1-gVirtualXRay_vs_Gate-detector_realistic_phantom

September 21, 2022

[1]:
```python
from IPython.display import display
from IPython.display import Image
from utils import * # Code shared across more than one notebook
```

[2]:
```python
output_path = "1-output_data/"

if not os.path.exists(output_path):
    os.mkdir(output_path)
```

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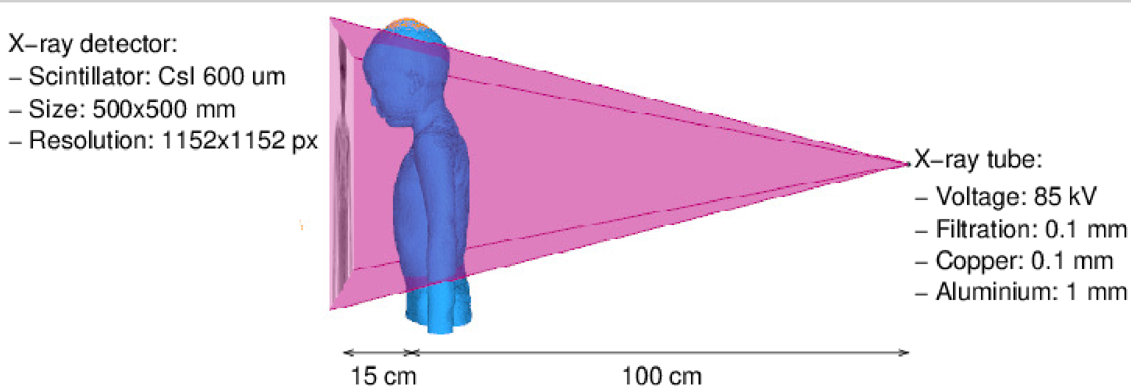
Purpose: In this notebook, we aim to demonstrate that gVirtualXRay is able to generate analytic simulations on GPU comparable to images generated with the state-of-the-art Monte Caro simulation packages. An anthropomorphic phantom is used. It corresponds to a 5-year old boy. We take into account i) a realistic beam spectrum (tube voltage and filtration) and ii) the energy response of the detector.

Material and Methods: We simulate an image with gVirtualXRay and compare it with a ground truth image. For this purpose, we use Gate, a wrapper for CERN's state-of-the-art Monte Caro simulation tool: Geant4. The number of tracked particles is 1e9.

In our simulation the source-to-object distance (SOD) is 1000mm, and the source-to-detector distance (SDD) is 1125mm. The beam spectrum is polychromatic. The voltage is 85 kV. The filtration is 0.1 mm of copper and 1 mm of aluminium. The energy response of the detector is considered. It mimics a 600-micron thick CsI scintillator.

[3]:
```python
Image(filename="pediatric_phantom_data/pediatric-setup.png")
```

[3]:



The sample is made of a 70x70x15mm box of water, in which 5 columns of 3 spheres of different radii (2, 3.5, and 5mm) have been inserted. A given material is associated to the spheres of each column (bone (cortical), blood (whole), brain (grey/white matter), breast tissue, and adipose tissue). The columns are ordered in decreasing density. We use the definitions of tissue substitutes provided in the ICRU Report 44 by the International Commission on Radiation Units and Measurements. The material composition is available at https://physics.nist.gov/PhysRefData/XrayMassCoef/tab2.html.

[4]:
```
Image(filename=output_path+"/pediatric_model.png", width=800)
```

[4]:

Results: The calculations were performed on the following platform:

[5]:
```
printSystemInfo()
```

```
OS:
        Linux 5.3.18-150300.59.54-default
        x86_64

CPU:
        AMD Ryzen 7 3800XT 8-Core Processor

RAM:
        63 GB
GPU:
        Name: NVIDIA GeForce RTX 2080 Ti
        Drivers: 510.73.08
        Video memory: 11 GB
```

The Monte Carlo simulation needed 5.36e6 HS06 seconds to complete.

It is equivalent to **8.68E+08** ms (i.e. ~10 days) on the system used. Only 51 ± 4 ms was needed with the GPU used.

The mean absolute percentage error (MAPE), also known as mean absolute percentage deviation (MAPD), between the two simulated images is **MAPE 3.12%**. The **zero-mean normalised cross-correlation is 99.96%**. The **Structural Similarity Index (SSIM) is 0.99**.

As MAPE is relatively low (about 3%), SSIM is high (close to 1), and ZNCC is high (close to 100%), we can conclude that this X-ray image simulated with gVirtualXRay on GPU in milliseconds is comparable to the same Monte Carlo simulation that ran for days.

1 Import packages

[6]:
```
%matplotlib inline

import os # Locate files

import math
import numpy as np # Who does not use Numpy?
import pandas as pd # Load/Write CSV files

import urllib, zipfile

import matplotlib

from matplotlib.cm import get_cmap
import matplotlib.pyplot as plt # Plotting
from matplotlib.colors import LogNorm # Look up table
from matplotlib.colors import PowerNorm # Look up table
import matplotlib.colors as mcolors

font = {'family' : 'serif',
        #'weight' : 'bold',
         'size'   : 22
       }
matplotlib.rc('font', **font)
# matplotlib.rc('text', usetex=True)

from scipy.stats import pearsonr # Compute the correlatio coefficient
from scipy.spatial import distance # Euclidean distance

from skimage.util import compare_images # Checkboard comparison between two␣
 ↪images
from skimage.metrics import structural_similarity as ssim
from sklearn.metrics import mean_absolute_percentage_error as mape
from skimage.metrics import structural_similarity as ssim
from skimage.transform import resize # Resample the images
```

```python
from tifffile import imread, imwrite # Load/Write TIFF files

import datetime # For the runtime

import base64
import SimpleITK as sitk
from stl import mesh
import random
from sitk2vtk import sitk2vtk

from gvxrPython3 import gvxr # Simulate X-ray images
from gvxrPython3 import json2gvxr # Set gVirtualXRay and the simulation up␣
 ↪using a JSON file
from gvxrPython3.utils import visualise

from utils import * # Code shared across more than one notebook
```

```
SimpleGVXR 2.0.2 (2022-09-14T19:31:53) [Compiler: GNU g++] on Linux
gVirtualXRay core library (gvxr) 2.0.2 (2022-09-14T19:31:52) [Compiler: GNU g++]
on Linux
```

2 Reference image

We first load the reference image that has been simulated using Gate wrapper for CERN's Geant4. Here we ignore scattering.

[7]:
```python
raw_reference = imread("pediatric_phantom_data/direct.tif")
Full_field = np.ones(raw_reference.shape) # Perfect full field image
Dark_field = np.zeros(Full_field.shape) # Perfect dark field image
```

Projections are then corrected to account for variations in beam homogeneity and in the pixel-to-pixel sensitivity of the detector. This is the projection with flat-field correction (**Proj**):

$$\mathbf{Proj} = \frac{I - D}{F - D} \tag{1}$$

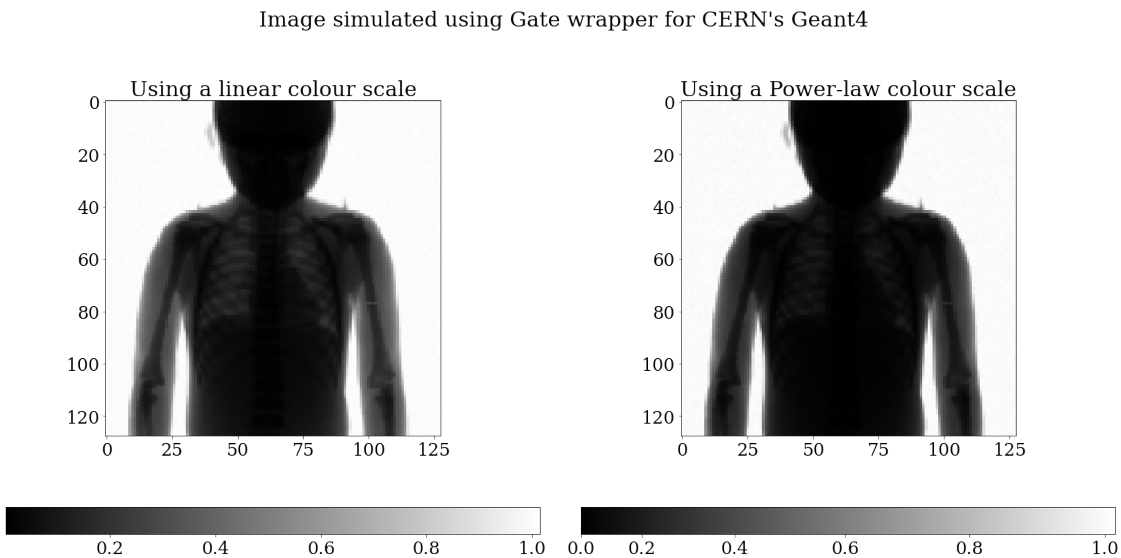
where F (full fields) and D (dark fields) are projection images without sample and acquired with and without the X-ray beam turned on respectively.

We now apply the flat-field correction to `Image`.

[8]:
```python
gate_image = (raw_reference - Dark_field) / (Full_field - Dark_field)
# gate_image = raw_reference / np.mean(Full_field)
```

We plot the image using a linear look-up table and a power-law normalisation.

[9]:
```python
displayLinearPowerScales(gate_image,
                         "Image simulated using Gate wrapper for CERN's Geant4",
                         output_path + "/reference_from_Gate-paediatrics")
```



3 Setting up gVirtualXRay

Before simulating an X-ray image using gVirtualXRay, we must create an OpenGL context.

[10]:
```
json2gvxr.initGVXR("notebook-1.json", "OPENGL")
```

```
Create an OpenGL context: 800x450

Tue Sep 20 22:02:30 2022 ---- Create window (ID: -1)
Tue Sep 20 22:02:30 2022 ---- Initialise GLFW
Tue Sep 20 22:02:30 2022 ---- Create an OpenGL window with a 3.2 context.
Tue Sep 20 22:02:30 2022 ---- Make the window's context current
Tue Sep 20 22:02:30 2022 ---- Initialise GLEW
Tue Sep 20 22:02:30 2022 ---- OpenGL vendor: NVIDIA Corporation
Tue Sep 20 22:02:30 2022 ---- OpenGL renderer: NVIDIA GeForce RTX 2080
Ti/PCIe/SSE2
Tue Sep 20 22:02:30 2022 ---- OpenGL version: 3.2.0 NVIDIA 510.73.08
Tue Sep 20 22:02:30 2022 ---- Use OpenGL 4.5.
Tue Sep 20 22:02:30 2022 ---- Initialise the X-ray renderer if needed and if
possible
```

3.1 X-ray source

We create an X-ray source. It is a point source.

[11]:
```
json2gvxr.initSourceGeometry()
```

```
Set up the beam
        Source position: [0.0, 1000.0, 0.0, 'mm']
        Source shape: PointSource
```

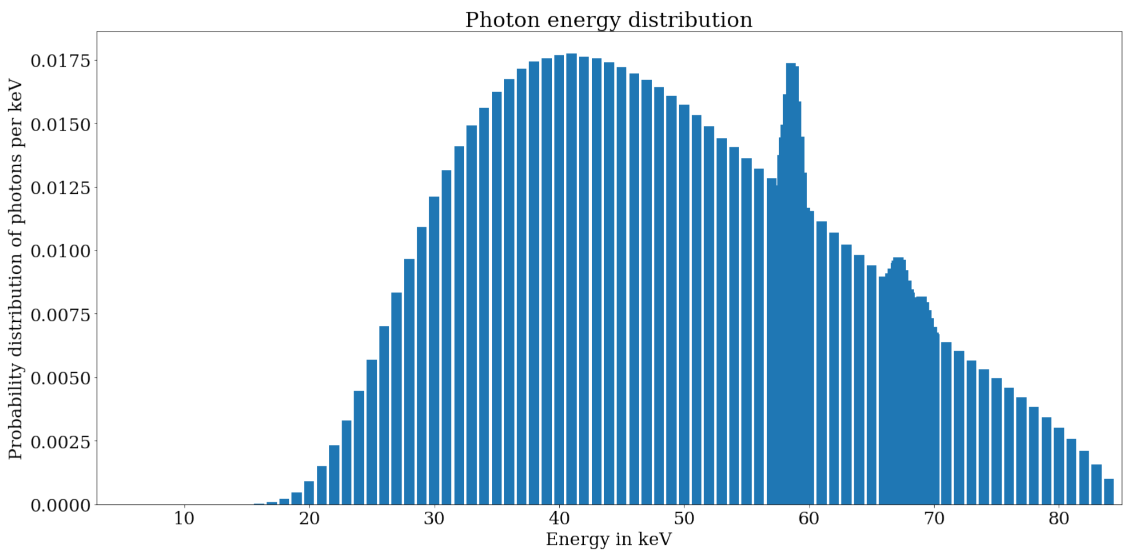
3.2 Spectrum

The spectrum is polychromatic.

[12]:
```
spectrum, unit, k, f = json2gvxr.initSpectrum(verbose=0)
energy_set = sorted(spectrum.keys())

count_set = []

for energy in energy_set:
    count_set.append(spectrum[energy])
```

Plot the spectrum

[13]:
```
k *= 1000
plotSpectrum(k, f, output_path + "/spectrum-paediatrics", xlim=[np.min(k), np.
 ↪max(k)])
```



3.3 Detector

Create a digital detector

[14]:
```
json2gvxr.initDetector()
```

```
Set up the detector
        Detector position: [0.0, -150.0, 0.0, 'mm']
        Detector up vector: [0, 0, -1]
        Detector number of pixels: [128, 128]
        Energy response: Gate_data/responseDetector.txt in MeV
        Pixel spacing: [3.90625, 3.90625, 'mm']
```

```
Tue Sep 20 22:02:31 2022 ---- Initialise the renderer
```

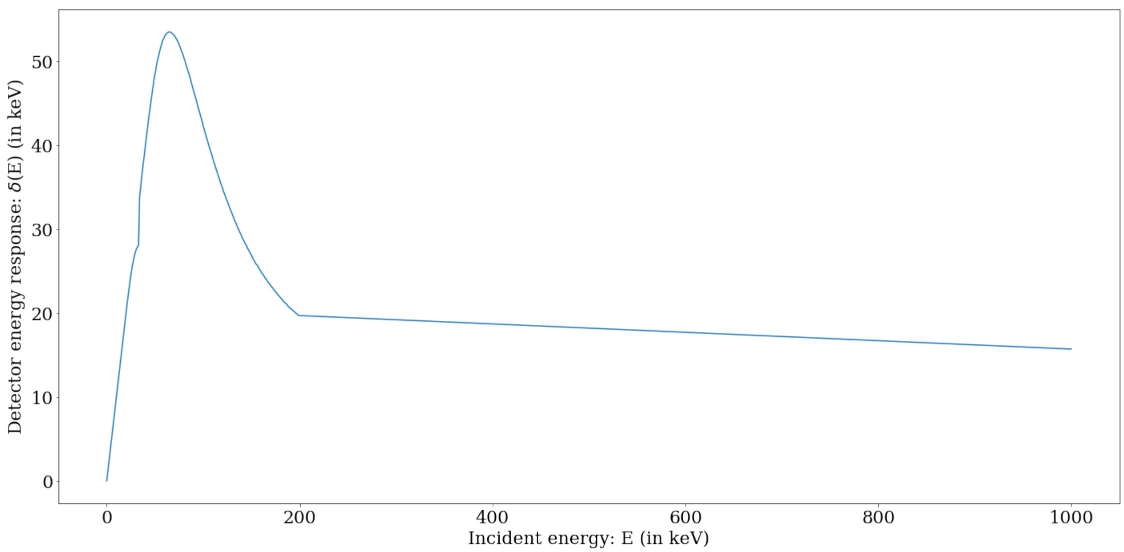
3.4 Model the energy response of the detector

Load the energy response

```
[15]: detector_response = np.loadtxt("Gate_data/responseDetector.txt")
```

Display the energy response

```
[16]: plt.figure(figsize= (20,10))
# plt.title("Detector response")
plt.plot(detector_response[:,0] * 1000, detector_response[:,1] * 1000)
plt.xlabel('Incident energy: E (in keV)')
plt.ylabel('Detector energy response: $\\delta$(E) (in keV)')

plt.tight_layout()

plt.savefig(output_path + '/detector_response.pdf')
plt.savefig(output_path + '/detector_response.png')
```



3.5 Converting the voxelised phantom to surface meshes

Download and unzip the phantom

```
[17]: if not os.path.exists("pediatric_phantom_data/Pediatric phantom.zip"):
    urllib.request.urlretrieve("https://drive.uca.fr/f/384a08b5f73244cf9ead/?
↪dl=1", "pediatric_phantom_data/Pediatric phantom.zip")
```

```
    with zipfile.ZipFile("pediatric_phantom_data/Pediatric phantom.zip","r") as␣
↪zip_ref:
        zip_ref.extractall("pediatric_phantom_data")
```

Load the phantom

[18]:
```
phantom = sitk.ReadImage("pediatric_phantom_data/Pediatric phantom/
↪Pediatric_model.mhd")
```

Load the labels

[19]:
```
df = pd.read_csv("pediatric_phantom_data/labels.dat")
```

Process every structure of the phantom

[20]:
```
if not os.path.exists("pediatric_phantom_data/meshes"):
    os.mkdir("pediatric_phantom_data/meshes")

if not os.path.exists("pediatric_phantom_data/segmentations"):
    os.mkdir("pediatric_phantom_data/segmentations")

meshes = []

for threshold, organ in zip(df["Label"], df["Organs"]):

    # Ignore air
    if organ != "Air":

        print("Process", organ)

        seg_fname = "pediatric_phantom_data/segmentations/" + organ + ".mha"
        mesh_fname = "pediatric_phantom_data/meshes/" + organ + ".stl"
        meshes.append(mesh_fname)

        # Only create the mesh if it does not exist
        if not os.path.exists(mesh_fname):

            # Only segment the image it is not done as yet
            if not os.path.exists(seg_fname):

                # Threshold the phantom
                binary_image = (phantom == threshold)

                # Smooth the binary segmentation
                smoothed_binary_image = sitk.AntiAliasBinary(binary_image)

                sitk.WriteImage(smoothed_binary_image, seg_fname)
            else:
```

```
                smoothed_binary_image = sitk.ReadImage(seg_fname)

            # Create a VTK image
            vtkimg = sitk2vtk(smoothed_binary_image, centre=True)

            vtk_mesh = extractSurface(vtkimg, 0)

#             print('Before decimation')
#             print(f'There are {mesh.GetNumberOfPoints()} points.')
#             print(f'There are {mesh.GetNumberOfPolys()} polygons.')

#             decimate = vtk.vtkDecimatePro()
#             decimate.SetInputData(mesh)
#             decimate.SplittingOn()
#             decimate.SetTargetReduction(30)
#             decimate.PreserveTopologyOn()
#             decimate.Update()

#             decimated = vtk.vtkPolyData()
#             decimated.ShallowCopy(decimate.GetOutput())

#             print('After decimation')
#             print(f'There are {decimated.GetNumberOfPoints()} points.')
#             print(f'There are {decimated.GetNumberOfPolys()} polygons.')
#             print(
#                 f'Reduction: {(mesh.GetNumberOfPolys() - decimated.
 ↪GetNumberOfPolys()) / mesh.GetNumberOfPolys()}')

#             print("\n\n")
#             writeSTL(decimated, mesh_fname)
            writeSTL(vtk_mesh, mesh_fname)
```

```
Process Muscle
Process Bone
Process Stomach-Interior
Process Cartilage
Process Brain
Process Bladder
Process Gallbladder
Process Heart
Process Kidneys-right
Process Kidneys-left
Process Small-Intestine
Process Large-Intestine
Process Liver
Process Lung-right
Process Lung-left
Process Pancreas
```

```
Process Spleen
Process Stomach
Process Thymus
Process Eyes-right
Process Eyes-left
Process Skull
Process Trachea
```

Load the samples. `verbose=2` is used to print the material database for Gate. To disable it, use `verbose=0` or `verbose=1`.

[21]:
```python
json2gvxr.initSamples(verbose=0)
```

```
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Muscle.stl        nb_faces:       1756726
nb_vertices:    5270178 bounding_box (in cm):   (-17.9687, -10.8887, -30.9017)
(16.6016, 11.1799, 28.6986)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Bone.stl  nb_faces:       541826  nb_vertices:
1625478 bounding_box (in cm):   (-16.7969, -23.6577, -30.9017)  (15.2152,
9.88865, 16.3501)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Stomach-Interior.stl      nb_faces:       9452
nb_vertices:    28356   bounding_box (in cm):   (-1.34334, -2.38867, -17.0041)
(4.16143, 3.05231, -8.50205)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Cartilage.stl     nb_faces:       163322
nb_vertices:    489966  bounding_box (in cm):   (-16.7615, -4.32288, -30.9017)
(15.5041, 8.717, 16.6771)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Brain.stl nb_faces:       124028  nb_vertices:
372084  bounding_box (in cm):   (-7.32082, -9.98695, 16.3501)   (7.50031,
5.78681, 28.1222)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Bladder.stl       nb_faces:       3712
nb_vertices:    11136   bounding_box (in cm):   (-3.78536, 2.11808, -30.9017)
(0.175804, 5.49461, -29.7572)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Gallbladder.stl   nb_faces:       4308
nb_vertices:    12924   bounding_box (in cm):   (-5.07422, -1.68659, -17.9851)
(-2.54188, 1.49065, -14.3881)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Heart.stl nb_faces:       48172   nb_vertices:
144516  bounding_box (in cm):   (-3.78536, -3.07617, -9.15606)  (6.32529,
5.68903, 1.30801)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Kidneys-right.stl nb_faces:       17512
nb_vertices:    52536   bounding_box (in cm):   (-7.69363, 1.73117, -18.9661)
(-2.47349, 7.23954, -10.4641)
```

```
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Kidneys-left.stl  nb_faces:       16388
nb_vertices:    49164   bounding_box (in cm):   (1.37053, 3.46679, -17.9851)
(6.44388, 7.74184, -8.82905)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Small-Intestine.stl       nb_faces:       118532
nb_vertices:    355596  bounding_box (in cm):   (-7.48809, -2.95731, -30.9017)
(7.59416, 8.32697, -12.0991)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Large-Intestine.stl       nb_faces:       94336
nb_vertices:    283008  bounding_box (in cm):   (-4.66426, -1.67902, -30.4112)
(7.11153, 6.16473, -13.4071)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Liver.stl nb_faces:       87800   nb_vertices:
263400  bounding_box (in cm):   (-9.35286, -3.73856, -19.2931)  (5.43096,
7.83896, -6.21304)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Lung-right.stl    nb_faces:       80364
nb_vertices:    241092  bounding_box (in cm):   (-9.47265, -3.16992, -8.82905)
(0.0788746, 8.15358, 6.54004)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Lung-left.stl     nb_faces:       70736
nb_vertices:    212208  bounding_box (in cm):   (0.397666, -2.26504, -9.81006)
(8.28139, 8.52371, 6.21304)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Pancreas.stl      nb_faces:       14592
nb_vertices:    43776   bounding_box (in cm):   (-2.8088, -0.240234, -17.0041)
(5.6632, 4.32215, -10.1371)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Spleen.stl        nb_faces:       25468
nb_vertices:    76404   bounding_box (in cm):   (1.48829, -0.611202, -14.7151)
(8.10404, 7.94215, -6.86704)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Stomach.stl       nb_faces:       28680
nb_vertices:    86040   bounding_box (in cm):   (-3.47804, -2.58413, -17.0041)
(5.05955, 4.0295, -7.84805)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Thymus.stl        nb_faces:       3136
nb_vertices:    9408    bounding_box (in cm):   (-0.846352, -1.87282, -1.30801)
(1.53113, 1.18326, 2.28901)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Eyes-right.stl    nb_faces:       3956
nb_vertices:    11868   bounding_box (in cm):   (-3.88504, -9.01112, 14.7151)
(-1.28679, -6.41928, 17.6581)
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Eyes-left.stl     nb_faces:       4116
nb_vertices:    12348   bounding_box (in cm):   (1.66718, -8.8147, 14.7151)
(4.47449, -6.12631, 17.6581)
```

```
Tue Sep 20 22:02:32 2022 ---- file_name:
pediatric_phantom_data/meshes/Skull.stl nb_faces:       327028  nb_vertices:
981084  bounding_box (in cm):   (-7.59598, -10.476, 7.84805)    (7.79064,
6.17931, 29.1032)
Tue Sep 20 22:02:33 2022 ---- file_name:
pediatric_phantom_data/meshes/Trachea.stl       nb_faces:       8588
nb_vertices:    25764   bounding_box (in cm):   (-3.48031, -0.996257, -2.61602)
(3.39865, 5.09486, 10.1371)
```

Get the total number of triangles

[22]:
```
number_of_triangles = 0

for sample in json2gvxr.params["Samples"]:
    label = sample["Label"]
    number_of_triangles += gvxr.getNumberOfPrimitives(label)
```

Visualise the phantom

[23]:
```
plot = visualise(use_log=True, use_negative=True)
plot.background_color = 0xffffff
```

```
Output()
```

[24]:
```
fname = output_path + '/pediatric_model.png'
if not os.path.isfile(fname):

    plot.fetch_screenshot() # Not sure why, but we need to do it twice to get␣
↪the right screenshot
    plot.fetch_screenshot()

    data = base64.b64decode(plot.screenshot)
    with open(fname,'wb') as fp:
        fp.write(data)
```

4 Run the simulation

Update the 3D visualisation and take a screenshot

[25]:
```
gvxr.displayScene()

gvxr.computeXRayImage()
gvxr.useLighing()
gvxr.useWireframe()
gvxr.setZoom(1549.6787109375)

angle = math.pi / 2.0
rotation_matrix_x = np.array([ 1, 0, 0, 0,
                               0, math.cos(angle), -math.sin(angle), 0,
```

```
                              0, math.sin(angle),  math.cos(angle), 0,
                              0, 0, 0, 1])

rotation_matrix_z = np.array([ math.cos(angle), -math.sin(angle), 0, 0,
                              math.sin(angle),  math.cos(angle), 0, 0,
                              0, 0, 1, 0,
                              0, 0, 0, 1])

rotation_matrix_x.shape = [4,4]
rotation_matrix_z.shape = [4,4]

transformation_matrix = np.identity(4)

transformation_matrix = np.matmul(rotation_matrix_x, transformation_matrix)
transformation_matrix = np.matmul(rotation_matrix_z, transformation_matrix)

gvxr.setSceneRotationMatrix(transformation_matrix.flatten())

gvxr.setWindowBackGroundColour(1, 1, 1)

gvxr.displayScene()
```

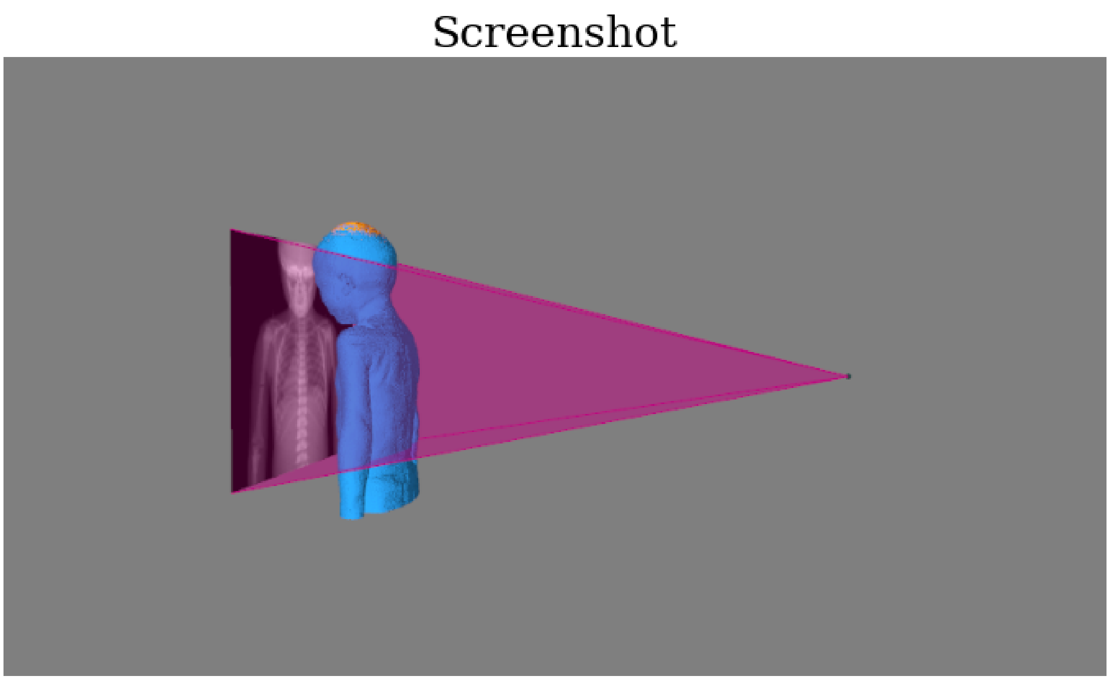
[26]:
```
screenshot = (255 * np.array(gvxr.takeScreenshot())).astype(np.uint8)
```

[27]:
```
fname = output_path + 'screenshot.png'
if not os.path.isfile(fname):

    plt.imsave(fname, screenshot)
```

[28]:
```
gvxr.setZoom(1549.6787109375)
gvxr.setSceneRotationMatrix([-0.19267332553863525, -0.06089369207620621, 0.
 ↪9793692827224731,  0.0,
                              0.9809651970863342,  -0.03645244985818863, 0.
 ↪19072122871875763, 0.0,
                              0.02408679760992527,  0.9974713325500488,  0.
 ↪06675821542739868, 0.0,
                              0.0,                 0.0,                 0.0, ␣
 ↪              1.0])

gvxr.setWindowBackGroundColour(0.5, 0.5, 0.5)

gvxr.useNegative()

gvxr.displayScene()
```

[29]:
```
screenshot = (255 * np.array(gvxr.takeScreenshot())).astype(np.uint8)
```

[30]:
```python
plt.figure(figsize= (10,10))
plt.title("Screenshot")
plt.imshow(screenshot)
plt.axis('off')

plt.tight_layout()

plt.savefig(output_path + '/screenshot-beam-on-paediatrics.pdf')
plt.savefig(output_path + '/screenshot-beam-on-paediatrics.png')
```



Compute an X-ray image 50 times (to gather performance statistics)

[31]:
```python
# gvxr.enableArtefactFilteringOnCPU()
gvxr.enableArtefactFilteringOnGPU()
# gvxr.disableArtefactFiltering() # Spere inserts are missing with GPU integration when a outer surface is used for the matrix


runtimes = []

for i in range(50):
    start_time = datetime.datetime.now()
    gvxr.computeXRayImage()
    end_time = datetime.datetime.now()
    delta_time = end_time - start_time
```

```
    runtimes.append(delta_time.total_seconds() * 1000)
```

Save an X-ray image

[32]:
```
# Compute the L-buffers on the GPU and integrate on the GPU
gvxr_image = np.array(gvxr.computeXRayImage())
gvxr_image = resize(gvxr_image, gate_image.shape)
imwrite(output_path + '/gvxr_image-raw-paediatrics.tif', gvxr_image.astype(np.
 ↪single))
```

Flat-field correction

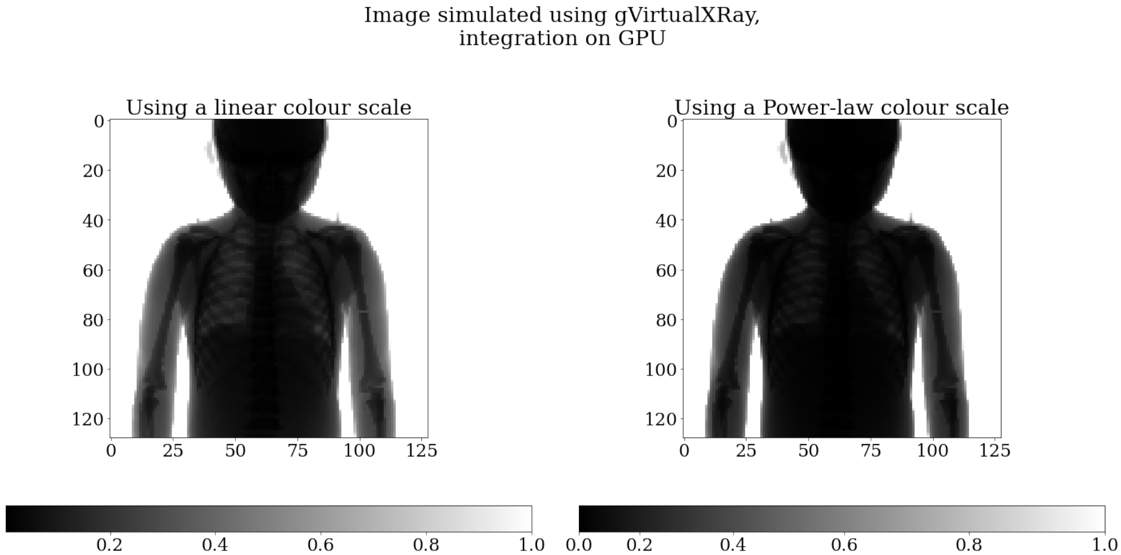
[33]:
```
total_energy_in_keV = 0.0
for energy, count in zip(energy_set, count_set):
    total_energy_in_keV += energy * count

total_energy_in_MeV = gvxr.getTotalEnergyWithDetectorResponse()
```

[34]:
```
white = np.ones(gvxr_image.shape) * total_energy_in_MeV
dark = np.zeros(gvxr_image.shape)

gvxr_image = (gvxr_image - dark) / (white - dark)
```

Save the corresponding image

[35]:
```
imwrite(output_path + '/gvxr_image-flat.tif', gvxr_image.astype(np.single))
```

[36]:
```
plt.figure(figsize= (20,10))

plt.suptitle("Image simulated using gVirtualXRay,\nintegration on GPU", y=1.02)

plt.subplot(121)
plt.imshow(gvxr_image, cmap="gray")
plt.colorbar(orientation='horizontal')
plt.title("Using a linear colour scale")

plt.subplot(122)
plt.imshow(gvxr_image, norm=PowerNorm(gamma=1./0.75), cmap="gray")
plt.colorbar(orientation='horizontal')
plt.title("Using a Power-law colour scale")

plt.tight_layout()

plt.savefig(output_path + '/gvxr_image-paediatrics.pdf')
plt.savefig(output_path + '/gvxr_image-paediatrics.png')
```



5 Comparison the analytic simulation with the Monte Carlo simulation

5.1 Quantitative validation

Compute image metrics between the two simulated images:

1. mean absolute percentage error (MAPE), also known as mean absolute percentage deviation (MAPD),
2. zero-mean normalised cross-correlation (ZNCC), and
3. Structural Similarity Index (SSIM).

We use these three metrics as one is a disimilarity measurement (MAPE), two are similarity measurement (ZNCC & SSIM). MAPE and ZNCC can be expressed as a percentage, which eases the interpretation of the numerical values. SSIM is a number between 0 and 1. A good value of MAPE s 0%; of ZNCC 100%, and SSIM 1.

[37]:
```
MAPE = mape(gate_image, gvxr_image)
ZNCC = np.mean((gate_image - gate_image.mean()) / gate_image.std() * (gvxr_image - gvxr_image.mean()) / gvxr_image.std())
SSIM = ssim(gate_image, gvxr_image, data_range=gate_image.max() - gate_image.min())

print("MAPE:", "{0:0.2f}".format(100 * MAPE) + "%")
print("ZNCC:", "{0:0.2f}".format(100 * ZNCC) + "%")
print("SSIM:", "{0:0.2f}".format(SSIM))
```

```
MAPE: 3.12%
ZNCC: 99.96%
SSIM: 0.99
```

```
[38]: runtime_avg = round(np.mean(runtimes))
      runtime_std = round(np.std(runtimes))
```

Print a row of the table for the paper

```
[39]: print("Paediatric -- polychromatic (85 kV), detector energy response & Gate & "␣
       ↪+
            "{0:0.2f}".format(100 * MAPE) + "\\%    &    " +
            "{0:0.2f}".format(100 * ZNCC) + "\\%    &    " +
            "{0:0.2f}".format(SSIM) + "    &    $" +
            str(json2gvxr.params["Detector"]["NumberOfPixels"][0]) + " \\pm " +␣
       ↪str(json2gvxr.params["Detector"]["NumberOfPixels"][1]) + "$    &    " +
            str(number_of_triangles) + "    &    " +
            "8.68E+08    &    " +
            "$" + str(runtime_avg) + " \\pm " + str(runtime_std) + "$ \\\\")
```

```
Paediatric -- polychromatic (85 kV), detector energy response & Gate & 3.12\%
&    99.96\%    &    0.99    &    $128 \pm 128$    &    3552778    &    8.68E+08
&    $42 \pm 3$ \\
```

In both cases, MAPE is very small (about 3%), ZNCC is very high (almost 100%), and SSIM is very high (almost 1). We can conclude that the two images are similar. The main difference lie in the Poisson noise affecting the Monte Carlo simulation.

5.2 Qualitative validation

Checkboard comparison

```
[40]: font = {'size'   : 12.5
             }
      matplotlib.rc('font', **font)
```

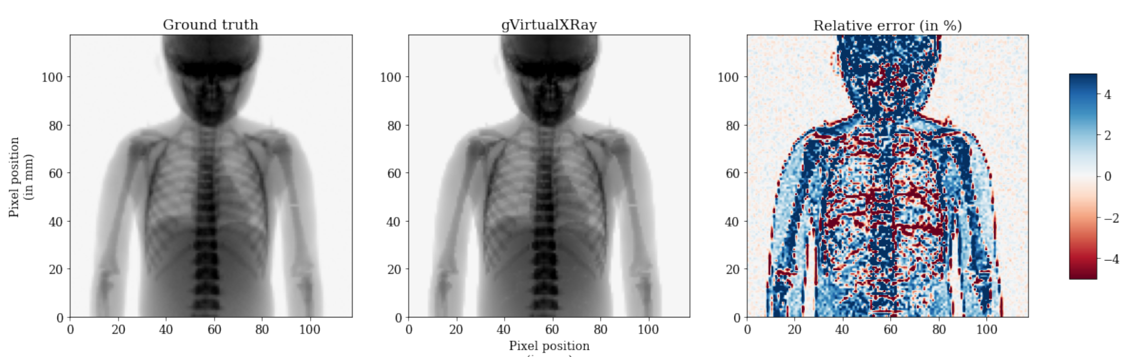
```
[41]: source_position = [json2gvxr.params["Source"]["Position"][0] * gvxr.
       ↪getUnitOfLength(json2gvxr.params["Source"]["Position"][3]) / gvxr.
       ↪getUnitOfLength("mm"),
                         json2gvxr.params["Source"]["Position"][1] * gvxr.
       ↪getUnitOfLength(json2gvxr.params["Source"]["Position"][3]) / gvxr.
       ↪getUnitOfLength("mm"),
                         json2gvxr.params["Source"]["Position"][2] * gvxr.
       ↪getUnitOfLength(json2gvxr.params["Source"]["Position"][3]) / gvxr.
       ↪getUnitOfLength("mm")
                        ]

      detector_position = [json2gvxr.params["Detector"]["Position"][0] * gvxr.
       ↪getUnitOfLength(json2gvxr.params["Detector"]["Position"][3]) / gvxr.
       ↪getUnitOfLength("mm"),
                           json2gvxr.params["Detector"]["Position"][1] * gvxr.
       ↪getUnitOfLength(json2gvxr.params["Detector"]["Position"][3]) / gvxr.
       ↪getUnitOfLength("mm"),
```

```
                        json2gvxr.params["Detector"]["Position"][2] * gvxr.
↪getUnitOfLength(json2gvxr.params["Detector"]["Position"][3]) / gvxr.
↪getUnitOfLength("mm")
                      ]

object_bbox = gvxr.getNodeAndChildrenBoundingBox("root", "mm")
object_position = [(object_bbox[0] + object_bbox[3]) / 2,
                   (object_bbox[1] + object_bbox[4]) / 2,
                   (object_bbox[2] + object_bbox[5]) / 2
                  ]

source_imager_distance = distance.euclidean(source_position, detector_position)
source_object_distance = distance.euclidean(source_position, object_position)

magnification = source_imager_distance / source_object_distance
```

[42]:
```
print("SID:", source_imager_distance, "mm")
print("SOD:", source_object_distance, "mm")
print("magnification:", magnification)
```

```
SID: 1150.0 mm
SOD: 1062.4489886902375 mm
magnification: 1.082404908133701
```

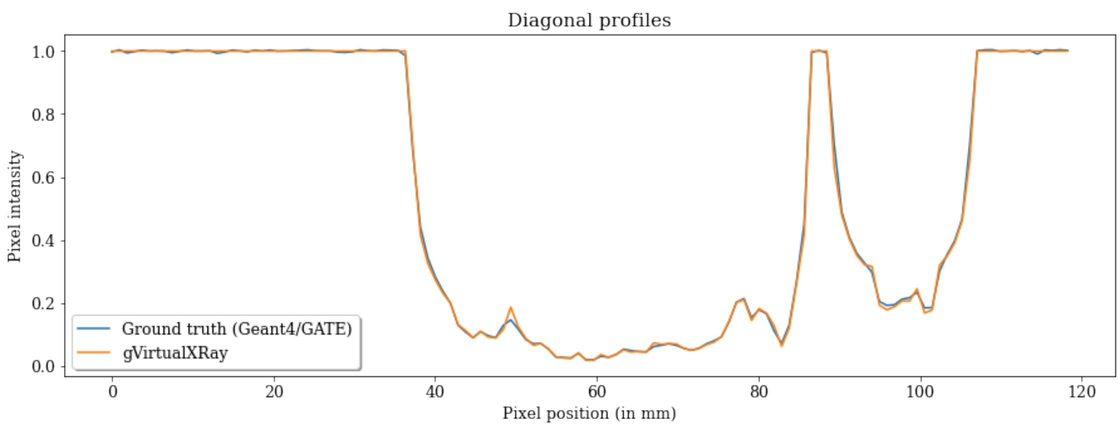
[43]:
```
detector_resolution = json2gvxr.params["Detector"]["NumberOfPixels"]
detector_size = json2gvxr.params["Detector"]["Size"]

pixel_pitch = np.array([detector_size[0] / detector_size[0] / gvxr.
↪getUnitOfLength("mm"),
            detector_size[1] / detector_size[1] / gvxr.getUnitOfLength("mm"),
])

fullCompareImages(gate_image,
                  gvxr_image,
                  "gVirtualXRay\n with integration on GPU",
                  output_path + "/full_comparison-paediatrics", pixel_pitch /␣
↪magnification, log=True)
```



Plot the profiles

[44]:
```
font = {'size'   : 12.5
       }
matplotlib.rc('font', **font)
```

[45]:
```
ground_truth_diag = np.diag(gate_image)
gvxr_diag = np.diag(gvxr_image)

x = np.linspace(0, len(ground_truth_diag), len(ground_truth_diag)) *␣
 ↪(pixel_pitch[0] / magnification)
plt.figure(figsize=(15, 5))

ax = plt.subplot(111)

ax.set_title("Diagonal profiles")

ax.plot(x, ground_truth_diag, label="Ground truth (Geant4/GATE)")
ax.plot(x, gvxr_diag, label="gVirtualXRay")

ax.legend(loc='best',
          ncol=1, fancybox=True, shadow=True)

plt.xlabel("Pixel position (in mm)")
plt.ylabel("Pixel intensity")

plt.savefig(output_path + '/profiles-paediatrics.pdf')
plt.savefig(output_path + '/profiles-paediatrics.png')
```



6 All done

Destroy the window

[46]:
```
gvxr.destroyAllWindows()
```

```
Tue Sep 20 22:02:42 2022 ---- Destroy all the windows
Tue Sep 20 22:02:42 2022 ---- Destroy window 0(0x558936cca360)
```