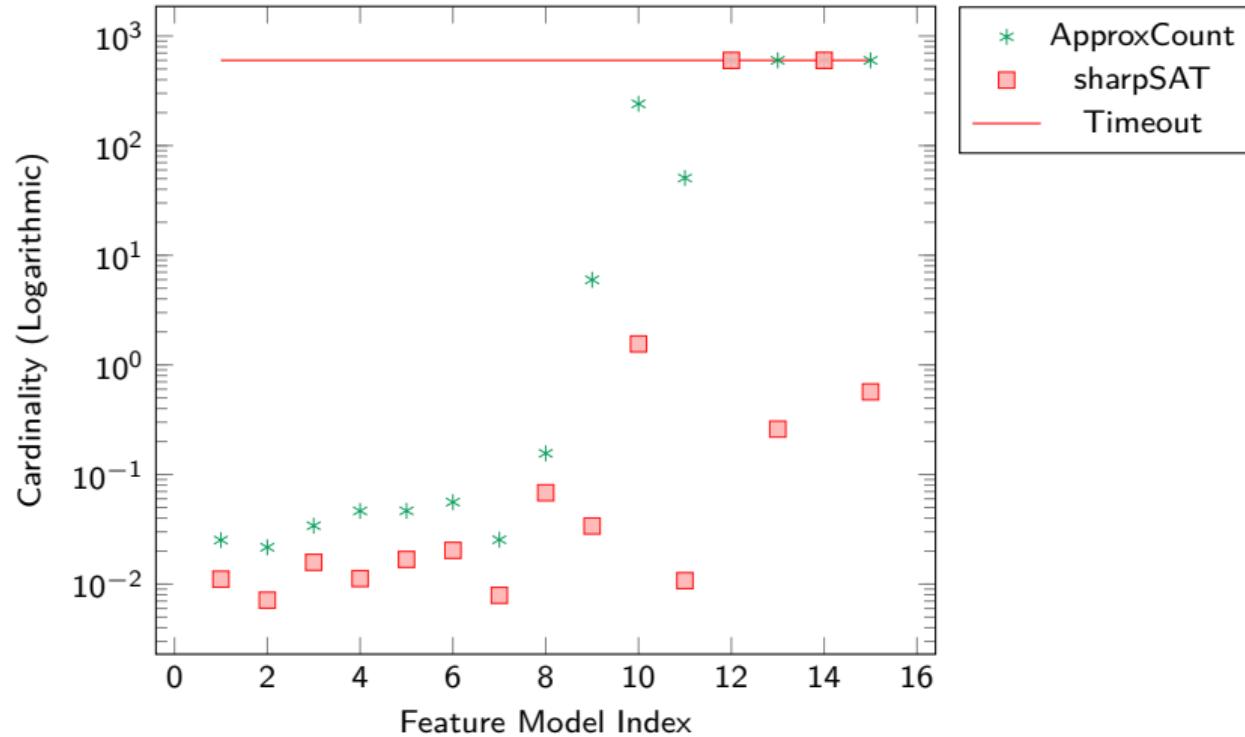
Evolution: Performance



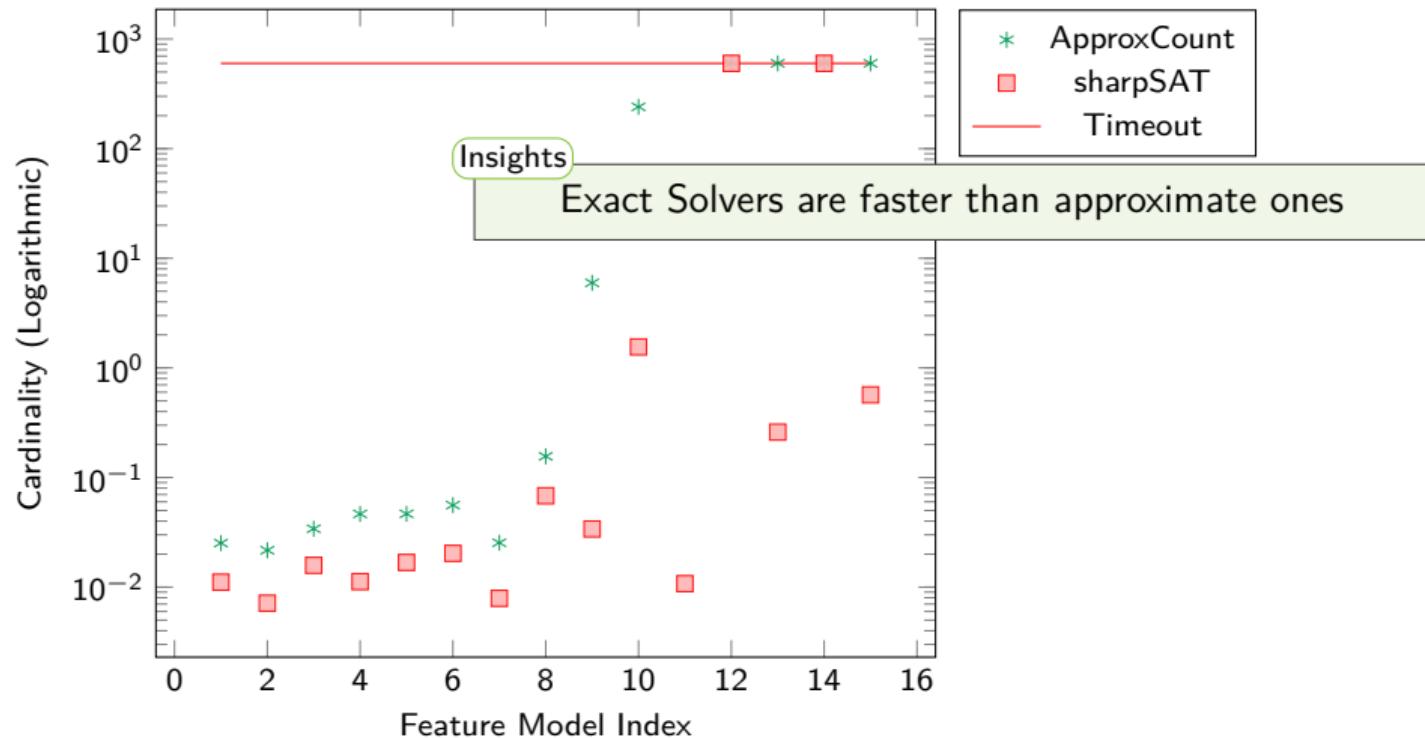
Evolution: Performance



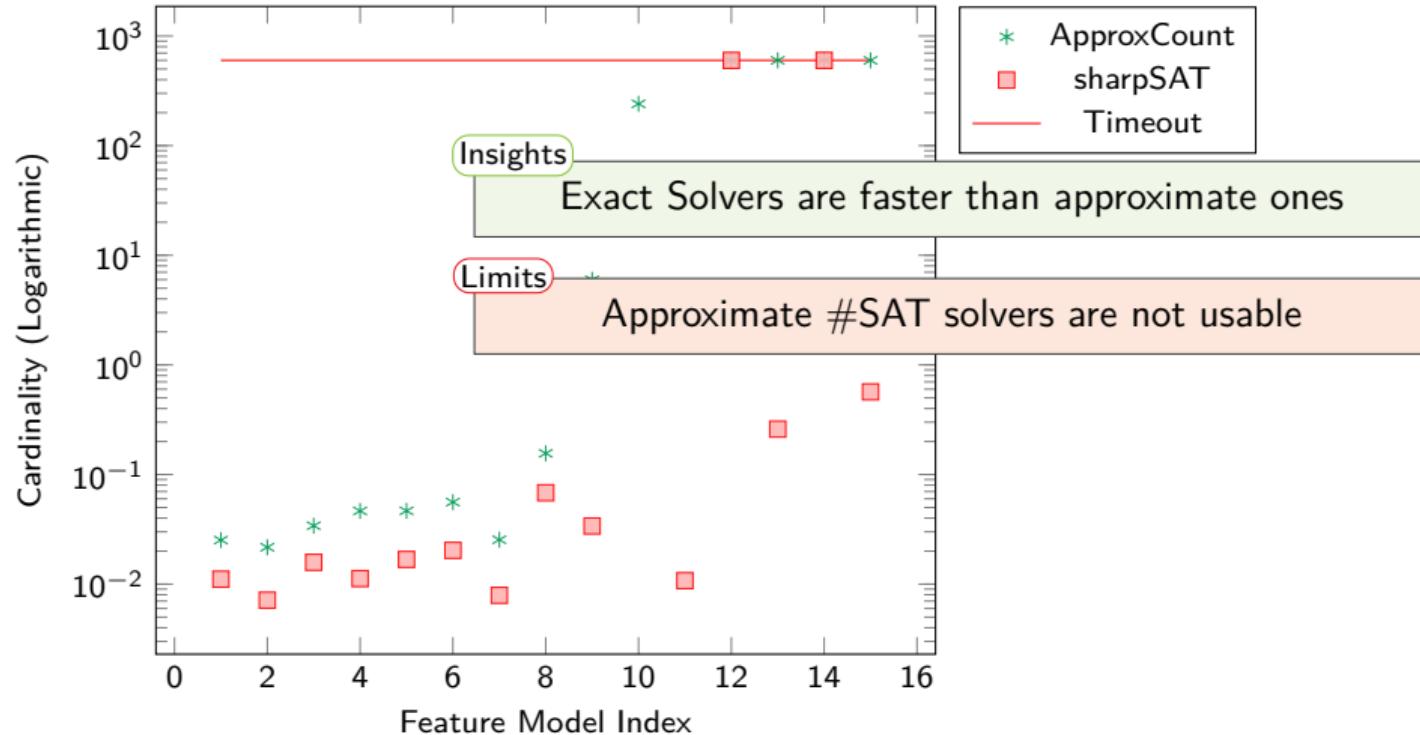
Approximate #SAT Solvers



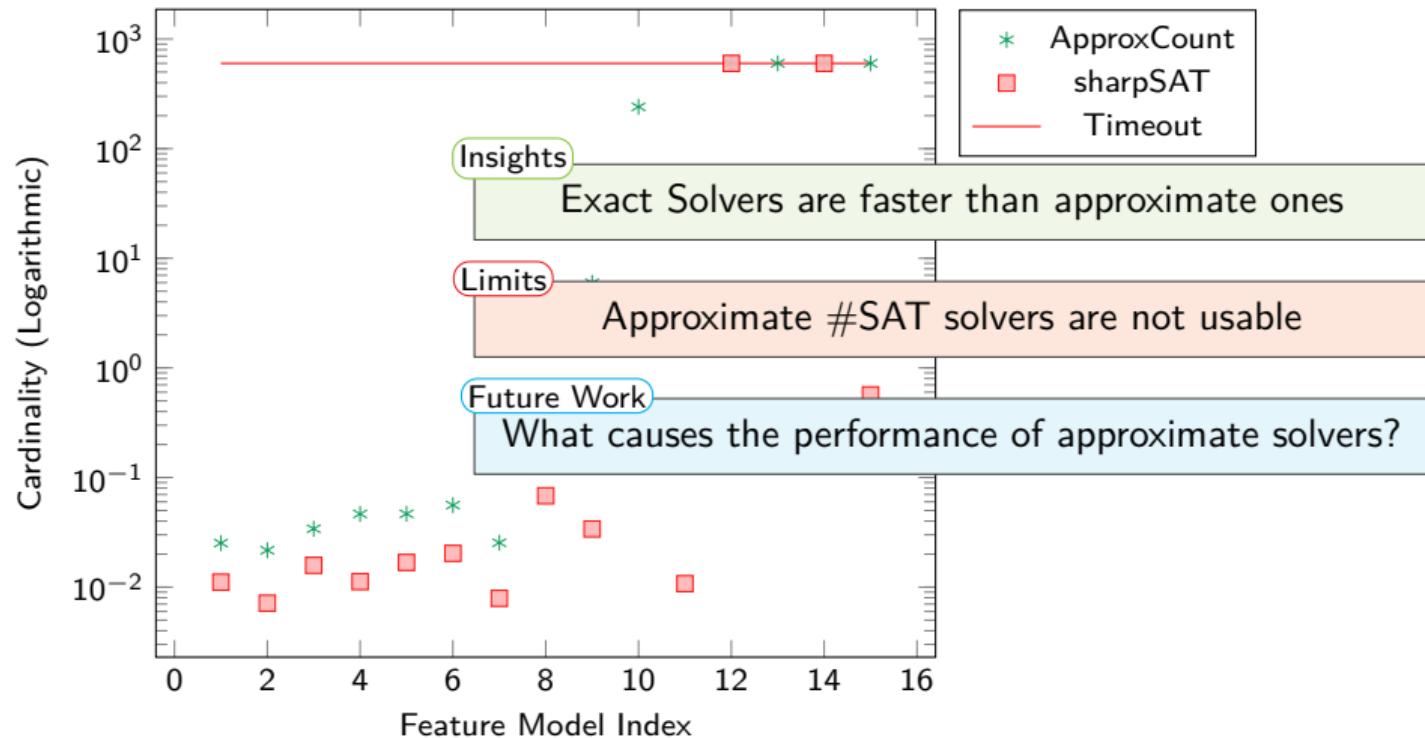
Approximate #SAT Solvers



Approximate #SAT Solvers



Approximate #SAT Solvers



Evaluating State-of-the-Art #SAT Solvers on Industrial Configuration Spaces

Insights

Majority of systems can be analyzed with #SAT solvers

DPLL: ✓ d-DNNF: ✓

Evaluating State-of-the-Art #SAT Solvers on Industrial Configuration Spaces

Insights

Majority of systems can be analyzed with #SAT solvers

DPLL: ✓ d-DNNF: ✓ BDD: ✗

Evaluating State-of-the-Art #SAT Solvers on Industrial Configuration Spaces

Insights

Majority of systems can be analyzed with #SAT solvers

DPLL: ✓ d-DNNF: ✓ BDD: ✗

Evaluating State-of-the-Art #SAT Solvers on Industrial Configuration Spaces

Insights

Majority of systems can be analyzed with #SAT solvers

DPLL: ✓ d-DNNF: ✓ BDD: ✗

Limits

Two systems could not be analyzed

Solvers may not scale to later models in evolution

Evaluating State-of-the-Art #SAT Solvers on Industrial Configuration Spaces

Insights

Majority of systems can be analyzed with #SAT solvers

DPLL: ✓ d-DNNF: ✓ BDD: ✗

Limits

Two systems could not be analyzed

Solvers may not scale to later models in evolution

Future Work

How to scale to hard systems?

What causes exponential growth in runtime during evolution?

Start Backup Slides

Nice, a question that can be somewhat answered with backup :)

Correlation Performances

Tabelle: Spearman Correlation between Structural Metrics and Runtime of #SAT Solvers

Metric	Coefficient Fastest	Coefficient Range
Number of Literals	0.89 (very strong)	0.82 (very strong)–0.89 (very strong)
Number of Clauses	0.87 (very strong)	0.80 (very strong)–0.87 (very strong)
Number of Features	0.85 (very strong)	0.73 (strong) –0.94 (very strong)
Number of Leaf Features	0.82 (very strong)	0.68 (strong) –0.92 (very strong)
Number of Constraints	0.81 (very strong)	0.67 (strong)–0.84 (very strong)
Cyclomatic Complexity	0.77 (strong)	0.64 (strong)–0.79 (strong)
Tree Depth	0.34 (weak)	0.29 (weak)–0.39 (weak)
Connectivity Density	0.20 (weak)	0.11 (very weak)–0.57 (moderate)
Ratio of Variability	0.11 (very weak)	-0.01 (very weak)–0.27 (weak)
Number of Top Features	0.06 (very weak)	-0.01 (very weak)–0.17 (very weak)
Flexibility of Configuration	0.07 (very weak)	-0.01 (very weak)–0.18 (very weak)