

# Medical Image Computing

## Assignment 3

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# Q1

Segmenting a Brain MR Image

$$q = 2$$

W



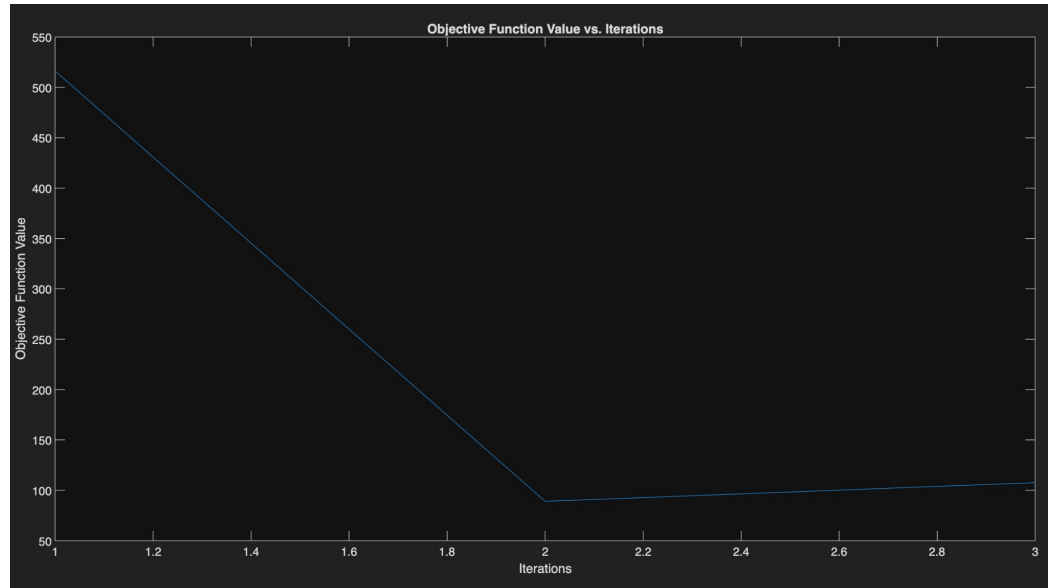
## Initial Estimate of membership



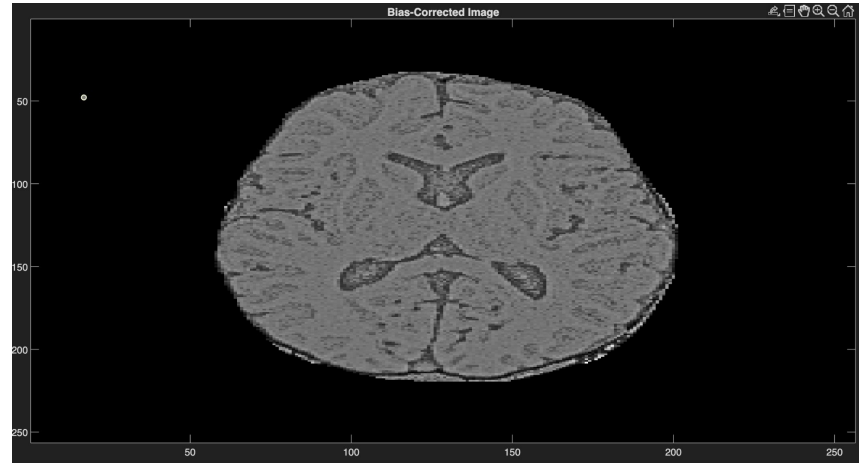
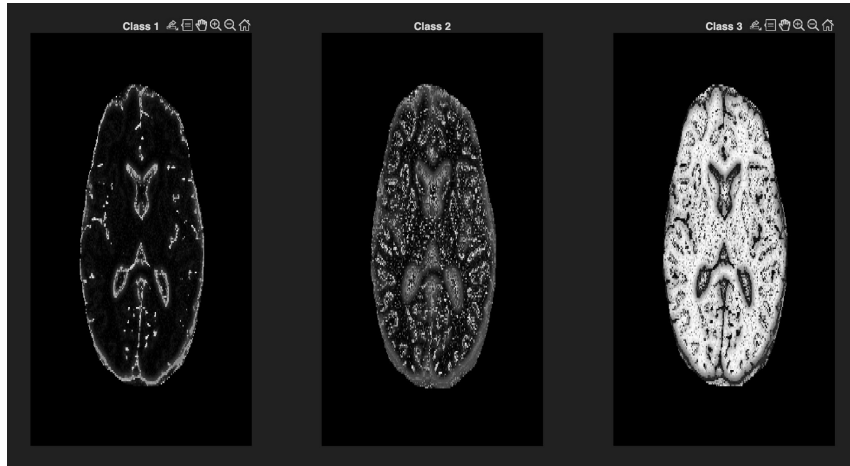
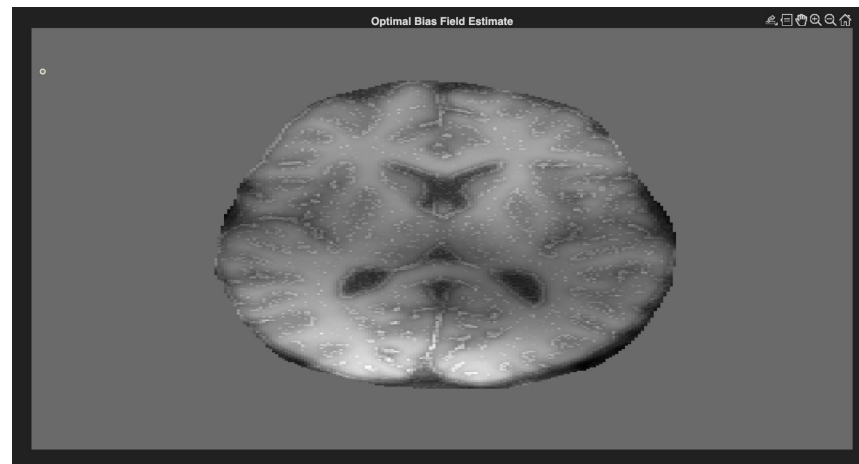
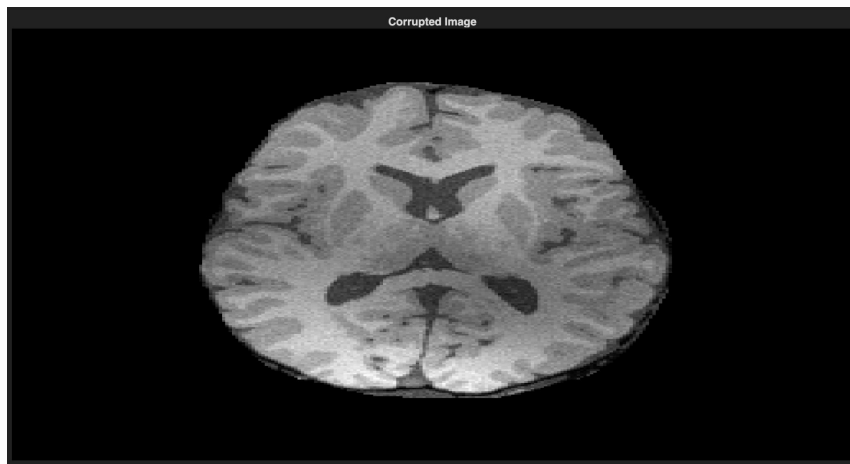
## Initial Estimate of class means

0.0654, 0.2246, 0.4518

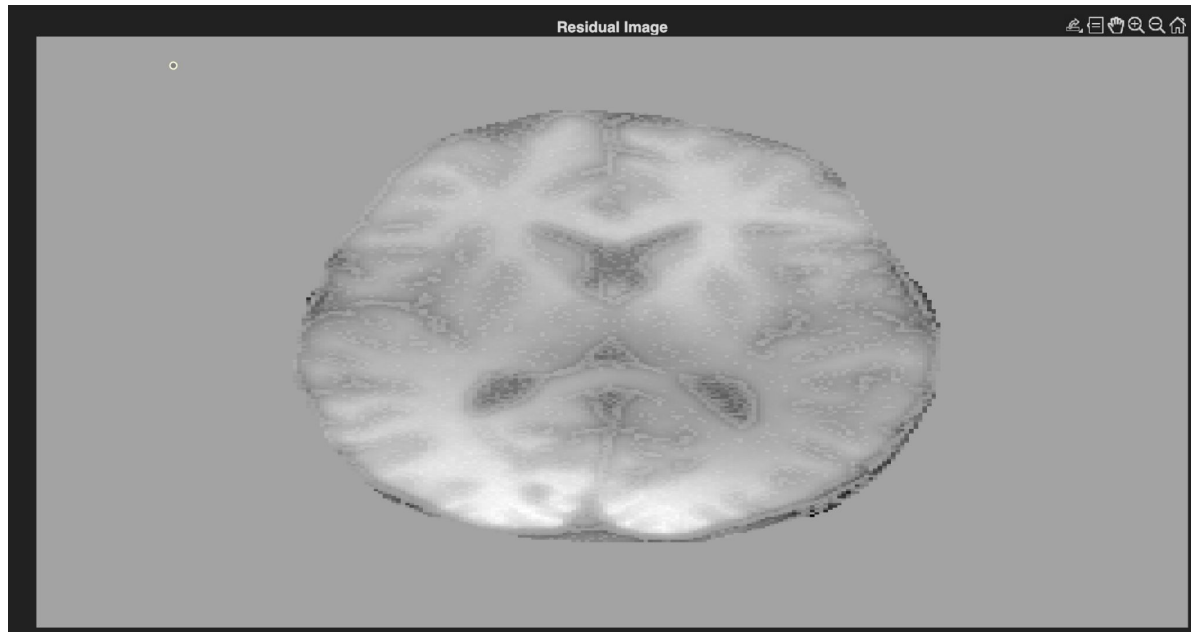
## Objective Function



## Part (f)



# Residual Image



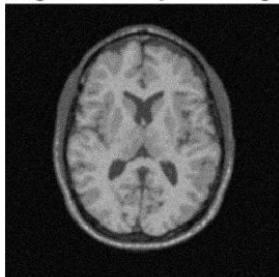
## Optimal Class Means

0.2517, 0.3605, 0.4332



## Q2 - Segmenting a Brain MRI Image using EM optimization algorithm

**Original Corrupted Image**

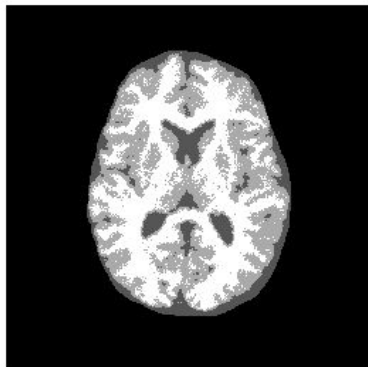


**Masked Original Corrupted Image**



# Initial Estimate of Labels and Parameters

**Initial Estimate of Labels**



## Label Image -

- Used k-means algorithm to get the initial estimate of labels and parameters ( $\mu_k, \sigma_k$ ) for  $k=1,2,3$
- Used a random initialization of the means at the first iteration of k-means and assigned clusters
- Updated means, and subsequently clusters until convergence

## Motivation to use K-means -

- White matter intensities, gray matter intensities, CSF intensities are usually in separate but overlapping ranges
- K-means gives a reasonable starting point without knowledge of gaussian parameters apriori

## Gaussian parameters - $\theta$ :

Initial cluster means: 0.27, 0.51, 0.63

Initial class standard deviations: 0.08, 0.04, 0.04

## Motivation:

Once K-means gives us a starting point of means, set the clusters according to the minimum distance of pixel from the cluster centres. On this subset of points, initialize standard deviation definition.

# Chosen Beta Value = 3

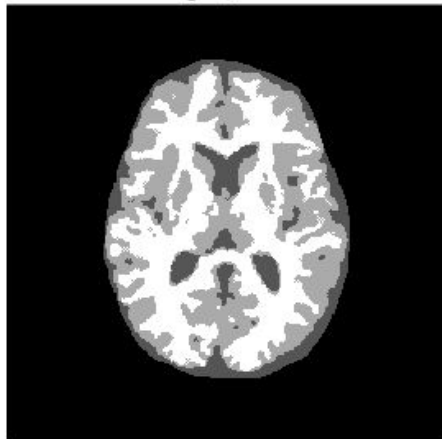
Note: Lower beta values give noisy label images, and higher beta values do not improve the estimate at Beta=3

## Class means estimate:

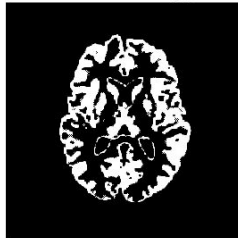
Initial cluster means: 0.27011, 0.50532, 0.62874

Final class means: 0.2820, 0.5135, 0.6279

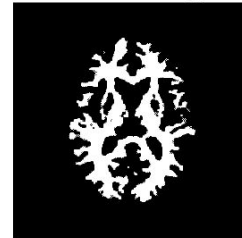
**Label image, beta = 3.00**



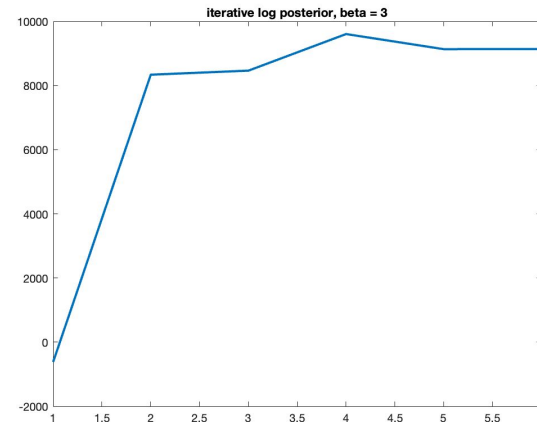
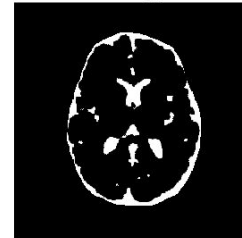
**Gray matter membership, beta = 3.00**



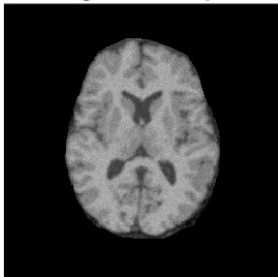
**White matter membership, beta = 3.00**



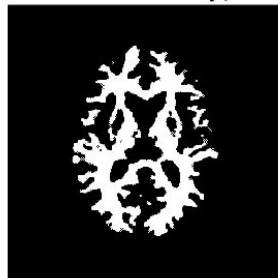
**CSF membership, beta = 3.00**



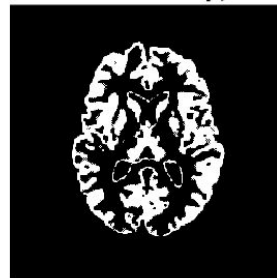
**Masked Original Corrupted Image**



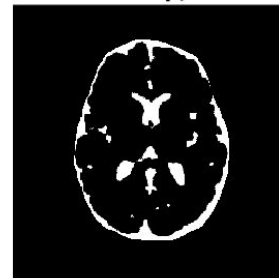
**White matter membership,  $\beta = 3.00$**



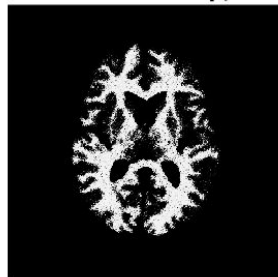
**Gray matter membership,  $\beta = 3.00$**



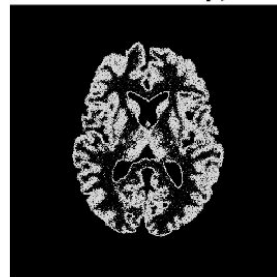
**CSF membership,  $\beta = 3.00$**



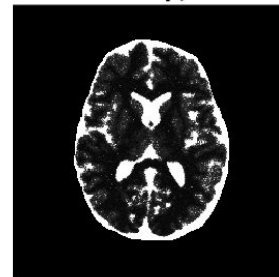
**White matter membership,  $\beta = 0.00$**



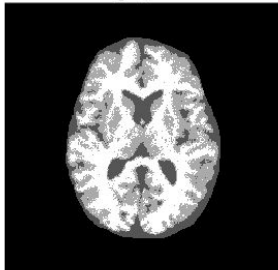
**Gray matter membership,  $\beta = 0.00$**



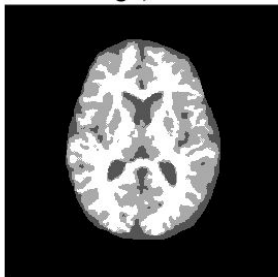
**CSF membership,  $\beta = 0.00$**



**Label image,  $\beta = 0.00$**

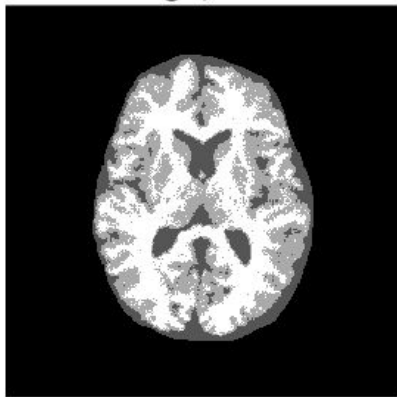


**Label image,  $\beta = 3.00$**

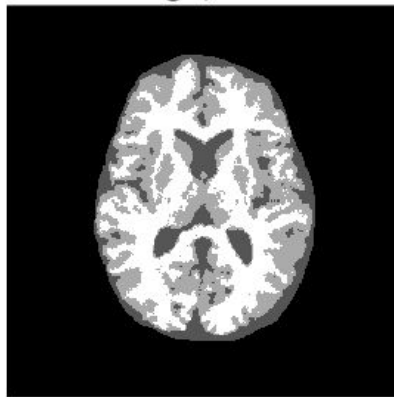


Beta = 0 vs 0.5 vs 3

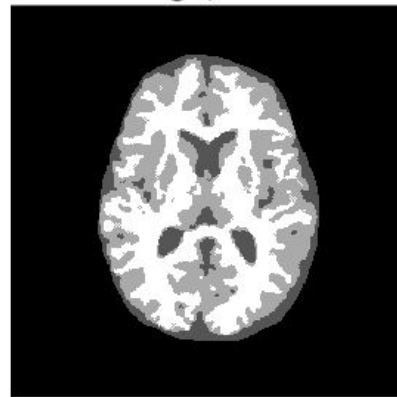
Label image, beta = 0.00



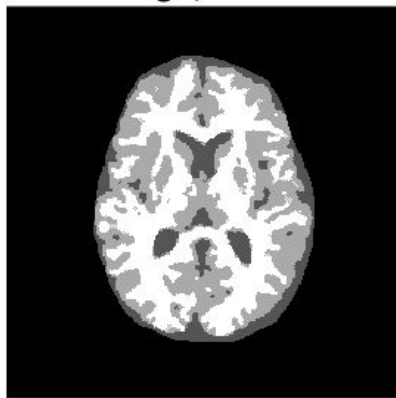
Label image, beta = 0.50



Label image, beta = 3.00



Label image, beta = 10.00



Label image, beta = 100.00

