

Part I: Ad-Hoc Approaches for Variability

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3. Compile-Time Variability with Clone-and-Own

Part II: Modeling & Implementing Features

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7. Languages for Features
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Recap: Software Product Lines

Features Have Dependencies

Specifying Valid Configurations

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4. Feature Modeling – Handout

Software Product Lines | Elias Kuiter, Thomas Thüm, Timo Kehrer | April 24, 2023

4. Feature Modeling

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Recap: Software Product Lines

[Lecture 1]

Software Product Line

[Northrop et al. 2012, p. 5]

“A **software product line** is

- a set of software-intensive systems
- that share a common, managed set of features
- satisfying the specific needs of a particular market segment or mission
- and that are developed from a common set of core assets in a prescribed way.”

[Software Engineering Institute, Carnegie Mellon University]

Product

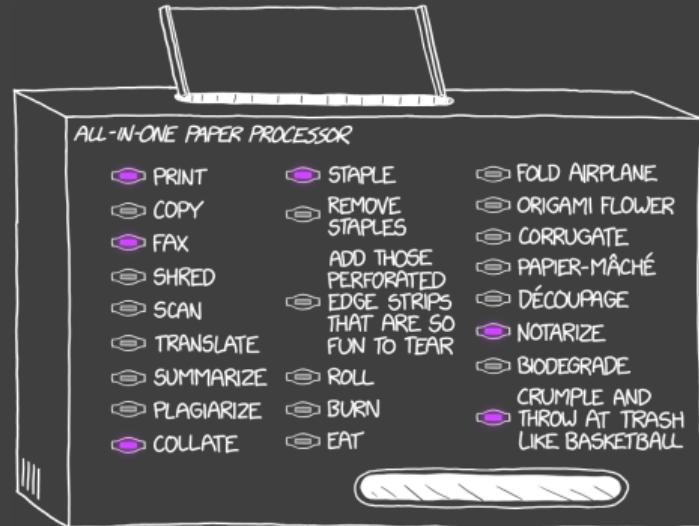
[Apel et al. 2013, p. 19]

“A **product of a product line** is specified by a valid feature selection (a subset of the features of the product line). A feature selection is **valid** if and only if it fulfills all feature dependencies.”

Feature

[Apel et al. 2013, p. 18]

“A **feature** is a characteristic or end-user-visible behavior of a software system.”



Features Have Dependencies

Ordering a Waffle ...



... with Sugar



... with Cherries



This is Nice, But ...

- plate and sugar seem to always be included, a fork is only included for some orders
⇒ limitations seem **arbitrary**
- children get special treatment
⇒ order process is **unfair**
- what exactly am I paying for?
⇒ investments are **unclear**

In This Lecture

1. how to **model and configure** features and their dependencies?
2. how to **store and communicate**?
3. how to **analyze and understand**?

Specifying Valid Configurations

Configuration

- a **configuration** over a set of features F selects and deselects features in F
- formally: a pair (S, D) such that $S, D \subseteq F$ and S, D are disjoint ($S \cap D = \emptyset$)
- is **complete** if all features are covered ($S \cup D = F$) and **partial** otherwise
- a complete configuration is **valid** if it “makes sense” in the domain and **invalid** otherwise
- we often abbreviate complete configurations with $S \equiv (S, F \setminus S)$

Feature set $F = \{\mathbf{ConfigDB}, \mathbf{Get}, \mathbf{Put}, \mathbf{Delete}, \mathbf{Transactions}, \mathbf{Windows}, \mathbf{Linux}\}$

Examples for **complete** configurations:

- **valid** (read-only database on Windows):
 $(\{C, G, W\}, \{P, D, T, L\})$
- **valid** (fully functional database on Linux):
 $(\{C, G, P, D, T, L\}, \{W\})$
- **invalid** (no operating system):
 $(\{C, G\}, \{P, D, T, W, L\})$
- **invalid** (transactions no read-only database):
 $(\{C, G, T, L\}, \{P, D, W\})$

Examples for **partial** configurations:

$(\{C, G\}, \{P, D\}), (\emptyset, \emptyset)$

Specifying Valid Configurations – Natural Language

Valid Configuration

A complete configuration over F is valid if it “makes sense” in the domain. ↵ “makes sense”?

Natural Language

- informal description of relationships between features in F
 - a complete configuration S is **valid** if it conforms to the description
- + succinct
- sometimes ambiguous
- not machine-readable

“A configurable database has an API that allows for at least one of the request types **Get**, **Put**, or **Delete**. Optionally, the database can support **transactions**, provided that the API allows for Put or Delete requests. Also, the database targets a supported operating system, which is either **Windows** or **Linux**.”

Specifying Valid Configurations – Configuration Map

Valid Configuration

A complete configuration over F is valid if it “makes sense” in the domain. ↵ “makes sense”?

Configuration Map

- a **configuration map** over F is a set of complete configurations $M \subseteq \mathcal{P}(F)$
- a complete configuration S is **valid** if it occurs in the configuration map ($S \in M$)
- also known as product map
- + precise
- not human-readable
- redundant, explodes in size ($0 \leq |M| \leq 2^{|F|}$)

Feature set $F = \{\text{ConfigDB}, \text{Get}, \text{Put}, \text{Delete}, \text{Transactions}, \text{Windows}, \text{Linux}\}$

Configuration map:

$\{C, G, W\}$	$\{C, G, L\}$
$\{C, P, W\}$	$\{C, P, L\}$
$\{C, G, P, W\}$	$\{C, G, P, L\}$
$\{C, D, W\}$	$\{C, D, L\}$
$\{C, G, D, W\}$	$\{C, G, D, L\}$
$\{C, P, D, W\}$	$\{C, P, D, L\}$
$\{C, G, P, D, W\}$	$\{C, G, P, D, L\}$
$\{C, P, T, W\}$	$\{C, P, T, L\}$
$\{C, G, P, T, W\}$	$\{C, G, P, T, L\}$
$\{C, D, T, W\}$	$\{C, D, T, L\}$
$\{C, G, D, T, W\}$	$\{C, G, D, T, L\}$
$\{C, P, D, T, W\}$	$\{C, P, D, T, L\}$
$\{C, G, P, D, T, W\}$	$\{C, G, P, D, T, L\}$

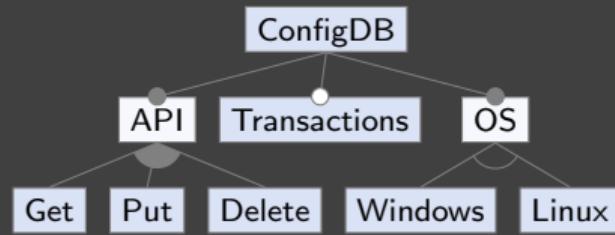
Specifying Valid Configurations – Configuration Map in Excel

	A	B	C	D	E	F	G
1	ConfigDB	Get	Put	Delete	Transactions	Windows	Linux
2	X	X				X	
3	X		X			X	
4	X	X	X			X	
5	X			X		X	
6	X	X		X		X	
7	X		X	X		X	
8	X	X	X	X		X	
9	X		X		X	X	
10	X	X	X		X	X	
11	X			X	X	X	
12	X	X		X	X	X	
13	X		X	X	X	X	
14	X	X	X	X	X	X	
15	X	X					X
16	X		X				X
17	X	X	X				X
18	X			X			X
19	X	X		X			X
20	X		X	X			X
21	X	X	X	X			X
22	X		X		X		X
23	X	X	X		X		X
24	X			X	X		X
25	X	X		X	X		X
26	X		X	X	X		X
27	X	X	X	X	X		X

Can we do better?

Feature Models – Syntax

[Apel et al. 2013; Kang et al. 1990, pp. 63–72; Batory 2005]



Transactions → *Put* ∨ *Delete*

Legend:

- Abstract Feature
- Concrete Feature
- Mandatory
- Optional
- ▲ Or Group
- △ Alternative Group

Feature Model

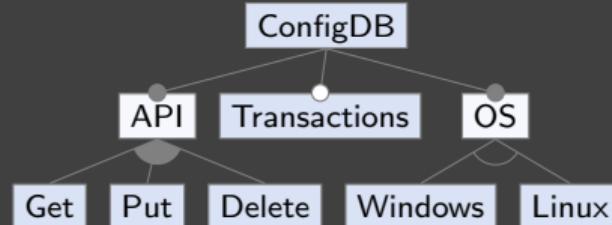
- hierarchy of features
- dependencies between features modeled by tree and cross-tree constraints
- **tree constraints**: defined by the hierarchy
- **cross-tree constraints**: propositional formulas over features
- **abstract features** are used to group other features
- **concrete features** have an implementation
- also known as feature diagram or feature tree
- notation for **optional/mandatory features** and **or/alternative groups**

Feature Models – Semantics

[Apel et al. 2013; Batory 2005]

Tree Constraints

- the **root feature** is always required
- each feature requires its parent
(aka. **parent-child-relationship**)
- an **optional feature** can be (de-)selected freely when its parent is selected
- a **mandatory feature** is required by its parent
- **or group**: at least one child feature must be selected when the parent is selected
- **alternative group**: exactly one child feature must be selected when the parent is selected

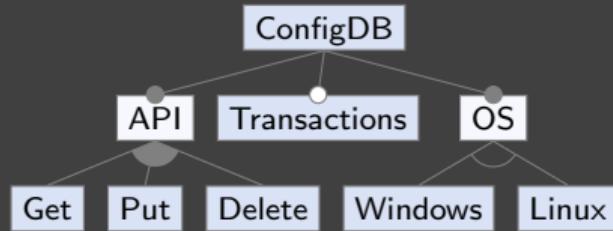


Transactions → *Put* ∨ *Delete*

Cross-Tree Constraints

- a list of **propositional formulas** expressing further dependencies between features
- each cross-tree constraint must be satisfied

Feature Models – Examples

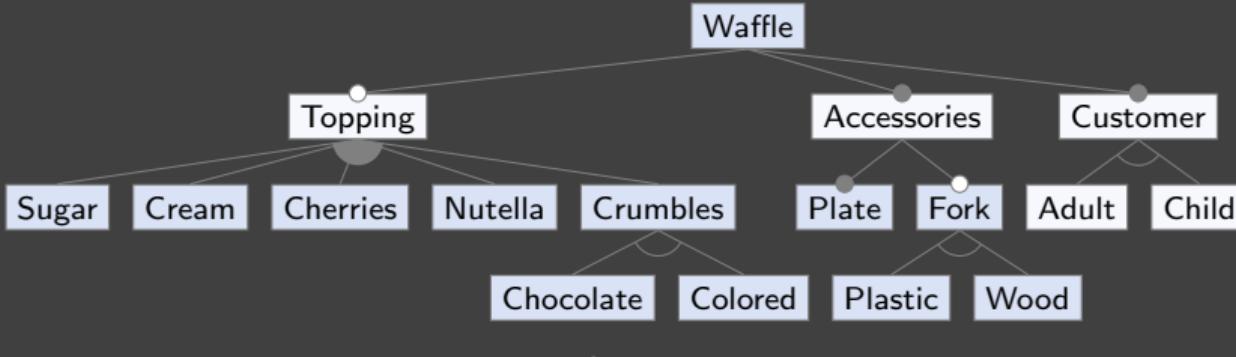


Transactions → *Put* ∨ *Delete*

Is This a Valid Configuration?

- **valid** (read-only database on Windows):
 $(\{C, A, G, O, W\}, \{P, D, T, L\})$
- **valid** (fully functional database on Linux):
 $(\{C, A, G, P, D, T, O, L\}, \{W\})$
- **invalid** (no operating system):
 $(\{C, A, G\}, \{P, D, T, O, W, L\})$
- **invalid** (transactions no read-only database):
 $(\{C, A, G, T, O, L\}, \{P, D, W\})$

Feature Models – Examples



- abstract and concrete features can be assigned arbitrarily
- groups can be used anywhere
- directly below groups, no optional or mandatory markers are allowed

Pros and Cons

Pro: Making Tacit Knowledge Explicit

"I think the best [about feature modeling] is you can see relationships, to actually know what configurations are allowed and what are not allowed. That was also not so easy to express in the past [...] This is from the developer's point of view. But it's also [...] important, because before we noticed that the same functionality was implemented twice within the same project, basically they haven't realized that. They implemented the same features." – Interview with Practitioners [Berger et al. 2014]

Pro: Tool Support



, Gears, pure::variants, ...

Con: Challenges

- **domain scoping:** which features?
- **feature interactions:** which dependencies?
- requires infrastructure, consulting, and training



Feature Models and Configurations – Summary

Lessons Learned

- features, dependencies between features, and configurations
- feature models: abstract and concrete features, tree and cross-tree constraints
- tree constraints: optional, mandatory, or group, alternative group

Further Reading

- Apel et al. 2013, Section 2.3, pp. 26–39
— introduction to feature modeling
- Thorsten Berger et al. (2013): A Survey of Variability Modeling in Industrial Practice
- Damir Nešić et al. (2019): Principles of Feature Modeling

Practice

1. sketch a feature model with features A, B, C, D, E, F that has exactly those 5 valid configurations (pen and paper preferred):
 $\{A, B\}$ $\{A, C, E\}$ $\{A, C, E, F\}$
 $\{A, B, D\}$ $\{A, C, F\}$
2. discuss in groups whether your feature models are syntactically correct and specify exactly the above configurations

4. Feature Modeling

4a. Feature Models and Configurations

4b. Transforming Feature Models

Representations and Transformations

UVL, the Universal Variability Language

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Representations and Transformations

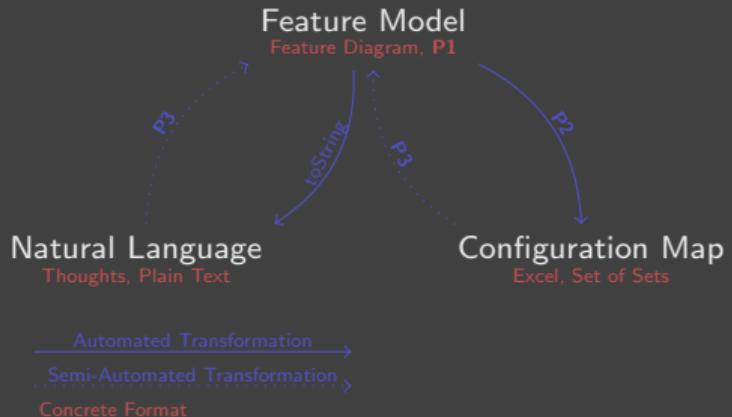
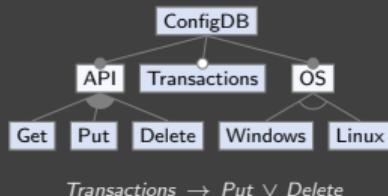
Natural Language

"A configurable database has an API that allows for at least one of the request types Get, Put, or Delete. Optionally, the database can support transactions, provided that the API allows for Put or Delete requests. Also, the database targets a supported operating system, which is either Windows or Linux."

Configuration Map

$\{C, G, W\}$	$\{C, G, L\}$
\vdots	\vdots
$\{C, G, P, D, T, W\}$	$\{C, G, P, D, T, L\}$

Feature Diagram (Graphical Feature Model)



Problems

- P1 How to express feature models **textually**?
- P2 How to (a) validate configurations and (b) get all valid configurations **automatically**?
- P3 (How to reverse engineer feature models?)

UVL, the Universal Variability Language [UVL]

features

ConfigDB

mandatory

API {abstract}

or

Get

Put

Delete

optional

Transactions

mandatory

OS {abstract}

alternative

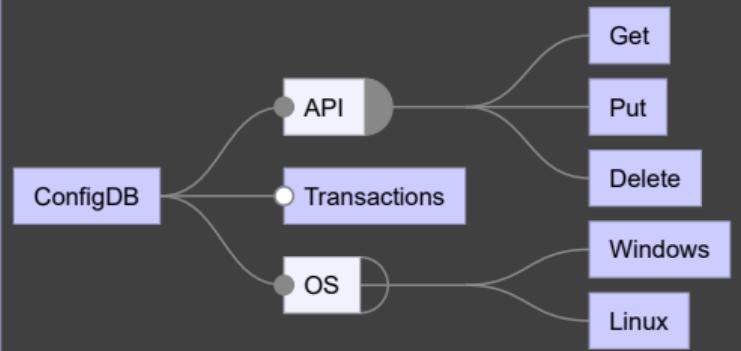
Windows

Linux

constraints

Transactions => Put | Delete

A Feature Model “Sideways”

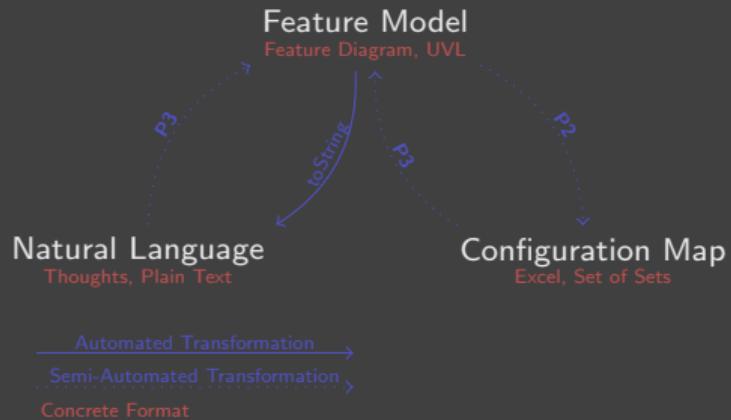


Transactions → Put ∨ Delete

Universal Variability Language (UVL)

- textual language for feature modeling
- adds advanced modeling constructs
(e.g., attributes, cardinalities, submodels, ...)

Representations and Transformations



Problems

- P1 How to express feature models **textually**?
- P2 How to (a) validate configurations and (b) get all valid configurations **automatically**?
- P3 (How to reverse engineer feature models?)

Solutions

- P1 Universal Variability Language \Rightarrow **Syntax**
- P2 **Semantics?**
- P3 –

Propositional Formulas – Recap

Syntax of Propositional Formulas

Inductive definition of **propositional formulas**:

- the **Boolean truth values** \top, \perp
- any **Boolean variable** X
- any **negation** $\neg\phi$ of a formula ϕ
- any **conjunction** ($\phi \wedge \psi$) of formulas ϕ and ψ
- any **disjunction** ($\phi \vee \psi$), **implication** ($\phi \rightarrow \psi$), or **biimplication** ($\phi \leftrightarrow \psi$)

Informal Semantics of Propositional Formulas

\top	“true” (or tautology)
\perp	“false” (or contradiction)
$\neg\phi$	“not ϕ ”
$\phi \wedge \psi$	“ ϕ and ψ ”
$\phi \vee \psi$	“ ϕ or ψ ” (inclusive or!)
$\phi \rightarrow \psi$	“if ϕ , then ψ ” (and else?)
$\phi \leftrightarrow \psi$	“ ϕ if and only if ψ ”

Operator Precedence: $\neg, \wedge, \vee, \rightarrow, \leftrightarrow$

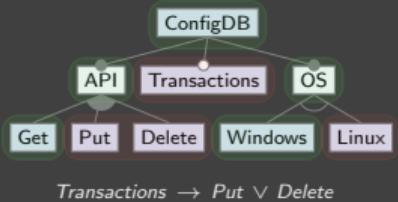
$$\text{Transactions} \rightarrow (\text{Put} \vee \text{Delete})$$

$$\equiv \text{Transactions} \rightarrow \text{Put} \vee \text{Delete}$$

$$\not\equiv (\text{Transactions} \rightarrow \text{Put}) \vee \text{Delete}$$

Propositional Formulas – Example

A Feature Model $FM \dots$



\dots as a Propositional Formula $\Phi(FM)$

$$\begin{aligned}\Phi(FM) = & \text{ConfigDB} \\ \wedge & (\text{API} \leftrightarrow \text{ConfigDB}) \\ \wedge & (\text{Transactions} \rightarrow \text{ConfigDB}) \\ \wedge & (\text{OS} \leftrightarrow \text{ConfigDB}) \\ \wedge & (\text{Get} \vee \text{Put} \vee \text{Delete} \leftrightarrow \text{API}) \\ \wedge & (\text{Windows} \vee \text{Linux} \leftrightarrow \text{OS}) \\ \wedge & \neg(\text{Windows} \wedge \text{Linux}) \\ \wedge & (\text{Transactions} \rightarrow \text{Put} \vee \text{Delete})\end{aligned}$$

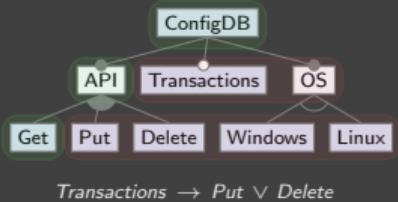
Is This a Valid Configuration?

$$\begin{aligned}\Phi(FM)(\{C, A, G, O, W\}) \\ \equiv \Phi(FM)((\{C, A, G, O, W\}, \{P, D, T, L\})) \\ \equiv & C \wedge (A \leftrightarrow C) \wedge (T \rightarrow C) \wedge (O \leftrightarrow C) \\ & \wedge (G \vee P \vee D \leftrightarrow A) \wedge (W \vee L \leftrightarrow O) \\ & \wedge \neg(W \wedge L) \wedge (T \rightarrow P \vee D) \\ \equiv & \top \wedge (\top \leftrightarrow \top) \wedge (\perp \rightarrow \top) \wedge (\top \leftrightarrow \top) \\ & \wedge (\top \vee \perp \vee \perp \leftrightarrow \top) \wedge (\top \vee \perp \leftrightarrow \top) \\ & \wedge \neg(\top \wedge \perp) \wedge (\perp \rightarrow \perp \vee \perp) \\ \equiv & \top \wedge \top \\ \equiv & \top\end{aligned}$$

⇒ **configuration is valid**
(read-only database on Windows)

Propositional Formulas – Example

A Feature Model $FM \dots$



\dots as a Propositional Formula $\Phi(FM)$

$$\begin{aligned}\Phi(FM) = & \text{ConfigDB} \\ \wedge & (\text{API} \leftrightarrow \text{ConfigDB}) \\ \wedge & (\text{Transactions} \rightarrow \text{ConfigDB}) \\ \wedge & (\text{OS} \leftrightarrow \text{ConfigDB}) \\ \wedge & (\text{Get} \vee \text{Put} \vee \text{Delete} \leftrightarrow \text{API}) \\ \wedge & (\text{Windows} \vee \text{Linux} \leftrightarrow \text{OS}) \\ \wedge & \neg(\text{Windows} \wedge \text{Linux}) \\ \wedge & (\text{Transactions} \rightarrow \text{Put} \vee \text{Delete})\end{aligned}$$

Is This a Valid Configuration?

$$\begin{aligned}\Phi(FM)(\{C, A, G\}) \\ \equiv \Phi(FM)((\{C, A, G\}, \{P, D, T, O, W, L\})) \\ \equiv & C \wedge (A \leftrightarrow C) \wedge (T \rightarrow C) \wedge (O \leftrightarrow C) \\ & \wedge (G \vee P \vee D \leftrightarrow A) \wedge (W \vee L \leftrightarrow O) \\ & \wedge \neg(W \wedge L) \wedge (T \rightarrow P \vee D) \\ \equiv & T \wedge (T \leftrightarrow T) \wedge (\perp \rightarrow T) \wedge (\perp \leftrightarrow T) \\ & \wedge (T \vee \perp \vee \perp \leftrightarrow T) \wedge (\perp \vee \perp \leftrightarrow \perp) \\ & \wedge \neg(\perp \wedge \perp) \wedge (\perp \rightarrow \perp \vee \perp) \\ \equiv & T \wedge T \wedge T \wedge \perp \wedge T \wedge T \wedge T \wedge T \\ \equiv & \perp\end{aligned}$$

⇒ configuration is invalid
(\nexists no operating system)

Propositional Formulas – Algorithm

Algorithm: Translate FM Into $\Phi(FM)$

1. translate each tree constraint
 - **Root feature:** R is always required
 - **Optional feature:** C requires P
 - **Mandatory feature:** Optional + P requires C
 - **Or group:** Optional + P requires at least one C_i
 - **Alternative group:** Optional + P requires exactly one C_i
2. conjoin translated tree constraints
$$\Phi(TC) \leftarrow \bigwedge_{tc \in TC} \Phi(tc)$$
3. conjoin **cross-tree constraints**
$$\Phi(CTC) \leftarrow \bigwedge_{ctc \in CTC} ctc$$
4. $\Phi(FM) \leftarrow \Phi(TC) \wedge \Phi(CTC)$

$$\begin{aligned}\Phi(\text{Root}) &= Root \\ \Phi\left(\begin{array}{c} P \\ \bullet \\ C \end{array}\right) &= C \rightarrow P \\ \Phi\left(\begin{array}{c} P \\ \bullet \\ C \end{array}\right) &= C \leftrightarrow P \\ \Phi\left(\begin{array}{c} P \\ \diagdown \quad \diagup \\ C_1 \quad \dots \quad C_n \end{array}\right) &= \bigvee_{1 \leq i \leq n} C_i \leftrightarrow P \\ \Phi\left(\begin{array}{c} P \\ \diagdown \quad \diagup \\ G_1 \quad \dots \quad C_n \end{array}\right) &= \bigvee_{1 \leq i \leq n} C_i \leftrightarrow P \\ &\wedge \bigwedge_{1 \leq i < j \leq n} \neg(C_i \wedge C_j)\end{aligned}$$

CNF as a Universal Formula Language

Recap: Conjunctive Normal Form

- a **literal** L is a variable X or its negation $\neg X$
- a **clause** C is a disjunction of literals $\bigvee_j L_j$
- a **conjunctive normal form (CNF)** is a conjunction of clauses $\bigwedge_i C_i = \bigwedge_i \bigvee_j L_j$
- intuitively: a set of “rules” to be satisfied
- any formula ϕ can be transformed into a CNF ϕ' that is logically equivalent ($\phi \Leftrightarrow \phi'$)

Recap: Laws of Propositional Logic

- implication: $\phi \rightarrow \psi \Leftrightarrow \neg\phi \vee \psi$
- biimplication: $\phi \leftrightarrow \psi \Leftrightarrow (\neg\phi \vee \psi) \wedge (\neg\psi \vee \phi)$
- De Morgan's laws: $\neg(\phi \wedge \psi) \Leftrightarrow \neg\phi \vee \neg\psi$
- distributivity: $(\phi \wedge \psi) \vee \chi \Leftrightarrow (\phi \vee \chi) \wedge (\psi \vee \chi)$

Transforming Part of $\Phi(FM)$ into $CNF(\Phi(FM))$

C	C
$\wedge (T \rightarrow C)$	$\wedge (\neg T \vee C)$
$\wedge (O \leftrightarrow C)$	$\wedge (\neg O \vee C) \wedge (\neg C \vee O)$
$\wedge (W \vee L \leftrightarrow O)$	$\wedge (\neg(W \vee L) \vee O)$
$\wedge \neg(W \wedge L)$	$\wedge (\neg O \vee W \vee L)$
	$\wedge \neg(W \wedge L)$

C	C
$\wedge (\neg T \vee C)$	$\wedge (\neg T \vee C)$
$\wedge (\neg O \vee C) \wedge (\neg C \vee O)$	$\wedge (\neg O \vee C) \wedge (\neg C \vee O)$
$\wedge ((\neg W \wedge \neg L) \vee O)$	$\wedge (\neg W \vee O) \wedge (\neg L \vee O)$
$\wedge (\neg O \vee W \vee L)$	$\wedge (\neg O \vee W \vee L)$
$\wedge (\neg W \vee \neg L)$	$\wedge (\neg W \vee \neg L)$

CNF as a Universal Formula Language – DIMACS

```
C  
   $\wedge (\neg T \vee C)$   
   $\wedge (\neg O \vee C) \wedge (\neg C \vee O)$   
   $\wedge (\neg W \vee O) \wedge (\neg L \vee O)$   
   $\wedge (\neg O \vee W \vee L)$   
   $\wedge (\neg W \vee \neg L)$ 
```

```
c 1 C  
c 2 T  
c 3 O  
c 4 W  
c 5 L  
p cnf 5 6  
1 0  
-2 1 0  
-3 1 0 -1 3 0  
-4 3 0 -5 3 0  
-3 4 5 0  
-4 5 0
```

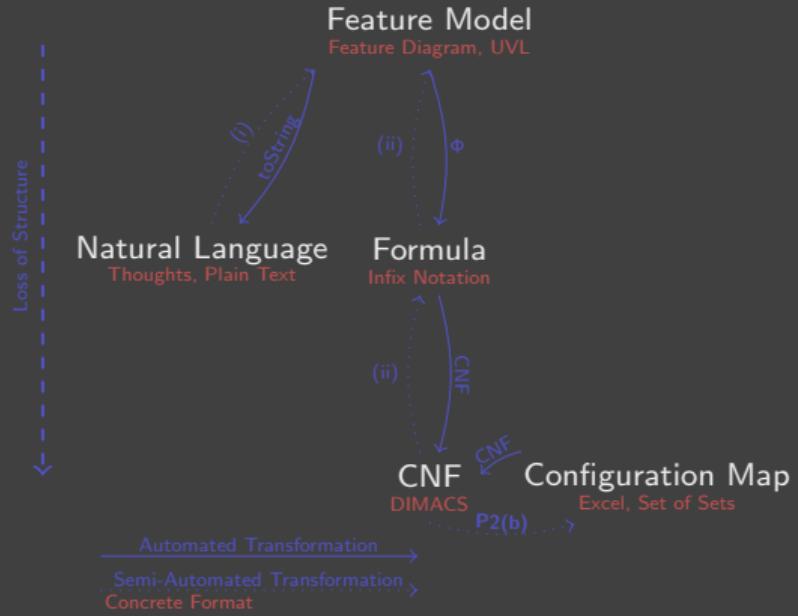
DIMACS Format

[DIMACS 1993]

- de facto industry standard for storing CNF
- machine-readable, automated analyses, ...
- comments start with c ...
- problem line:
`p cnf #variables #clauses`
- clause $\bigvee_i L_i$ translates to $L_1 \dots L_n 0$
- intuitively:

$0 \}$ means $\left\{ \begin{array}{l} \wedge \\ \vee \\ \neg \end{array} \right\}$

Representations and Transformations



Problems

- P1 How to express feature models **textually**?
- P2 How to
 - (a) validate configurations and
 - (b) get all valid configurations**automatically**?
- P3 (How to reverse engineer feature models?)

Solutions

- P1 Universal Variability Language \Rightarrow **Syntax**
- P2 Propositional Formulas \Rightarrow **Semantics**
 - (a) evaluate feature-model formula
 - (b) Lecture 4c
- P3 (i) e.g., Bakar et al. 2015
(ii) e.g., Czarnecki and Wasowski 2007

Transforming Feature Models – Summary

Lessons Learned

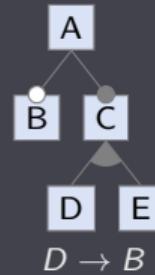
- to understand large configuration spaces, we need formal semantics and machine-readable representations
- propositional formulas satisfy many (though not all) needs for such a representation

Further Reading

- Don Batory (2005): Feature Models, Grammars, and Propositional Formulas
- UVL — official website for the Universal Variability Language with examples, grammar, literature pointers
- Alexander Knüppel et al. (2017): Is There a Mismatch Between Real-World Feature Models and Product-Line Research?

Practice

1. translate the following feature diagram into a propositional formula:



2. check formulas of your colleagues

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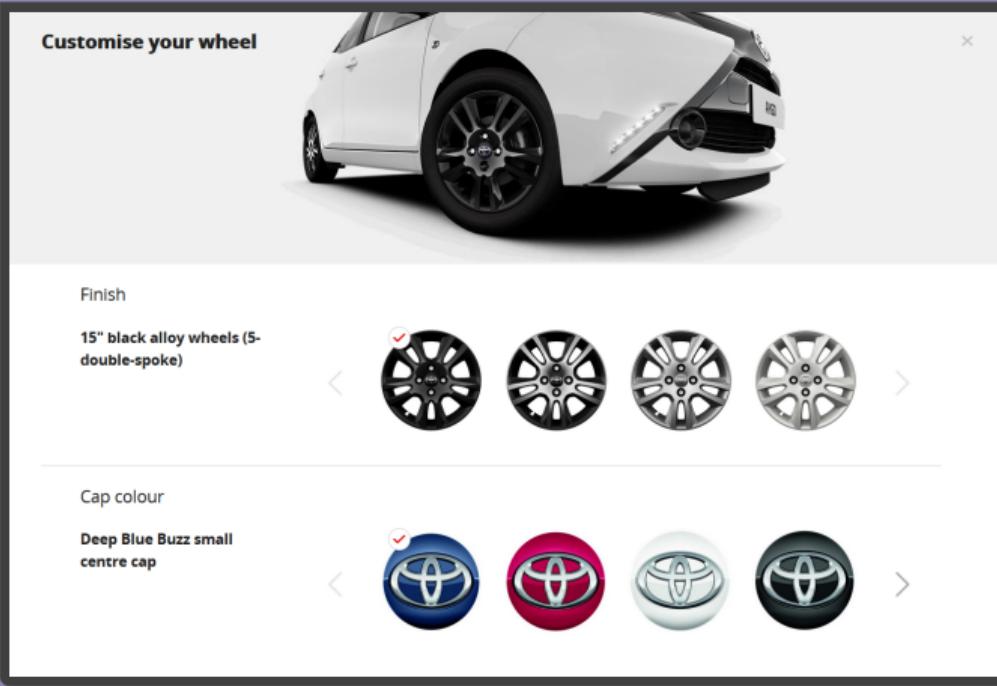
Automated Analyses in FeatureIDE

Summary

FAQ

Configurators in the Wild – Cars

Configuring a car ...



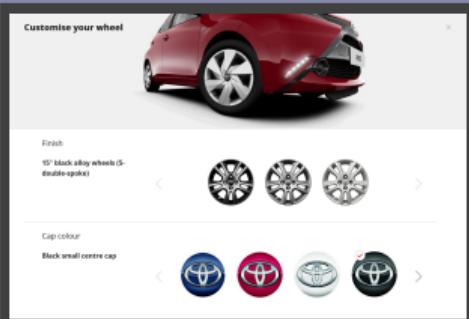
... is complicated!

1. the default configuration
2. we want **black cap**
3. we want **white wheels**
4. black cap unavailable, red selected automatically (not blue!)
5. fine, back to **black wheels**
6. and, back to **black cap**
7. **confirm selection** to continue with selection of the car color
8. we want a **red car**
9. popup dialog: black wheels unavailable (no automatic selection! preview of unavailable wheels!)

what now? back to Step 3?

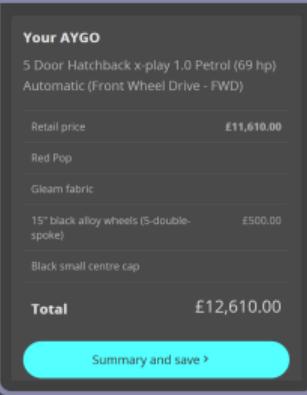
Configurators in the Wild – Cars

Configuring a Car ...

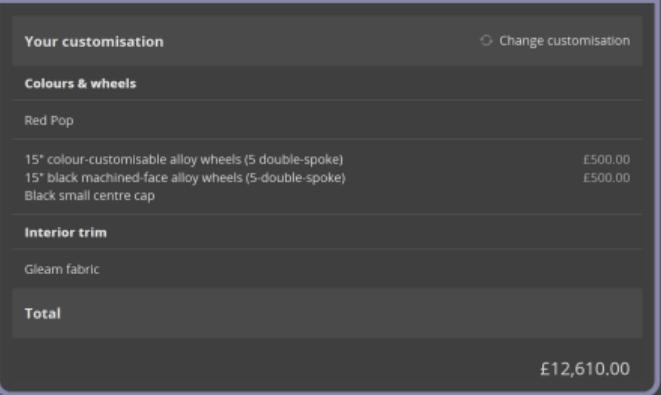


10. cancel the dialog

with a Weird Price



with 8 Wheels!



- canceling the dialog was not considered and lead to an invalid state (i.e., configuration)
- humans check these configurations, but some errors are only found during production
- many constraints: appear arbitrary, not explained

Configurators in the Wild – Cars

Configuring a German Car

[example from Lecture 1]

Configuration Assistant.

► Show instructions

Your most recent action requires your configuration to be adjusted.

Your choice

+ Enhanced Bluetooth telephone with USB & Voice Control + £ 350.00

Adding

+ BMW Navigation £ 0.00

Removing

- Enhanced Bluetooth with wireless charging - £ 395.00

- Navigation system Professional £ 0.00

- WiFi hotspot preparation £ 0.00

- Media package - Professional - £ 900.00

- Online Entertainment £ 0.00

- Microsoft Office 365 - £ 150.00

Why does the telephone conflict with Microsoft Office?

Configurators in the Wild – Notebooks

Configuring a Notebook

Display

14.0" FHD (1920x1080), LED backlight, 300 nits, 16:9 aspect ratio, 700:1 contrast ratio, 72% gamut, 170° viewing angle, IPS, Touch

SELECTED

14.0" WQHD (2560x1440), LED backlight, 300 nits, 16:9 aspect ratio, 700:1 contrast ratio, 72% gamut, 170° viewing angle, IPS, Touch

+ £91.20

14.0" HDR WQHD (2560x1440) with Dolby Vision™, LED backlight, 500 nits, 16:9 aspect ratio, 1500:1 contrast ratio, 100% gamut, 170° viewing angle, IPS, Touch
Please note this display is only available with WWAN/mobile broadband.

+ £159.60

Display

14.0" FHD (1920x1080), LED backlight, 300 nits, 16:9 aspect ratio, 700:1 contrast ratio, 72% gamut, 170° viewing angle, IPS, Touch

Invalid configuration

0

+ £91.20

14.0" WQHD (2560x1440), LED backlight, 300 nits, 16:9 aspect ratio, 700:1 contrast ratio, 72% gamut, 170° viewing angle, IPS, Touch



14.0" HDR WQHD (2560x1440) with Dolby Vision™, LED backlight, 500 nits, 16:9 aspect ratio, 1500:1 contrast ratio, 100% gamut, 170° viewing angle, IPS, Touch
Please note this display is only available with WWAN/mobile broadband

LOADING...

SELECTED

can detect mistakes, but provides no explanations or fixes

Configurators in the Wild – Notebooks

Still Configuring a Notebook

Microsoft Productivity Software

None	SELECTED
Microsoft Office 365 Home	+ £59.99
Microsoft Office 365 Personal	+ £79.99
Microsoft Office Home and Student 2016	+ £119.99
Microsoft Office Home and Business 2016	+ £229.99
Adobe Acrobat Standard 2017 and Microsoft Office Home and Business 2016	+ £399.60
Adobe Acrobat Standard 2017 and Microsoft Office	+ £628.80

Microsoft Office Not Included

For your best experience, Lenovo recommends selecting a Microsoft Office product with your new purchase.



NEED HELP DECIDING?

Roll over each product to get specific details on each Office product

allows some feature combinations and not others, prices are opaque

Automated Analysis of Feature Models

Open Questions

- How do such configurators work?
- How to avoid inconsistencies?
- How to provide explanations and fixes?
- How to get all valid configurations automatically? (P2(b))

Automated Analysis of Feature Models

- up until now: **creation and transformation** of feature models
- now: **analysis** of feature models to improve our understanding of a configuration space
- for brevity: product = valid configuration

Asking Questions About Feature Models

- Is a given configuration valid?
- Is there any product at all?
How many/which products are there?
- Is a given feature (de-)selectable at all?
How many/which products include it?
- Is a given partial configuration consistent?
How many/which products include it?
- (Which features always occur together?)
- (Is a given constraint redundant?)
- (How do two feature model versions differ?)
- (Why is ...? How to fix ...?)

SAT, #SAT, and AllSAT

Recap: Boolean Satisfiability Problem (SAT)

- **decision problem:** is there any assignment A that satisfies a given formula?
- formally: $SAT(\phi) \Leftrightarrow \exists A: \phi(A) = \top$
- known to be **NP-complete**:
in theory, difficult to solve if $P \neq NP$;
in practice, solvability depends on domain
- answered by **SAT solvers**:
highly-optimized, off-the-shelf tools;
competitively developed over several decades;
takes a CNF in DIMACS format as input

- $X \rightarrow Y$ is satisfiable
- $X \vee \neg X$ is satisfiable (even a tautology)
- $X \wedge \neg X$ is not satisfiable (why?)

Sharp Satisfiability Problem (#SAT)

- **counting problem:** how many assignments satisfy a given formula?
- $\#SAT(\phi) = |\{A \mid \phi(A) = \top\}|$
- known to be **#P-complete**:
at least as hard as SAT (probably harder)
- answered by **#SAT solvers**

Solution Enumeration Problem (AllSAT)

- **enumeration problem:** which assignments satisfy a given formula?
- $AllSAT(\phi) = \{A \mid \phi(A) = \top\}$
- at least as hard as #SAT (probably harder)
- answered by **AllSAT solvers**

Automated Analysis of Feature Models

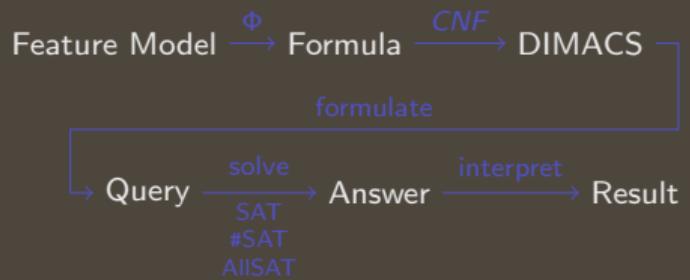
Asking Questions About Feature Models

- Is a given configuration valid? \Rightarrow evaluate
- Is there any valid configuration at all?
How many/which valid configurations are there?
- Is a given feature (de-)selectable at all?
How many/which valid configurations include it?
- Is a given partial configuration consistent?
How many/which valid configurations include it?

Choosing the Right Solver

- “is?” \approx SAT solver query
- “how many?” \approx #SAT solver query
- “which?” \approx AllSAT solver query

Typical Feature-Model Analysis Process



for brevity, we assume that $\phi = \text{CNF}(\Phi(FM))$
for a given feature model FM

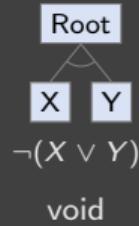
Consistency, Cardinality, and Enumeration – Feature Model

Consistency of Feature Models (SAT)

Void/Consistent Feature Model

- are there grave modeling errors?
- is it possible to configure any product at all?

$$\phi \xrightarrow{\text{SAT}} \perp/\top \xrightarrow[\top]{\perp} \begin{array}{l} FM \text{ is void} \\ FM \text{ is consistent} \end{array}$$



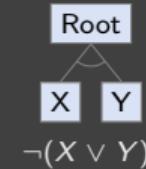
Cardinality of Feature Models (#SAT)

How Many Products Are There?

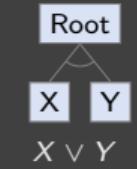
$$\phi \xrightarrow{\#SAT} |C|$$

Variability Factor: Share of Products?

$$\phi \xrightarrow{\#SAT} |C| \longrightarrow \frac{|C|}{2^{|F|}}$$



0 products, VF 0



2 products, VF $\frac{2}{8}$

Consistency, Cardinality, and Enumeration – Feature Model

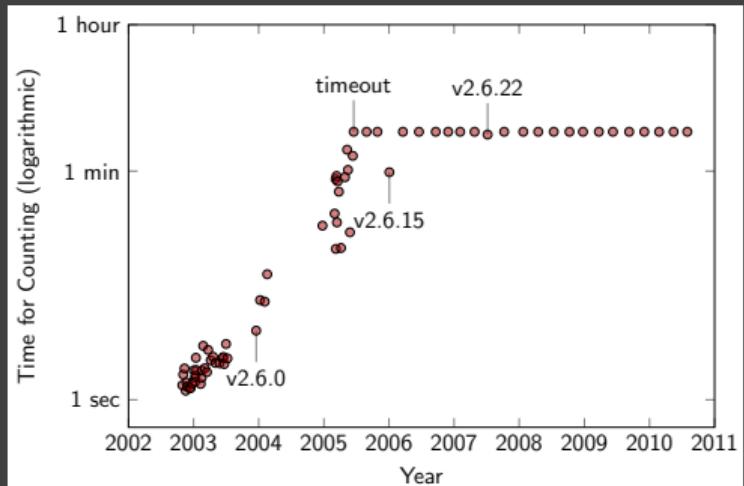
Feasibility of SAT-Based Analyses

Is SAT-Based Analysis “Easy”?

- provocative claim: “SAT-based analysis of feature models is easy” [Mendonca et al. 2009]
- easy = performs much better than expected (although NP-complete)
- easy = fast?
 - what about formulating the query? (e.g., CNF transformation)
 - what about many queries? (e.g., what we discuss next)

Feasibility of #SAT-Based Analyses

Time to Count Products of Linux



- the solver from 2023 can solve models from 2003
- can we analyze the models from 2023 in 2043?

Consistency, Cardinality, and Enumeration – Feature Model

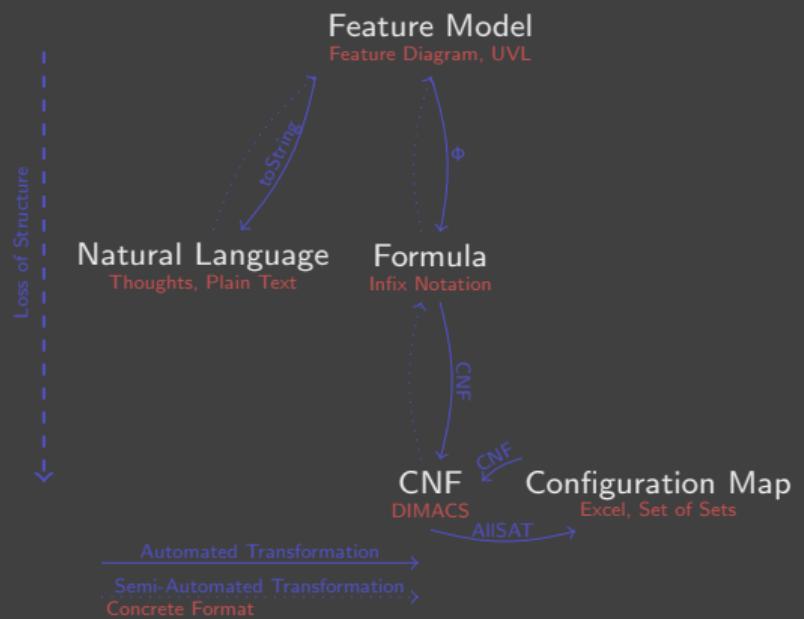
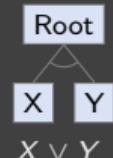
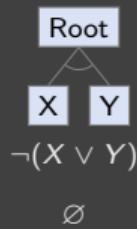
Enumeration of Feature Models (AllSAT)

Which Products Are There?

- P2(b): How to get all products?

$$\phi \xrightarrow{\text{AllSAT}} C$$

AllSAT does not scale to realistic feature models!
50 features, configurations ≈ 1 Byte ≈ 1 Petabyte



Consistency, Cardinality, and Enumeration – Features

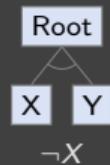
Consistency of Features (SAT)

Core/Dead Feature

- can a feature F be (de-)selected at all?

$$\phi \wedge F \xrightarrow{\text{SAT}} \perp/\top \xrightarrow{\perp} F \text{ is dead}$$
$$\phi \wedge F \xrightarrow{\text{SAT}} \perp/\top \xrightarrow{\top} F \text{ is not dead}$$

$$\phi \wedge \neg F \xrightarrow{\text{SAT}} \perp/\top \xrightarrow{\perp} F \text{ is core}$$
$$\phi \wedge \neg F \xrightarrow{\text{SAT}} \perp/\top \xrightarrow{\top} F \text{ is not core}$$



X is dead, $Root$ and Y are core

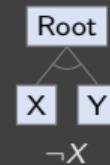
Cardinality of Features (#SAT)

How Many Products Include Feature F ?

$$\phi \wedge F \xrightarrow{\#SAT} |\{S \in C \mid F \in S\}|$$

Commonality: How Dead is This Feature?

$$\phi \wedge F \xrightarrow{\#SAT} |\{S \in C \mid F \in S\}| \rightarrow \frac{|\{S \in C \mid F \in S\}|}{|C|}$$



X : 0 products, $Root$ and Y : 1 products

Consistency, Cardinality, and Enumeration – Partial Configurations

Consistency of Partial Configurations (SAT)

Valid Partial Configuration

Is a partial configuration $C = (S, D)$ consistent with the feature model?

$$\phi \wedge \bigwedge_{s \in S} s \wedge \bigwedge_{d \in D} \neg d \xrightarrow{\text{SAT}} \perp / \top \xrightarrow{\perp} C \times \begin{cases} \top \\ \perp \end{cases} C \checkmark$$

Cardinality of Partial Configurations (#SAT)

How Many Products Are Still Configurable for C ?

$$\phi \wedge \dots \xrightarrow{\#SAT} |\{(S', D') \in C \mid S' \subseteq S, D' \subseteq D\}|$$

Root



$X \rightarrow Y$

$(\{\text{Root}\}, \{X\}) \checkmark$

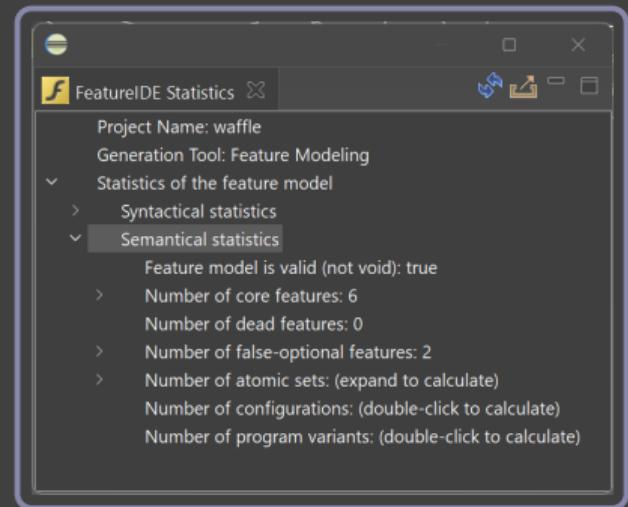
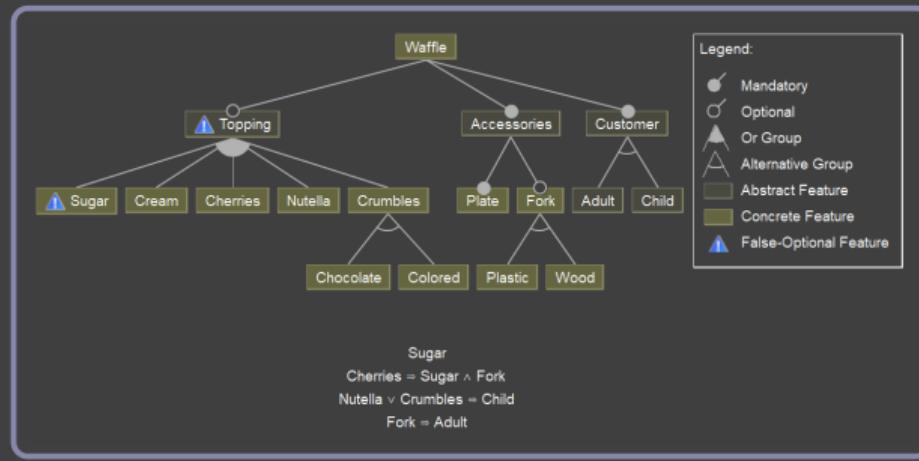
Root



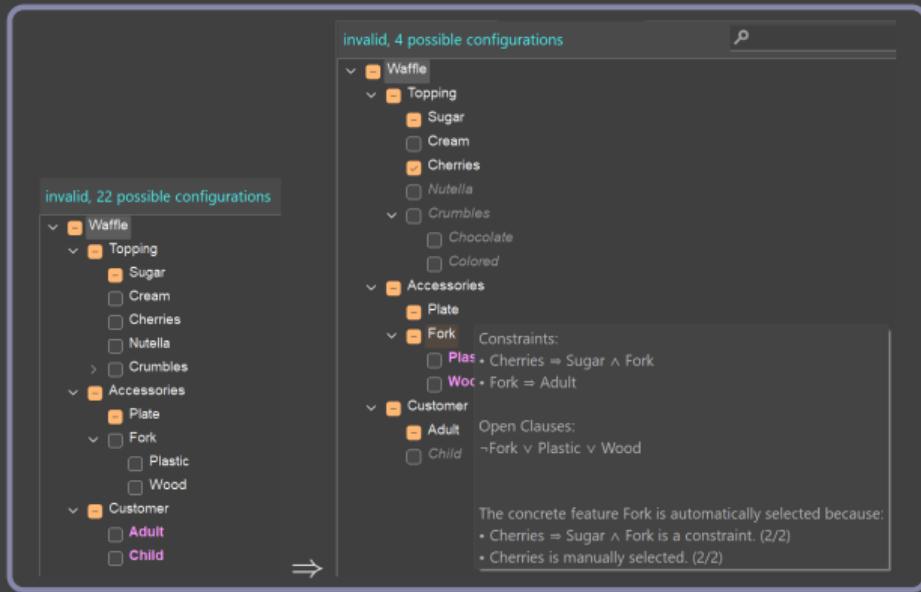
$X \rightarrow Y$

$(\{\text{Root}\}, \{X\})$: 2 products

Automated Analyses in FeatureIDE – Feature-Model Editor



Automated Analyses in FeatureIDE – Configuration Editor

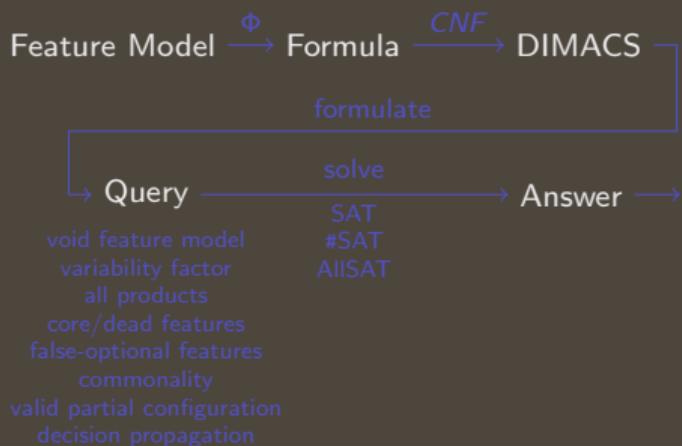


Decision Propagation

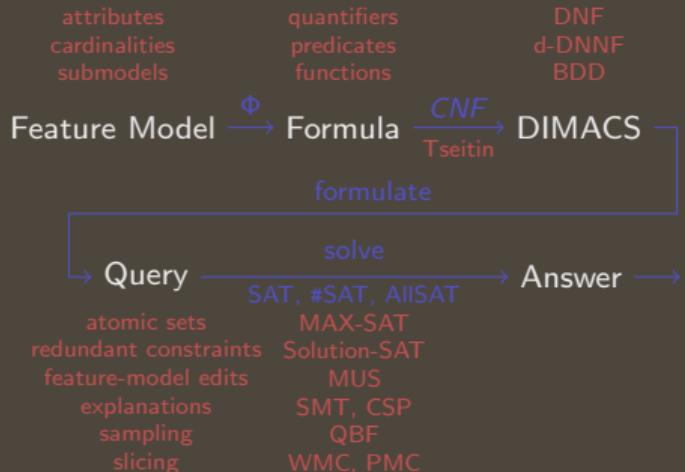
- after each decision (i.e., click) ...
 - ... select features that are now **conditionally core**
 - ... deselect features that are now **conditionally dead**
- this way it is impossible to configure an invalid product
- explanations for all propagated decisions

Automated Analysis of Feature Models

The Road So Far ...



... and Beyond



- develop new analyses
- improve efficiency of existing analyses
- investigate correctness and compositionality

Analyzing Feature Models – Summary

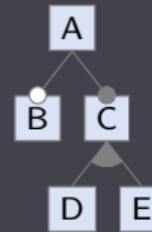
Lessons Learned

- with solvers, we can build reliable configurators for product lines
- SAT-based analyses: void feature model, core/dead features, decision propagation
- #SAT-based analyses: variability factor, feature commonality

Further Reading

- Apel et al. 2013, Section 10.1, pp. 244–254
 - introduction to feature-model analysis
- David Benavides et al. (2010): Automated Analysis of Feature Models 20 Years Later: A Literature Review
 - old but extensive literature survey
- Chico Sundermann et al. (2021): Applications of #SAT Solvers on Feature Models
 - experiments on the scalability of #SAT solvers

Practice



think of a constraint that would make exactly one feature dead

FAQ – 4. Feature Modeling

Lecture 4a

- What is feature modeling? When is it needed?
- How can we specify valid combinations of features?
- What is a complete, partial, valid, invalid configuration?
- What are (dis-)advantages of natural language, configuration map, and feature models?
- What is the graphical syntax and semantics of feature models?
- Give an example feature model!

Lecture 4b

- What representations of feature models are available? Are they equivalent?
- How to represent feature models textually?
- What is UVL (used for)?
- How to identify whether a configuration is valid?
- How to translate feature model into a propositional formula?
- What are DIMACS and KConfig (used for)?
- Would you recommend Excel for feature model? Why (not)?

Lecture 4c

- Why can configuration become challenging?
- How can we identify problems with feature models and configurations?
- How can feature models be analyzed? What analyses are available?
- What solvers can be used to analyze feature models?
- What is the difference between SAT, #SAT, and ALLSAT?
- Why are solvers useful when creating configurations?