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cppEDM is a C++ implementation of empirical dynamic modeling (EDM) algorithms. It is designed as an application programming interface (API) with functions stored in the libEDM.a library.

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Introduction

cppEDM is a C++ implementation of empirical dynamic modeling (EDM) algorithms. Core algorithms are listed in table 1. It is primarily a functional programming implementation with application programming interface (API) functions accepting parameters and returning data objects. EDM functions are accessed from a user-compiled library created from C++ source files and a unix-like compiler supporting the C++11 standard. cppEDM shares many high-level design attributes with the pyEDM package.

Algorithm	API Interface	Reference
Simplex projection	Simplex()	Sugihara and May (1990)
Sequential Locally Weighted Global Linear Maps (S-map)	SMap()	Sugihara (1994)
Predictions from multivariate embeddings	<pre>Simplex(), SMap()</pre>	Dixon et. al. (1999)
Convergent cross mapping	CCM()	Sugihara et. al. (2012)
Multiview embedding * Not yet implemented		Ye and Sugihara (2016)

Convenience functions to prepare and evaluate data are listed in table 2.

Function	Purpose	Parameter Range
Embed()	Timeseries delay dimensional embedding	User defined
EmbedDimension()	Evaluate prediction skill vs. embedding dimension	E = [1, 10]
<pre>PredictInterval()</pre>	Evaluate prediction skill vs. forecast interval	Tp = [1, 10]
PredictNonlinear()	Evaluate prediction skill vs. SMap nonlinear localisation	θ = 0.01, 0.1, 0.3, 0.5, 0.75, 1, 1.5, 2, 3, 4, 5, 6, 7, 8, 9
ComputeError()	Pearson correlation, MAE, RMSE	

Installation

cppEDM is available at github.com/SugiharaLab/cppEDM.

The libEDM.a library can be built by running "make" in the cppEDM/src/ directory. This copies libEDM.a into the cppEDM/lib/ directory, where it can be linked to user applications.

cppEDM requires a C++11 standard compiler, and the Eigen C++ template library (eigen.tuxfamily.org/).

Once libEDM.a is built, there are a series of test applications in the cppEDM/tests/ directory. The applications can be built with the "make" command, and then executed at the command line.

Class Objects

Two C++ class objects are used for data access and parameter coordination, the DataFrame and Parameters classes, described below.

DataFrame

The DataFrame class is the fundamental data object of cppEDM. It stores data in a contiguous block of memory using the C++ valarray type in a row-major format.

A DataFrame can be initialised with data from a csv file by calling the DataFrame constructor with path and fileName parameters. The WriteData(path, file) class method can be called explicitly to write data to a csv format file.

All data input files are assumed to be in csv format. The files are assumed to have a single line header with column names, and it is required that the first column be a vector of times or time indices.

Primary DataFrame access functions are listed in table 3.

DataFrame Method	Parameters	Type	Purpose
(row, column)	size_t row size_t column	double or int	Access data element
DataFrame(path, file)	string path string fileName	DataFrame <double></double>	Create DataFrame from csv file
WriteData(path, file)	string outputFilePath string outputFileName		Write DataFrame to file
<pre>Elements()</pre>		valarray	Access data valarray
NColumns()		size_t	Get number of columns
NRows()		size_t	Get number of rows
size()		size_t	Get number of elements
ColumnNames()		vector< string >	Access column names
ColumnNameToIndex()		<pre>map<string, size_t=""></string,></pre>	Access column name to index map
<pre>MaxRowPrint()</pre>		size_t	Access maximum number of rows to ostream
Column(col)	size_t col	valarray	Get data vector at column
Row(row)	size_t row	valarray	Get data vector at row
VectorColumnName(column)	string column	valarray	Get data vector at column with name
DataFrameFromColumnIndex (columns)	vector <size_t></size_t>	DataFrame <double></double>	Get DataFrame subset from column indices
DataFrameFromColumnNames (columns)	vector <string></string>	DataFrame <double></double>	Get DataFrame subset from column names
WriteRow(row, array)	<pre>size_t row std::valarray<t> array</t></pre>		Write valarray to row
WriteColumn(col, array)	size_t col valarray <t> array</t>		Write valarray to column

Parameters

The Parameters class is used to store and access API function parameters in a unified object. Generally this is an internal object that does not need to be instantiated, accessed or dynamically modified. API parameter names and purpose are listed in table 4.

Parameter	Type	Default	Purpose
pathIn	string	"./"	Input data file path
dataFile	string	II II	Data file name
pathOut	string	"./"	Output file path
predictFile	string	II II	Prediction output file
lib	string	II II	library start : stop row indices
pred	string	II II	prediction start : stop row indices
E	int	0	Data dimension
Tp	int	0	Prediction interval
knn	int	0	Number nearest neighbors
tau	int	1	Embedding delay
theta	float	0	SMap localisation
columns	string	II II	Column names or indices for prediction
target	string	II II	Target library column name or index
embedded	bool	false	Is data an embedding?
verbose	bool	false	Echo messages
smapFile	string	II II	SMap coefficient output file
libSizes_str	string	II II	CCM library sizes
sample	int	0	CCM number of random samples
random	bool	true	CCM use random samples?
seed	unsigned	0	RNG seed, 0 = random seed

Application Programming Interface (API)

Embed

Create a data block of Takens time-delay embedding from each of the columns in the csv file or dataFrame. The columns parameter can be a list of column names, or a list of column indices. If columns is a list of indices, then column names are created as V1, V2...

Note: The returned DataFrame will have tau*(E-1) fewer rows than the input data from the removal of partial vectors as a result of the embedding.

Note: The returned DataFrame will not have the time column.

```
//-----
// Overload 1: Explicit data file path/name
//-----
DataFrame< double > Embed ( std::string path
                std::string dataFile = "",
                       E = 0,
                int
                int tau = 0,
                std::string columns = "",
                bool verbose = false );
//-----
// Overload 2: DataFrame provided
//-----
DataFrame< double > Embed ( DataFrame< double > dataFrame,
                int
                            tau = 0,
                std::string
                          columns = "",
                bool
                            verbose = false );
//-----
// Called from Embed to create the time-delay embedding
//-----
DataFrame< double > MakeBlock ( DataFrame< double >
                                  dataFrame,
                   int
                                  Ε,
                                  tau,
                   std::vector<std::string> columnNames,
                   bool
                                  verbose );
```

Simplex

Simplex projection of the input data file or DataFrame. The returned DataFrame has 3 columns "Time", "Observations", "Predictions". nan values are inserted where there is no observation or prediction. See the Parameters table for parameter definitions.

lib and pred specify [start stop] row indices of the input data for the library and predictions.

If embedded is false the data columns are embedded to dimension E with delay tau. If embedded is true the data columns are assumed to be a multivariable data block.

If knn is not specified, it is set equal to E+1.

```
//-----
// Overload 1: Explicit data file path/name
//----
std::string predictFile = "",
               std::string pred
               bool
                    verbose
                            = true );
//-----
// Overload 2: DataFrame provided
//-----
DataFrame<double> Simplex( DataFrame< double >,
               std::string pathOut = "./",
               std::string predictFile = "",
               std::string lib = "1 10",
std::string pred = "11 20",
               std::string pred
              int E = 0,
int Tp = 1,
int knn = 0,
int tau = 1,
std::string columns = "",
                            = "",
               std::string target
```

= true);

SMap

SMap projection of the input data file or DataFrame. See the Parameters table for parameter definitions.

SMap() returns a SMapValues structure:

```
struct SMapValues {
    DataFrame< double > predictions;
    DataFrame< double > coefficients;
};
```

The predictions DataFrame has 3 columns "Time", "Observations", "Predictions". nan values are inserted where there is no observation or prediction. If predictFile is provided the predictions will be written to it in csv format.

The coefficients DataFrame will have E+2 columns. The first column is the "Time" vector, the remaining E+1 columns are the SMap SVD fit coefficients.

1ib and pred specify [start, stop] row indices of the input data for the library and predictions.

If embedded is false the data columns are embedded to dimension E with delay tau. If embedded is true the data columns are assumed to be a multivariable data block. If smapFile is provided the coefficients will be written to it in csy format.

If knn is not specified, it is set equal to the library size. If knn is specified, it must be greater than E.

```
// Overload 1: Explicit data file path/name
//-----
SMapValues SMap( std::string pathIn = "./data/",
                 std::string dataFile = "",
std::string pathOut = "./",
std::string predictFile = "",
std::string lib = "1 10",
                                             = "11 20",
                 std::string pred
                 int
                             E
                                              = 0,
                 int Tp
int knn
int tau
double theta
                                              = 1,
                                              = 0,
                                              = 1.
                                              = 0,
                 std::string columns
                                              = "",
                 std::string target
                                              = "",
                 std::string smapFile
std::string jacobians
                                            = "",
                                                     // Not implemented
                           embedded
                 bool
                                             = false,
                                             = true );
                 bool
                             verbose
```

```
//-----
// Overload 2: DataFrame provided
//-----
SMapValues SMap( DataFrame< double >,
             std::string pathOut = "./",
std::string predictFile = "",
std::string lib = "1 10",
                                = "11 20",
             std::string pred
             int
                    E
                                  = 0,
                                  = 1,
             int
                     Тp
                     knn
             int
                                  = 0,
             int
                     tau
                                  = 1,
             double theta
                                  = 0,
             std::string columns
                                  = "",
                                  = "",
             std::string target
             std::string smapFile = "",
std::string jacobians = "",
                                         // Not implemented
                  embedded
             bool
                                  = false,
             bool
                     verbose
                                  = true );
```

CCM

Convergent cross mapping via Simplex of the first element in columns against target. See the Parameters table for parameter definitions.

The returned DataFrame has 3 columns. The first column is "LibSize", the second and third columns are Pearson correlation coefficients for "column: target" and "target: column" cross mapping.

libSizes specifies a string with "start stop increment" row values, i.e. "10 80 10" will evaluate library sizes from 10 to 80 in increments of 10.

If random is true, N = sample are radomly selected from the subset of each library size. If seed=0, then a random seed is generated for the random number generator. Otherwise, seed is used to initialise the random number generator.

If random is false, sample is ignored and contiguous library rows up to the current library size are used.

Note: Cross mappings are performed between column: target, and target: column. The default is to do this in separate threads. Threading can be disabled in the makefile by removing -DCCM THREADED.

Note: The entire library size is used in the Simplex prediction at each library subset size.

```
//-----
// Overload 2: DataFrame provided
//-----
DataFrame<double> CCM( DataFrame< double >,
               std::string pathOut = "./",
               std::string predictFile = "",
                    \mathbf{E} = \mathbf{0},
               int
                                = 0,
               int
                       Тp
                                = 0,
               int
                       knn
               int
                                = 1,
                       tau
                                = "",
               std::string columns
               std::string target
                                = "",
               std::string libSizes
                                = "",
                     sample
               int
                                = 0,
                                = true,
                      random
               bool
               unsigned seed
                                = 0,
                                       // seed=0: use RNG
```

EmbedDimension

Evaluate Simplex prediction skill for embedding dimensions from 1 to 10. The returned DataFrame has columns "E" and "rho". See the Parameters table for parameter definitions.

Note: nThreads defines the number of worker threads for the 10 embeddings.

```
// Overload 1: Explicit data file path/name
//-----
DataFrame<double> EmbedDimension( std::string pathIn = "./data/",
                       std::string dataFile = "",
                       std::string pathOut = "./",
                       std::string predictFile = "",
                       bool embedded = false,
                       bool
                              verbose
                                        = true,
                       unsigned nThreads
                                        = 4 );
//----
// Overload 2: DataFrame provided
//----
DataFrame<double> EmbedDimension( DataFrame< double >,
                       std::string pathOut
                       std::string predictFile = "",
                       std::string lib = "1 10",
                                       = "11 20",
                       std::string pred
                       int
                               Τp
                                        = 1,
                               tau
                       int
                       std::string columns = 1,
std::string target = "",
                       bool embedded bool verbose
                                        = false,
                                        = true,
                       unsigned nThreads = 4);
```

PredictInterval

Evaluate Simplex prediction skill for forecast intervals from 1 to 10. The returned DataFrame has columns "Tp" and "rho". See the Parameters table for parameter definitions.

Note: nThreads defines the number of worker threads for the 10 prediction interval forecasts.

```
//-----
// Overload 1: Explicit data file path/name
//-----
DataFrame<double> PredictInterval( std::string pathIn = "./data/",
                   std::string dataFile = "",
std::string pathOut = "./",
                   std::string predictFile = "",
                   unsigned nThreads = 4 );
//----
// Overload 2: DataFrame provided
//-----
DataFrame<double> PredictInterval( DataFrame< double >,
                   std::string pathOut
                   std::string predictFile = "",
                   bool embedded = false,
bool verbose = true,
unsigned nThreads = 4);
```

PredictNonlinear

Evaluate SMap prediction skill for localisation parameter θ from 0.01 to 9. The returned DataFrame has columns "theta" and "rho". See the Parameters table for parameter definitions.

Note: nThreads defines the number of worker threads for the 15 θ value forecasts.

```
//-----
// Overload 1: Explicit data file path/name
//-----
DataFrame<double> PredictNonlinear( std::string pathIn = "./data/",
                           std::string dataFile = "",
                           std::string pathOut = "./",
                           std::string predictFile = "",
                           std::string lib = "1 10",
                           std::string pred
                                            = "11 20",
                           int
                                    E
                           int
                                    Τp
                                            = 1,
                           int
                                    tau
                           std::string columns = "",
std::string target = "",
                           bool embedded = false,
                           bool
                                    verbose
                                             = true,
                           unsigned
                                    nThreads
                                             = 4);
//-----
// Overload 2: DataFrame provided
DataFrame<double> PredictNonlinear( DataFrame< double >,
                           std::string pathOut = "./",
                           std::string predictFile = "",
                           std::string lib = "1 10",
                           std::string pred
                                            = "11 20",
                           int
                                    E
                                            = 0,
                           int
                                    Тp
                                             = 1,
                           int
                                    tau
                           std::string columns
                                             = "",
                           std::string target
                           bool embedded bool verbose
                                             = false,
                                             = true,
                           unsigned nThreads
                                             = 4 );
```

ComputeError

Compute Pearson correlation coefficient, maximum absolute error (MAE) and root mean square error (RMSE) between two vectors.

ComputeError() returns a VectorError struct:

Application Notes

All data input files are assumed to be in csv format. The files are assumed to have a single line header with column names, and it is required that the first column be a vector of times or time indices.

SMap() should be called with DataFrame that have columns explicitly corresponding to dimensions E. This means that if a multivariate data set is used, it should Not be called with an embedding from Embed() since Embed() will add lagged coordinates for each variable. These extra columns will then not correspond to the intended dimensions in the matrix inversion and prediction reconstruction. In this case, use the embedded parameter set to true so that the columns selected correspond to the proper dimension.

Example Application

This application is assumed to be located in the etc/ directory. Otherwise, adust the -I and -L compiler flags and the Simplex path argument accordingly. The file etc/Test.cc shows sample invocations for API functions.

```
// g++ TestApp.cc -o TestApp -std=c++11 -g -I../src -L../lib -lstdc++ -lEDM
#include "Common.h"
//-----
int main( int argc, char *argv[] ) {
   try {
       //----
       // embedded=false : Simplex embeds data file columns to E=3
       //----
       DataFrame<double> dataFrame =
          Simplex( "../data/", "block 3sp.csv",
                  "./", "Block3sp E3.csv",
                  "1 100", "101 195", 3, 1, 0, 1,
                  "x t y t z t", "x t", false, true );
       dataFrame.MaxRowPrint() = 12; // Set number of rows to print
       std::cout << dataFrame;</pre>
       VectorError ve = ComputeError(
          dataFrame.VectorColumnName( "Observations" ),
          dataFrame.VectorColumnName( "Predictions" ) );
       std::cout << "rho " << ve.rho << " RMSE " << ve.RMSE
                << " MAE " << ve.MAE << std::endl << std::endl;
   }
   catch ( const std::exception& e ) {
     std::cout << "Exception caught in main:\n";</pre>
     std::cout << e.what() << std::endl;</pre>
     return -1;
   }
   catch (...) {
     std::cout << "Unknown exception caught in main.\n";</pre>
     return -1;
   }
   std::cout << "Normal termination.\n";</pre>
   return 0;
}
```

Code Notes

- 1) The OSX XCode compiler/linker seems to be incompatible with the C++11 standard implementation allowing template classes to be distributed into declarations (.h) and implementation (.cc). To support OSX, DataFrame.h contains both declarations and implementations. See: etc/libstdc++_Notes.txt.
- 2) The code relies heavily on class and data containers without explicit heap allocation. This facilitates garbage collection. However, using copy-on-return for large data objects is likely a performance issue. If the code encounters massive data objects/large problems, this may warrant investigation.
- 3) Eigen template library. The recommended SVD solver is the BDCSVD that scales to large problems. However, the Eigen documentation states:

This algorithm is unlikely to provide accurate results when compiled with unsafe math optimizations. For instance, this concerns Intel's compiler (ICC), which performs such optimization by default unless you compile with the -fp-model precise option. Likewise, the -ffast-math option of GCC or clang will significantly degrade accuracy.

See: eigen.tuxfamily.org/dox/group TutorialLinearAlgebra

However, when running the SMap circle.csv test, this solver (with default parameters) produces occasional divergence. We have therefore defaulted to the JacobiSVD solver.

4) Eigen template library. Eigen allows replacement of it's internal template library routines with direct calls to BLAS/LAPACK libraries. See: https://eigen.tuxfamily.org/dox/TopicUsingBlasLapack.html This may offer performance and stability advantages.

References

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