

Medical Image Computing

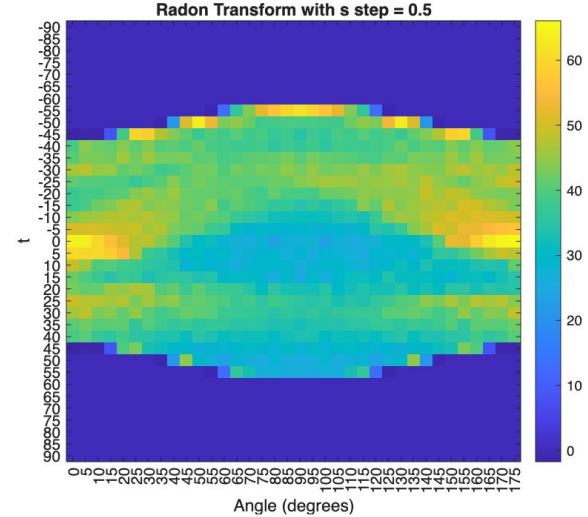
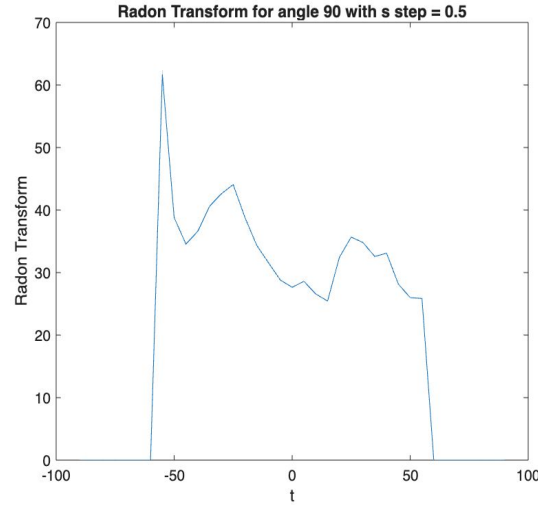
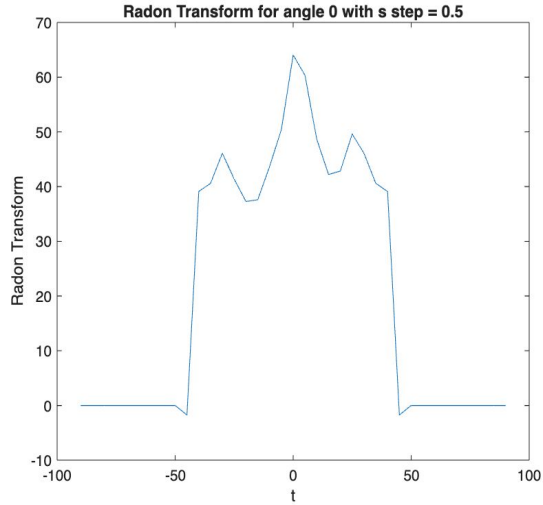
Assignment 2

Shreyas Grampurohit (21D070029)
Soham Nivargi (21D070074)

Q1 - X-Ray Computed Tomography: Radon Transform

Step size = 0.5

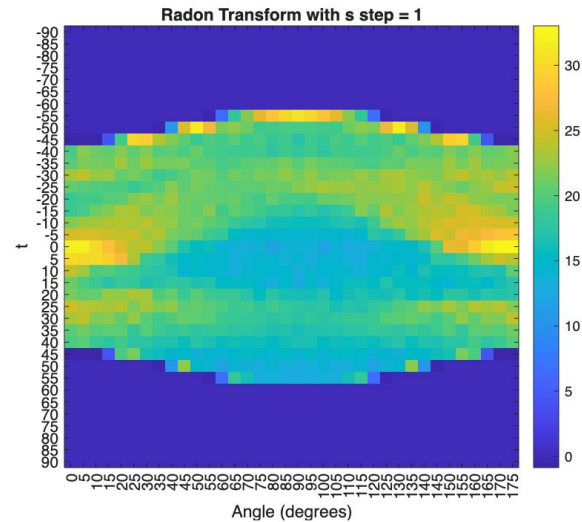
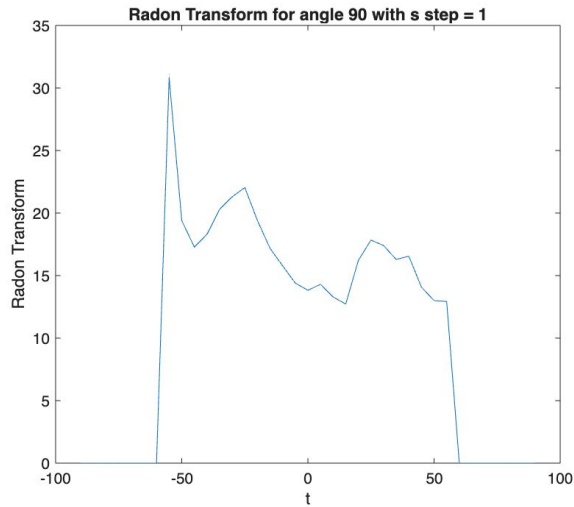
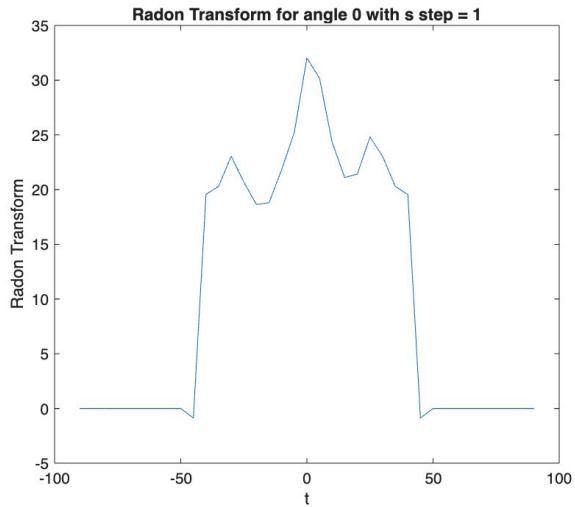
$ds \leq 1$, nyquist
criterion



bicubic interpolation. uses large neighbourhood – so deals better with rough images

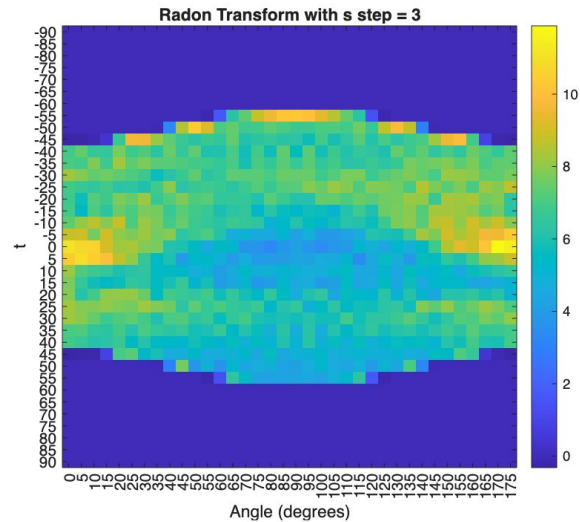
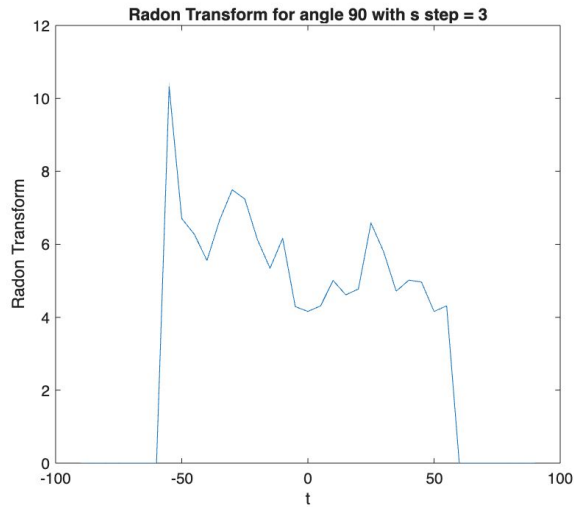
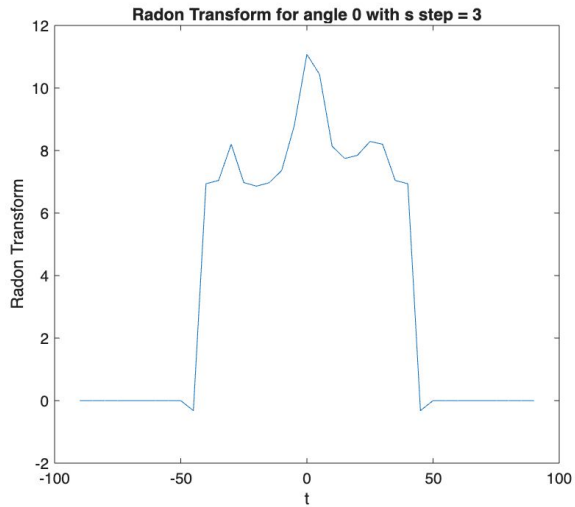
Q1 - X-Ray Computed Tomography: Radon Transform

Step size = 1

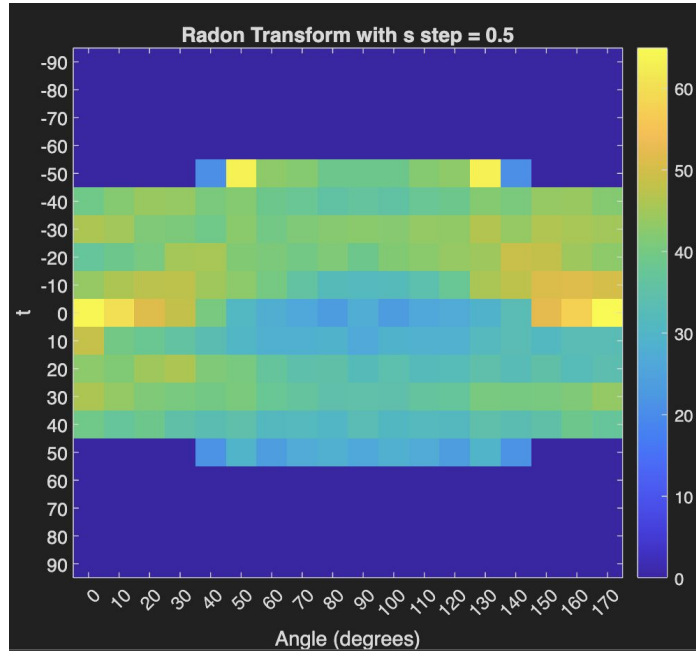


Q1 - X-Ray Computed Tomography: Radon Transform

Step size = 3



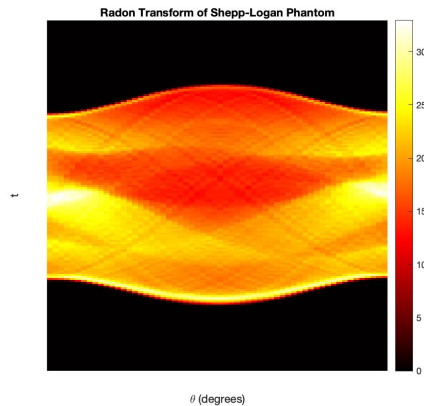
with half the number of angles and ts – lesser radiations,
but information loss



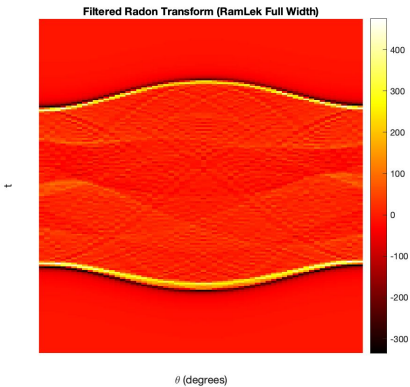
Q2 - X-Ray Computed Tomography: Reconstruction by Filtered Backprojection (FBP)



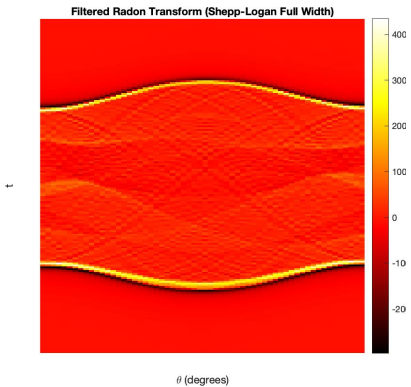
Radon Transform of phantom vs Filtered Radon Transforms for Full-width and Half-width Filters



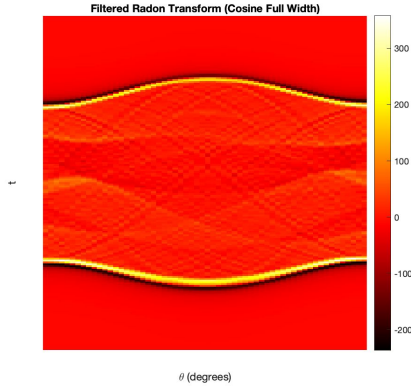
Radon Transform



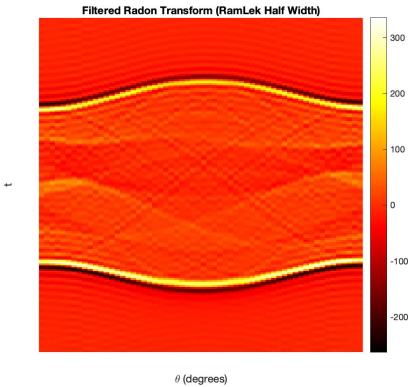
Full-width RamLek FRT



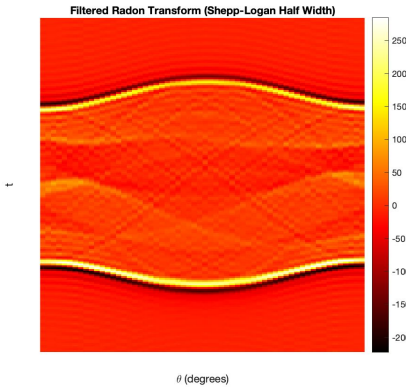
Full-width Shepp-Logan FRT



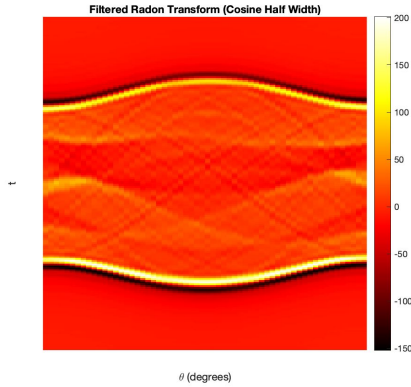
Full-width Cosine FRT



Half-width RamLek FRT



Half-width Shepp-Logan FRT



Half-width Cosine FRT

FBP Analysis

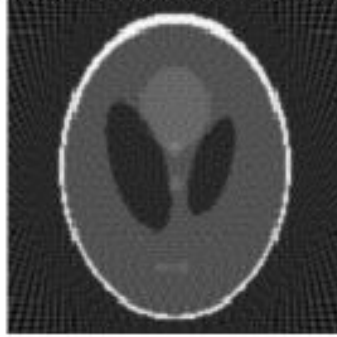
- The RamLak filter -
 - $A(w) = |w| \cdot \text{rect}(L)$; which amplifies higher frequencies, ie., noise and thus creates a noisy reconstruction than the other two filters. For half-width L , the image omits higher frequencies which results in image smoothing but some unavoidable loss of information
- The Shepp-logan filter -
 - $A(w) = |w| \cdot \text{rect}(L) \cdot \text{sinc}(w/2L)$ which lessens the amplification of noise and is thus better than the RamLak filter. Similar to RamLak half-width, the image gets smoothed.
- Cosine Filter
 - $A(w) = |w| \cdot \text{rect}(L) \cdot \cos(\pi w/2L)$ which further lessens amplification of noise and better than both other filters.

Filtered Backprojection(FBP) for Full-width and Half-width Filters vs FBP using Matlab In-built library

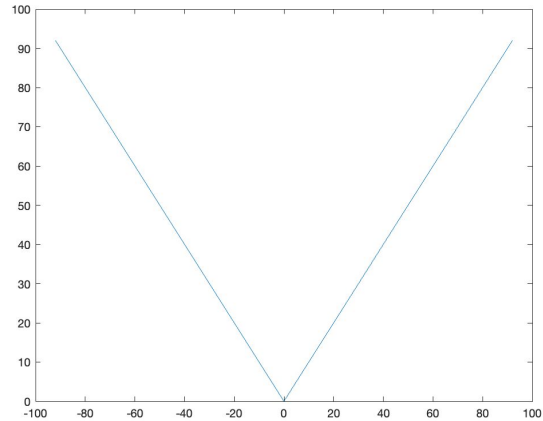
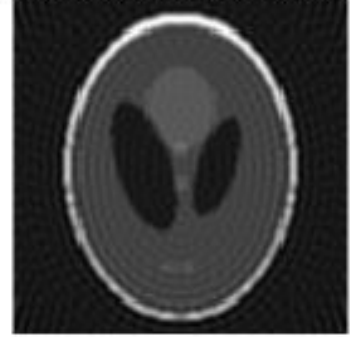
Ram-Lak Reference Reconstruction



Ram-Lak Full Width Reconstruction



Ram-Lak Half Width Reconstruction

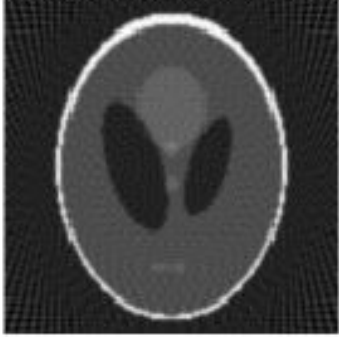


Shepp-Logan Phantom

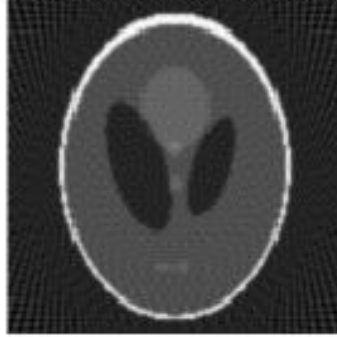


Filtered Backprojection(FBP) for Full-width and Half-width Filters vs FBP using Matlab In-built library

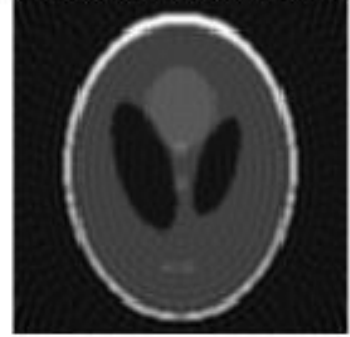
Shepp-Logan Reference Reconstruction



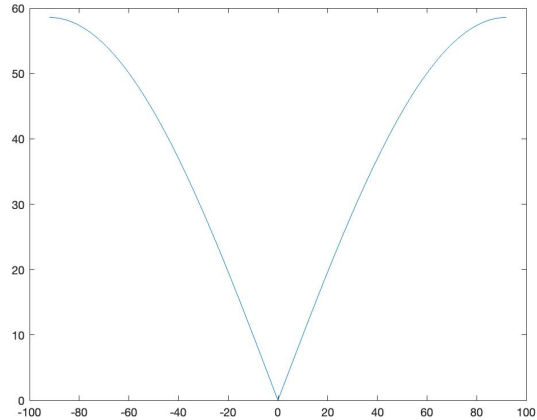
Shepp-Logan Full Width Reconstruction



Shepp-Logan Half Width Reconstruction

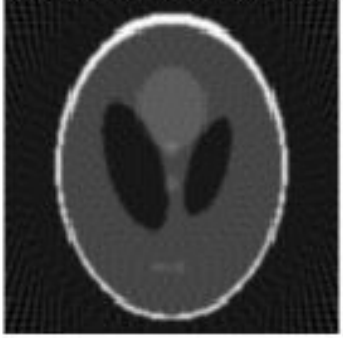


Shepp-Logan Phantom

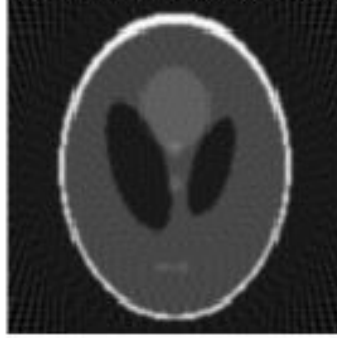


Filtered Backprojection(FBP) for Full-width and Half-width Filters vs FBP using Matlab In-built library

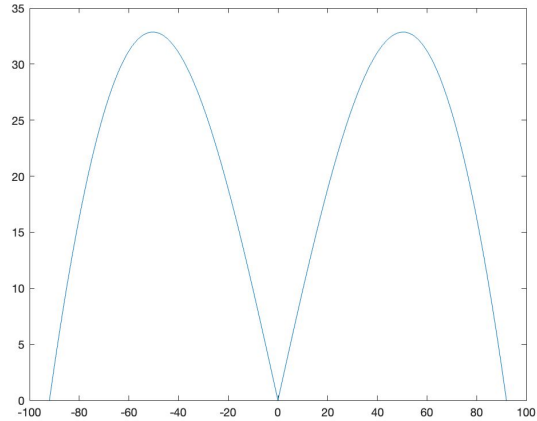
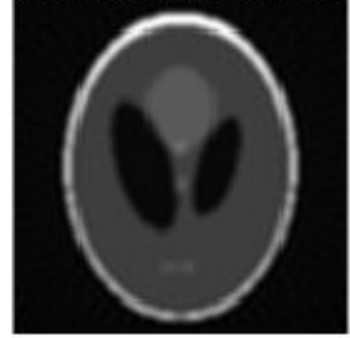
Cosine Reference Reconstruction



Cosine Full Width Reconstruction



Cosine Half Width Reconstruction



Shepp-Logan Phantom

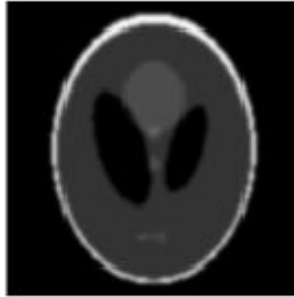


Ram-Lak Filtered Backprojection(FBP) for Blurred Images

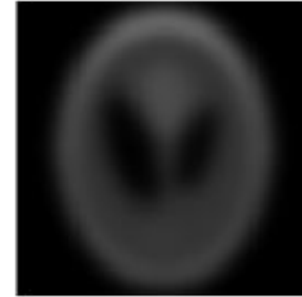
S0



S1



S5

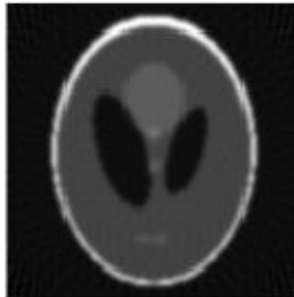


R0



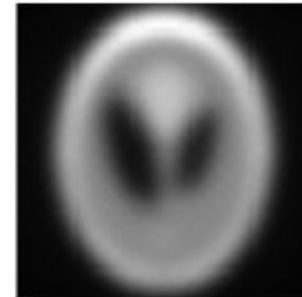
RRMSE = 0.6463

R1



RRMSE = 0.2828

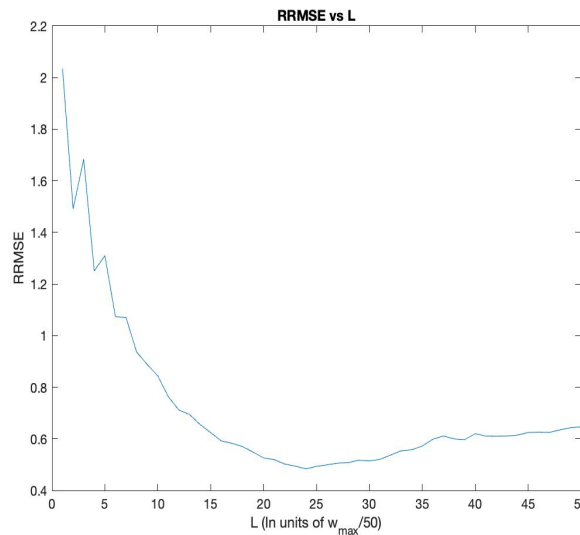
R5



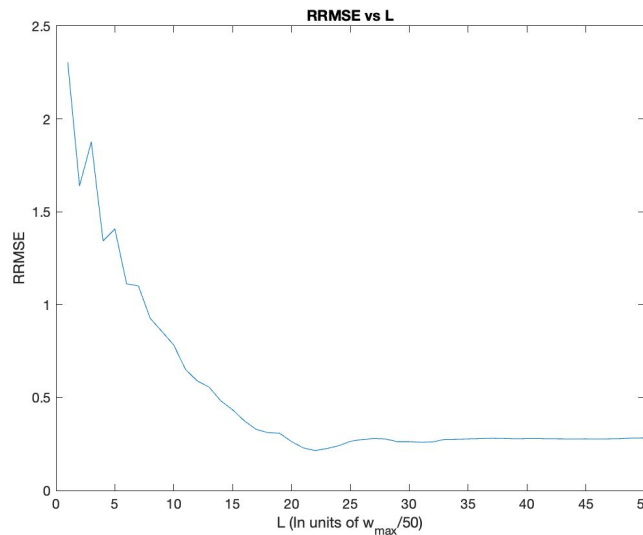
RRMSE = 1.6110

Since, the whole frequency band is considered, the image with gaussian blurring with a standard deviation of 1 already smoothens the input image and thus the reconstruction is closer to it. The image with standard deviation smoothens the image too much causing artifacts in reconstruction.

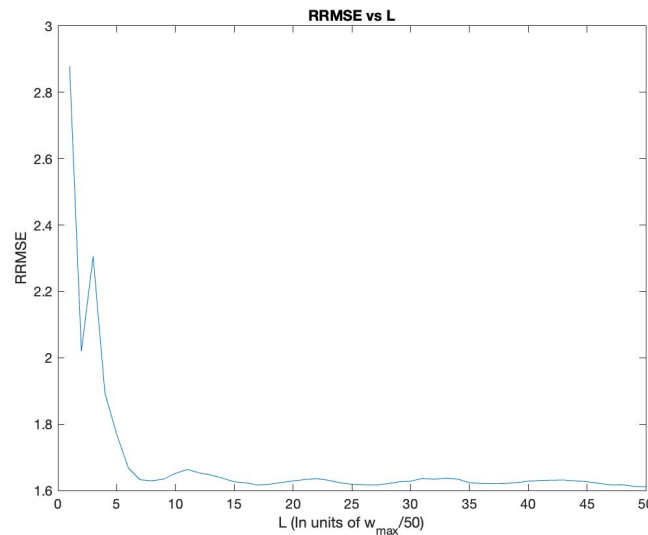
RRMSE for Ram-Lak Filtered Backprojection(FBP) for different Filter Lengths



S0 image



S1 image

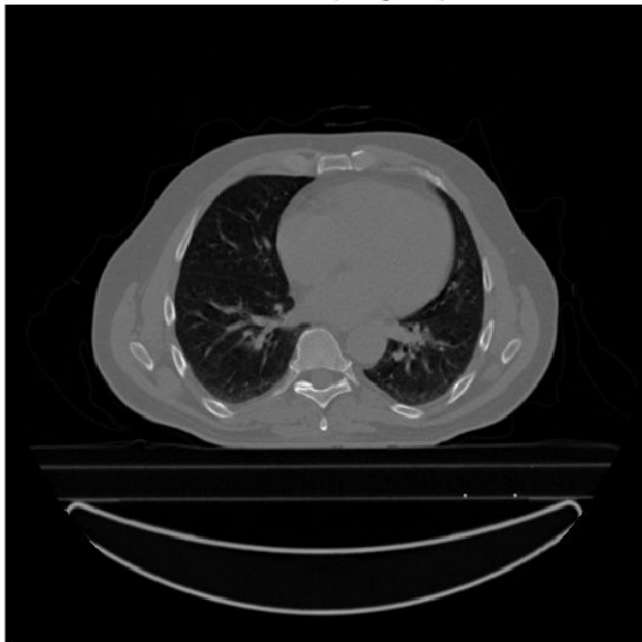


S5 image

The RRMSE reduces as a larger length filter is taken, it reaches a minimum almost around half width of maximum frequencies and almost remains constant later.

Q3 - X-Ray Computed Tomography: Incomplete Data

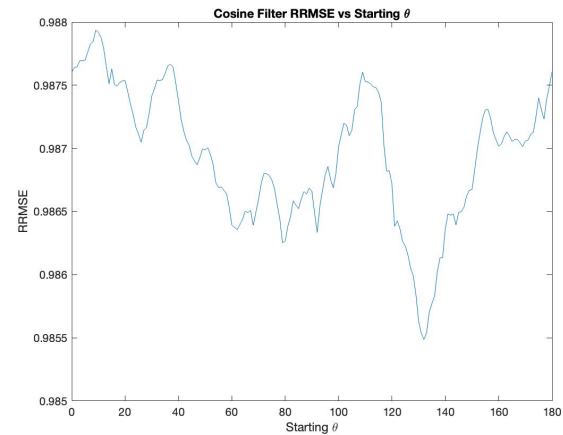
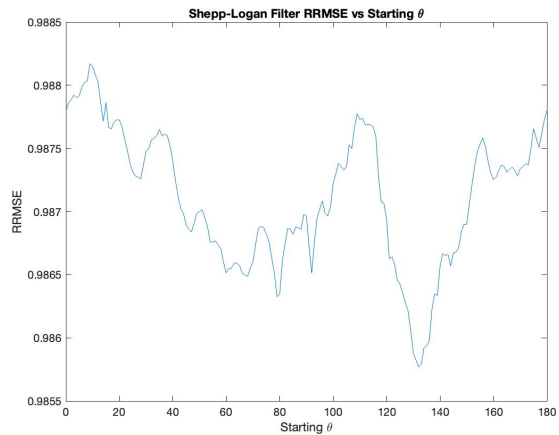
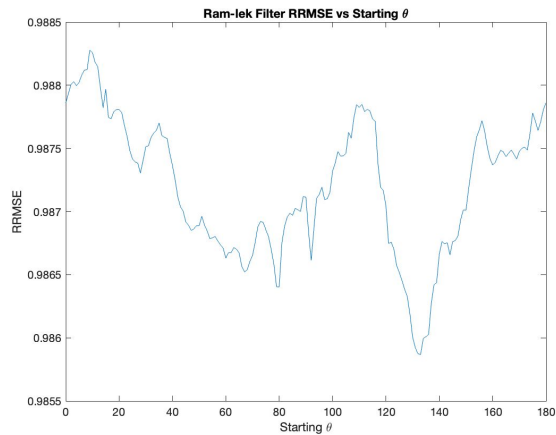
Chest CT (Original)



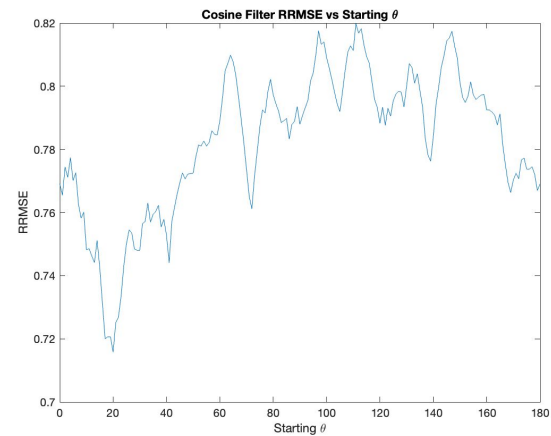
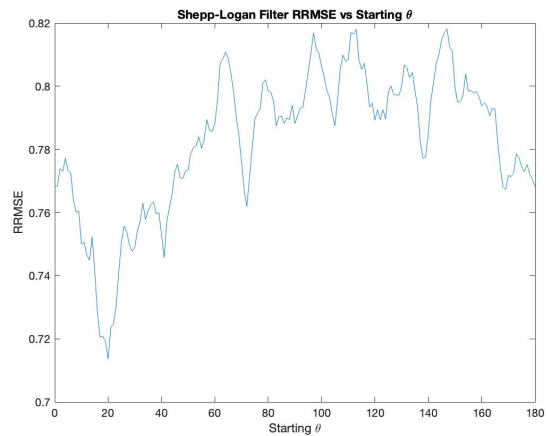
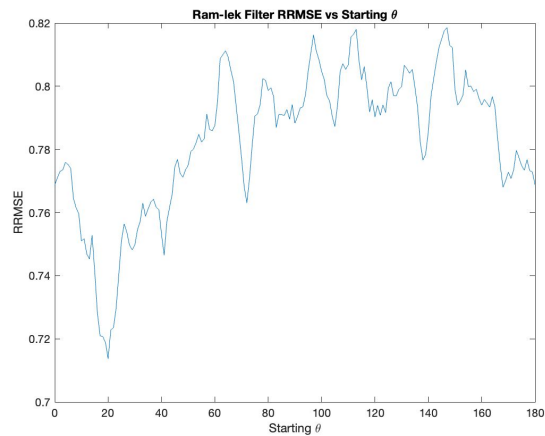
My Phantom (Original)



CHEST CT Data



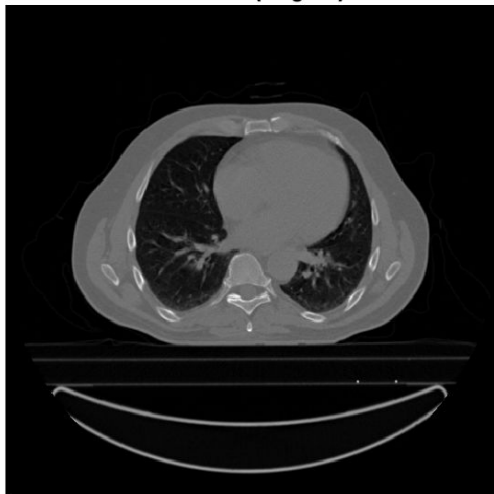
My phantom Data



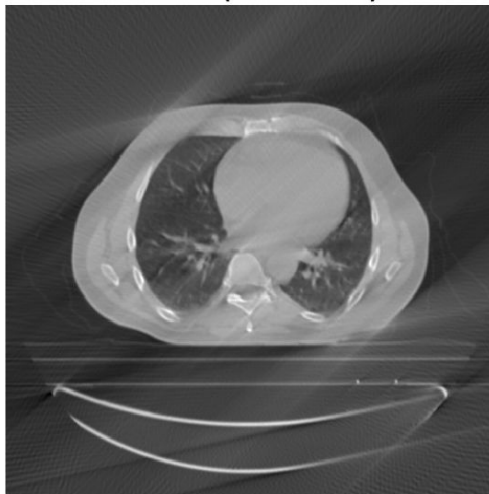
RRMSE vs Starting angle(θ) (all three filters for both datasets)

FBP with θ for which RRMSE is least

Chest CT (Original)



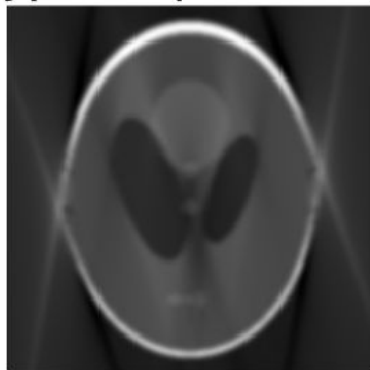
Chest CT (reconstructed)



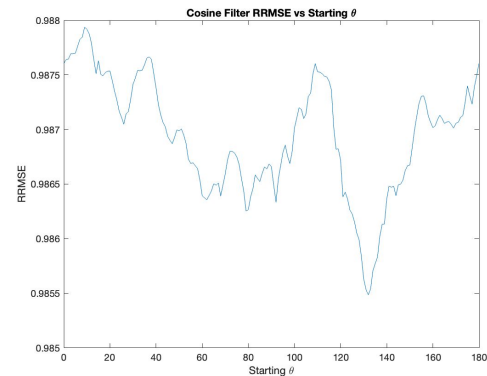
My Phantom (Original)



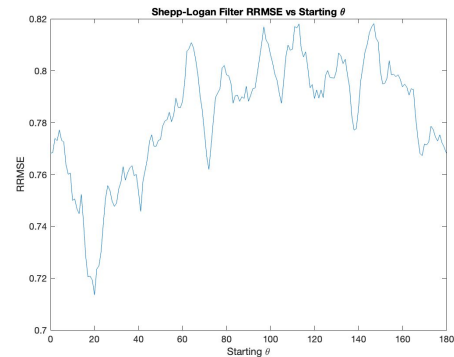
My phantom (reconstructed)



Chosen θ for Chest CT data = 132°
(using cosine filter)



Chosen θ for My phantom data = 20°
(using Shepp-Logan filter)



Q4: Algebraic Reconstruction Technique (ART)

```
function row = get_imaging_row(n, angle, t, integration_params)
    weight_matrix = zeros(n, n);
    x0 = 1 + (n - 1) / 2;
    y0 = 1 + (n - 1) / 2;

    s_step = integration_params.s_step;
    s_range = - (n - 1) * sqrt(2) / 2 : s_step : (n - 1) * sqrt(2) / 2;

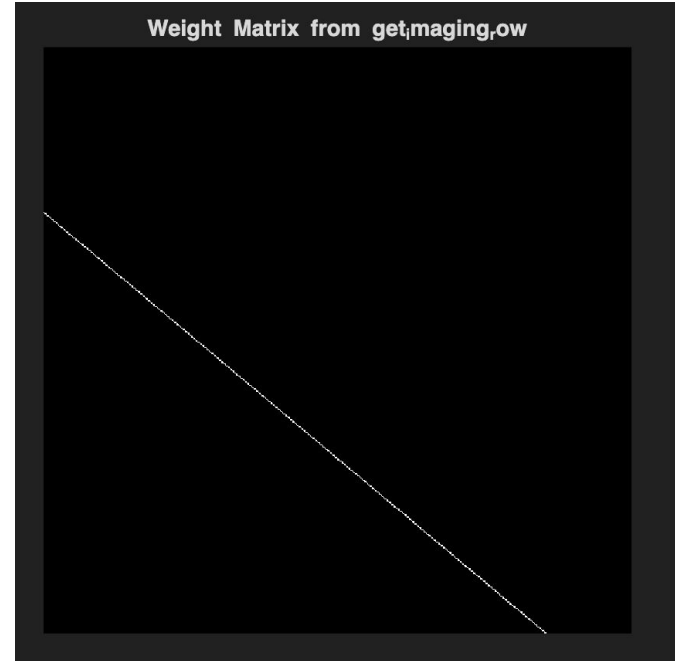
    for s = s_range
        x = x0 + t * cos(angle) - s * sin(angle);
        y = y0 + t * sin(angle) + s * cos(angle);

        x_round = round(x);
        y_round = round(y);

        if (x_round < 1 || x_round > n || y_round < 1 || y_round > n)
            continue;
        end

        weight_matrix(x_round, y_round) = weight_matrix(x_round, y_round) + 1;
    end

    row = weight_matrix(:)';
end
```



C:\shreyasgrampurohit\Documents\College_Academia\Sem8\mic\Medical-Image-Computing\code\q4\myART.m

```
function x = myART(x0, permutation, b, ts, angles, art_params, integration_params)
    lambda = art_params.lambda;
    max_iter = art_params.max_iter;
    global_tol = art_params.tol;

    x = x0;
    n = sqrt(length(x0));
    for iter = 1:max_iter
        x_old = x;
        for i = permutation
            angle = angles(floor((i-1)/length(ts)) + 1);
            t_idx = mod(i-1, length(ts)) + 1;
            t = ts(t_idx);
            a_i = get_imaging_row(n, angle, t, integration_params);

            % ART update
            residual = b(i) - dot(a_i, x);
            x = x + lambda * residual * a_i / norm(a_i)^2;
        end

        % Global convergence check
        if norm(x - x_old) < global_tol
            disp(['Converged at iteration ', num2str(iter)]);
            break;
        end
        if iter == max_iter
            disp('Maximum iterations reached');
        end
    end
end
```

