

# L9 - Recursion II

Thursday, April 2, 2020 10:43 PM

## Recursion

### Recursive Formulation/Recursive Decomposition

To conceive/decompose a problem in terms of simpler problem (**of the same nature as that of the original problem**) and some trivial activities.

In other words, in the solution to the problem, the same problem re-occurs, many times, on a smaller size (simpler problem(s)) until the result is achieved.

## Single Basis

## Factorial

$$Fact(n) = \begin{cases} 1 & ; \\ n * Fact(n - 1) & ; \end{cases} \quad \begin{array}{ll} \text{if } n = 1 & \text{Basis step} \\ \text{if } n > 1 & \text{Recursive step} \end{array}$$

## Sum of n numbers

$$Sum(n) = \begin{cases} 0 & ; \\ Sum(n - 1) + \text{last element} & ; \end{cases} \quad \begin{array}{ll} \text{if } n = 0; & \text{Basis step} \\ \text{if } n > 0; & \text{Recursive step} \end{array}$$

## Print a list of Elements

Display the list of elements/numbers in reverse order

$$print(n) = \begin{cases} \text{display } n^{th} \text{ (first) element;} & \\ \text{display } n^{th} \text{ (last) element and then print}(n - 1); & \end{cases} \quad \begin{array}{ll} \text{if } n = 1; & \text{Basis Step} \\ \text{if } n > 1; & \text{Recursive Step} \end{array}$$

## Print a list of Elements

Display the list of elements/numbers in reverse order

$$print(n) = \begin{cases} \text{do nothing (finish);} & \text{if } n = 0 \\ \text{display } n^{\text{th}} \text{ (last) element and then print}(n-1); & \text{if } n > 0 \end{cases};$$

Print(Arr, n)

1. If  $n == 1$
2. display Arr[n]
3. return
4. else if  $n > 1$
5. display Arr[n]
6. Print(Arr, n-1)

Print2(Arr, n)

1. If  $n == 0$
2. return
3. display Arr[n]
4. Print2(Arr, n-1)

Arr: 2 15 7

Print2(Arr,3) -> print2(Arr, 2) -> print2(Arr, 1) -> print2(Arr,0)

<- 7      <- 15      <- 2      <-

### Multiple Basis Steps

### Fibonacci

$$fib(n) = \begin{cases} 0; & \text{if } n = 0 & \text{Basis Step} \\ 1; & \text{if } n = 1 & \text{Basis Step} \\ fib(n-1) + fib(n-2); & \text{if } n > 1 & \text{Recursive Step} \end{cases}$$

Recursive\_Fibonacci(n)

1. If  $n \leq 1$
2. return n
3. return Recursive\_Fibonacci(n-1) + Recursive\_Fibonacci(n-2)

if  $n == 0$

return 0

if  $n == 1$

return 1

Palindrome  $\in$ , *a*, *ab*, *aab*, *aaba*, *aa*, *aba*,

str: *abc*defed*cba*

str[1..11] = str[1..n]

first == last

$$pal(str, first, last) = \begin{cases} true; & \text{if } n \leq 1 \text{ (if } first \geq last) \\ false; & \text{if } n > 1 \text{ and } firstElement \neq lastElement \\ pal(str, first + 1, last - 1); & \text{if } n > 1 \text{ and } firstElement == lastElement \end{cases}$$

pal(str, first, last)

1. if first >= last
2. return true
3. if str[first] != str[last]
4. return false
5. return pal(str, first+1, last-1)

Examples:

str: "aaa"

pal("aaa",1,3) -> pal("aaa",2,2)

<- true <- true

str: "abba"

pal("abba",1,4) -> pal("abba",2,3) -> pal("abba",3,2)

<- true <- true <- true

str: "aaaaabaa"

pal("aaaaabaa",1,8) -> pal("aaaaabaa",2,7) -> pal("aaaaabaa",3,6)

<- false <- false <- false