



Marcus Kessel marcus.kessel@uni-mannheim.de, Colin Atkinson colin.atkinson@uni-mannheim.de

Agenda

- **Program Analysis**
 - Static vs Dynamic
- Test-Driven Software Experimentation Software testing is an empirical, continuous activity
- Stimulus Response Matrices (SRMs)
- **Differential Testing**
 - Test oracles
 - Regression testing
 - (Program-based) Mutation testing
 - N-version testing
- Stimulus Response Hypercubes (SRHs)
- Measuring Code Coverage

Static vs Dynamic Program Analysis

Static Analysis

- Analyzes code <u>without</u> execution
 - reasons over abstract code representations (e.g., AST, PDGs)
- No run-time activity required
- Analyzes all possible paths (if reachable)
 - → typically more complete and overapproximates
- Used for code understanding, static code analyzers (e.g., linting, code metrics ...), symbolic execution, model checking etc.

Dynamic Analysis (Software Testing)

- Analyzes code behaviour <u>at run-time</u>
 - executes the code on a set of inputs, observing behaviour, performance etc.
- Requires run-time activity
- Only observes actual paths taken
 - → typically more precise and underestimates
- Testing activities (unit, integration, system etc.)

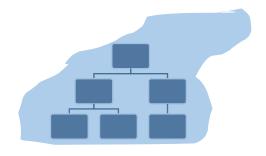
BUT: Rice's theorem states that for any non-trivial property P of the set of partial functions (or programs), it is undecidable to determine whether a given program satisfies this property (cf. halting problem)

→ Approaches complement each other, a combination of both is often used in practice

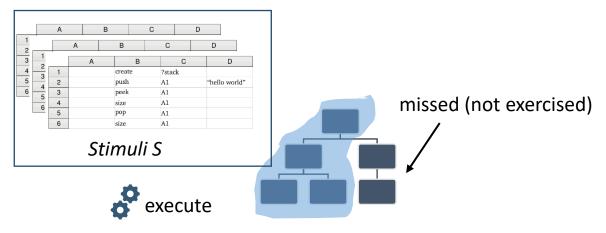


Static vs Dynamic Program Analysis – Example

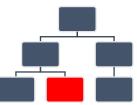




Static Call Graph
 (all reachable paths)→ no information about run-time data



Dynamic Call Graph (paths exercised by a set of tests) → monitors run-time behavior



Note: sometimes some subpaths are not reachable (e.g., dead code)

Software Testing – An Empirical Activity

- Uncertainty and unpredictability software is inherently complex and dynamic (i.e., hard to predict all possible outcomes and scenarios)
 - uncertainty requires empirical investigation through experimentation (i.e., software testing)
- Exploratory nature testing is a process of exploration
 - we attempt to uncover previously unknown issues or defects (cf. Dijkstra)

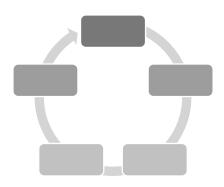
"Program testing can be used to show the presence of bugs, but never to show their absence!"

- Data-driven decision-making testing generates vast amounts of data (e.g., test results, traces, metrics etc.) to make informed decisions about the system's behaviour and quality
 - testers heavily rely on this data to inform their strategies and decisions
- Experimentation and iteration testing involves repeated experimentation with different (or equal) inputs, scenarios or configurations to gather evidence about the software's behaviour
 - iterative process allows testers to refine their understanding of the system and identify potential issues
- Human involvement human-centric activity that requires expertise, experience and creativity
 - next to coverage criteria, testers use their empirical knowledge and understanding of software development, programming languages, and testing techniques to design and execute tests

Software Testing – Continuous Activity

- Software testing is an empirical, continuous activity ...
 - Based on observation and experimentation
 - Focused on gathering evidence and data
 - Able to adapt to changing requirements or new information
 - Influenced by human judgment and experience
- This perspective emphasizes the importance of continuous learning, iteration, and improvement in software testing
 - aided by automated testing (cf. agile coding practices)
 - unit testing frameworks, continuous integration





Test-Driven Software Experimentation

- A Test-Driven Software Experiment (TDSE) involves the execution of software subjects and the observation and analysis of their "de facto" run-time behaviour (i.e., run-time semantics)
 - "Test-Driven Software Experiments (TDSEs) are experiments that involve <u>controlled</u> testing of software subjects (i.e., code modules) under various conditions, revealing important properties of the code's run-time behavior that cannot be predicted solely through static analysis"
 - Controlled testing: Repeatable observations for (deterministic) software in a controlled environment
 - different environments may cause different observations
- Practitioners
 - Evaluate code and tools, making informed decisions for adoption and integration (e.g., code recommendation)
- Researchers
 - Empirically validate tools and techniques involving the execution of software subjects (e.g., benchmarking tools like test generators)
- Educators

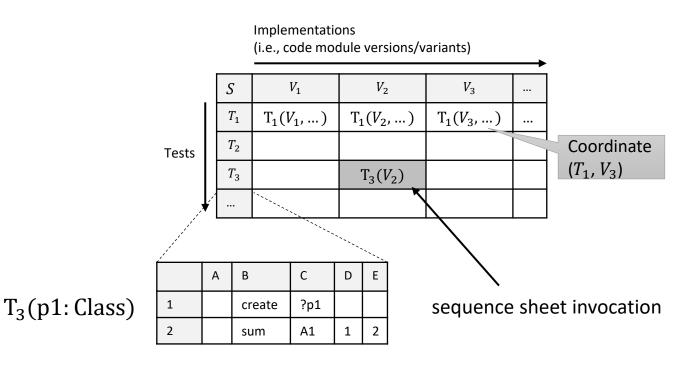
Supporting data structures needed

Teaching activities (e.g., test-driven exercises)



Stimulus Matrices (SMs) – Input

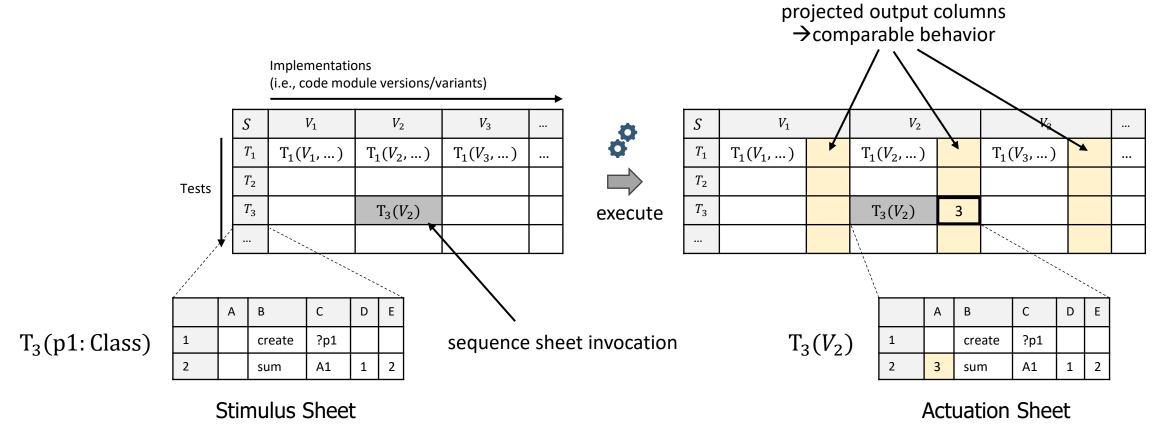
- Typically for one functional abstraction S
 - i.e., functionality under consideration
 - given by its interface
 - desired behaviour in terms of set of input/output mappings (e.g., sequence sheets)
- Configuration of test/code implementations pairs for execution
 - Columns: One or more Implementations V_i
 - Rows: One or more Tests T_j (sequence sheets)
 - Typically sequence sheets (Normal, parameterized)



Stimulus Response Matrices (SRMs) – Output

Stimulus Response Matrices store run-time responses

Note: Assume that we ignore the first row

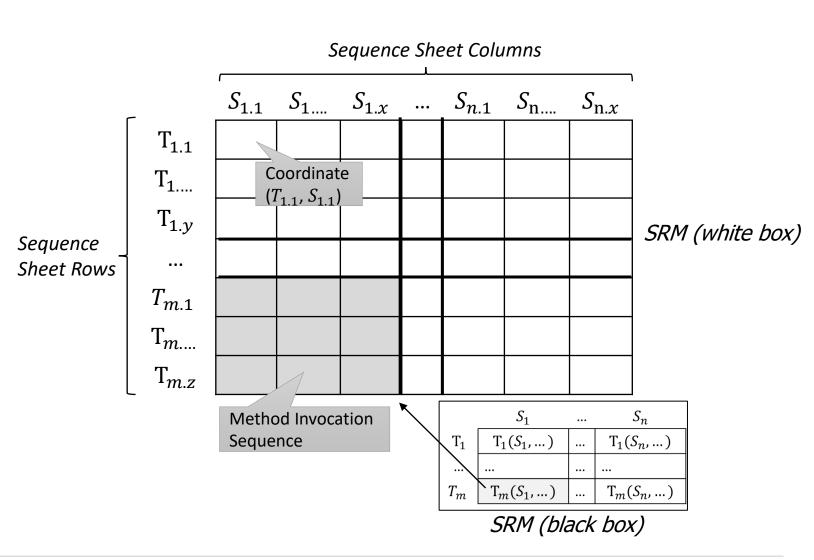


Stimulus Matrix

Stimulus Response Matrix

Stimulus Response Matrices (SRMs) – Records

- In general, SRMs store all cells of sequence sheets using two views
 - black box: sequence sheet body hidden
 - white box: sequence sheet body visible
 - can navigate SRM and select sequence sheet rows/columns/cells of interest
- In addition to functional records (output column), SRMs can also store non-functional information



SRM Example – Greatest Common Divisor

<u>Problem:</u> GCD (Greatest Common Divisor)

Interface: gcd(int, int)->int

output operation

test(p1:Class, p2:int, p3:int)

	Α	В	С	D	E
1		create	?p1		
2		gcd	A1	?p2	?p3
				1	

inputs

Tests

test_m

V1

 $test_m(V1, x, y)$

N versions (code module implementations)

	V1	V2	V3	 V _n
test1	test(V1,03,07)	test(V2, 03,07)	test(V3, 03,07)	test(V _n , 03,07)
test2	test(V1,10,15)	test(V2,10,15)	test(V3,10,15)	test(V _{rv} 10,15)
test3	test(V1,49,14)	test(V2,49,14)	test(V3,49,14)	test(V _{rv} 49,14)
test _m	test _m (V1, x, y)	$test_m(V2, x, y)$	test _m (V3, x, y)	$test_m(V_n, x, y)$



V3



 V_n

 $test_m(V_n, x, y)$

	Α	В	С	D	Е
1		create	V1		
2	1	gcd	A1	3	7

test1 test(V1,03,07) test(V2,03,07) test(V3,03,07) -7 $test(V_n, 03, 07)$ test2 test(V1,10,15) test(V2,10,15) test(V3,10,15) -15 test(V_n, 10, 15) test3 test(V1,49,14) test(V2,49,14) test(V3,49,14) $test(V_n, 49, 14)$ 28

V2

 $test_m(V2, x, y)$

Note: Assume that we ignore the first row

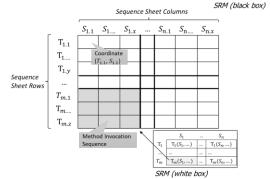
comparison of observed outputs

 $test_m(V3, x, y)$

Queue Example – Complex Sequences

- Assume the functional abstraction of a queue data abstraction
 - SRMs store a de-collapsed view on rows of sheets (e.g., output column)

De-collapsed sheet rows



	Output O	peration	Inputs (incl. s	service)
	Α	В	С	D
	A	Ь		
1	<instance></instance>	create	`MyQueue	
2	TRUE	enqueue	A1	1
3	TRUE	enqueue	A1	2
4	1	peek	A1	
5	2	size	A1	
6	1	dequeue	A1	
7	1	size	A1	

Actuation Sheet

test1(MyQueue)

		MyQueue		 V _n	
	test1	test1(MyQueue)	<instance></instance>		
•	2		TRUE		
	3		TRUE		
	4		1		
	5		2		
	6		1		
	7		1		
	test2	test2(MyQueue)			

Stimulus Response Matrix

Differential Testing & SRMs

- In general, Differential testing is a software testing technique that involves comparing the behaviour of two or more versions of a program, typically to detect differences in their functionality
- In practice, many testing activities can be related to differential testing
 - Test oracles compare expected behaviour to actual behaviour of unit under test
 - Specified oracles (input/output mappings, pre-/post conditions, specification lang. ...)
 - Cross-checking oracles using different implementations of the same functionality
 - Regression testing compare old version of code unit with new version (i.e., verify that code modifications do not change run-time semantics)
 - Mutation testing compare original version of code unit to mutated versions
 - N-version testing compare behaviour of two or more versions of a program and settle (agree) on common behaviour (e.g., critical, dependable software)
- SRMs support and facilitate differential testing

Test Oracles – Specified Oracle

- A test oracle uses expected outputs ("ground truth") to decide whether a test passed or failed
 - represented as a virtual implementation version in SRMs
 - taken from output column of sheets

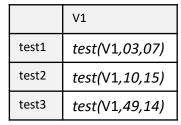
	Α	В	С	D	E
1		create	V1		
2	1	gcd	A1	3	7

	А	В	С	D	E
1		create	V1		
2	5	gcd	A1	10	15

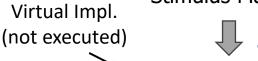
	А	В	С	D	E
1		create	V1		
2	7	gcd	A1	49	14

Stimulus Sheets

Expected outputs



Stimulus Matrix



	_				
	Oracle		V1		
test1	test(V1,03,07)	1	test(V1,03,07)	1	
test2	test(V1,10,15)	5	test(V1,10,15)	5	
test3	test(V1,49,14)	7	test(V1,49,14)	11	

Stimulus Response Matrix

Actual (observed) outputs

		L				
	Α		В	С	D	E
1			create	V1		
2	1		gcd	A1	3	7

	Α	В	С	D	E
1		create	V1		
2	5	gcd	A1	10	15

	А	В	С	D	E
1		create	V1		
2	11	gcd	A1	49	14

Actuation Sheets

Compare expected outputs with actual, observed outputs

Test Oracles – Cross-Checking Oracle

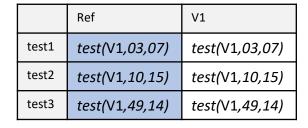
- Reference system Ref serves as cross-checking oracle in SRM
 - available reference implementation (e.g., different sort algorithms should return the same outputs for inputs)

	А	В	С	D	E
1		create	V1		
2		gcd	A1	3	7

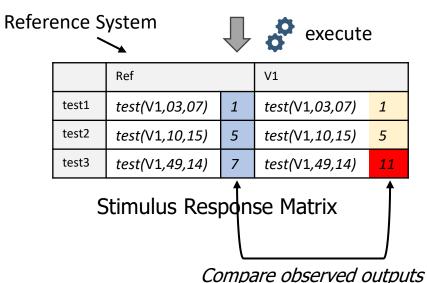
	Α	В	С	D	E
1		create	V1		
2		gcd	A1	10	15

	Α	В	С	D	E	
1		create	V1			
2		gcd	A1	49	14	

Stimulus Sheets



Stimulus Matrix



	Α	В	С	D	E
1		create	V1		
2	1	gcd	A1	3	7

	Α	В	С	D	Е	
1		create	V1			
2	5	gcd	A1	10	15	

	А	В	С	D	E	
1		create	V1			
2	11	gcd	A1	49	14	

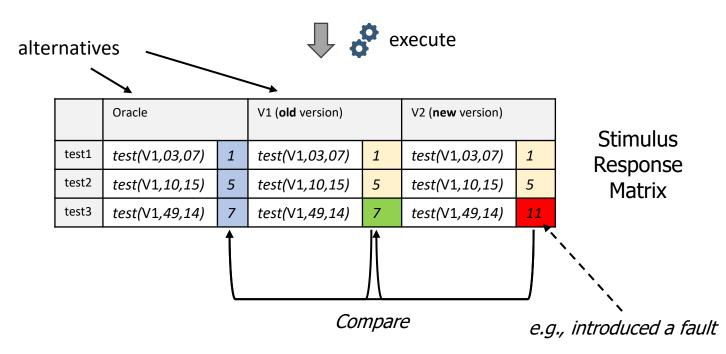
Actuation Sheets

Regression Testing

- Regression testing verifies that the software still behaves as expected (i.e., functions correctly) after updates
 - added features
 - fixed faults
 - refactoring, etc.
- Typical realizations
 - re-run existing tests on new version
 - old version may become your (cross-checking) oracle

	V1 (old version)	V2 (new version)
test1	test(V1,03,07)	test(V1,03,07)
test2	test(V1,10,15)	test(V1,10,15)
test3	test(V1,49,14)	test(V1,49,14)

Stimulus Matrix



Mutation Testing – Program-based Grammars

- Recall syntax-based testing of grammars
- The original and most widely known application of syntax-based testing is to modify programs
- Operators modify a ground string (program under test) to create mutant programs
 - Mimic typical programmer mistakes (e.g., incorrect variable name)
 - Encourage common test heuristics (e.g., cause expressions to be 0)
- Mutant programs must compile correctly (valid strings)
- Mutants are not tests, but used **to find tests** \rightarrow assessing test set quality
 - Fundamental Premise: In practice, if the software contains a fault, there will usually be a set of mutants that can be killed only by a test case that also detects that fault
- Once mutants are defined, tests must be found to cause mutants to fail when executed
- This is called "killing mutants"

Mutation Testing – Operators Example

- ABS Absolute Value Insertion
- 2. AOR Arithmetic Operator Replacement
- 3. ROR Relational Operator Replacement
- 4. COR Conditional Operator Replacement
- 5. SOR Shift Operator Replacement
- 6. LOR Logical Operator Replacement
- 7. ASR Assignment Operator Replacement
- 8. UOI Unary Operator Insertion
- 9. UOD Unary Operator Deletion
- 10. SVR Scalar Variable Replacement
- 11. BSR Bomb Statement Replacement

```
2. AOR — Arithmetic Operator Replacement.
```

Each occurrence of one of the arithmetic operators +, -, *, /, and % is replaced by each of the other operators.

```
Examples:

a = m * (o + p);

\Delta 1 = m + (o + p);

\Delta 2 = m * (o * p);

\Delta 3 = m / (o + p);
```

Remember: Mutated strings (here code) should be close to the original ...

→ Researchers select appropriate operators through empirical assessments

Mutation Testing – Killing Mutants

Given a mutant $m \in M$ for a ground string program Pand a test t, t is said to kill m if and only if the output of t on P is different from the output of t on m.

- If mutation operators are designed well, the resulting tests will be very powerful
- Different operators must be defined for different programming languages and different goals
- Testers can keep adding tests until all mutants have been killed
 - Dead mutant: A test has killed it
 - Stillborn mutant: Syntactically illegal
 - Trivial mutant: Almost every test can kill it
 - Equivalent mutant: No test can kill it (same behavior as original)

Mutation Testing – Test Requirements

Mutation Coverage (MC): For each $m \in M$, TR contains exactly one requirement, to kill *m*.

- Recall the conditions from lecture L2 for a software failure to be observed -
 - Reachability: The test causes the faulty statement to be reached (in mutation the mutated statement)
 - Infection: The test causes the faulty statement to result in an incorrect state
 - Propagation: The incorrect state propagates to incorrect output
 - + Revealability (observability): The tester must observe part of the incorrect output
 - → Together, these are also know as the RIPR model
- This leads to two variants of mutation coverage ...

Mutation Testing – Strong vs Weak Mutation Coverage

Strongly killing mutants – satisfies all conditions (assumed in the remainder ...)

Given a mutant $m \in M$ for a program P and a test t, t is said to strongly kill m if and only if the output of t on P is different from the output of t on m

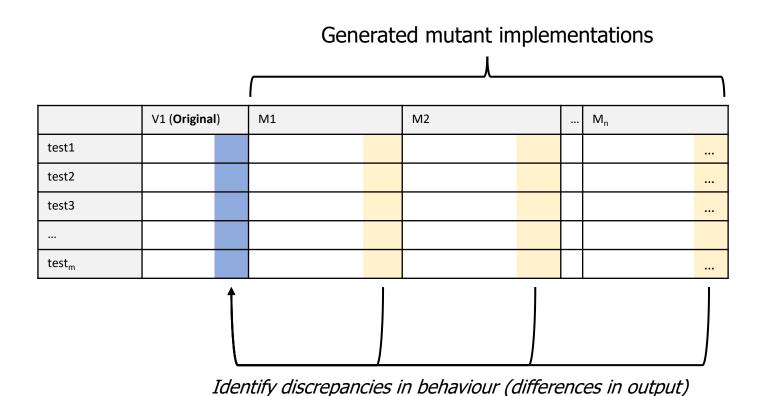
Weakly killing mutants

Given a mutant $m \in M$ that modifies a location / in a program P, and a test t, t is said to weakly kill m if and only if the state of the execution of P on t is different from the state of the execution of m on t immediately after I

Weakly killing satisfies reachability and infection, but <u>not</u> propagation

Mutation Testing – SRMs

Basic SRM setting for strong mutation testing



Mutation Testing – Min Example

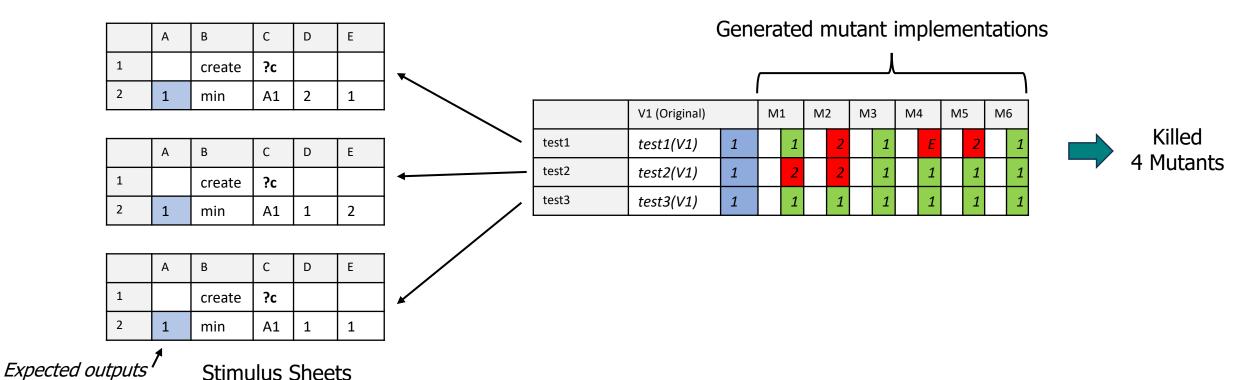
Original Method int min (int A, int B) int minVal; minVal = A;if (B < A)minVal = B;return (minVal); } // end Min

6 mutants
Each represents a separate program

```
With Embedded Mutants
int min (int A, int B)
                           Replace one variable
                           with another
     int minVal;
     minVal ≠∕A;
                            Replaces operator
\Delta 1 minVal = B;
     if (B < A)
                              Immediate runtime
\triangle 2 if (B > A)
                              failure ... if reached
\triangle 3 if (B < minVal)
                              Immediate runtime
          minVal ≠ 🛱;
                              failure if B==0, else
          Bomb ();
\Delta 4
                              does nothing
          minVal = A;
\Delta 5
\Delta 6
          minVal = failOnZero (B);
     return (minVal);
} // end Min
```

Mutation Testing – SRM Min Example

- Setting for Min Example
- Assume there are 3 tests, and 6 mutants (see slide before)
 - a mutant is killed if there is at least one test with at least one disagreement in the expected outputs



Mutation Testing – Equivalent Mutants

Mutant 3 (M3) in the *min()* example is behaviourally equivalent to the original implementation:

- The infection condition is "(B < A) != (B < minVal)"
- However, the previous statement was "minVal = A''
- Substituting, we get: "(B < A) != (B < A)"
 - This is a logical contradiction!

Thus no input can kill this mutant

Mutation Score & SRMs – Example

- We can work out the mutation score directly from SRMs
- Mutation Score
 - Number mutants generated for killing (= 6)
 - i.e., set of test requirements
 - Number of killed mutants (= 4)
 - Score: $4/6 \rightarrow \sim 66\%$
- Important: that we can't reach 100% because of equivalent mutant M3
- Generally, only disagreements to explicit expected values are considered (i.e., marked in blue) – if missing, no comparison is made
 - similar to unit testing assumptions (i.e., missing assertion checks)

	V1 (Original)		V1 (Original) M1 M		M	2	M3		M4		M5		M6	
test1	test1(V1)	1	1		2		1		Ε		2		1	
test2	test2(V1)	1	2		2		1		1		1		1	
test3	test3(V1)	1	1		1		1		1		1		1	

one output discrepancy in test2 (column)

→ M1 killed

two output discrepancies in test1, test2 (column)

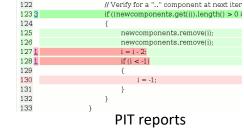
→ M2 killed



Mutation Testing – Final Words

- Mutation is widely considered the strongest test criterion ("gold standard")
 - And most expensive! (run-time requirements in larger code bases ...)
 - By far the most test requirements (each mutant)
 - Usually the most tests
- Mutation subsumes other criteria by including specific mutation operators
- Tool examples

 - Java: PIT https://pitest.org/, Python: mutpy, mutmut ...



(green line coverage, red mutation coverage)

- Provide reports (may report other criteria as well) etc. \rightarrow lookup their suggested default set of mutation operators
- Can be integrated into automated testing workflows (i.e., continuous integration)
 - Typically compatible to existing unit testing frameworks/drivers

N-version Testing

- compare behaviour of two or more versions of a program and settle (agree) on common behaviour (i.e., responses in terms of outputs)
 - Traditional hypothesis: multiple versions have been developed by independent developers for the same behavior specification
 - assumes that different developers make different mistakes
- Proposed for critical, dependable software (e.g., avionics)
 - correct behavior is identified by majority vote at run-time (for instance)
 - other voting mechanisms possible
- can also be used for practical assessment of multiple implementation candidates where one final candidate is to be selected
 - i.e., fit-for-purpose evaluations in code recommenders
 - however, may require adaptation of the code candidates interfaces

SRM

	V1	V2	V3	V4	V5
test1	1	7	-7	1	1
test2	5	15	-15	5	5
test3	7	14	28	7	7
test4	12	60	60	12	12
tgen1	1	1	1	2158	2158
tgen2	1	1	1	503	503
tgen3	-15	1	-15	-15	-15
					,

cluster size = 2Oracle

1 =3	Test-based Voting
7 = 1 -7 = 1	1
1 / 1 -	5
	7
	12
	1
	503
	-15

Cluster-based Voting					
1					
5					
7					
12					
2158					
503					
-15					

Software Code Evolution – Continuous Integration

 Test-driven development methods work best when the current version of the software can be run against all tests at any time

A *continuous integration server* rebuilds the system, returns, and reverifies tests whenever *any* update is checked into the repository

- Mistakes are caught earlier
- Other developers are aware of changes early
- The rebuild and reverify must happen as soon as possible
- Thus, tests need to execute quickly

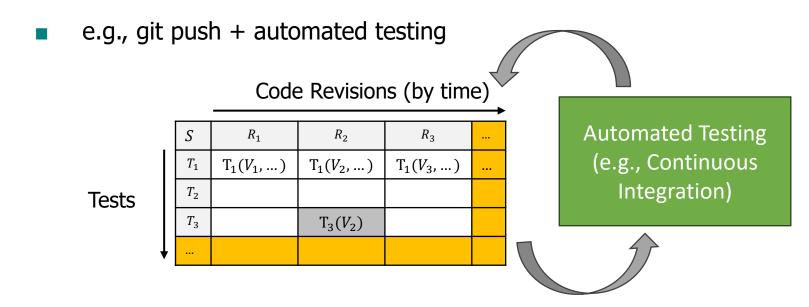


e.g., Jenkins weather report

A *continuous integration server* doesn't just run tests, it decides if a modified system is still correct

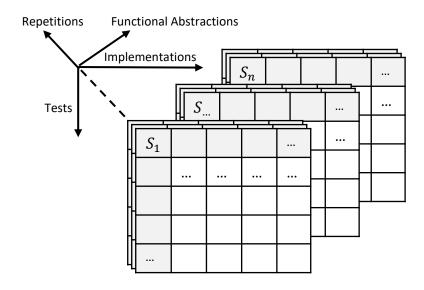
Software Code Evolution – Continuous Lifecycle

- Over time, as the production code evolves, the set of tests for the code implementation evolves as well
 - tests may be added (e.g., "bug-fixing" tests), updated or removed to maintain/improve reliability
- if changes are made to the implementation
 - code revisions (new versions) are added from time to time and are automatically verified for correctness



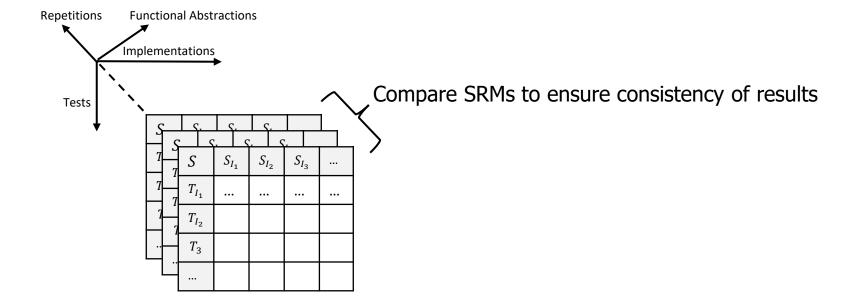
Stimulus Response Hypercubes – SRHs

- Aggregate multiple SRMs into a cube structure (cf. data warehousing applications)
- Navigate across multiple dimensions to inform decision-making and test reporting
 - Functional abstractions S_i
 - Tests
 - Implementations
 - Repetitions
 - ...
- Enables software analytics
 - Reason over data (e.g., metrics etc.)



Repeatability – Checking for Test Flakiness

- Test flakiness refers to the phenomenon where automated tests occasionally fail or behave unexpectedly, even when there
 are no actual issues with the code being tested
 - Random failures
 - Inconsistent behaviour
 - False positives/negatives
- Causes, for instance
 - Source of randomness
 - Concurrency issues
 - External services (e.g., DBs)
- Consequences, for instance
 - Maintenance costs
 - Confidence erodes
 - May mask actual issues with the code



Advanced Topics – An Example

- Test set minimization of a test set T
 - Problem: Imagine you code base as well as the test sets evolve over time → Scalability?
 - Goal: Identify a minimal set of tests to improve efficiency, thus minimize run-time costs (time, money etc.) also see test set prioritization (only running those tests affected by a change)
 - Idea: if a pair of tests satisfy the same test requirement, we can drop either of these, while still satisfy the same test requirements
 - E.g., identifying redundant tests based on the killing of the same mutants for a pair of tests→ drop one redundant test
 - Similar to mutation matrices

	V1 (Original)		M1		M2		M3		M4	
test1		1		1		1		7		1
test2		5		0		5		5		5
test3		7		7		7		1		7



assume that test1 and test2 kill the same mutant M3 \rightarrow drop test1 or test3

Measuring Code Coverage in Practice

- a way to quantify how much of a program's code is exercised during automated tests at run-time
 - provides insight into the thoroughness of the test suite by measuring the percentage of code that has been exercised
 - can be used to identify non-exercised code elements
- Typical types of code coverage
 - Line coverage (or statement coverage)
 - Branch coverage
 - Method/function or class coverage
- Typical metrics reported (note: should be carefully interpreted!)
 - Percentage of code covered/missed etc.
- Tool examples
 - Java: JaCoCo, (Open) Clover, ...
 - Python: Coverage.py, ...



Element	Missed Instructions	Cov.	Missed Branches	Cov.	Missed	Cxty 🗢	Missed	Lines	Missed	Methods =	Missed	Classes *
org.jacoco.core		97%		91%	143	1,537	125	3,631	19	746	2	147
@org.jacoco.examples	<u> </u>	58%	1	64%	24	53	97	193	19	38	6	12
@org.jacoco.agent.rt		75%		83%	32	130	75	344	21	80	7	22
@jacoco-maven-plugii	1 =	90%	=	82%	35	193	49	465	8	116	1	23
@org.jacoco.cli		97%	1	100%	4	109	10	275	4	74	0	20
@org.jacoco.report		99%		99%	4	572	2	1,345	1	371	0	64
@org.jacoco.ant	=	98%		99%	4	162	8	428	3	110	0	19
@org.jacoco.agent		86%		75%	2	10	3	27	0	6	0	1
Total	1,438 of 28,925	95%	183 of 2,386	92%	248	2,766	369	6,708	75	1,541	16	308

Conclusion

- Software testing is an empirical activity in general → Test-Driven Software Experimentation
 - Testing is done in a continuous manner (tests co-evolve with the units under test)
- Differential testing with SRMs
 - Test oracles (specified and cross-checking oracles)
 - Regression testing
 - Mutation testing / score
 - N-version testing
- SRHs for continuous testing
 - Repeatability and test flakiness
- Advanced topics e.g., test set minimization
- Measuring Code Coverage

Literature

- Software Testing
 - Ammann, Paul, and Jeff Offutt. *Introduction to software testing*. Cambridge University Press, 2017.
 - Barr, Earl T., et al. "The oracle problem in software testing: A survey." *IEEE transactions on software engineering* 41.5 (2014): 507-525.
 - Chen, Liming, and Algirdas Avizienis. "N-version programming: A fault-tolerance approach to reliability of software operation." Proc. 8th IEEE Int. Symp. on Fault-Tolerant Computing (FTCS-8). Vol. 1. 1978.
- **Data Structures**
 - **Publications**
 - Marcus Kessel, Colin Atkinson, Promoting open science in test-driven software experiments, Journal of Systems and Software, Volume 212, 2024, 111971, ISSN 0164-1212, https://doi.org/10.1016/j.jss.2024.111971
 - Marcus Kessel, LASSO an observatorium for the dynamic selection, analysis and comparison of software, Dissertation, 2023 - https://madoc.bib.uni-mannheim.de/64107/
 - LASSO Platform
 - https://softwareobservatorium.github.io/