## 1

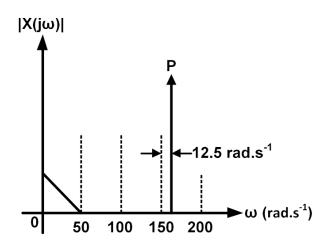
## NCERT Physics 12.10.9 Q

## ee23btech11223 - Soham Prabhakar More

**Question:** x(t) is a real continuous-time signal whose magnitude frequency response  $|X(j\Omega)|$  is shown below. After sampling x(t) at 100  $rad.s^{-1}$ , the spectral point P is down-converted to \_\_\_\_\_  $rad.s^{-1}$  in the spectrum of the sampled signal.

where k is the nearest integer to  $\frac{162.5}{100}$ , which is 2 Thus,

$$\omega = 37.5 \, rad \, s^{-1} \tag{9}$$



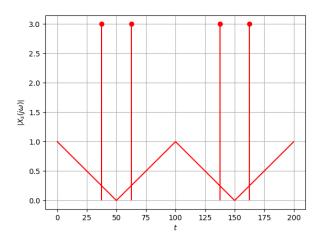


Fig. 2: Plot of  $|X_s(j\omega)|$ 

**Solution:** The sampling function is:

$$w(t) = \sum_{k=-\infty}^{\infty} \delta\left(t - \frac{k}{100}\right) \tag{1}$$

$$W(j\omega) = 100 \sum_{k=-\infty}^{\infty} \delta(j(\omega - 100k))$$
 (2)

then the sampled function:

$$x_s(t) = x(t)w(t) \tag{3}$$

$$X_{s}(j\omega) = X(j\omega) * W(j\omega)$$
 (4)

$$X_{s}(j\omega) = \int_{-\infty}^{\infty} X(j\theta) W(j(\omega - \theta)) d\theta$$
 (5)

$$X_{s}(j\omega) = 100 \sum_{k=-\infty}^{\infty} \int_{-\infty}^{\infty} X(j\theta) \, \delta(j(\omega - 100k - \theta)) \, d\theta$$
(6)

$$X_s(j\omega) = 100 \sum_{k=-\infty}^{\infty} X(j(\omega - 100k))$$
 (7)

Thus, The down sampled point is at:

$$\omega = |162.5 - 100k| \tag{8}$$