

Basic Imports

```
In [1]: import numpy as np
from diffractio import mm, um, degrees
from diffractio.scalar_sources_XY import Scalar_source_XY
from diffractio.scalar_masks_XY import Scalar_mask_XY

# Setting up
length = 1 * mm
num_data = 512
x0 = np.linspace(-length / 2, length / 2, num_data)
y0 = np.linspace(-length / 2, length / 2, num_data)
wavelength = 0.633 * um
```

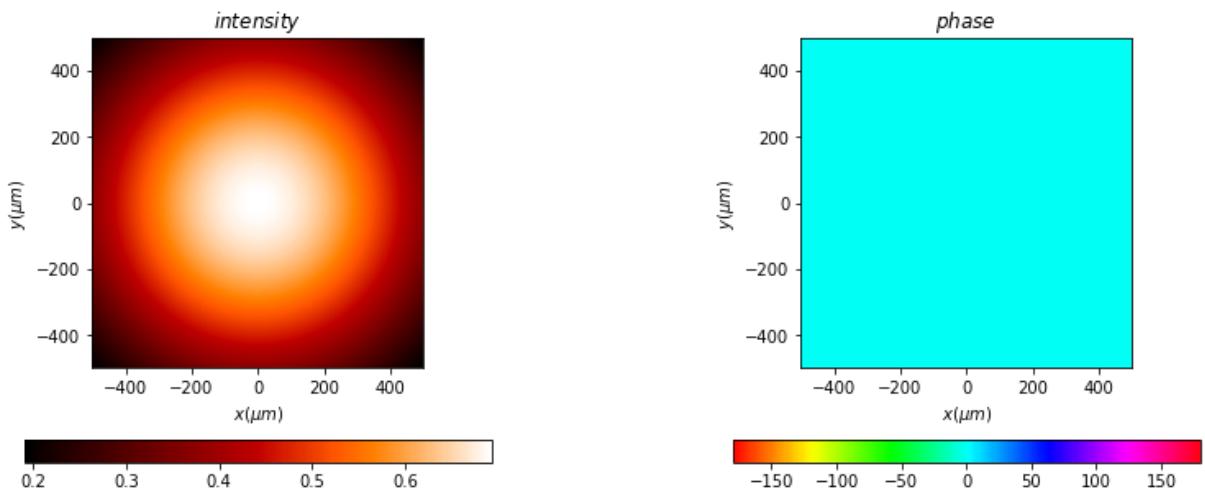
number of processors: 12

Setting up source

- Gaussian Beam (LASER)

```
In [2]: # Gaussian Beam Source - like a LASER
u0 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
u0.gauss_beam(r0=(0, 0), w0=(800 * um, 800 * um), z0=0.0)
u0.draw(kind='field', logarithm=True)
```

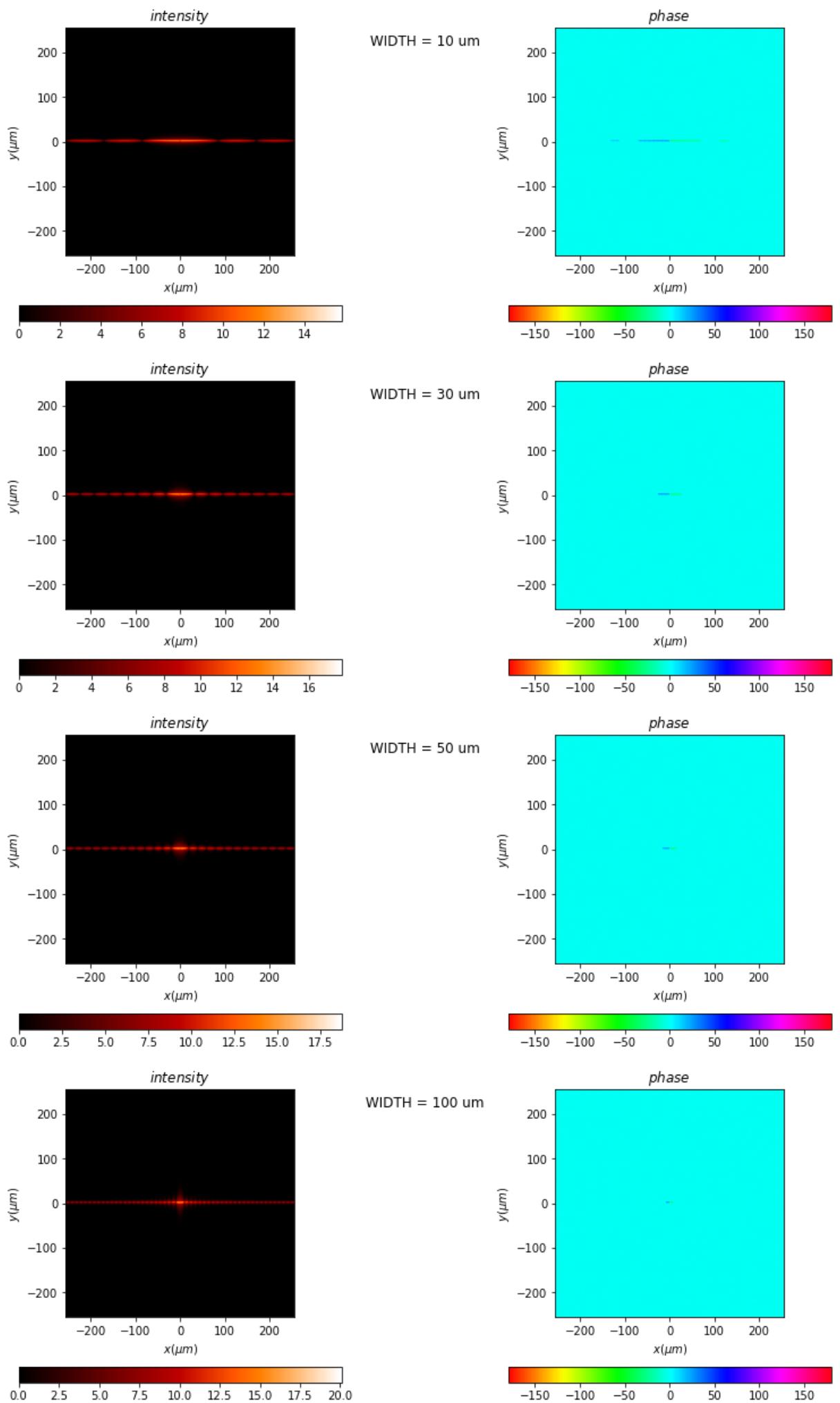
```
Out[2]: (<matplotlib.image.AxesImage at 0x272b852da60>,
<matplotlib.image.AxesImage at 0x272b87cc220>,
None,
None)
```

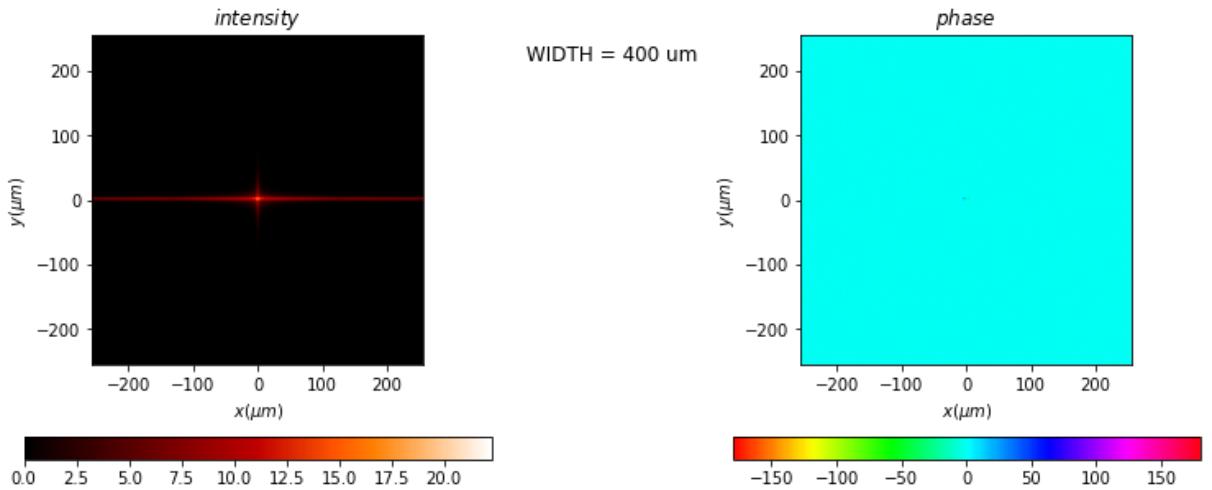


Slits

- Fraunhofer Diffraction Patterns for different slit widths

```
In [3]: widths = [10, 30, 50, 100, 400] # in um
for width in widths:
    varSlit = Scalar_mask_XY(x0, y0, wavelength)
    varSlit.slit(
        x0=0 * um,
        size=width * um
    )
    # varSlit.draw(kind='field', logarithm=True)
    a_varSlit = (u0 * varSlit).fft(z=1 * mm, new_field=True)
    a_varSlit.draw(title=f" WIDTH = {width} um ", kind='field', logarithm=True)
```





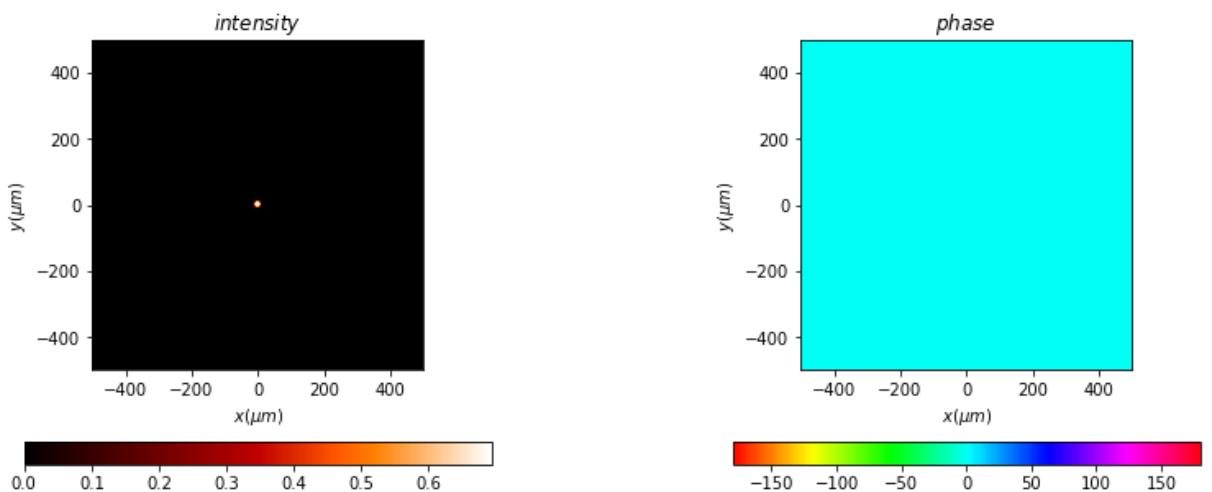
The intensity variation matches the expected profile.

Pinhole

- Fraunhofer Diffraction Patterns for different pinhole radii

```
In [4]: # Showcasing a pinhole
circ = Scalar_mask_XY(x0, y0, wavelength)
circ.circle(
    r0=(0 * um, 0 * um),
    radius=(10 * um, 10 * um),
    angle=0
)
circ.draw(kind='field', logarithm=True)
```

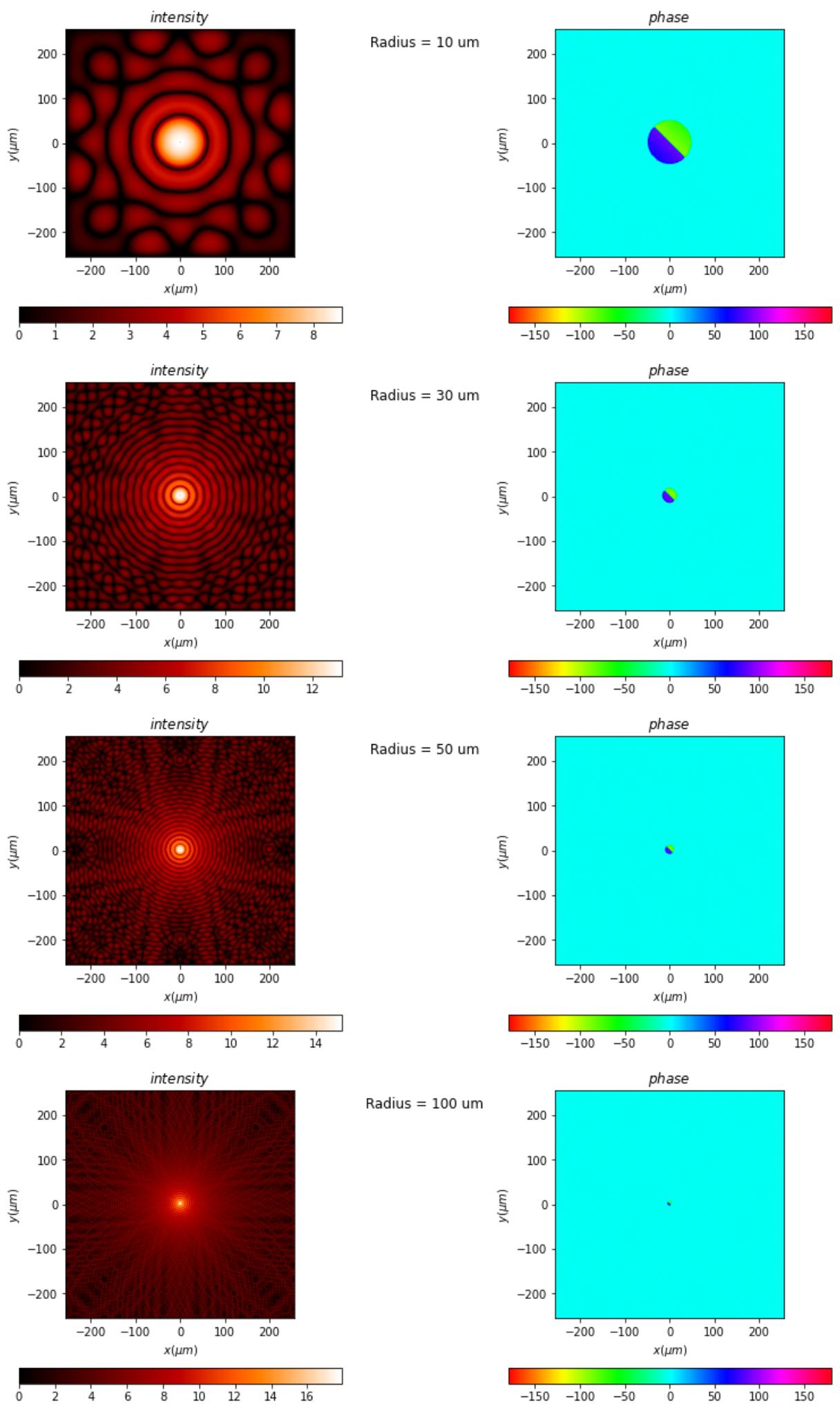
```
Out[4]: ((<matplotlib.image.AxesImage at 0x272bd337eb0>,
<matplotlib.image.AxesImage at 0x272bd3aa6a0>),
None,
None)
```

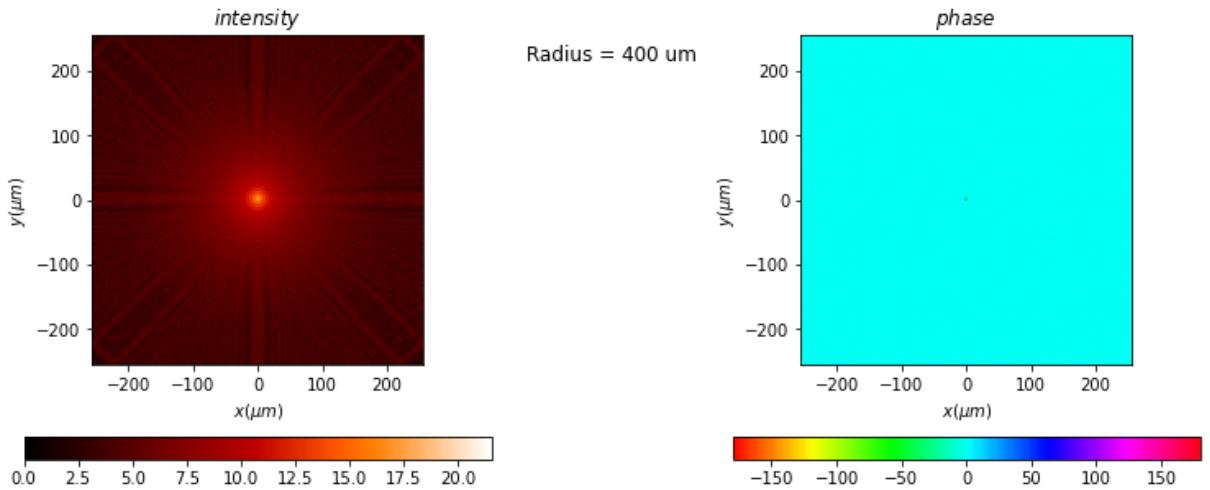


Diffraction pattern for multiple pinholes having different radius

```
In [5]: radii = [10, 30, 50, 100, 400] # in um
for rad in radii:
    circ = Scalar_mask_XY(x0, y0, wavelength)
    circ.circle(
        r0=(0 * um, 0 * um),
        radius=(rad * um, rad * um),
        angle=0
    )

    a_circ = (u0 * circ).fft(z=1 * mm, new_field=True)
    a_circ.draw(title=f" Radius = {rad} um ", kind='field', logarithm=True)
```





We observe the well-known Airy Disk in all cases, as theoretically expected.

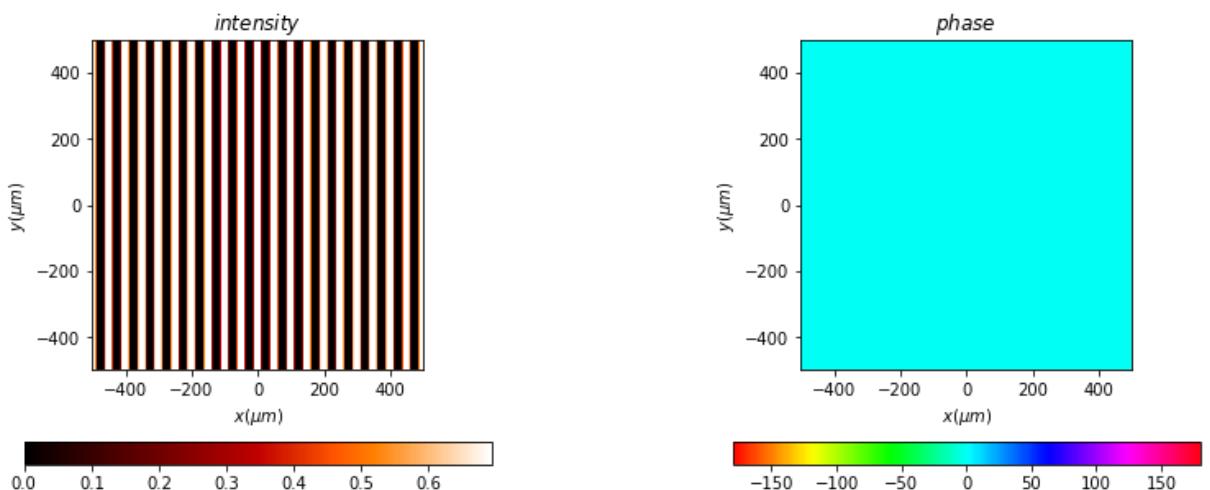
Grating

- Fraunhofer Diffraction Patterns for grating

```
In [6]: grating = Scalar_mask_XY(x0, y0, wavelength)
grating.romchi_grating(
    period=50 * um,
)

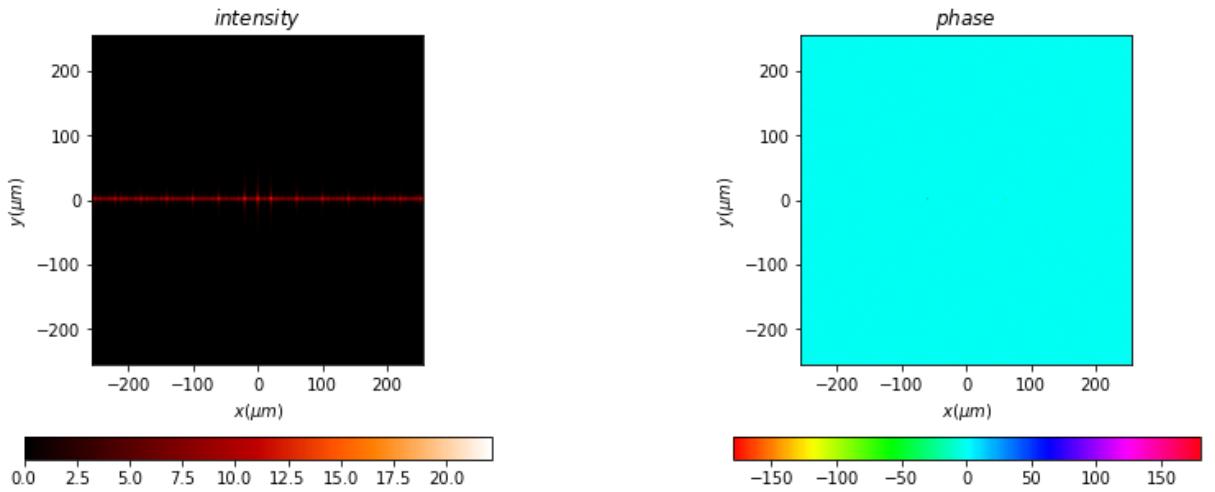
grating.draw(kind='field', logarithm=True)
```

```
Out[6]: ((<matplotlib.image.AxesImage at 0x272bf6b80a0>,
    <matplotlib.image.AxesImage at 0x272bcbed820>),
None,
None)
```



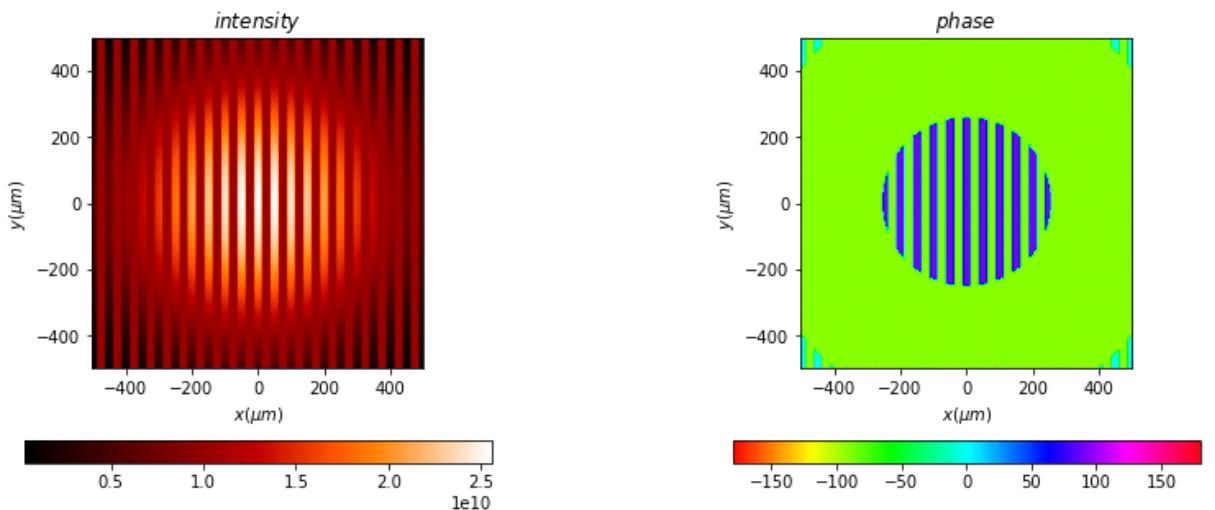
```
In [7]: # Fourier Plane - No Filter
a_L1 = (u0 * grating).fft(z=1 * mm, new_field=True)
a_L1.draw(kind='field', logarithm=True)
```

```
Out[7]: ((<matplotlib.image.AxesImage at 0x272b95608e0>,
    <matplotlib.image.AxesImage at 0x272b954b0a0>),
None,
None)
```



```
In [8]: a_L2 = a_L1.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
a_L2.draw(kind='field', logarithm=False)
```

```
Out[8]: (<matplotlib.image.AxesImage at 0x272b95ee6a0>,
<matplotlib.image.AxesImage at 0x272b928b970>,
None,
None)
```



```
In [ ]:
```

Mesh

Compare results with figures in Eisenkraft (1977)

```
In [1]: import numpy as np
from diffractio import mm, um, degrees
from diffractio.scalar_sources_XY import Scalar_source_XY
from diffractio.scalar_masks_XY import Scalar_mask_XY

# Setting up
length = 1 * mm
num_data = 512
x0 = np.linspace(-length / 2, length / 2, num_data)
y0 = np.linspace(-length / 2, length / 2, num_data)
wavelength = 0.633 * um
```

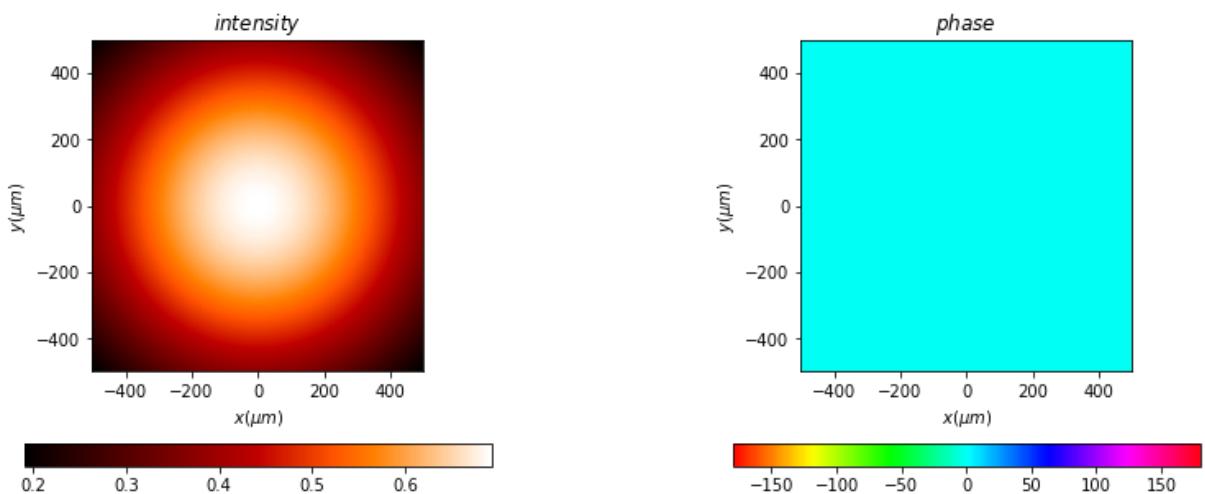
number of processors: 12

Setting up source(s)

- Gaussian Beam (LASER)

```
In [2]: # Gaussian Beam Source - Like a LASER
u0 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
u0.gauss_beam(r0=(0, 0), w0=(800 * um, 800 * um), z0=0.0)
u0.draw(kind='field', logarithm=True)
```

```
Out[2]: ((<matplotlib.image.AxesImage at 0x249d2c1ea60>,
          <matplotlib.image.AxesImage at 0x249d2ebc220>),
          None,
          None)
```



Mesh

```
In [3]: mesh = Scalar_mask_XY(x0, y0, wavelength)
mesh.grating_2D(
    period=50 * um,
    fill_factor=0.5,
    angle=0 * degrees
)
mesh.draw(kind='field', logarithm=True)
```

```
Out[3]: ((<matplotlib.image.AxesImage at 0x249d36f11c0>,
          <matplotlib.image.AxesImage at 0x249d3960940>),
          None,
          None)
```

Basic Imports

```
In [1]: import numpy as np
from diffractio import mm, um, degrees
from diffractio.scalar_sources_XY import Scalar_source_XY
from diffractio.scalar_masks_XY import Scalar_mask_XY

# Setting up
length = 1 * mm
num_data = 512
x0 = np.linspace(-length / 2, length / 2, num_data)
y0 = np.linspace(-length / 2, length / 2, num_data)
wavelength = 0.633 * um
```

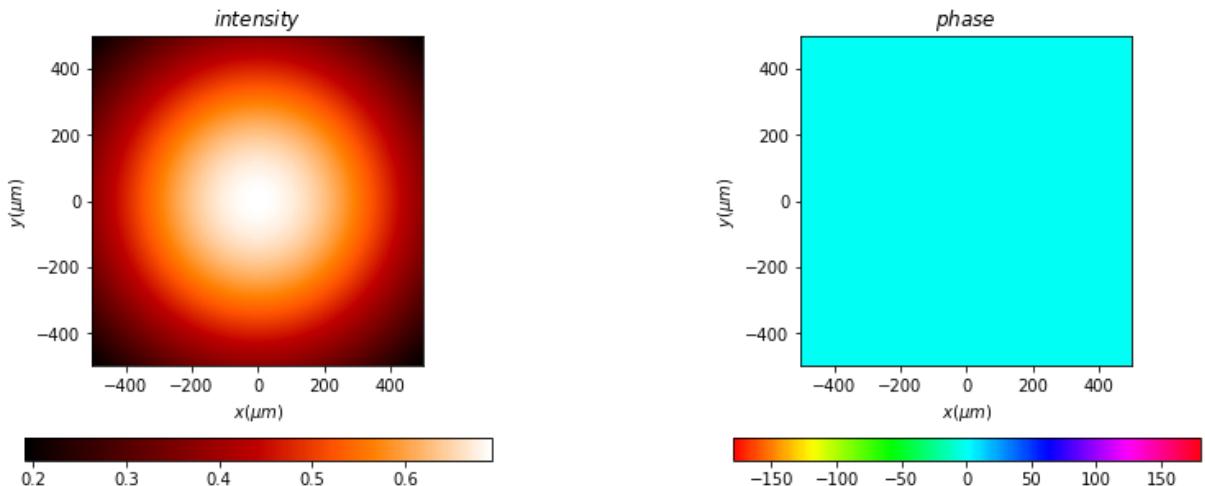
number of processors: 12

Setting up source

- Gaussian Beam (LASER)

```
In [2]: # Gaussian Beam Source - like a LASER
u0 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
u0.gauss_beam(r0=(0, 0), w0=(800 * um, 800 * um), z0=0.0)
u0.draw(kind='field', logarithm=True)
```

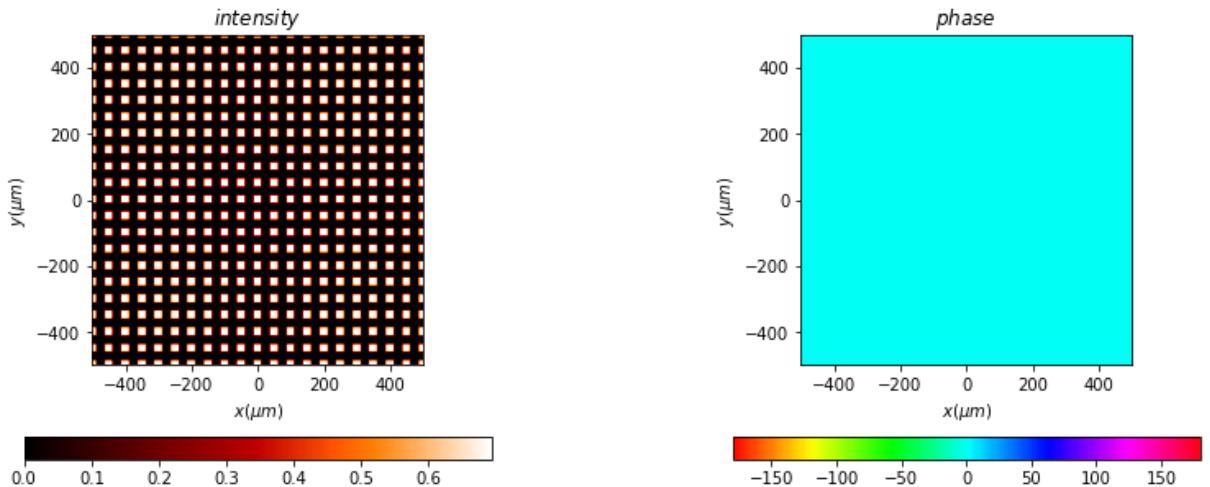
```
Out[2]: (<matplotlib.image.AxesImage at 0x272b852da60>,
<matplotlib.image.AxesImage at 0x272b87cc220>,
None,
None)
```



Slits

- Fraunhofer Diffraction Patterns for different slit widths

```
In [3]: widths = [10, 30, 50, 100, 400] # in um
for width in widths:
    varSlit = Scalar_mask_XY(x0, y0, wavelength)
    varSlit.slit(
        x0=0 * um,
        size=width * um
    )
    # varSlit.draw(kind='field', logarithm=True)
    a_varSlit = (u0 * varSlit).fft(z=1 * mm, new_field=True)
    a_varSlit.draw(title=f" WIDTH = {width} um ", kind='field', logarithm=True)
```

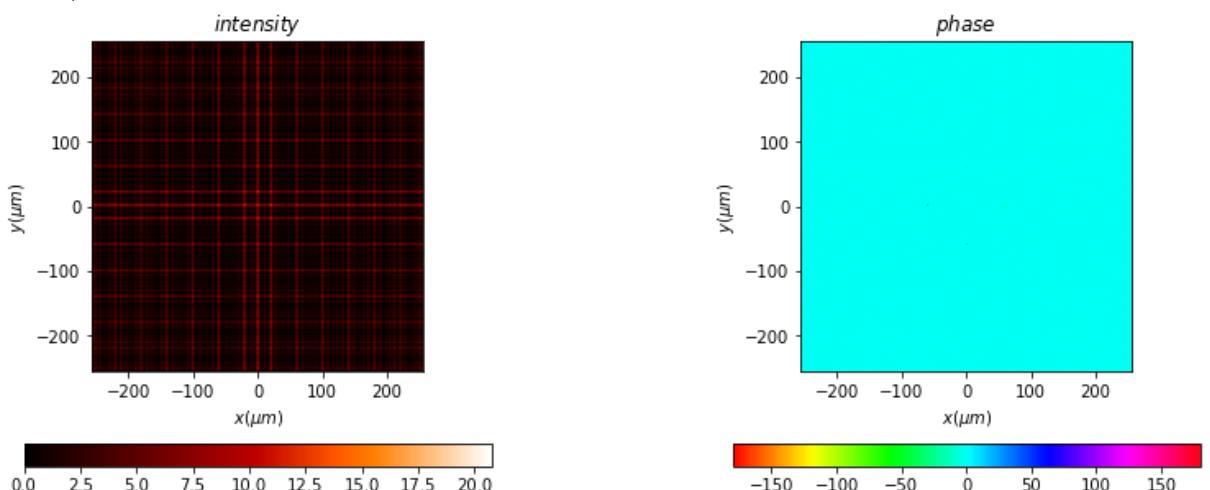


```
In [4]: # angledMesh = Scalar_mask_XY(x0, y0, wavelength)
# angledMesh.grating_2D(
#     period=50 * um,
#     fill_factor=0.5,
#     angle=45 * degrees
# )

# angledMesh.draw(kind='field', logarithm=True)
```

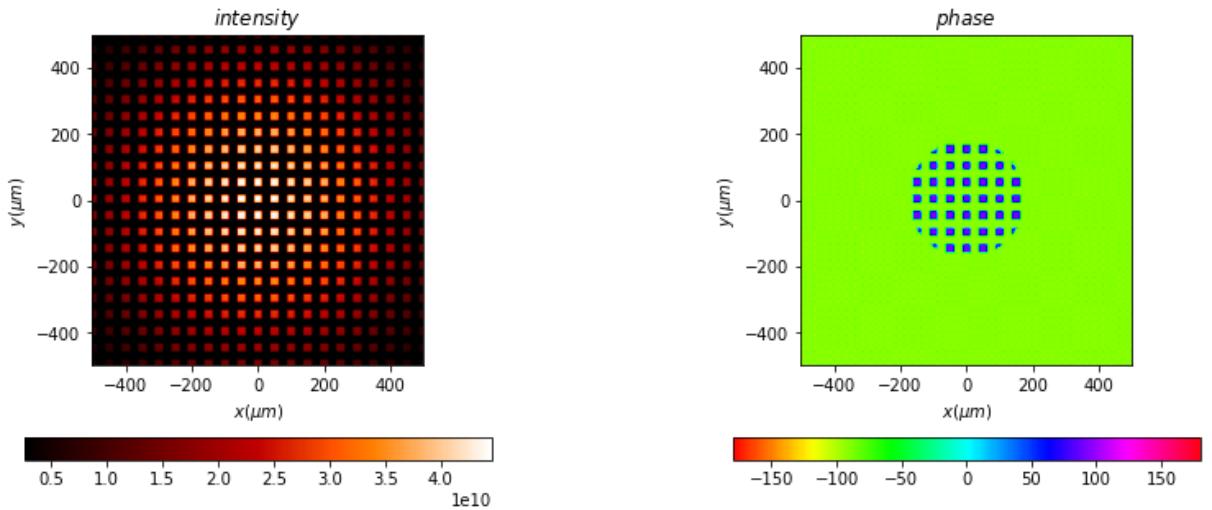
```
In [5]: # Fourier Plane - No Filter
a_L1 = (u0 * mesh).fft(z=1 * mm, new_field=True)
a_L1.draw(kind='field', logarithm=True)
```

```
Out[5]: (<matplotlib.image.AxesImage at 0x249d356fe80>,
<matplotlib.image.AxesImage at 0x249d3607670>),
None,
None)
```



```
In [6]: # This is how, it'd look without any filter, at the Observation screen
a_L2 = a_L1.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
a_L2.draw(kind='field', logarithm=False)
```

```
Out[6]: (<matplotlib.image.AxesImage at 0x249d3deaee0>,
<matplotlib.image.AxesImage at 0x249d6a856d0>),
None,
None)
```

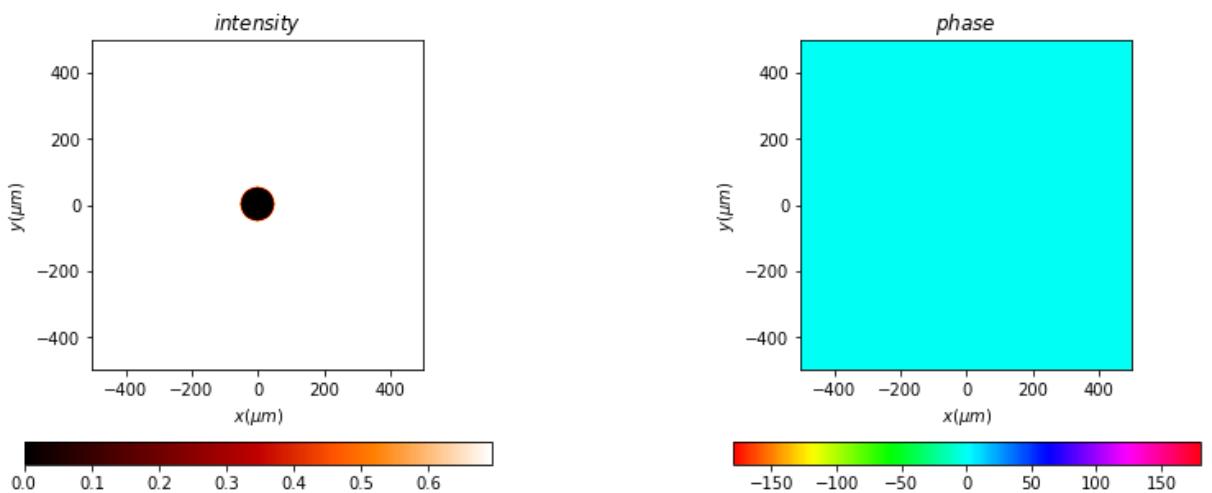


Masks / Filters

- Center Dot - High Pass
- Square - Low Pass
- Square + Center Dot
- Vertical Slit
- Horizontal Slit
- Angled Slit

```
In [7]: cDot = Scalar_mask_XY(x0, y0, wavelength)
cDot.ring(
    r0=(0 * um, 0 * um),
    radius1=(50 * um, 50 * um),
    radius2=(1000 * um, 1000 * um)
)
cDot.draw(kind='field', logarithm=True)
```

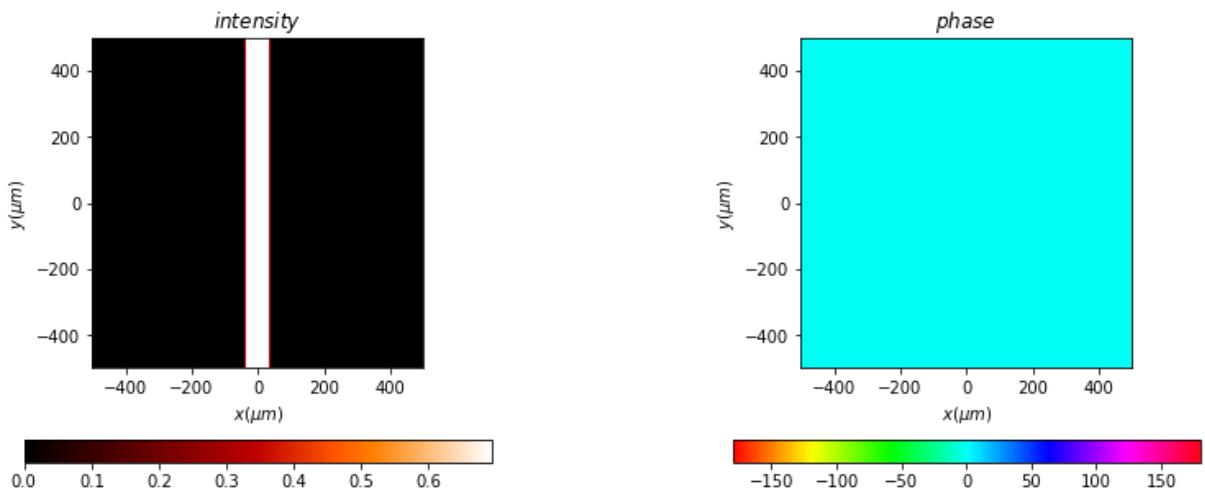
```
Out[7]: (<matplotlib.image.AxesImage at 0x249d6b5e460>,
          <matplotlib.image.AxesImage at 0x249d6bcdbe0>),
None,
None)
```



```
In [8]: vert = Scalar_mask_XY(x0, y0, wavelength)
vert.slit(
    x0=0 * um,
    size=75 * um
)
vert.draw(kind='field', logarithm=True)
```

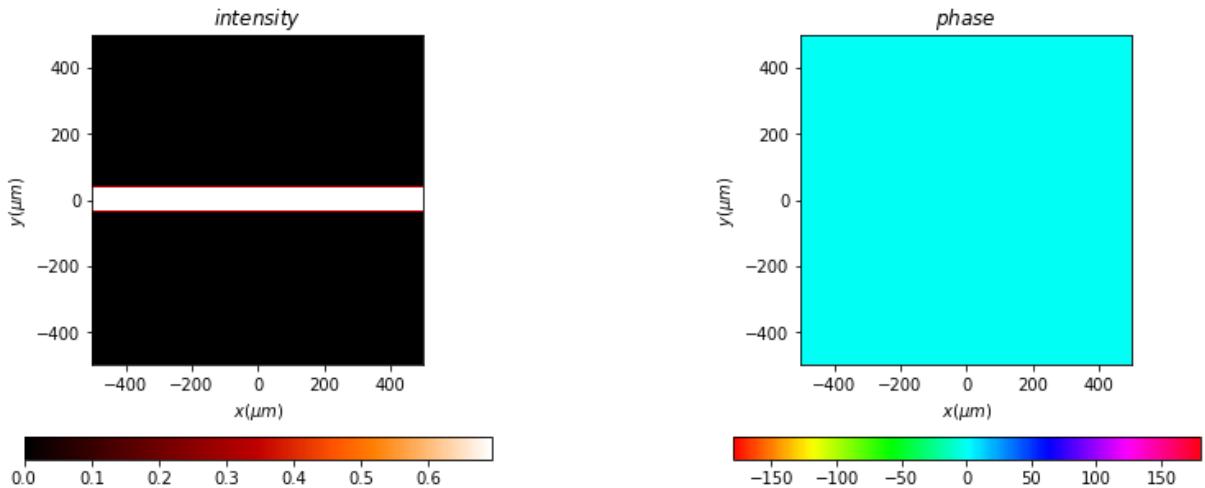
```
Out[8]: (<matplotlib.image.AxesImage at 0x249d3695460>,
```

```
<matplotlib.image.AxesImage at 0x249d2e91ac0>),
None,
None)
```



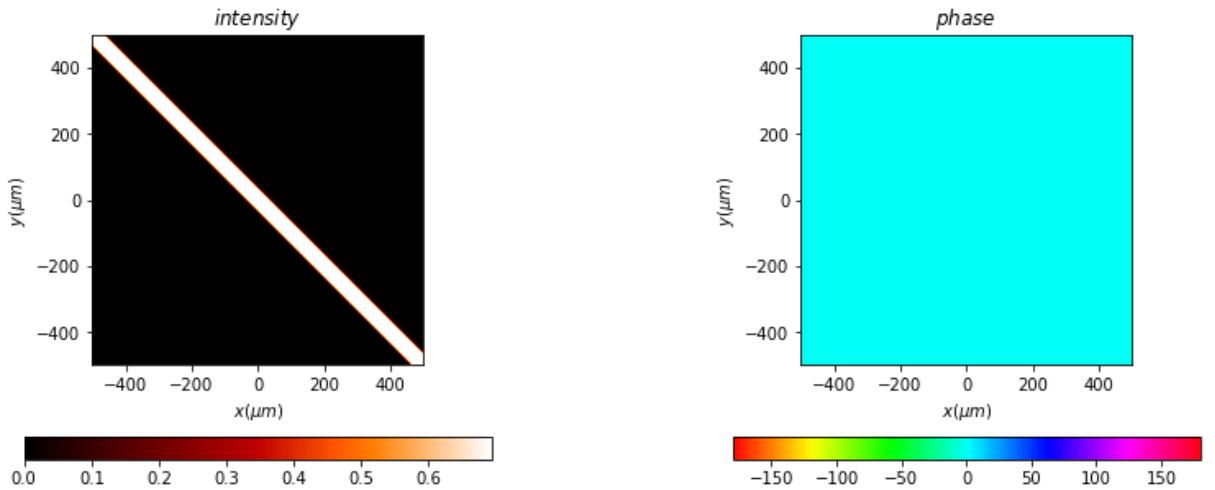
```
In [9]: horiz = Scalar_mask_XY(x0, y0, wavelength)
horiz.slit(
    x0=0 * um,
    size=75 * um,
    angle=np.pi / 2
)
horiz.draw(kind='field', logarithm=True)
```

```
Out[9]: (<matplotlib.image.AxesImage at 0x249d8190130>,
<matplotlib.image.AxesImage at 0x249d81e08e0>),
None,
None)
```



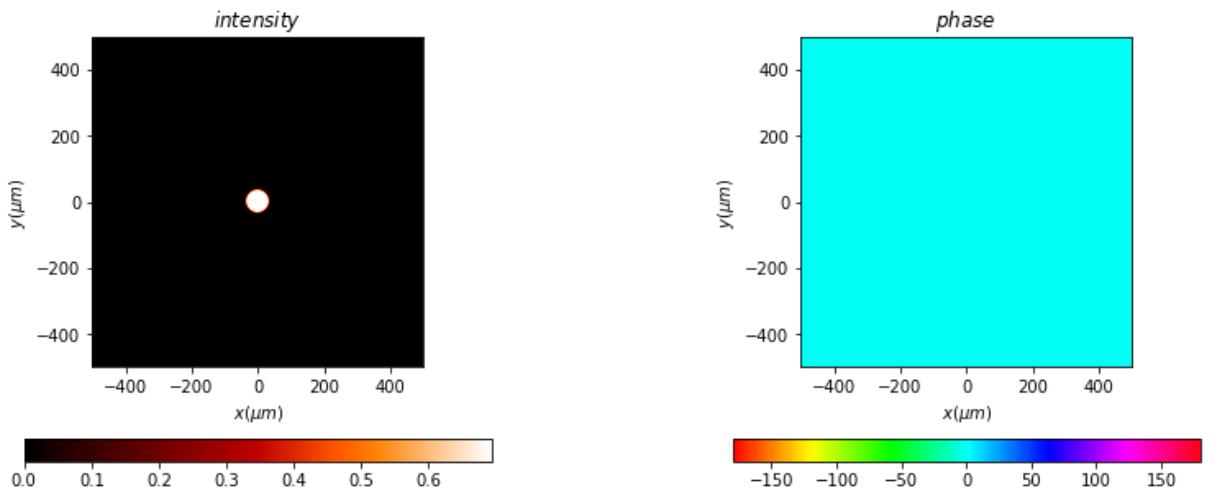
```
In [10]: angled = Scalar_mask_XY(x0, y0, wavelength)
angled.slit(
    x0=0 * um,
    size=50 * um,
    angle=np.pi / 4
)
angled.draw(kind='field', logarithm=True)
```

```
Out[10]: (<matplotlib.image.AxesImage at 0x249d8f35a00>,
<matplotlib.image.AxesImage at 0x249d8f90220>),
None,
None)
```



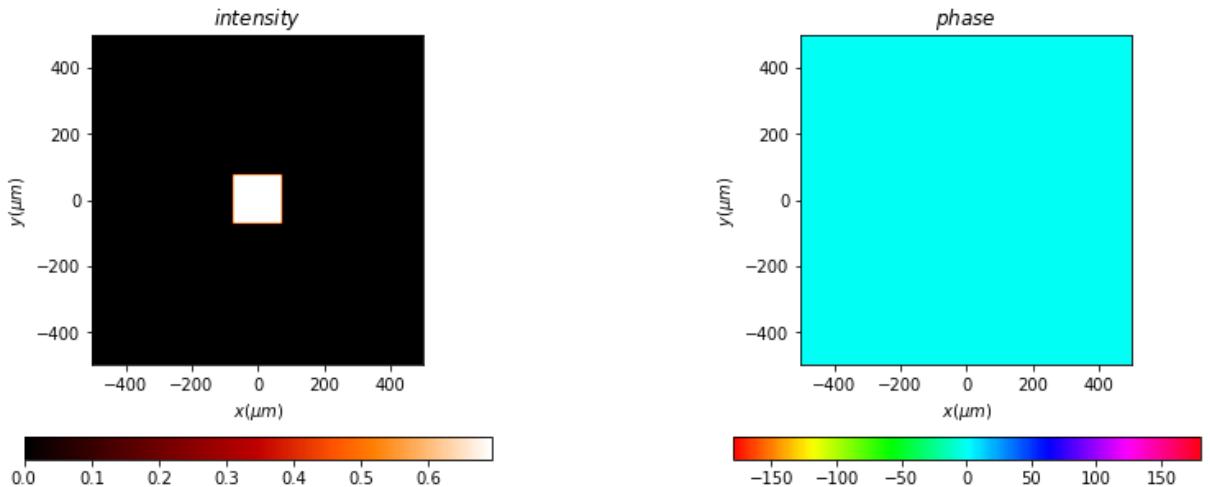
```
In [11]: circ = Scalar_mask_XY(x0, y0, wavelength)
circ.circle(
    r0=(0 * um, 0 * um),
    radius=(35 * um, 35 * um),
    angle=0
)
circ.draw(kind='field', logarithm=True)
```

```
Out[11]: (<matplotlib.image.AxesImage at 0x249d90575e0>,
<matplotlib.image.AxesImage at 0x249d90d0910>,
None,
None)
```



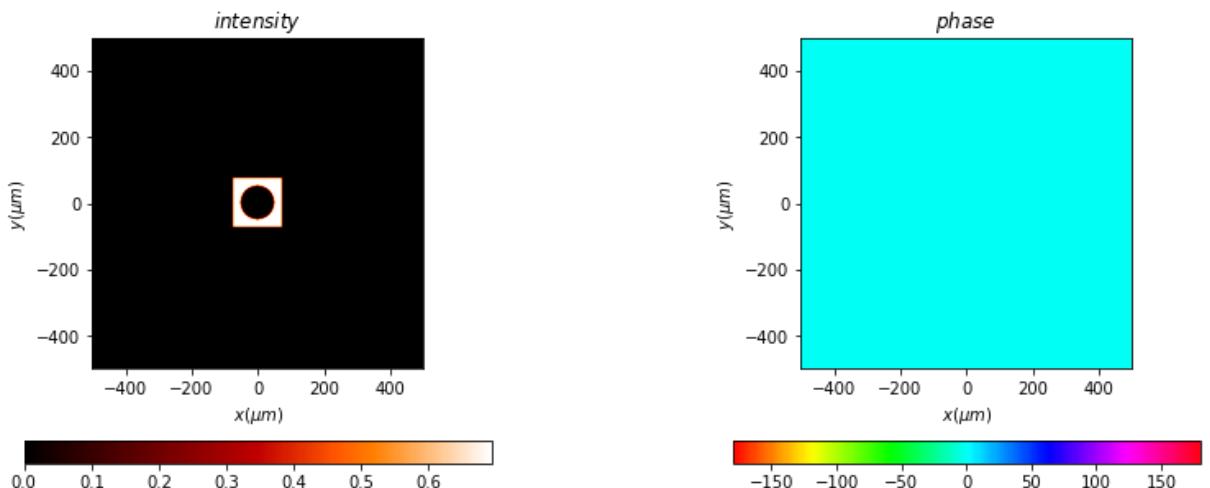
```
In [12]: sq = Scalar_mask_XY(x0, y0, wavelength)
sq.square(
    r0=(0 * um, 0 * um),
    size=(150 * um, 150 * um),
    angle=0,
)
sq.draw(kind='field', logarithm=True)
```

```
Out[12]: (<matplotlib.image.AxesImage at 0x249da61ddc0>,
<matplotlib.image.AxesImage at 0x249da698070>,
None,
None)
```



```
In [13]: # Adding two filters
sqCirc = sq * cDot
sqCirc.draw(kind="field", logarithm=True)
```

```
Out[13]: (<matplotlib.image.AxesImage at 0x249da6da160>,
<matplotlib.image.AxesImage at 0x249d8146f70>,
None,
None)
```



Returns wave after encountering filter and then L2

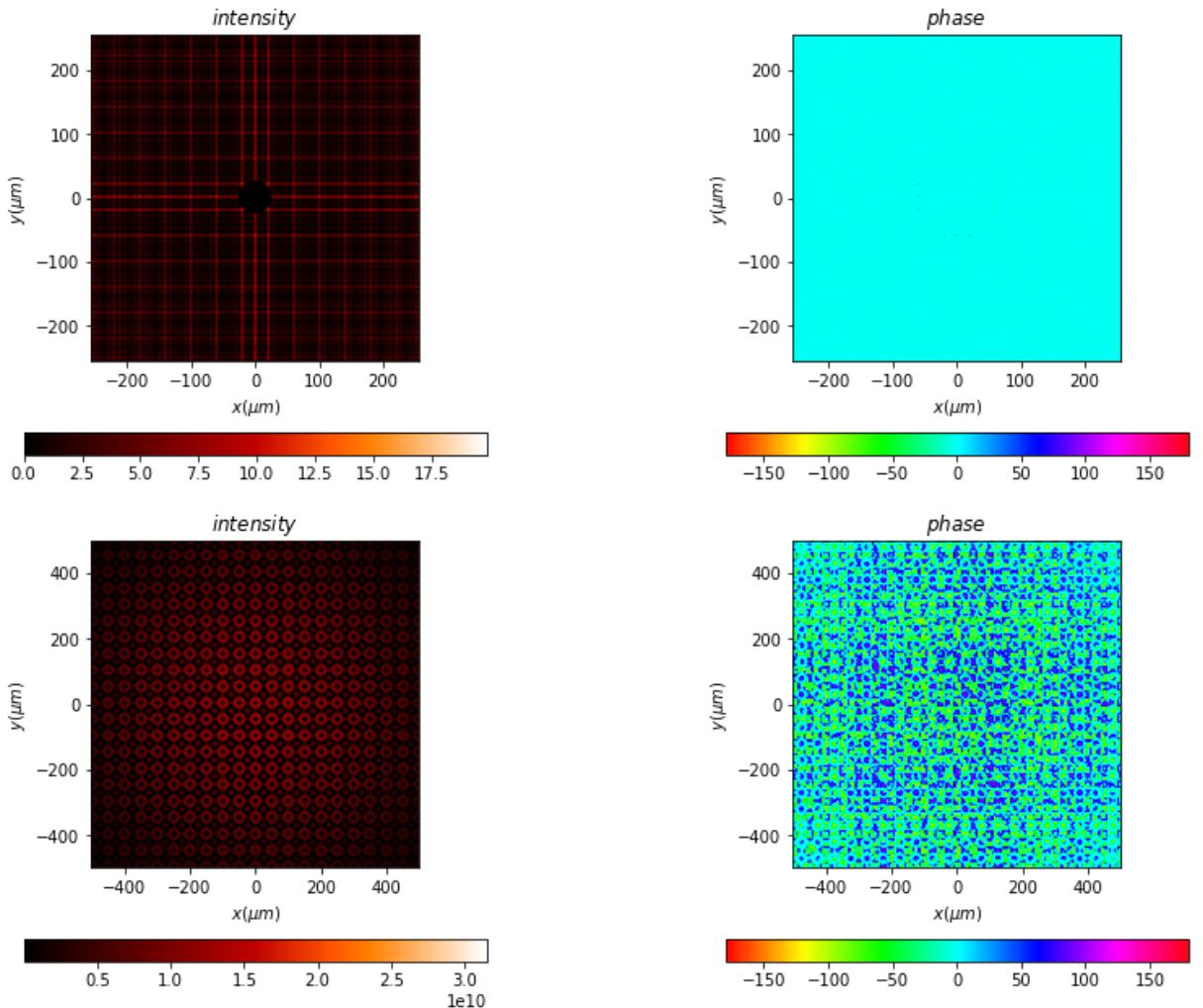
```
In [14]: def sim(a_L1, mask):
    """
    a_L1: Wave after passing through Lens 1
    mask: Mask or Filter to apply
    """
    a_L1_Mask = a_L1 * mask
    a_L1_Mask_L2 = a_L1_Mask.fft(z=1 * mm, shift=False, remove0=False, new_field=True)

    return a_L1_Mask, a_L1_Mask_L2
```

Center Dot - High Pass - EDGE DETECTION

```
In [15]: a_L1_cD, a_L1_cD_L2 = sim(a_L1, cDot)
a_L1_cD.draw(kind='field', logarithm=True)
a_L1_cD_L2.draw(kind='field', logarithm=False)
```

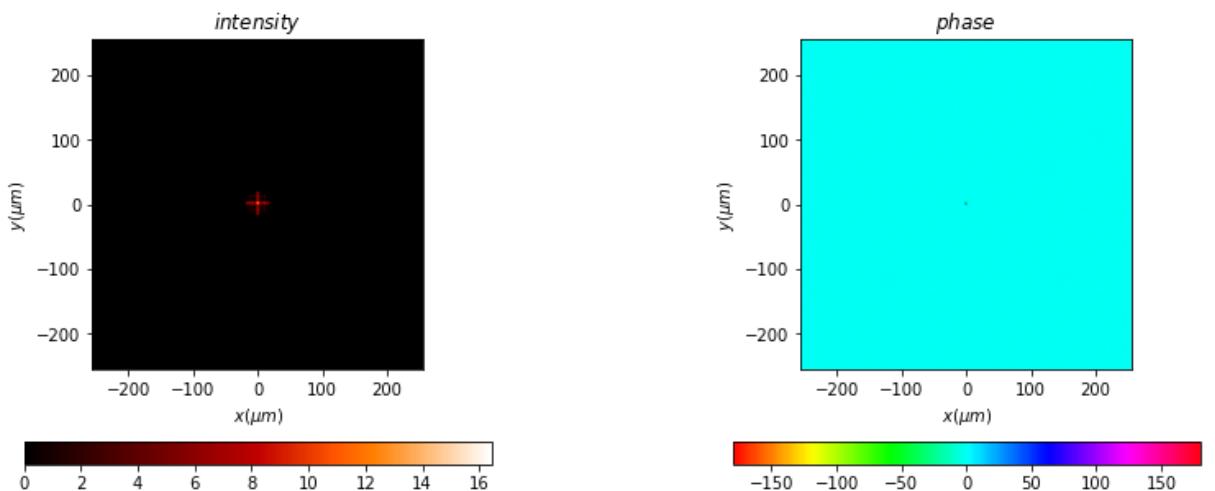
```
Out[15]: (<matplotlib.image.AxesImage at 0x249db350ee0>,
<matplotlib.image.AxesImage at 0x249dbe436d0>,
None,
None)
```

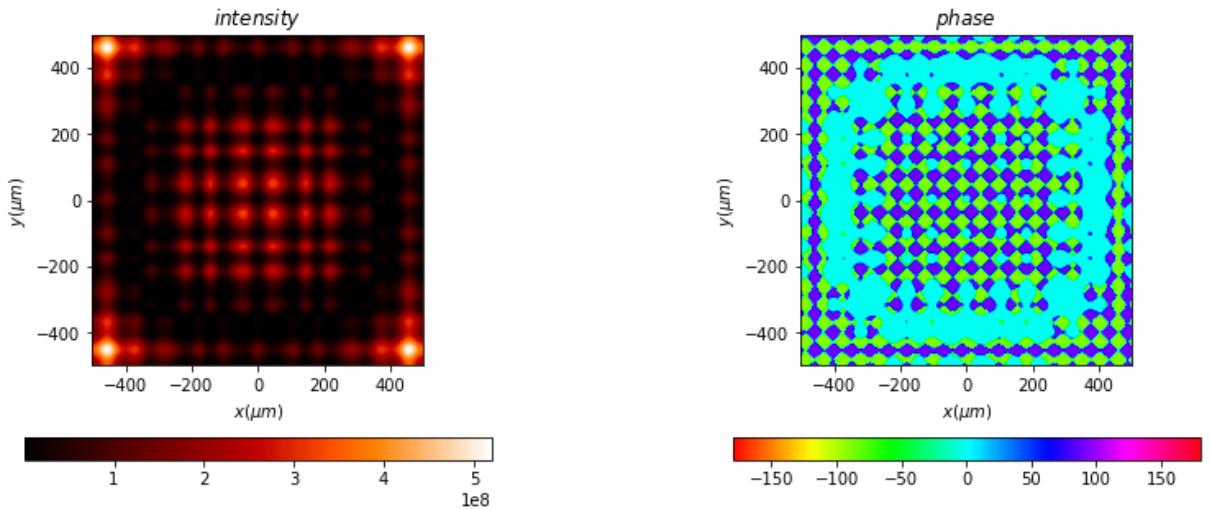


Circle - Low Pass - Blurred Output

```
In [16]: a_L1_Circ, a_L1_Circ_L2 = sim(a_L1, circ)
a_L1_Circ.draw(kind='field', logarithm=True)
a_L1_Circ_L2.draw(kind='field', logarithm=False)
```

```
Out[16]: (<matplotlib.image.AxesImage at 0x249dce2a00>,
<matplotlib.image.AxesImage at 0x249dcf4dd00>),
None,
None)
```

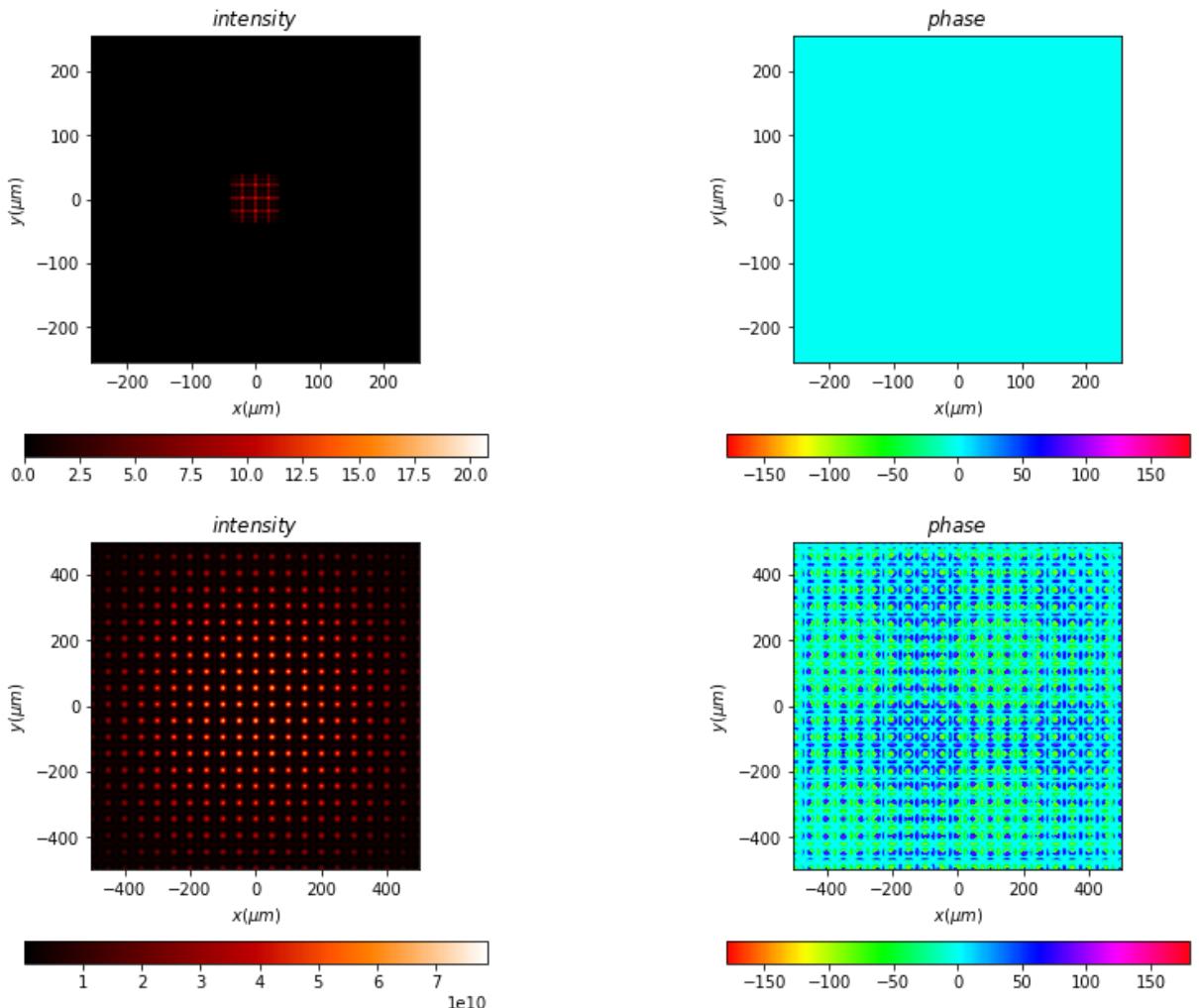




Square

```
In [17]: a_L1_Sq, a_L1_Sq_L2 = sim(a_L1, sq)
a_L1_Sq.draw(kind='field', logarithm=True)
a_L1_Sq_L2.draw(kind='field', logarithm=False)
```

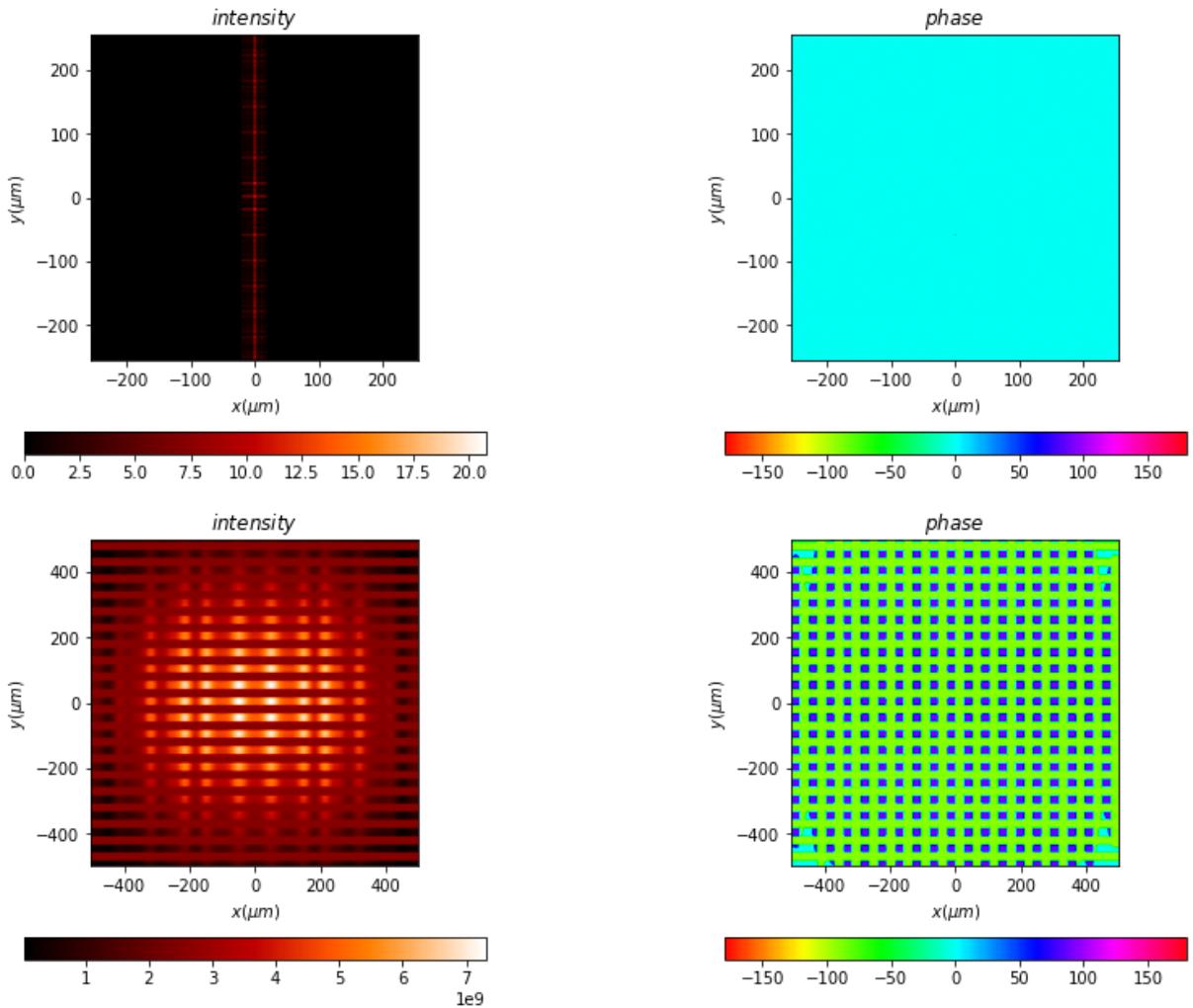
```
Out[17]: ((<matplotlib.image.AxesImage at 0x249d8f9f0d0>,
<matplotlib.image.AxesImage at 0x249dcea9220>),
None,
None)
```



Vertical Slit

```
In [18]: a_L1_Vert, a_L1_Vert_L2 = sim(a_L1, vert)
a_L1_Vert.draw(kind='field', logarithm=True)
a_L1_Vert_L2.draw(kind='field', logarithm=False)
```

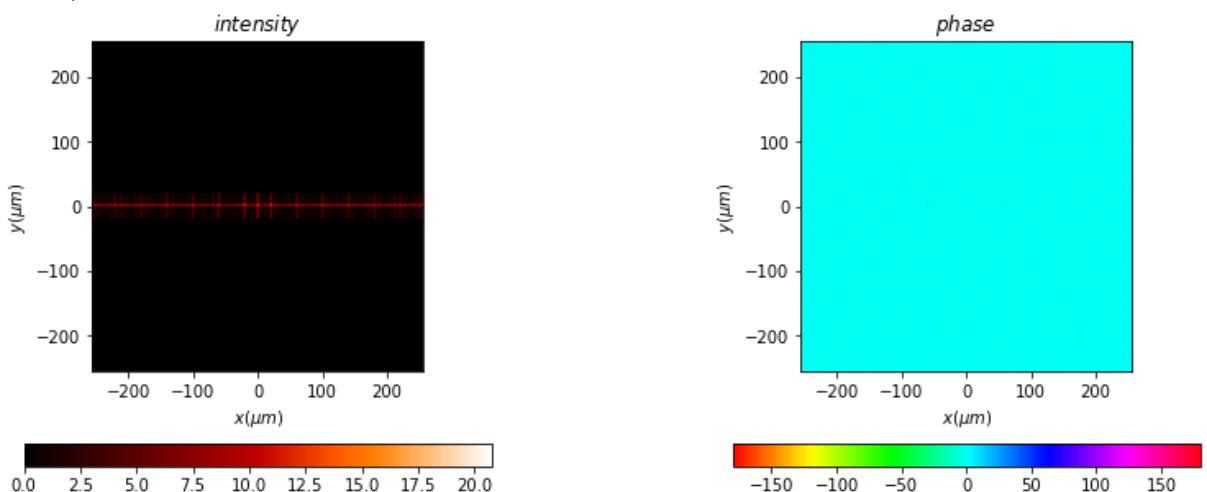
```
Out[18]: ((<matplotlib.image.AxesImage at 0x249de599910>,
    <matplotlib.image.AxesImage at 0x249dbfe10d0>),
None,
None)
```

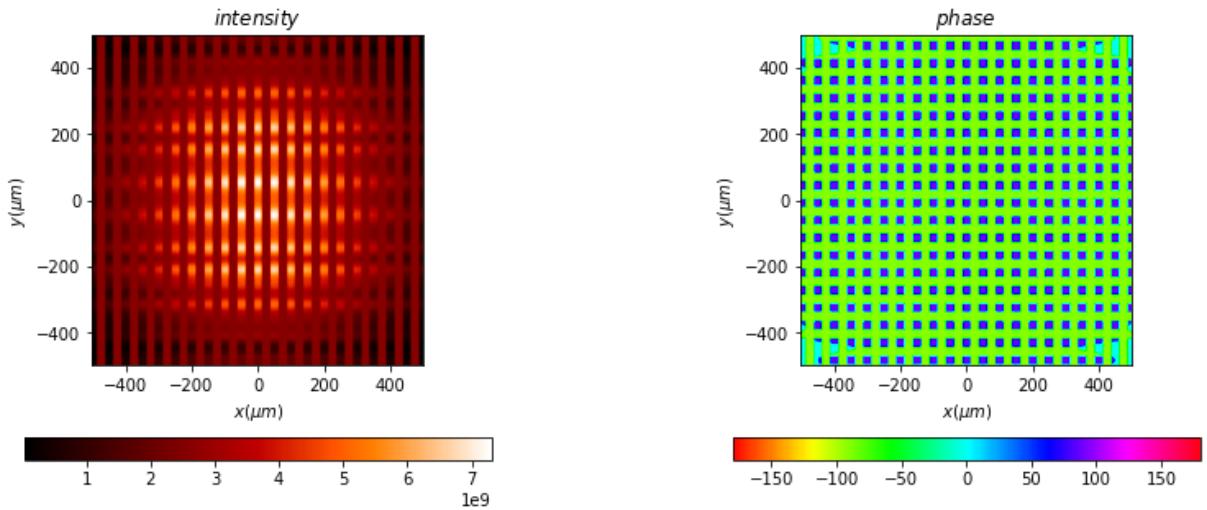


Horizontal Slit

```
In [19]: a_L1_Horiz, a_L1_Horiz_L2 = sim(a_L1, horiz)
a_L1_Horiz.draw(kind='field', logarithm=True)
a_L1_Horiz_L2.draw(kind='field', logarithm=False)
```

```
Out[19]: ((<matplotlib.image.AxesImage at 0x249df20fd30>,
    <matplotlib.image.AxesImage at 0x249df27bfa0>),
None,
None)
```

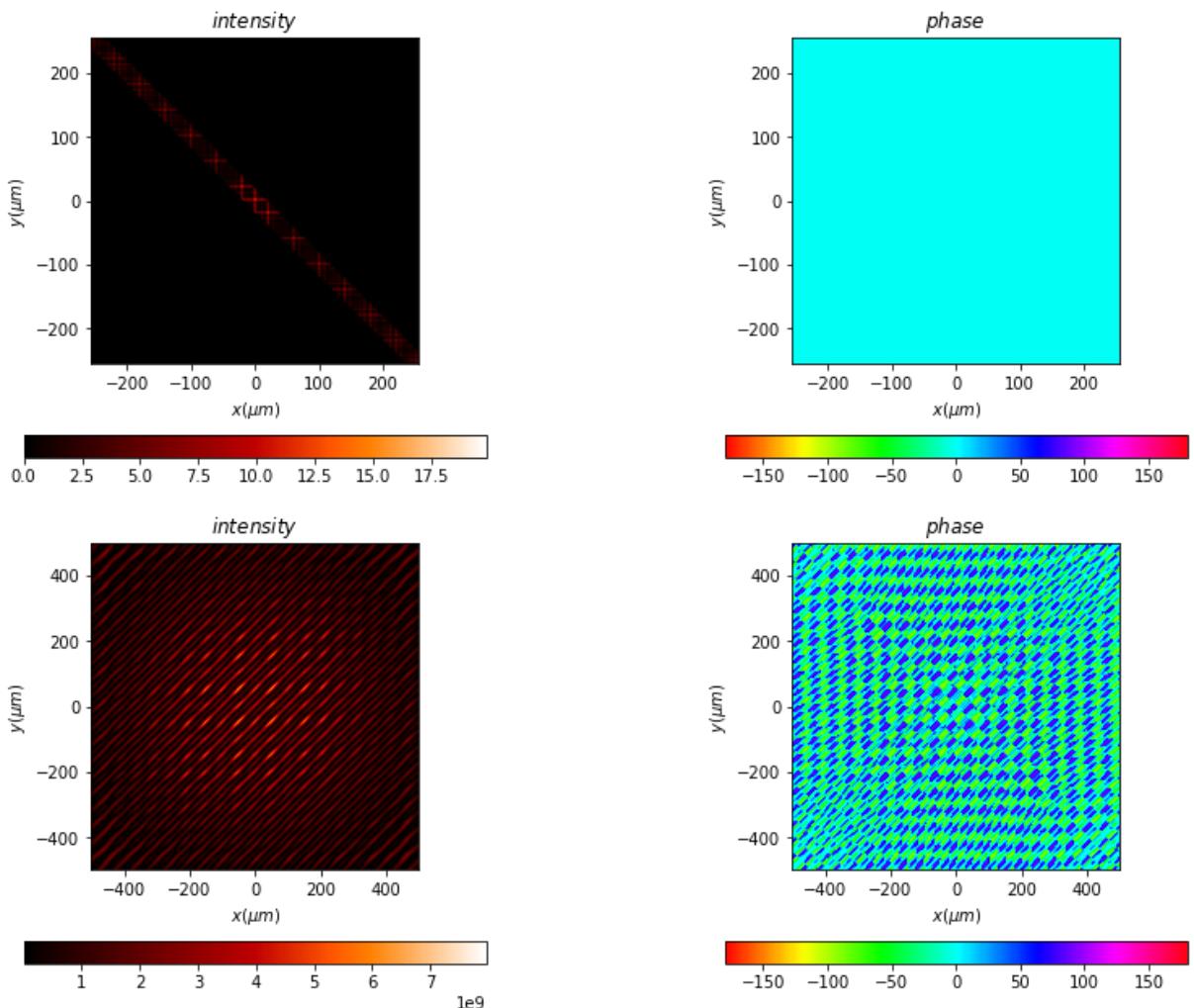




Angled Slit

```
In [20]: a_L1_Angled, a_L1_Angled_L2 = sim(a_L1, angled)
a_L1_Angled.draw(kind='field', logarithm=True)
a_L1_Angled_L2.draw(kind='field', logarithm=False)
```

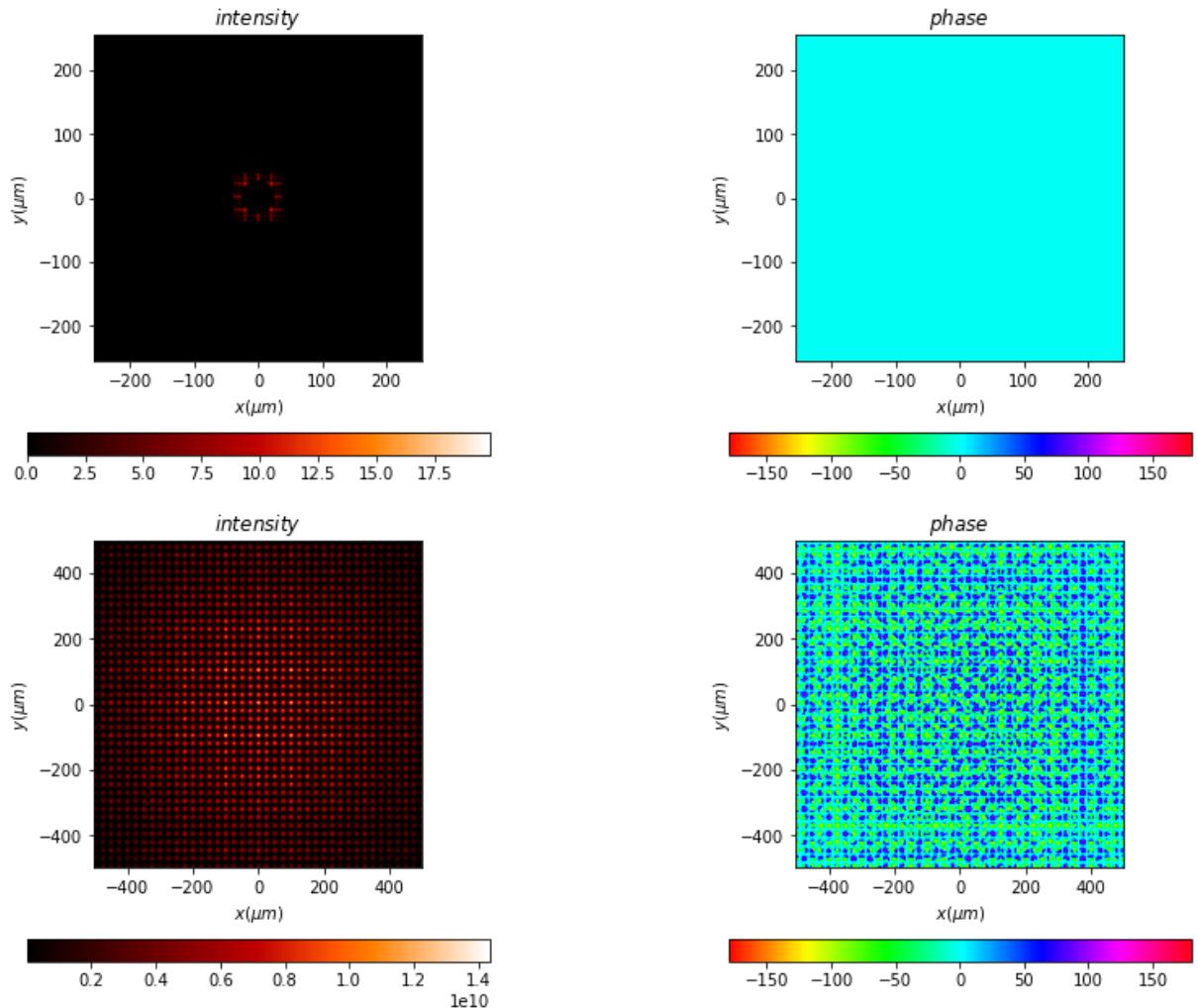
```
Out[20]: (<matplotlib.image.AxesImage at 0x249e117e220>,
<matplotlib.image.AxesImage at 0x249e2a88490>,
None,
None)
```



Square + Circle

```
In [21]: a_L1_SqCirc, a_L1_SqCirc_L2 = sim(a_L1, sqCirc)
a_L1_SqCirc.draw(kind='field', logarithm=True)
a_L1_SqCirc_L2.draw(kind='field', logarithm=False)
```

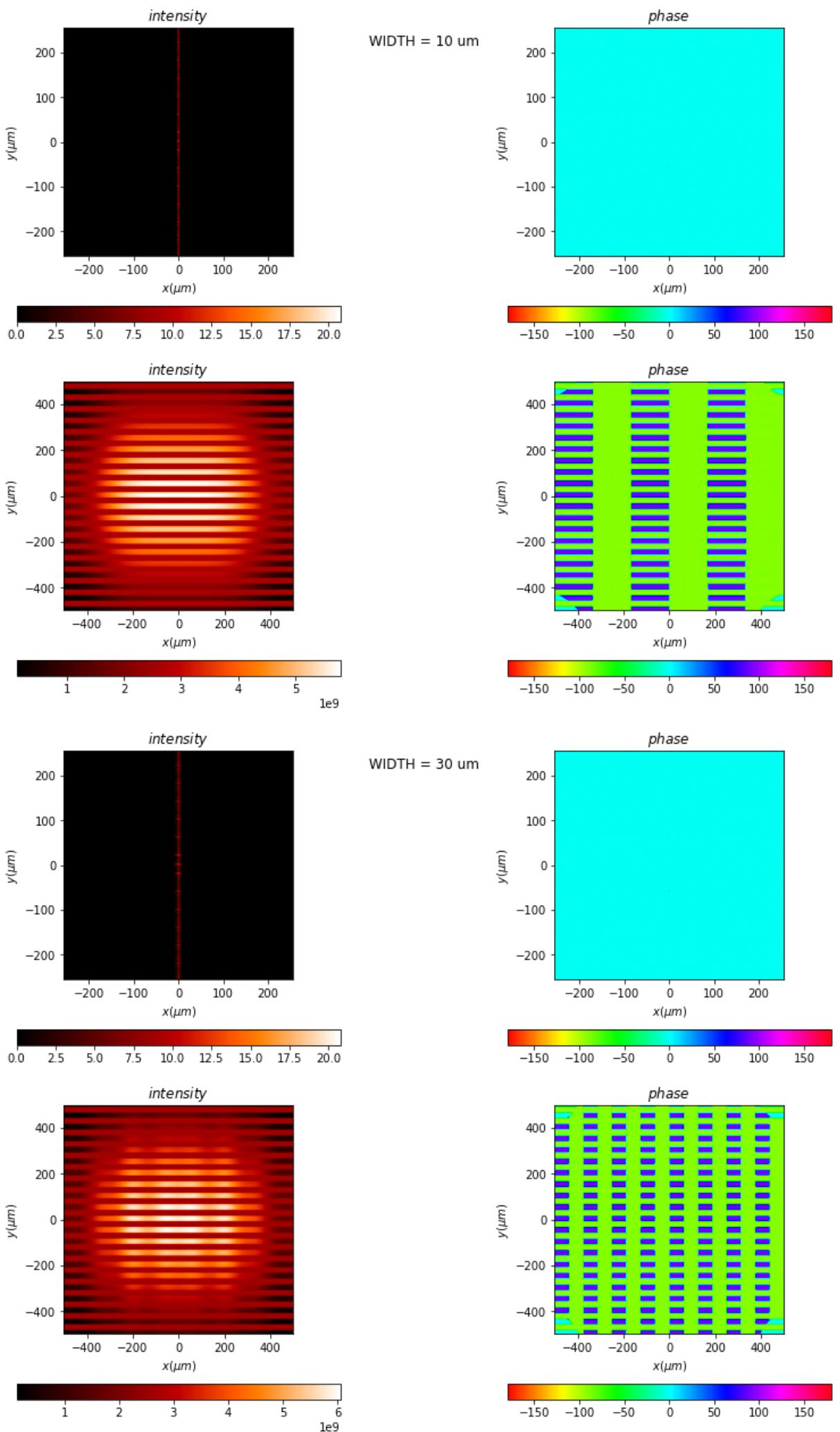
```
Out[21]: ((<matplotlib.image.AxesImage at 0x249dcfb4f0>,
    <matplotlib.image.AxesImage at 0x249dcfc3580>),
None,
None)
```

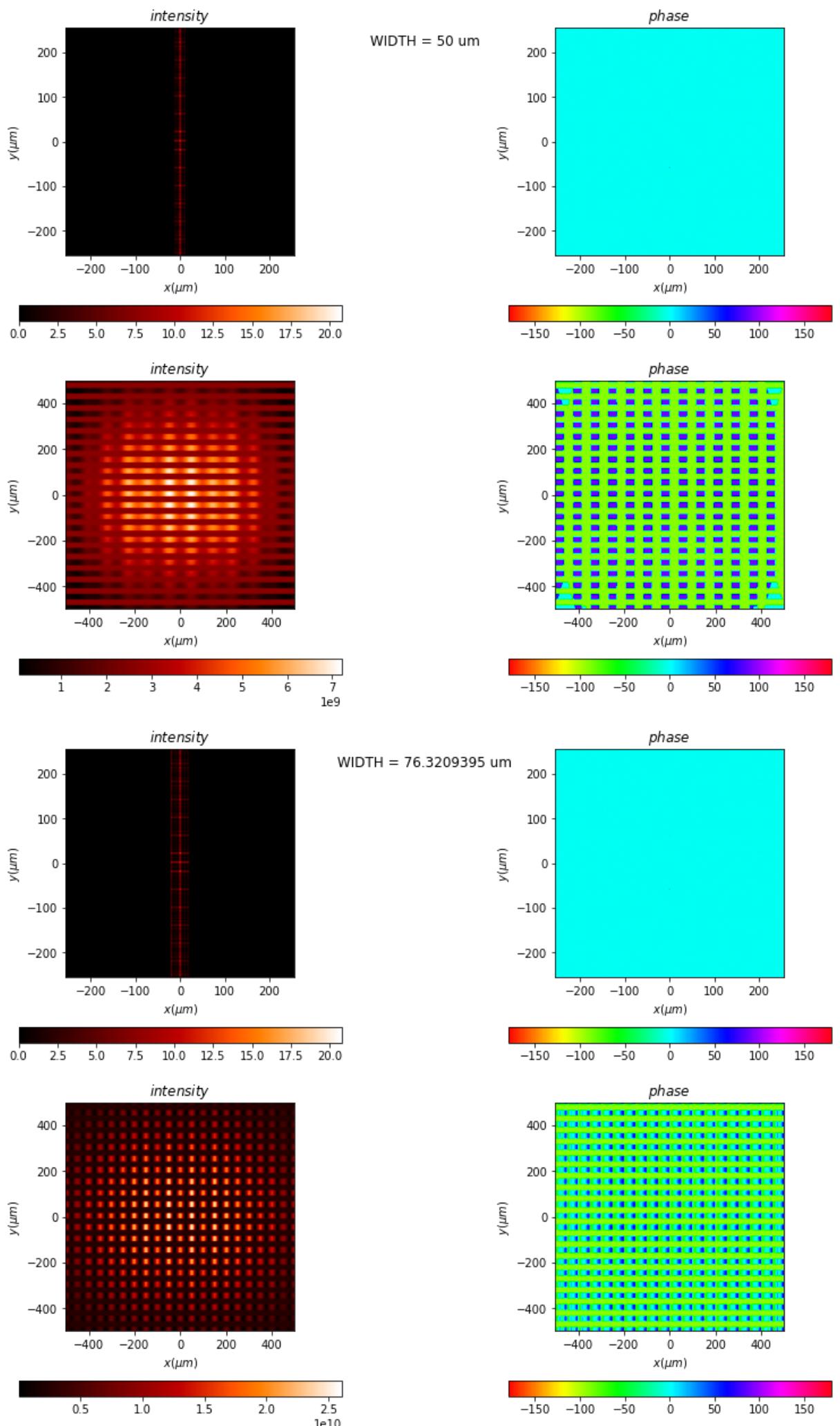


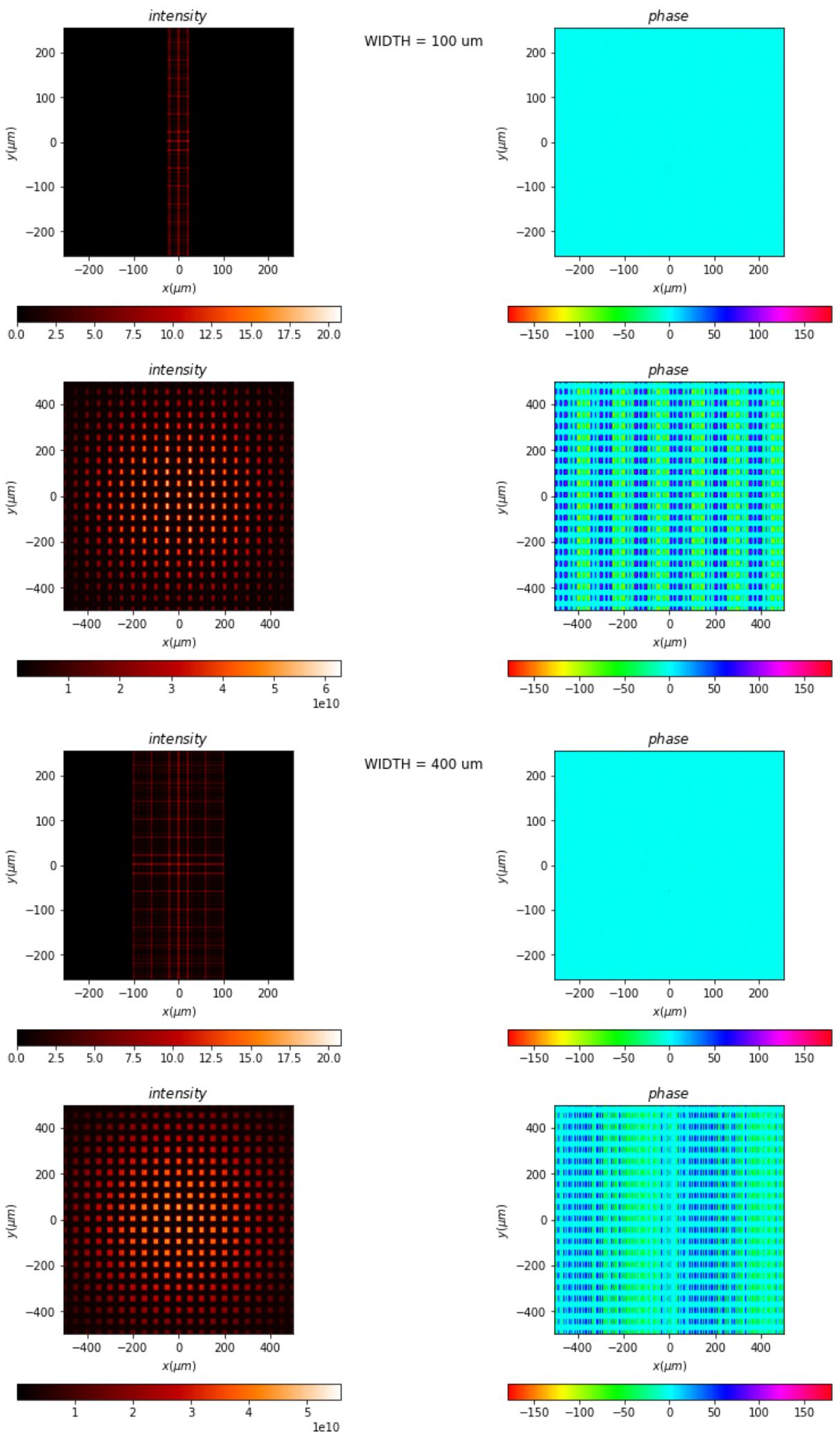
Variable Slit Widths

```
In [22]: widths = [10, 30, 50, 76.3209395, 100, 400] # in um
for width in widths:
    varSlit = Scalar_mask_XY(x0, y0, wavelength)
    varSlit.slit(
        x0=0 * um,
        size=width * um
    )
#    varSlit.draw(kind='field', logarithm=True)

    a_L1_VarSlit, a_L1_VarSlit_L2 = sim(a_L1, varSlit)
    a_L1_VarSlit.draw(title=f" WIDTH = {width} um ", kind='field', logarithm=True)
    a_L1_VarSlit_L2.draw(kind='field', logarithm=False)
```







Half-tone Image - Low & High-pass Filtering and Edge Enhancement / Dark-Field Illumination

Compare results with figures in Eisenkraft (1977)

```
In [1]: import numpy as np
from diffractio import mm, um, degrees
from diffractio.scalar_sources_XY import Scalar_source_XY
from diffractio.scalar_masks_XY import Scalar_mask_XY

# Setting up
length = 1 * mm
num_data = 512
x0 = np.linspace(-length / 2, length / 2, num_data)
y0 = np.linspace(-length / 2, length / 2, num_data)
wavelength = 0.633 * um
```

number of processors: 12

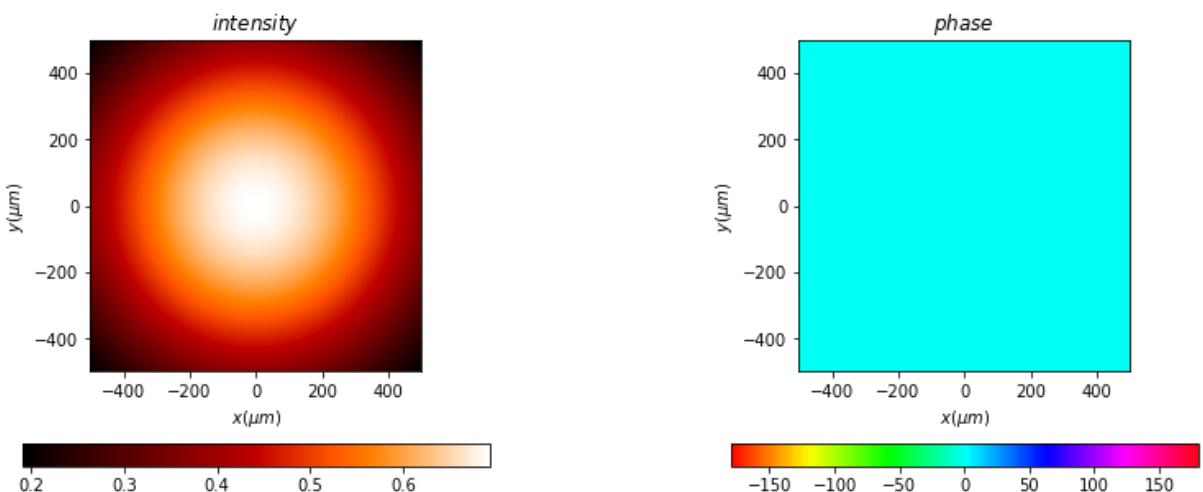
Setting up source(s)

- Gaussian Beam (LASER)
- Experiments (Either only requires modification in filter shapes)
 - Plane Wave
 - Spherical Wave

```
In [2]: # Gaussian Beam Source - like a LASER
u0 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)

u0.gauss_beam(r0=(0, 0), w0=(800 * um, 800 * um), z0=0.0)
u0.draw(kind='field', logarithm=True)
```

```
Out[2]: ((<matplotlib.image.AxesImage at 0x2c0a2a9daf0>,
<matplotlib.image.AxesImage at 0x2c0a2d3d2b0>),
None,
None)
```



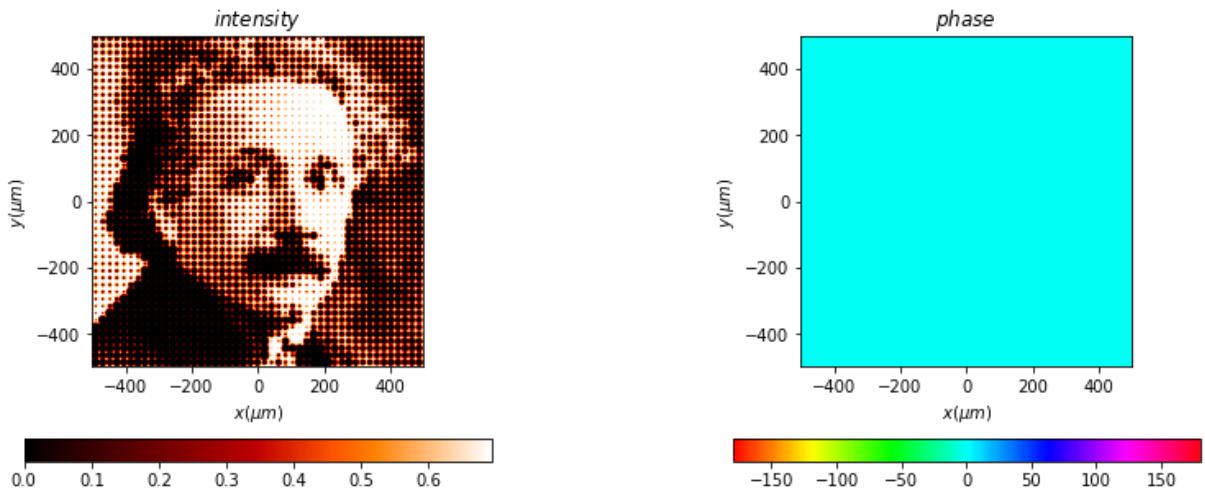
```
In [3]: # # Plane Wave Source
# u1 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
# u1.plane_wave()
# u1.draw(kind='field', logarithm=True)
```

```
In [4]: # # Spherical Wave Source
# u2 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
# u2.spherical_wave(z0=1, mask=False)
# u2.draw(kind='field', logarithm=True)
```

Image

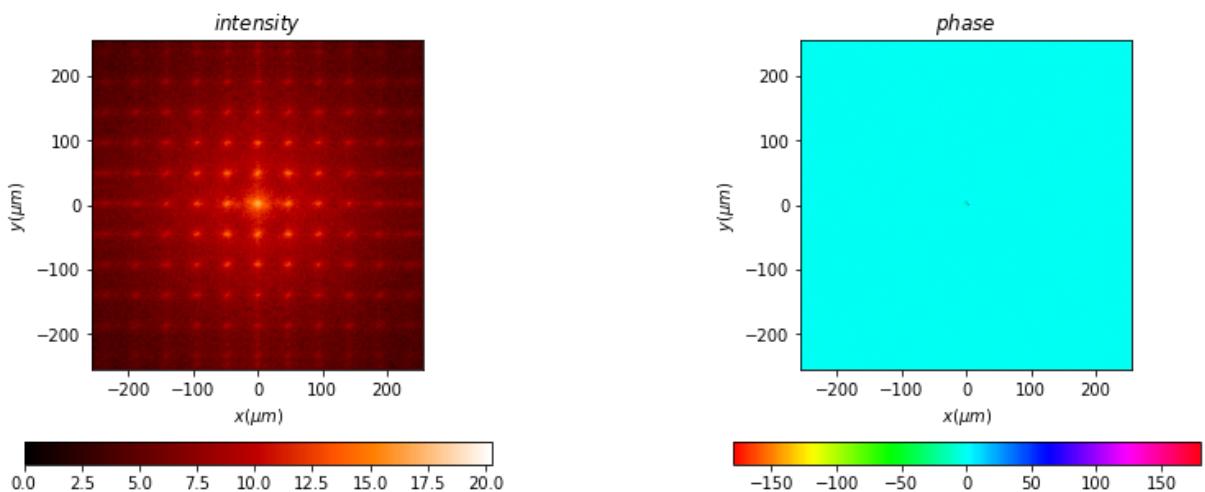
```
In [5]: y15 = Scalar_mask_XY(x0, y0, wavelength)
y15.image(
    filename="y-15-HT.png",
    normalize=True,
    canal=2,
)
y15.draw(kind='field', logarithm=True)
```

```
Out[5]: ((<matplotlib.image.AxesImage at 0x2c0a313e520>,
<matplotlib.image.AxesImage at 0x2c0a37bfca0>),
None,
None)
```



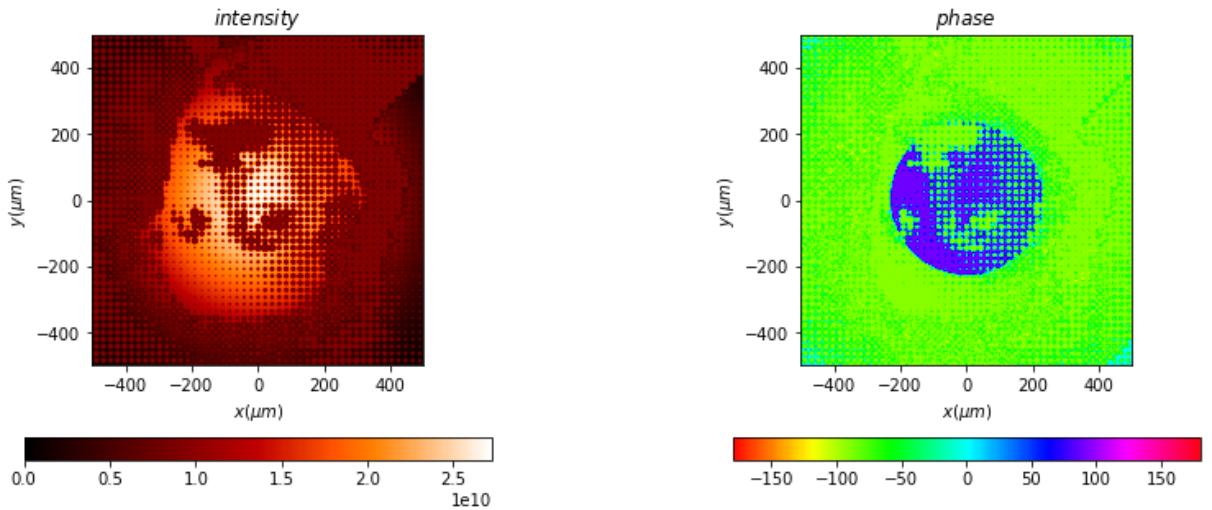
```
In [6]: # Fourier Plane - No Filter
a_L1 = (u0 * y15).fft(z=1 * mm, new_field=True)
a_L1.draw(kind='field', logarithm=True)
```

```
Out[6]: ((<matplotlib.image.AxesImage at 0x2c0a384fc40>,
<matplotlib.image.AxesImage at 0x2c0a3922430>),
None,
None)
```



```
In [7]: # This is how, it'd look without any filter, at the Observation screen
a_L2 = a_L1.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
a_L2.draw(kind='field', logarithm=False)
```

```
Out[7]: ((<matplotlib.image.AxesImage at 0x2c0a3e44310>,
<matplotlib.image.AxesImage at 0x2c0a3e93ac0>),
None,
None)
```

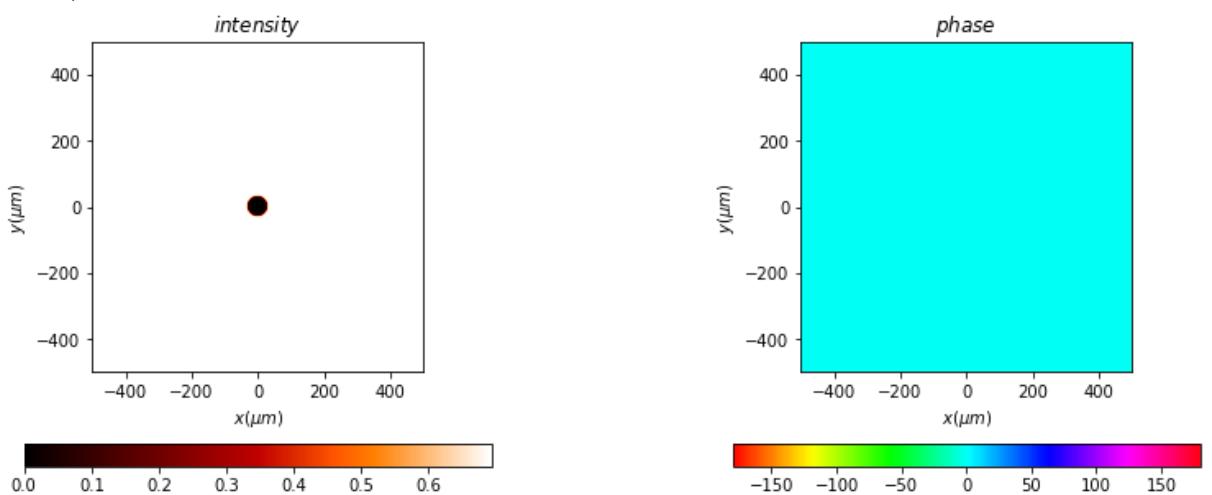


Masks / Filters

- Center Dot - High Pass
- Square - Low Pass
- Square + Center Dot -
- Vertical Slit
- Horizontal Slit
- Angled Slit

```
In [8]: cDot = Scalar_mask_XY(x0, y0, wavelength)
cDot.ring(
    r0=(0 * um, 0 * um),
    radius1=(30 * um, 30 * um),
    radius2=(1000 * um, 1000 * um)
)
cDot.draw(kind='field', logarithm=True)
```

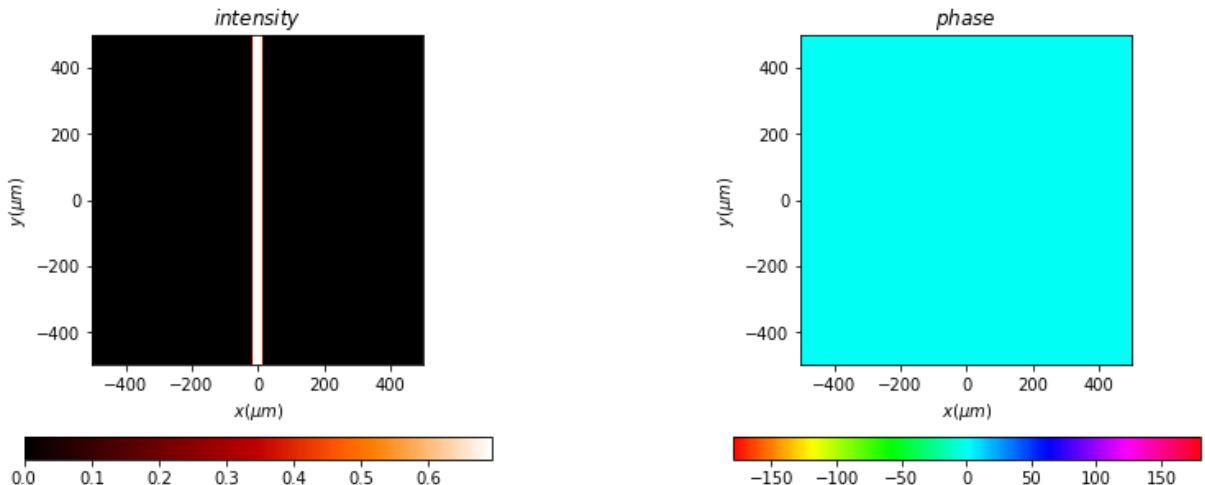
```
Out[8]: (<matplotlib.image.AxesImage at 0x2c0a7d6dc40>,
          <matplotlib.image.AxesImage at 0x2c0a7e04430>,
          None,
          None)
```



```
In [9]: vert = Scalar_mask_XY(x0, y0, wavelength)
vert.slit(
    x0=0 * um,
    size=30 * um
)
vert.draw(kind='field', logarithm=True)
```

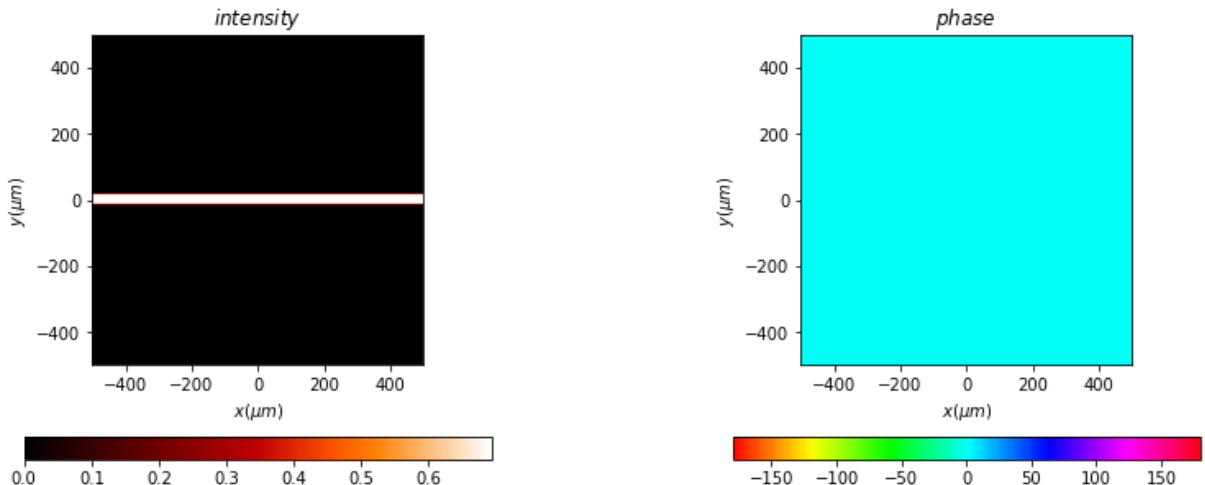
```
Out[9]: (<matplotlib.image.AxesImage at 0x2c0a7d2fb80>,
```

```
<matplotlib.image.AxesImage at 0x2c0a30a7970>),
None,
None)
```



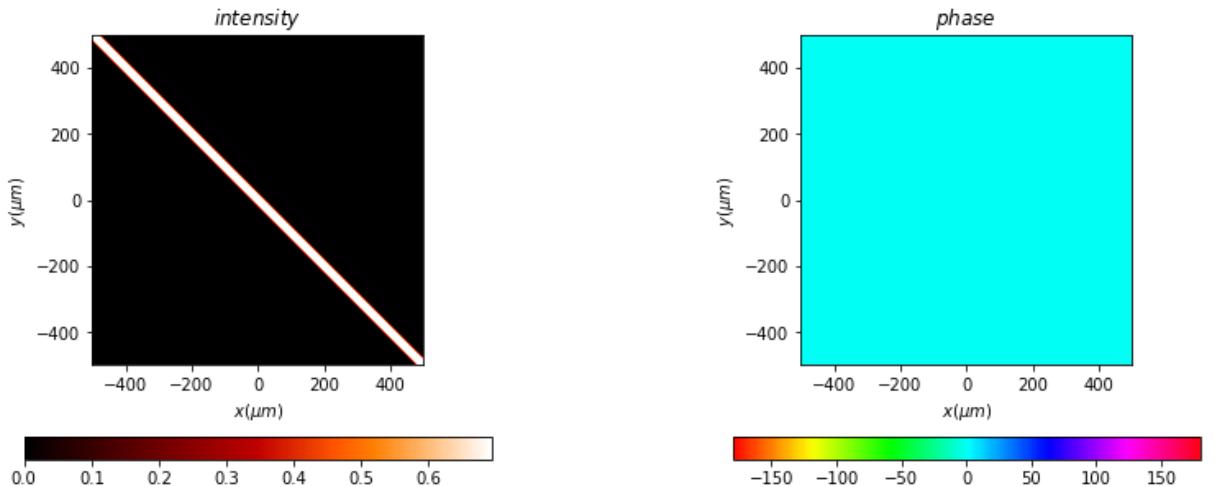
```
In [10]: horiz = Scalar_mask_XY(x0, y0, wavelength)
horiz.slit(
    x0=0 * um,
    size=30 * um,
    angle=np.pi / 2
)
horiz.draw(kind='field', logarithm=True)
```

```
Out[10]: (<matplotlib.image.AxesImage at 0x2c0a8de2730>,
<matplotlib.image.AxesImage at 0x2c0a8e6ceb0>),
None,
None)
```



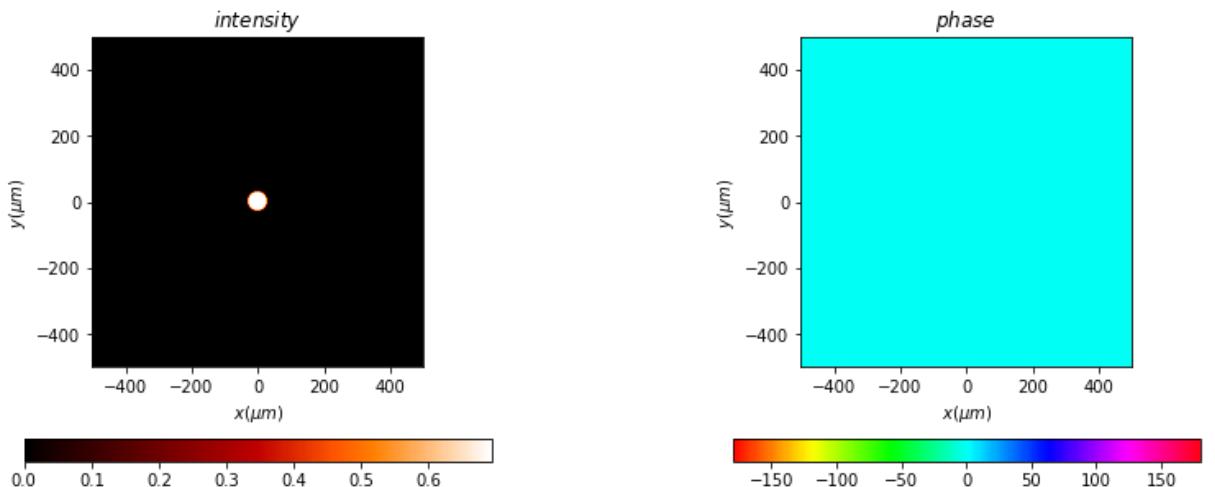
```
In [11]: angled = Scalar_mask_XY(x0, y0, wavelength)
angled.slit(
    x0=0 * um,
    size=30 * um,
    angle=np.pi / 4
)
angled.draw(kind='field', logarithm=True)
```

```
Out[11]: (<matplotlib.image.AxesImage at 0x2c0aa1de160>,
<matplotlib.image.AxesImage at 0x2c0aa22e940>),
None,
None)
```



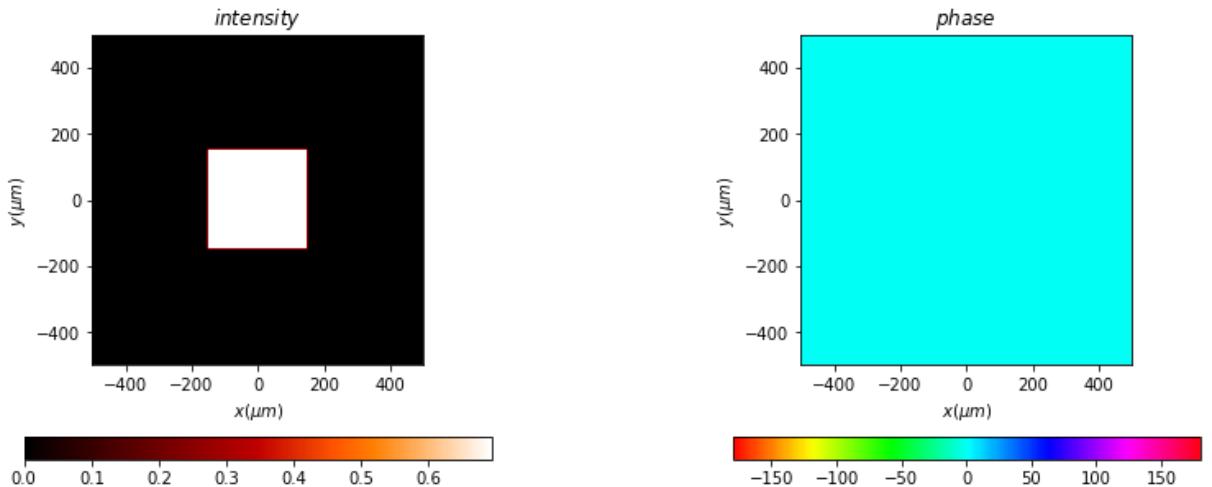
```
In [12]: circ = Scalar_mask_XY(x0, y0, wavelength)
circ.circle(
    r0=(0 * um, 0 * um),
    radius=(30 * um, 30 * um),
    angle=0
)
circ.draw(kind='field', logarithm=True)
```

```
Out[12]: (<matplotlib.image.AxesImage at 0x2c0aa304d00>,
<matplotlib.image.AxesImage at 0x2c0aa372880>,
None,
None)
```



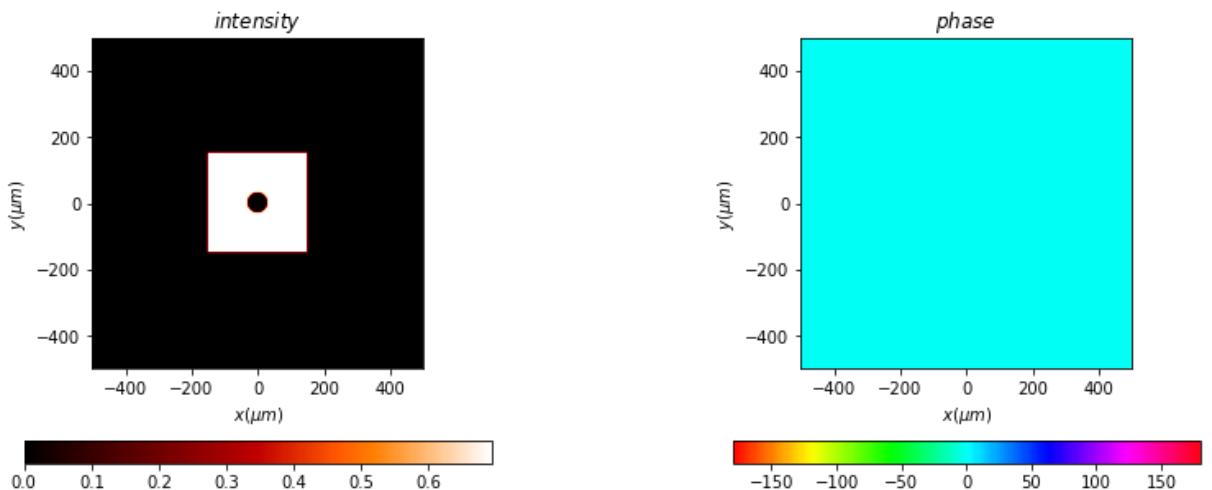
```
In [13]: sq = Scalar_mask_XY(x0, y0, wavelength)
sq.square(
    r0=(0 * um, 0 * um),
    size=(300 * um, 300 * um),
    angle=0,
)
sq.draw(kind='field', logarithm=True)
```

```
Out[13]: (<matplotlib.image.AxesImage at 0x2c0aae98c10>,
<matplotlib.image.AxesImage at 0x2c0aaefde80>,
None,
None)
```



```
In [14]: # Adding two filters
sqCirc = sq * cDot
sqCirc.draw(kind="field", logarithm=True)
```

```
Out[14]: (<matplotlib.image.AxesImage at 0x2c0aae94a60>,
<matplotlib.image.AxesImage at 0x2c0a8dc96a0>,
None,
None)
```



Returns wave after encountering filter and then L2

```
In [15]: def sim(a_L1, mask):
    """
    a_L1: Wave after passing through Lens 1
    mask: Mask or Filter to apply

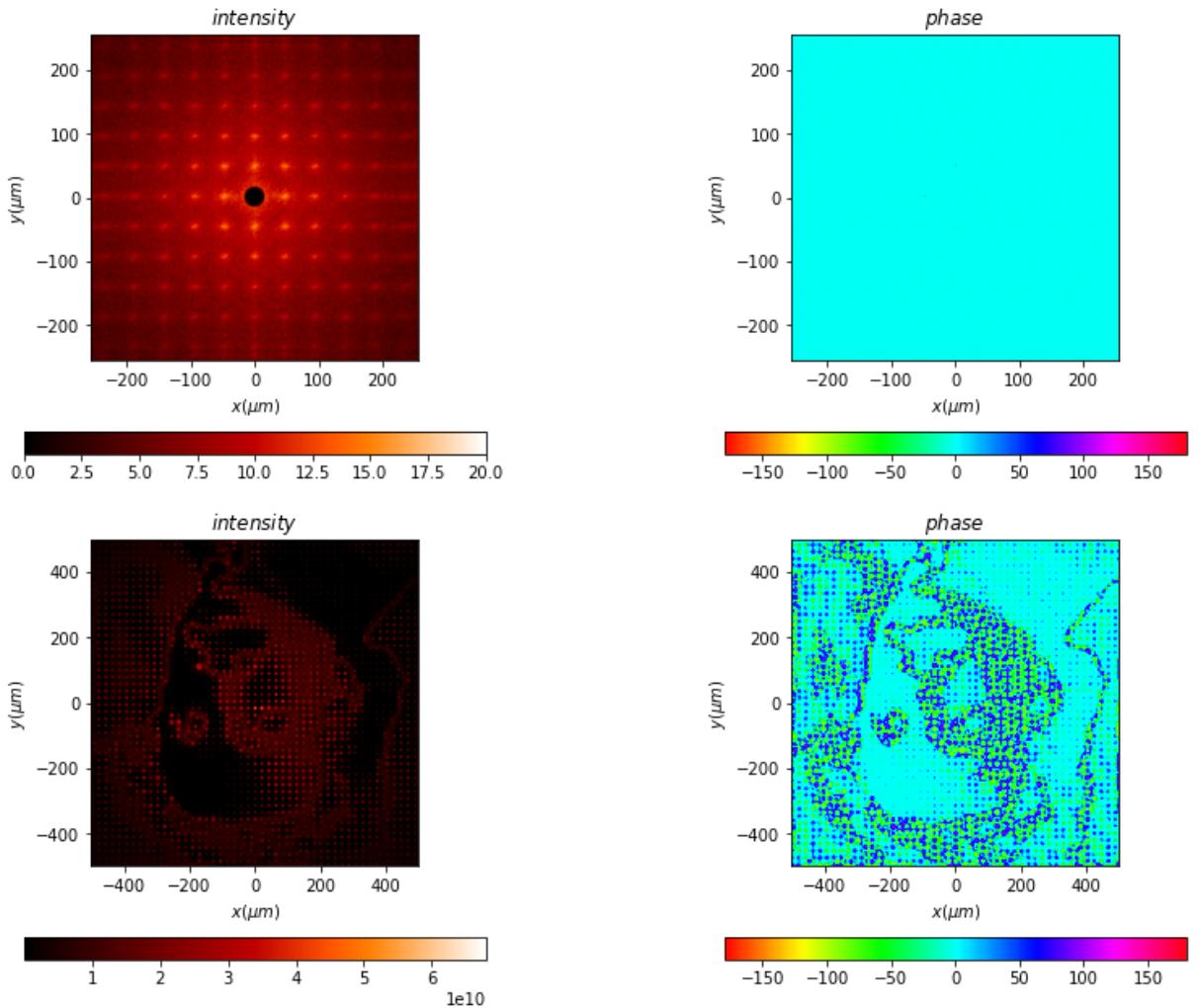
    """
    a_L1_Mask = a_L1 * mask
    a_L1_Mask_L2 = a_L1_Mask.fft(z=1 * mm, shift=False, remove0=False, new_field=True)

    return a_L1_Mask, a_L1_Mask_L2
```

Center Dot - High Pass - HT Structure Visible - EDGE DETECTION

```
In [16]: a_L1_cD, a_L1_cD_L2 = sim(a_L1, cDot)
a_L1_cD.draw(kind='field', logarithm=True)
a_L1_cD_L2.draw(kind='field', logarithm=False)
```

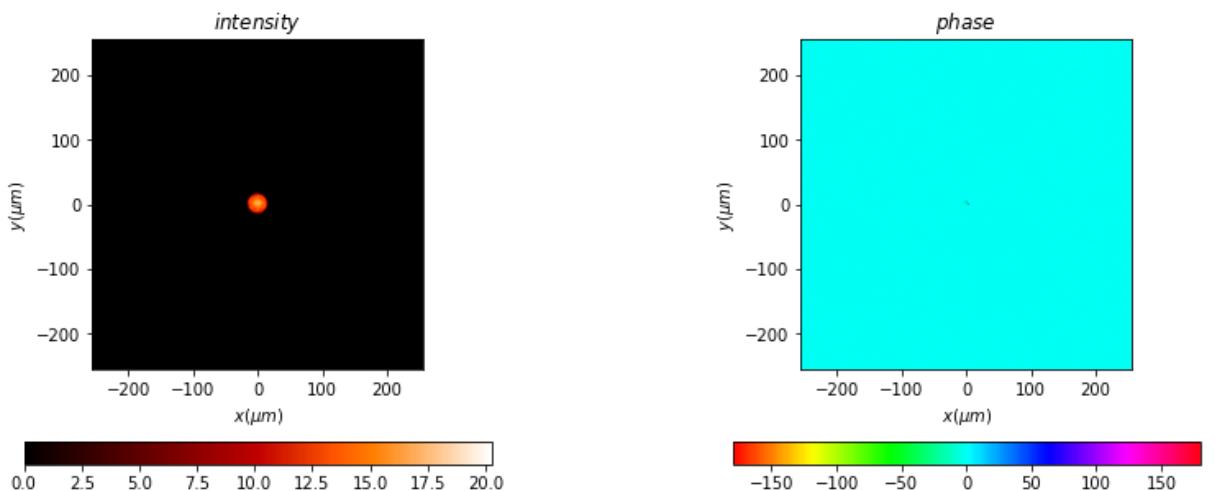
```
Out[16]: (<matplotlib.image.AxesImage at 0x2c0ac627f10>,
<matplotlib.image.AxesImage at 0x2c0ac69d700>,
None,
None)
```

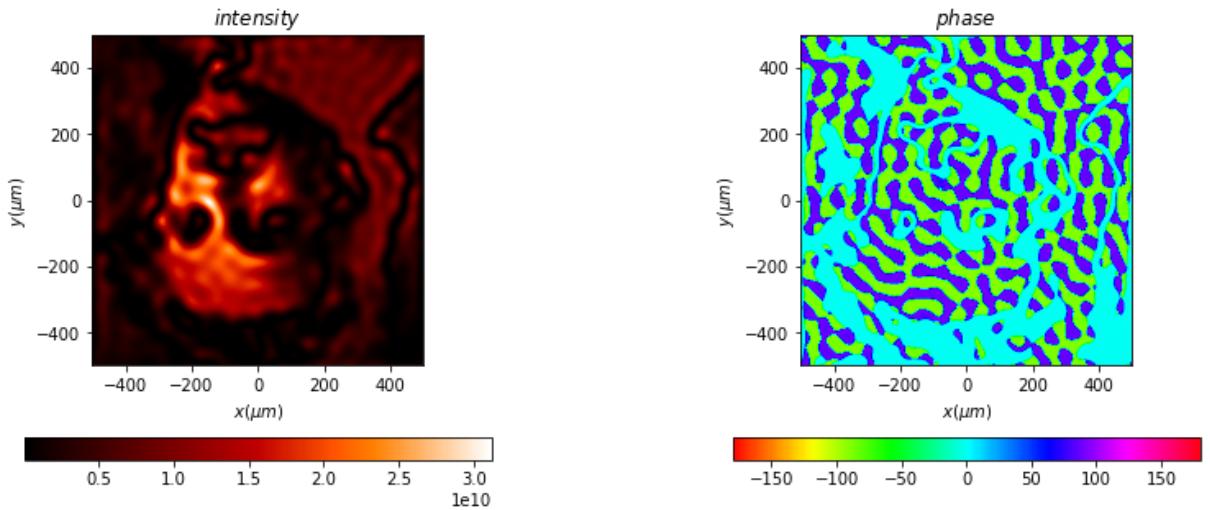


Circle - Low Pass - Blurred Output

```
In [17]: a_L1_Circ, a_L1_Circ_L2 = sim(a_L1, circ)
a_L1_Circ.draw(kind='field', logarithm=True)
a_L1_Circ_L2.draw(kind='field', logarithm=False)
```

```
Out[17]: (<matplotlib.image.AxesImage at 0x2c0ae2eedf0>,
<matplotlib.image.AxesImage at 0x2c0b1ef8130>),
None,
None)
```

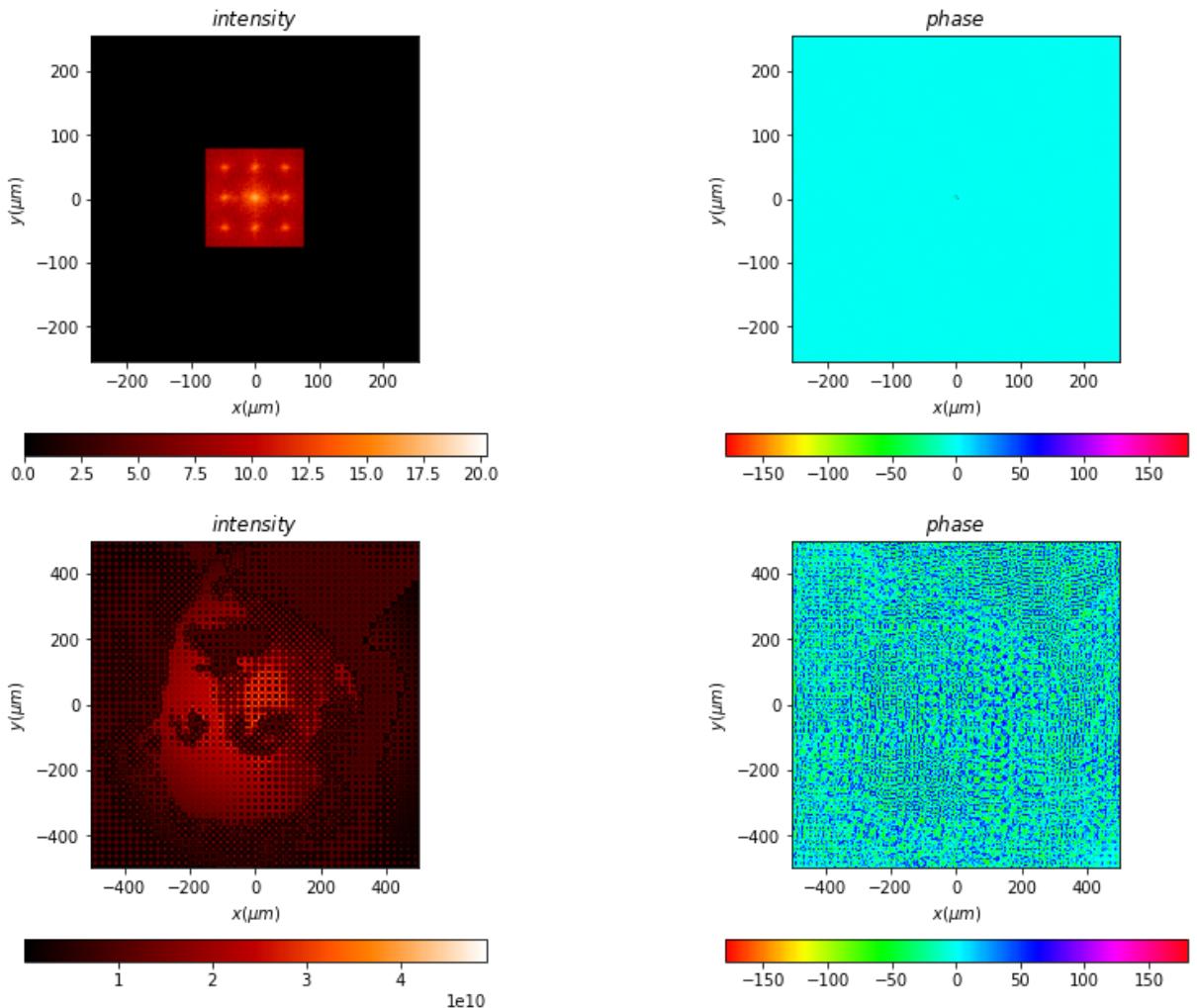




Square

```
In [18]: a_L1_Sq, a_L1_Sq_L2 = sim(a_L1, sq)
a_L1_Sq.draw(kind='field', logarithm=True)
a_L1_Sq_L2.draw(kind='field', logarithm=False)
```

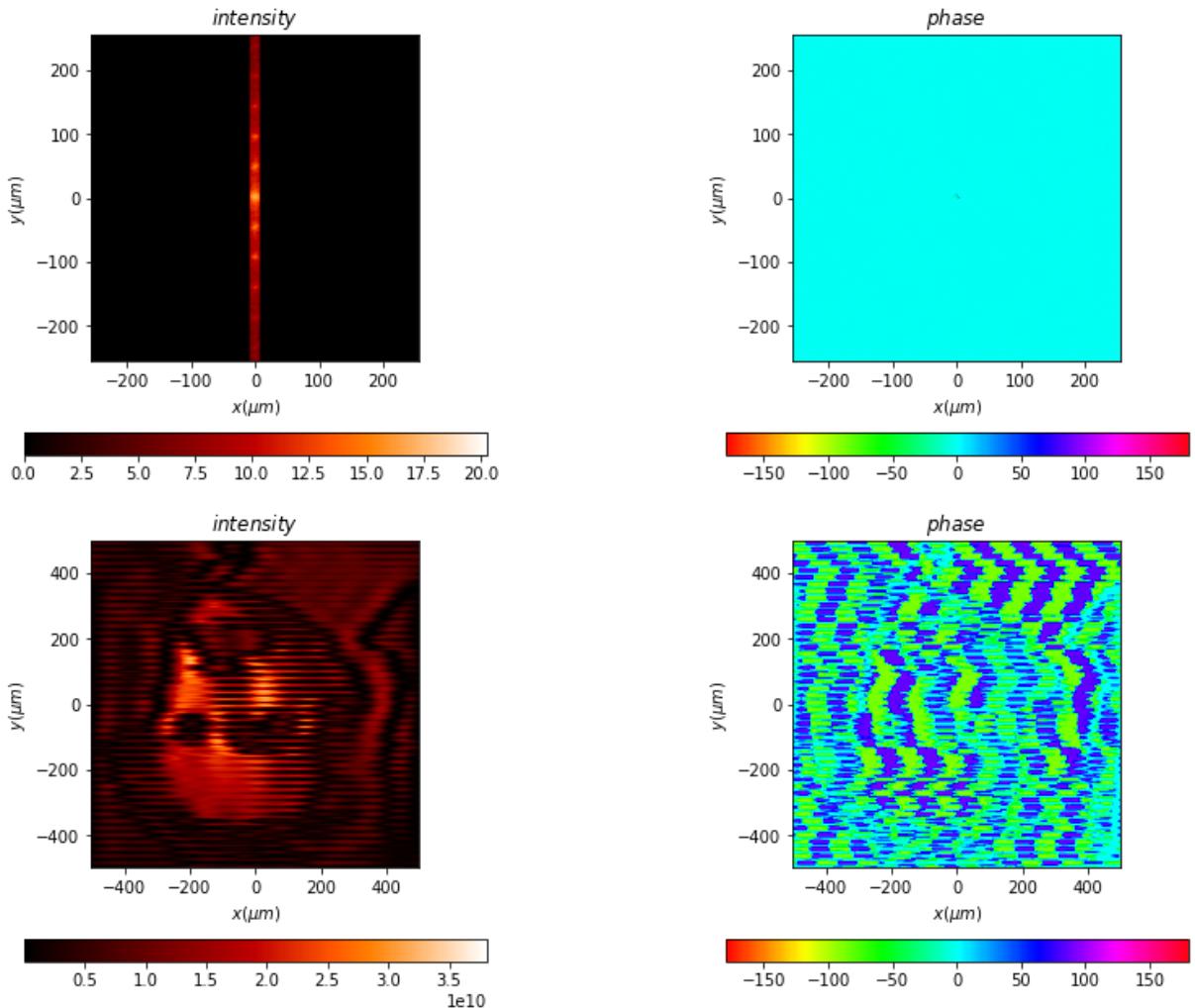
```
Out[18]: ((<matplotlib.image.AxesImage at 0x2c0b1c24a90>,
 <matplotlib.image.AxesImage at 0x2c0b1a80fd0>),
None,
None)
```



Vertical Slit

```
In [19]: a_L1_Vert, a_L1_Vert_L2 = sim(a_L1, vert)
a_L1_Vert.draw(kind='field', logarithm=True)
a_L1_Vert_L2.draw(kind='field', logarithm=False)
```

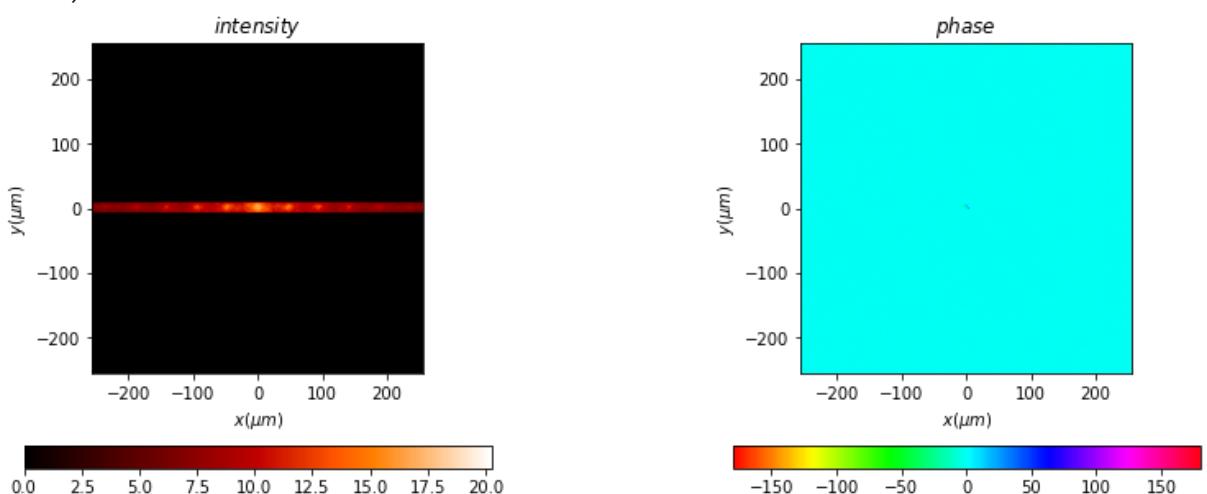
```
Out[19]: ((<matplotlib.image.AxesImage at 0x2c0ac560be0>,
    <matplotlib.image.AxesImage at 0x2c0ae248880>),
None,
None)
```

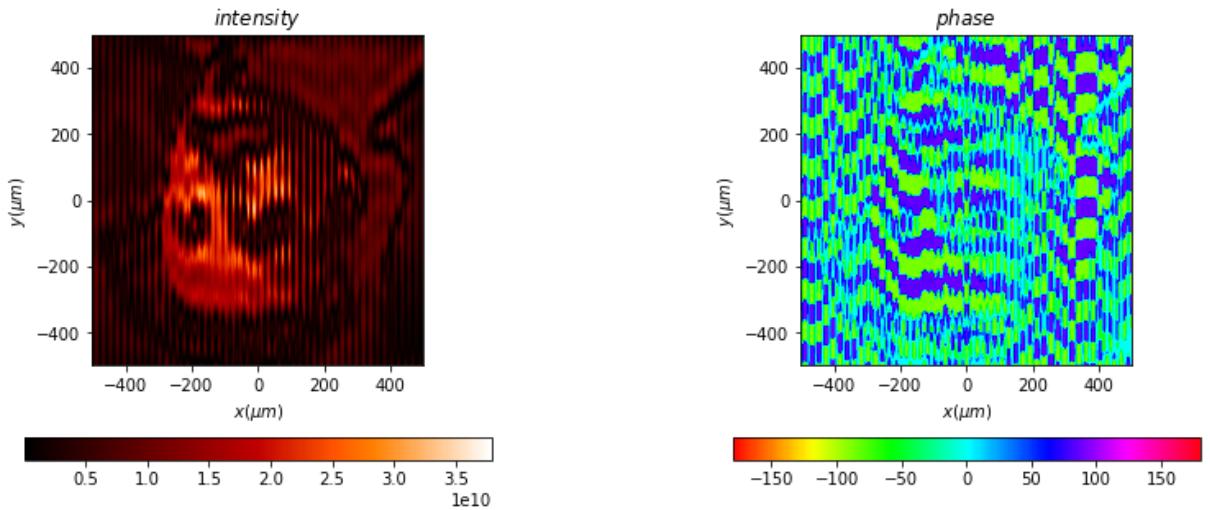


Horizontal Slit

```
In [20]: a_L1_Horiz, a_L1_Horiz_L2 = sim(a_L1, horiz)
a_L1_Horiz.draw(kind='field', logarithm=True)
a_L1_Horiz_L2.draw(kind='field', logarithm=False)
```

```
Out[20]: ((<matplotlib.image.AxesImage at 0x2c0b48461f0>,
    <matplotlib.image.AxesImage at 0x2c0b48af460>),
None,
None)
```

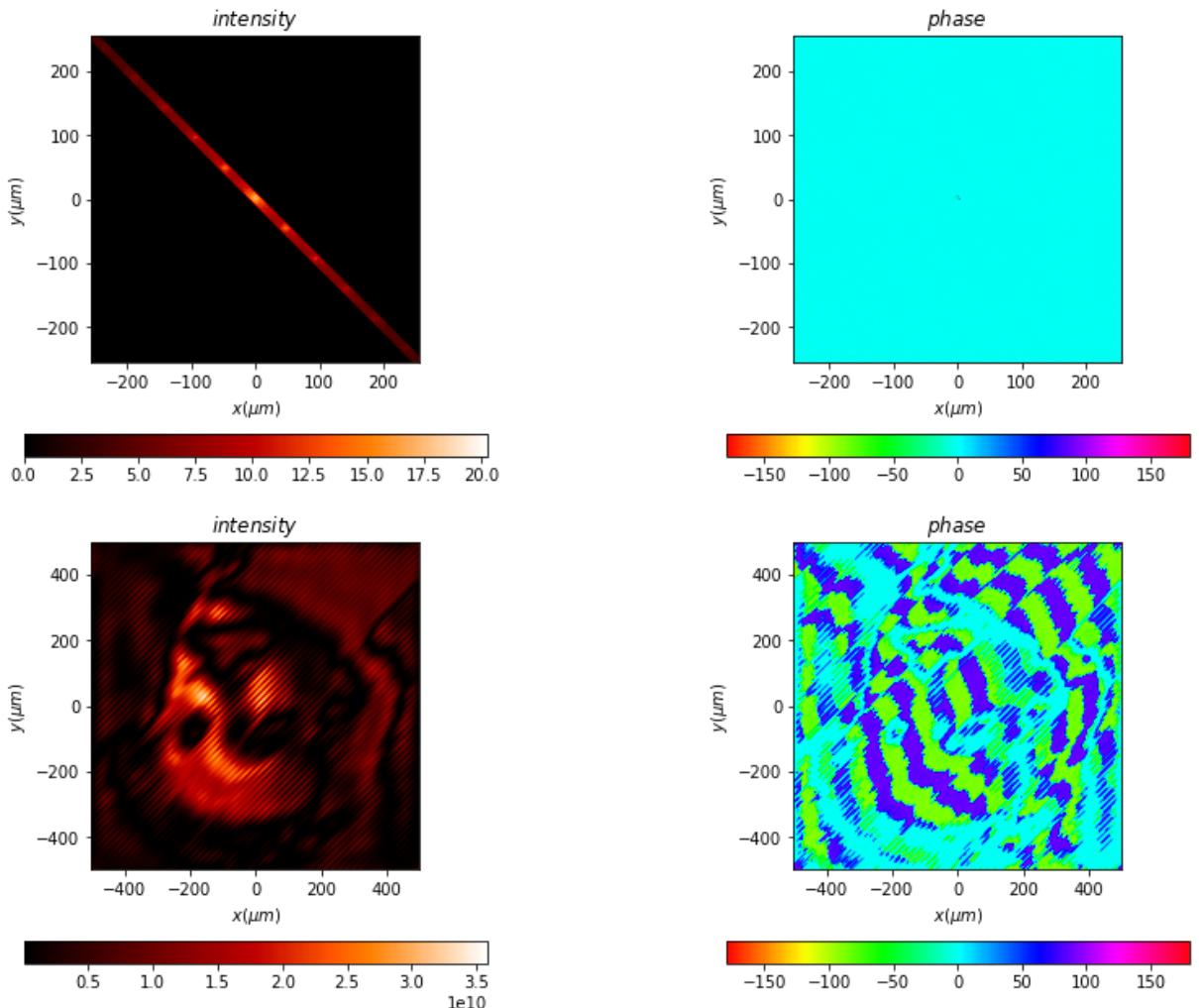




Angled Slit

```
In [21]: a_L1_Angled, a_L1_Angled_L2 = sim(a_L1, angled)
a_L1_Angled.draw(kind='field', logarithm=True)
a_L1_Angled_L2.draw(kind='field', logarithm=False)
```

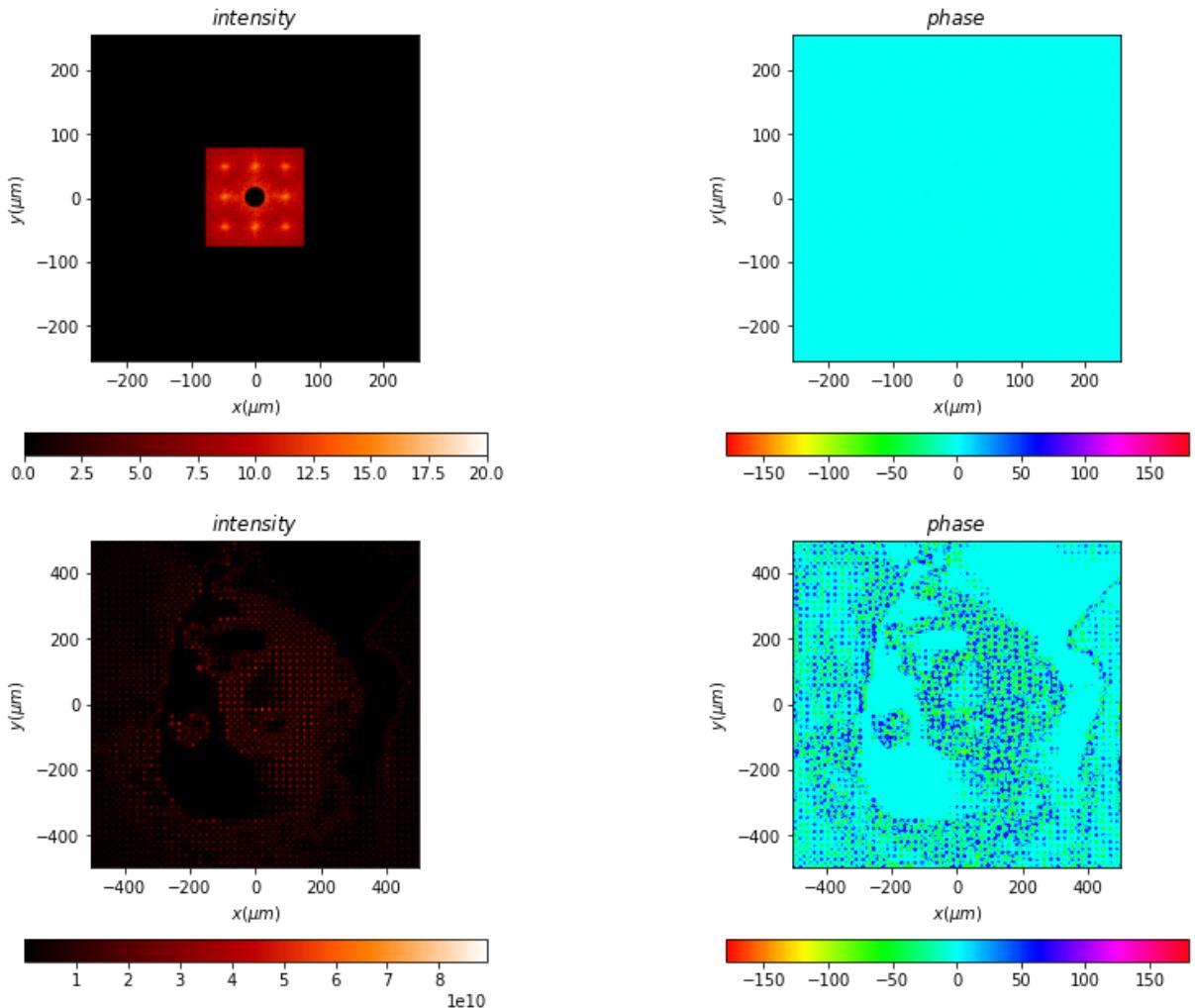
```
Out[21]: (<matplotlib.image.AxesImage at 0x2c0b4f0e6a0>,
<matplotlib.image.AxesImage at 0x2c0b7a1a910>,
None,
None)
```



Square + Circle - Dark-Field Illumination / Edge Enhancement

```
In [22]: a_L1_SqCirc, a_L1_SqCirc_L2 = sim(a_L1, sqCirc)
a_L1_SqCirc.draw(kind='field', logarithm=True)
a_L1_SqCirc_L2.draw(kind='field', logarithm=False)
```

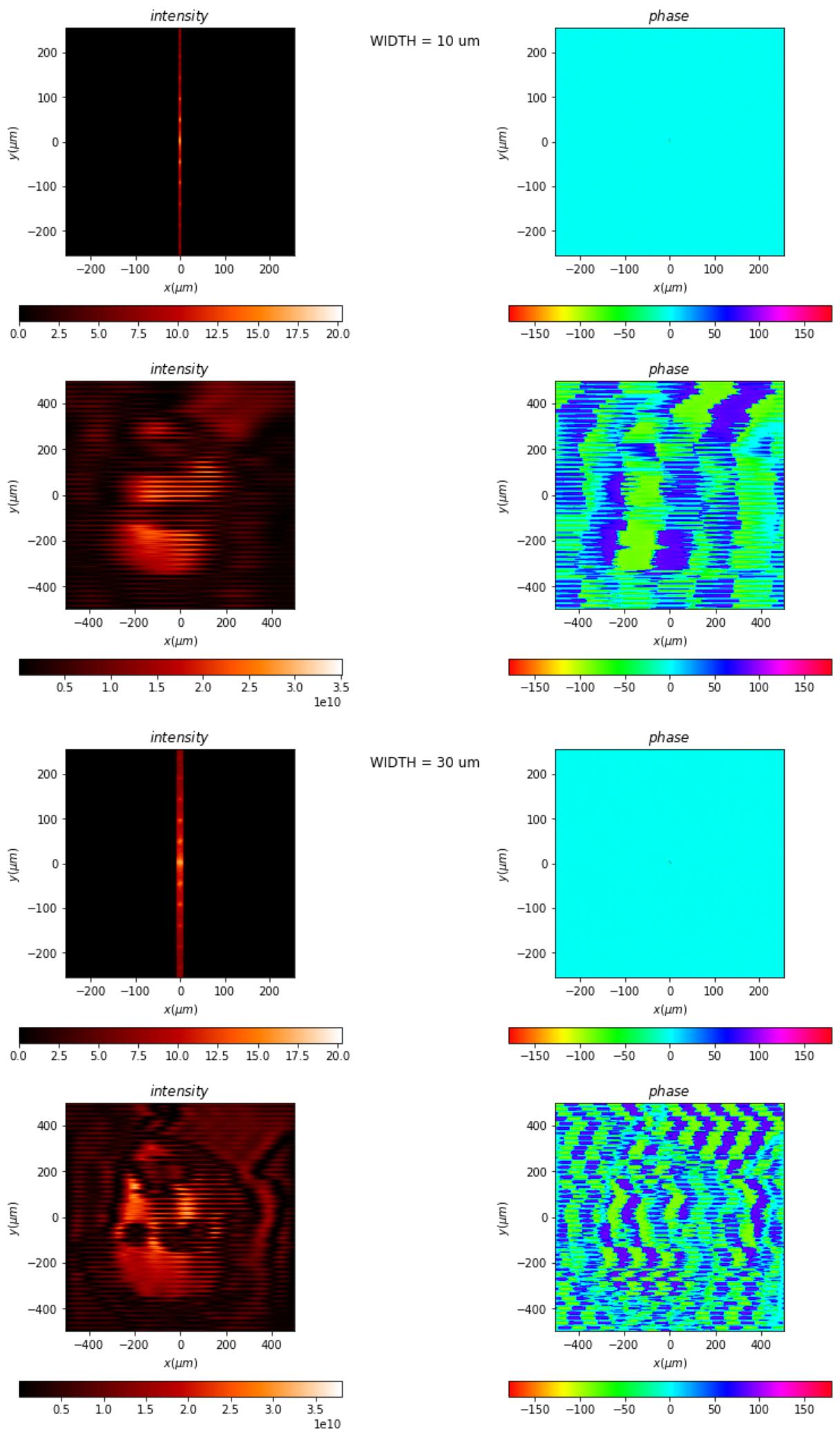
```
Out[22]: ((<matplotlib.image.AxesImage at 0x2c0ac53f4f0>,
    <matplotlib.image.AxesImage at 0x2c0b1a87fa0>),
None,
None)
```

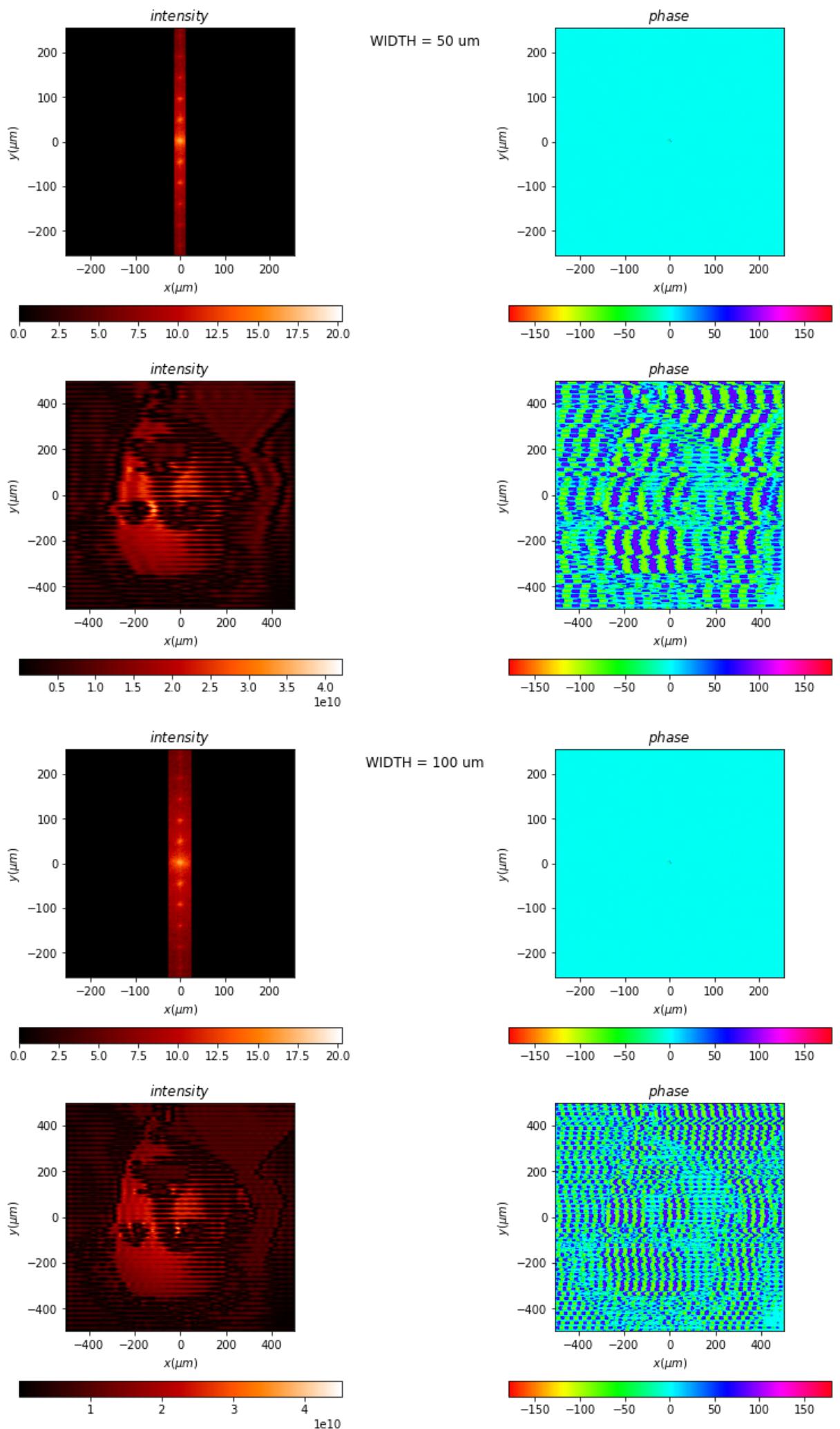


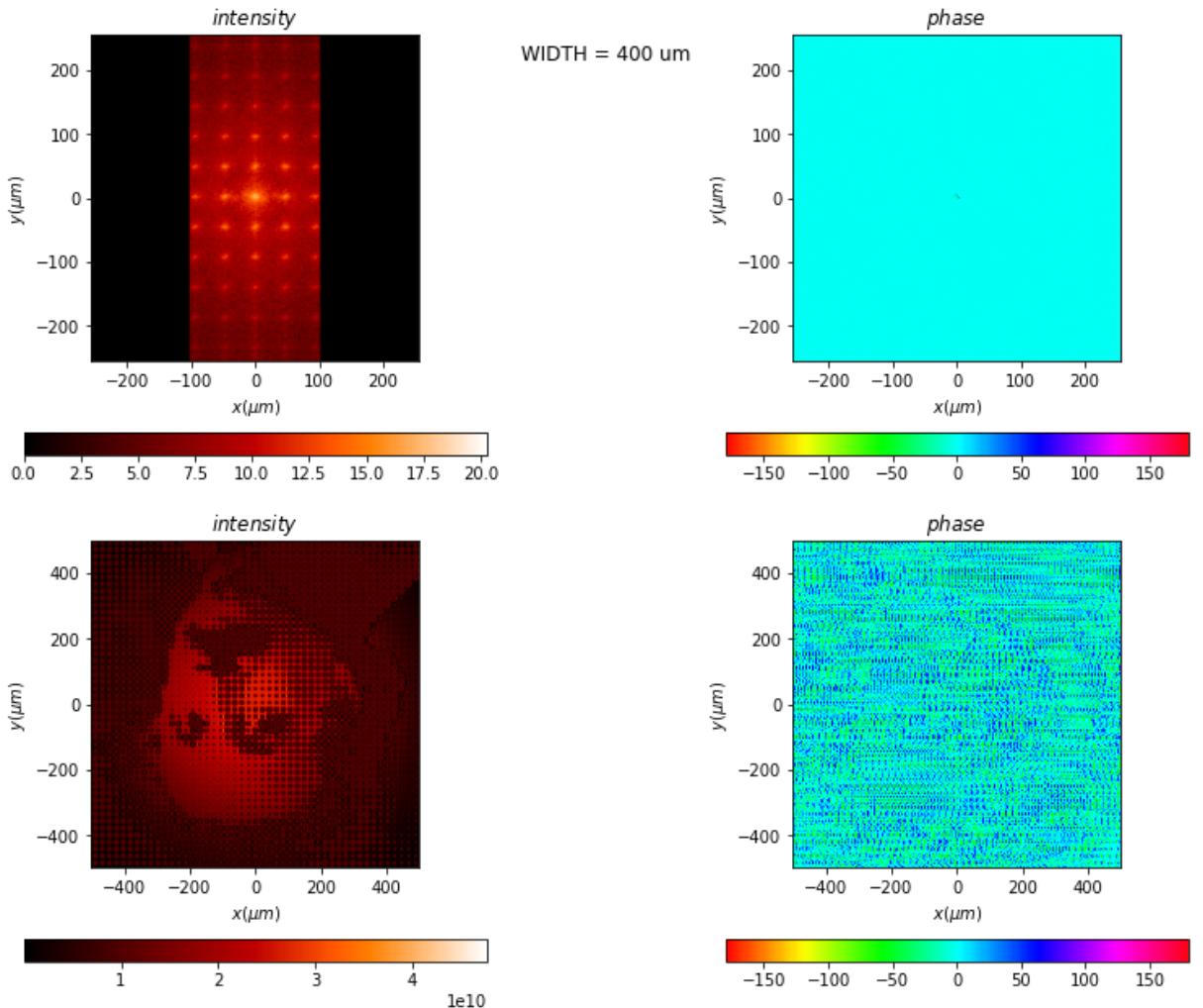
Variable Slit Widths

```
In [23]: widths = [10, 30, 50, 100, 400] # in um
for width in widths:
    varSlit = Scalar_mask_XY(x0, y0, wavelength)
    varSlit.slit(
        x0=0 * um,
        size=width * um
    )
#    varSlit.draw(kind='field', logarithm=True)

    a_L1_VarSlit, a_L1_VarSlit_L2 = sim(a_L1, varSlit)
    a_L1_VarSlit.draw(title=f"WIDTH = {width} um ", kind='field', logarithm=True)
    a_L1_VarSlit_L2.draw(kind='field', logarithm=False)
```







In []:

Alphabets - Spatial Filtering and Character Recognition

```
In [1]: import numpy as np
from diffractio import mm, um, degrees
from diffractio.scalar_sources_XY import Scalar_source_XY
from diffractio.scalar_masks_XY import Scalar_mask_XY

# Setting up
length = 1 * mm
num_data = 512
x0 = np.linspace(-length / 2, length / 2, num_data)
y0 = np.linspace(-length / 2, length / 2, num_data)
wavelength = 0.633 * um
```

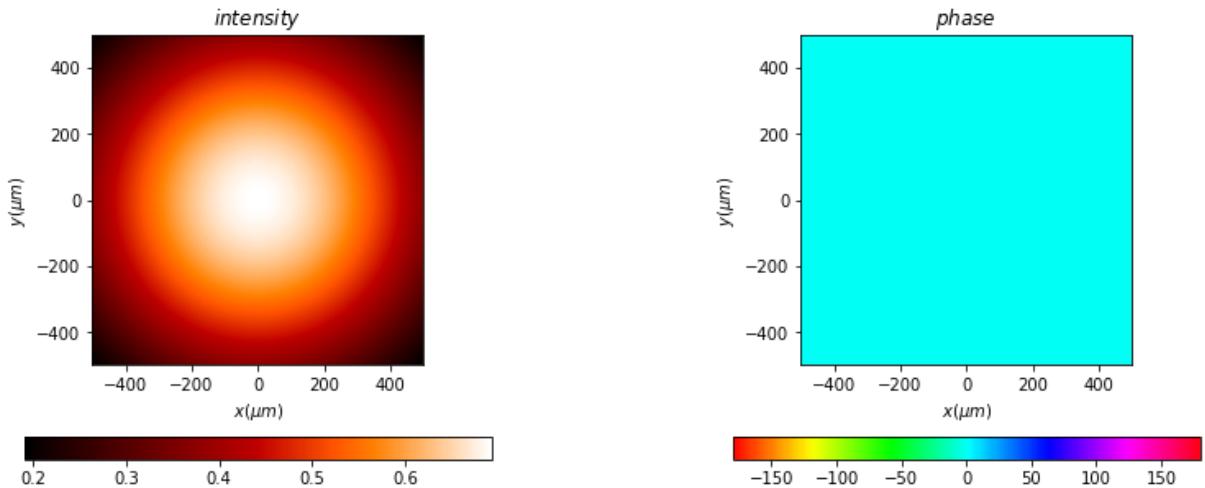
number of processors: 12

Setting up source

- Gaussian Beam (LASER)

```
In [2]: # Gaussian Beam Source - Like a LASER
u0 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
u0.gauss_beam(r0=(0, 0), w0=(800 * um, 800 * um), z0=0.0)
u0.draw(kind='field', logarithm=True)
```

```
Out[2]: ((<matplotlib.image.AxesImage at 0x218cbf0da60>,
          <matplotlib.image.AxesImage at 0x218cc1ad220>),
          None,
          None)
```

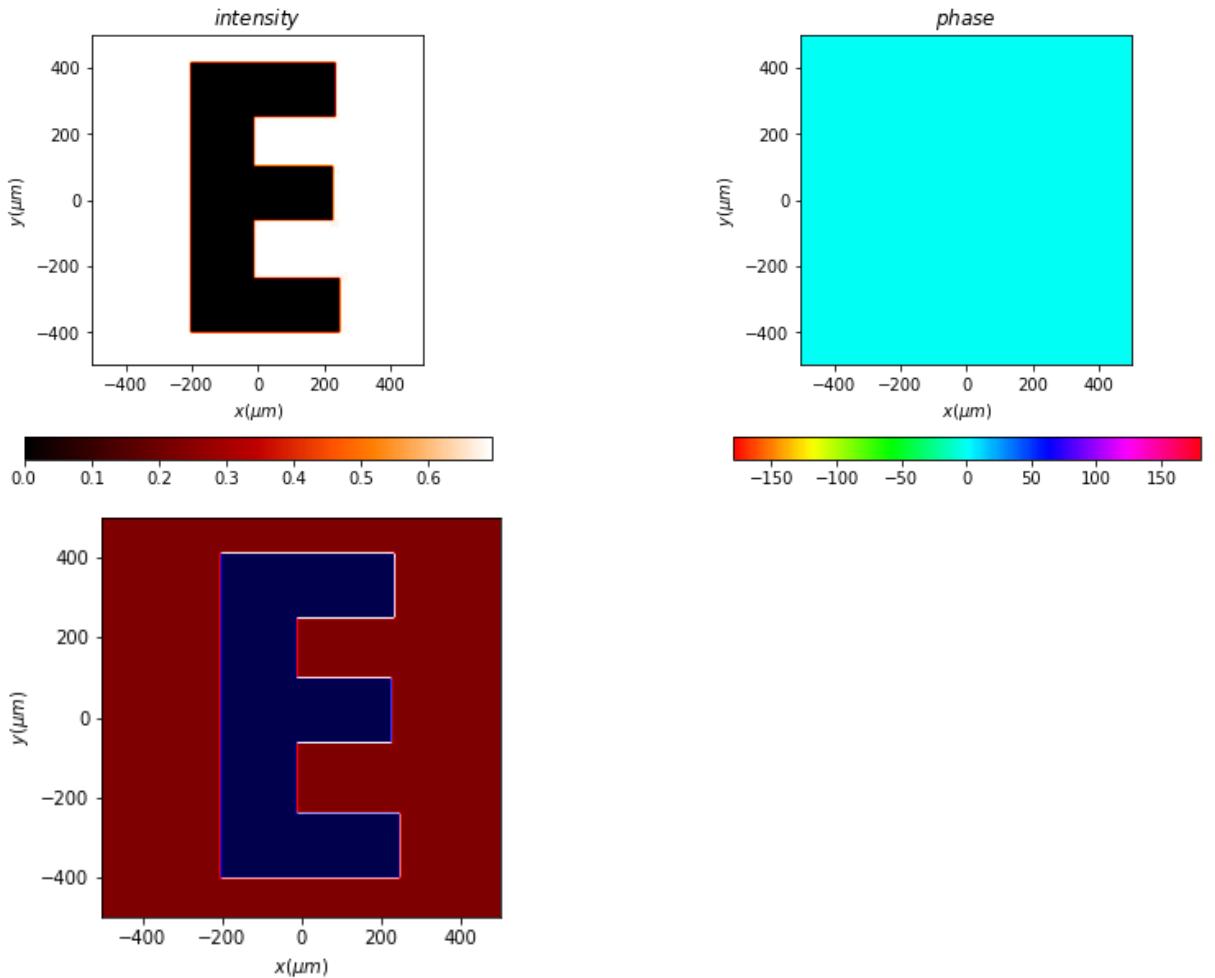


E & F

```
In [3]: E = Scalar_mask_XY(x0, y0, wavelength)
E.image(
    filename="E.png",
    normalize=True,
    canal=0,
)

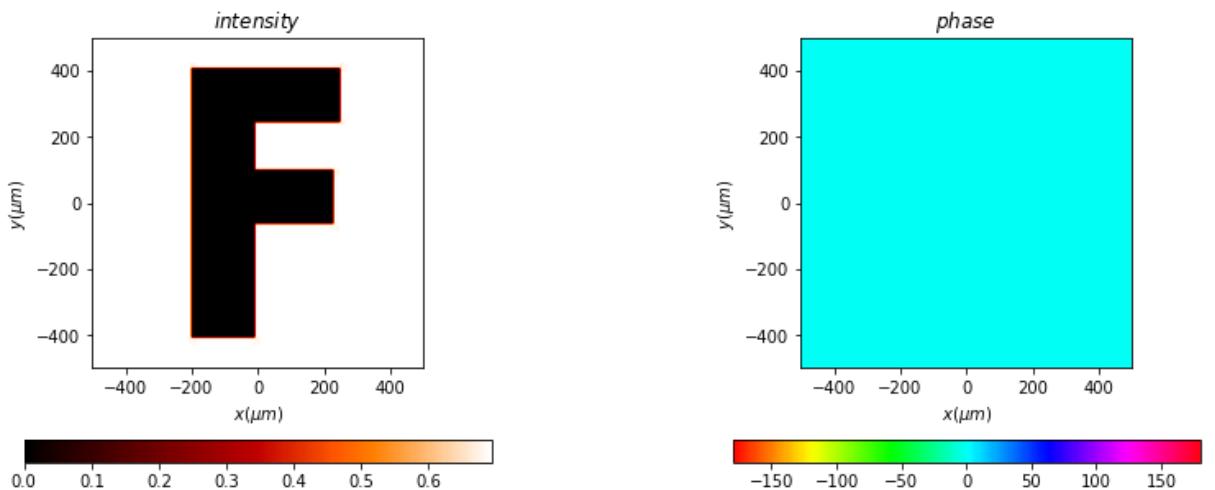
E.draw(kind='field', logarithm=True)
E.draw(kind='real_field', logarithm=True)
```

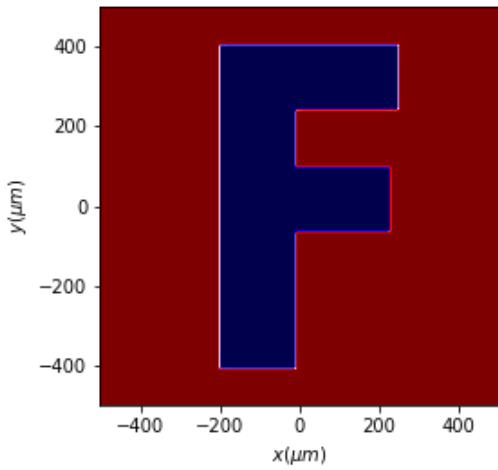
```
Out[3]: (<Figure size 432x288 with 1 Axes>,
          <AxesSubplot:xlabel='$x (\mu m)$', ylabel='$y (\mu m)$'>,
          <matplotlib.image.AxesImage at 0x218cca87dc0>)
```



```
In [4]: F = Scalar_mask_XY(x0, y0, wavelength)
F.image(
    filename="F.png",
    normalize=True,
    canal=0,
)
F.draw(kind='field', logarithm=True)
F.draw(kind='real_field', logarithm=True)
```

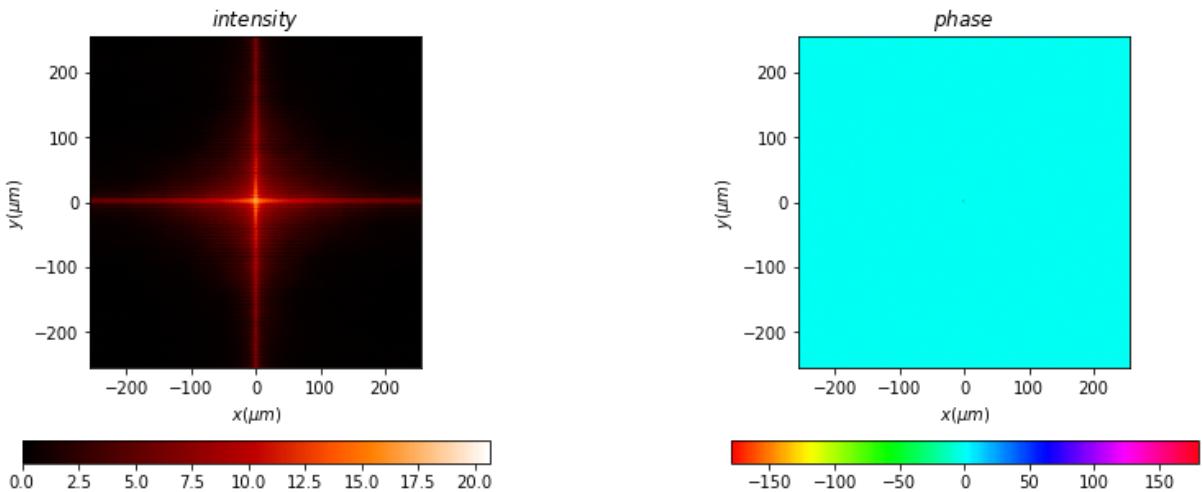
```
Out[4]: (<Figure size 432x288 with 1 Axes>,
<AxesSubplot:xlabel='$x (\mu\text{m})$', ylabel='$y (\mu\text{m})$'>,
<matplotlib.image.AxesImage at 0x218cd0785b0>)
```





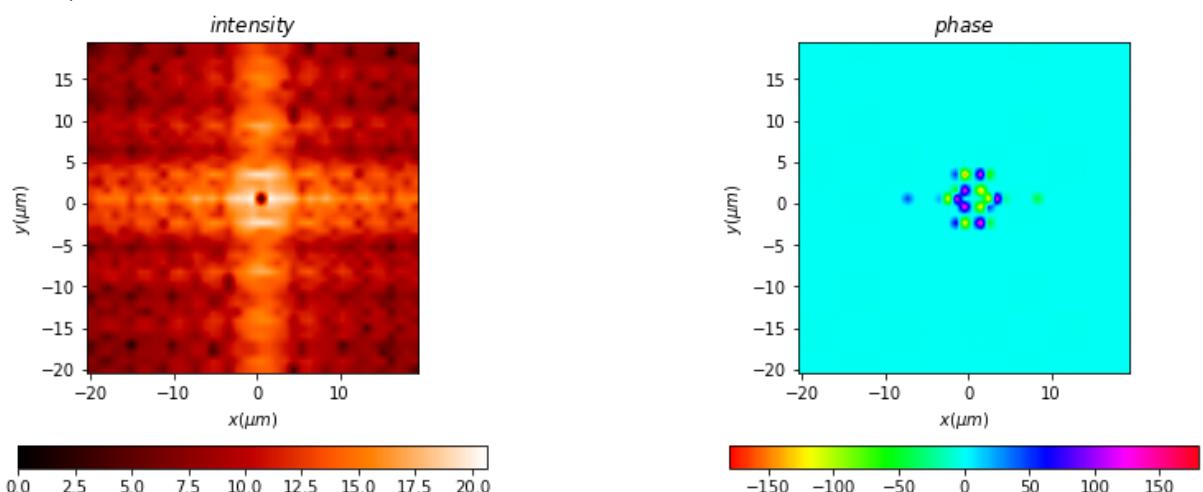
```
In [5]: # Fourier Plane - No Filter
E_a_L1 = (u0 * E).fft(z=1 * mm, new_field=True)
E_a_L1.draw(kind='field', logarithm=True)
```

```
Out[5]: (<matplotlib.image.AxesImage at 0x218d0d64190>,
<matplotlib.image.AxesImage at 0x218d0e0e910>),
None,
None)
```



```
In [6]: # A closer look
E_a_L1_Crop = E_a_L1.cut_resample(x_limits=(-20, 20), y_limits=(-20, 20), new_field=True)
E_a_L1_Crop.draw(kind='field', logarithm=True)
```

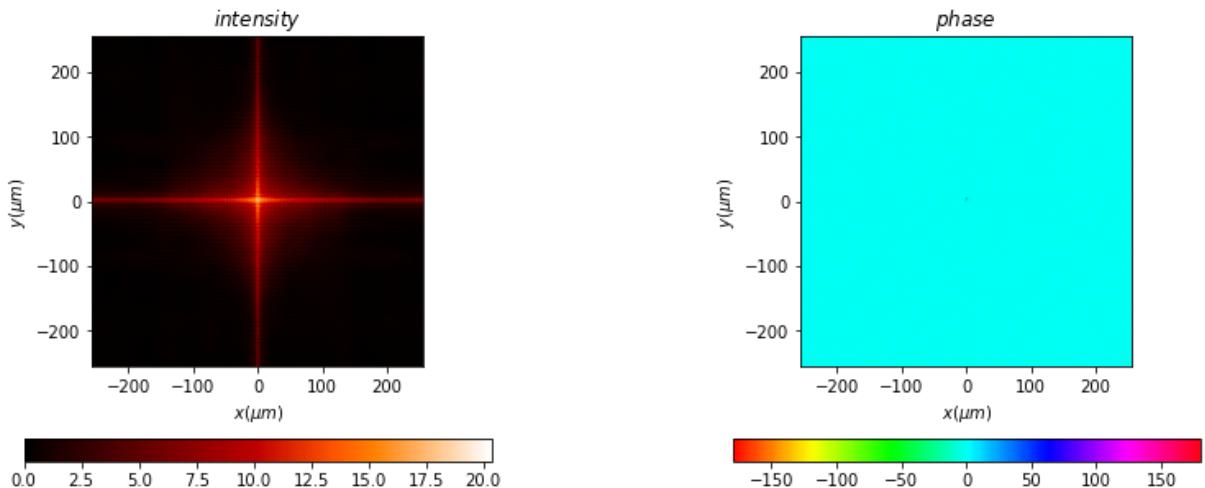
```
Out[6]: (<matplotlib.image.AxesImage at 0x218d0d9ac10>,
<matplotlib.image.AxesImage at 0x218cd043400>),
None,
None)
```



```
In [7]: # Fourier Plane - No Filter
```

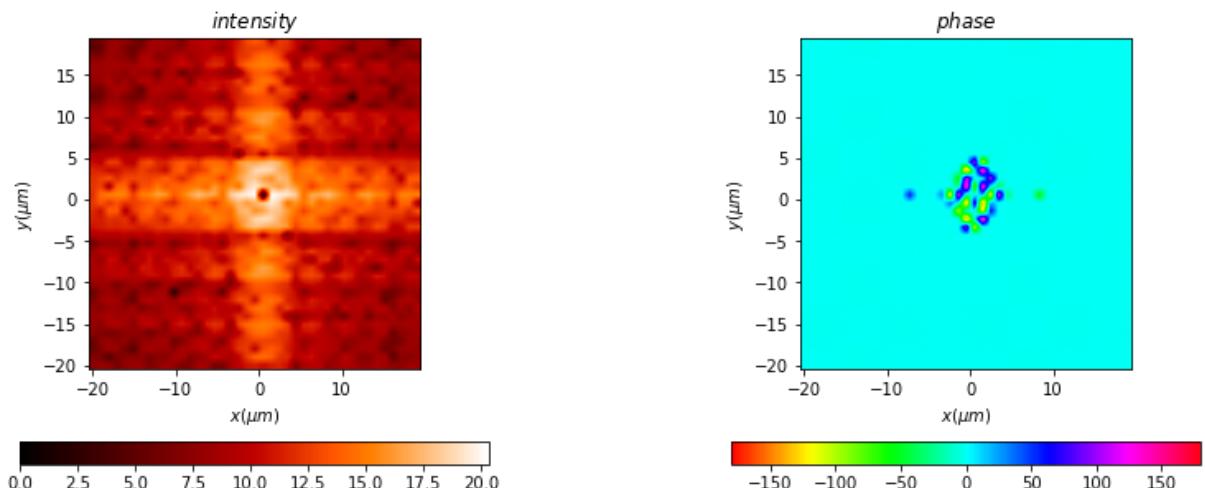
```
F_a_L1 = (u0 * F).fft(z=1 * mm, new_field=True)
F_a_L1.draw(kind='field', logarithm=True)
```

Out[7]: ((<matplotlib.image.AxesImage at 0x218d0e9a940>,
<matplotlib.image.AxesImage at 0x218ccb75520>),
None,
None)



In [8]: # A closer look
F_a_L1_Crop = F_a_L1.cut_resample(x_limits=(-20, 20), y_limits=(-20, 20), new_field=True)
F_a_L1_Crop.draw(kind='field', logarithm=True)

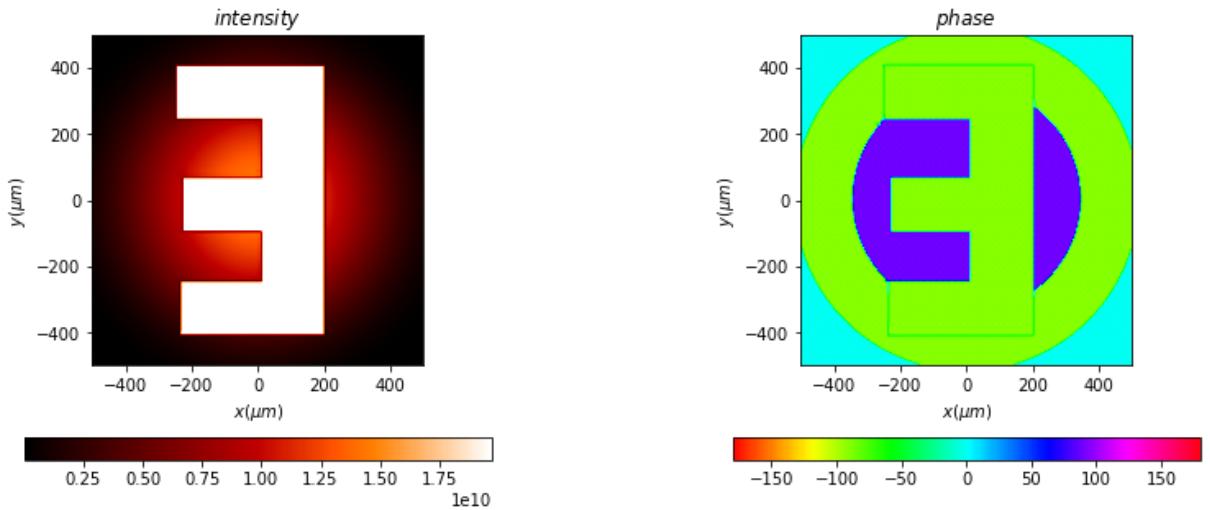
Out[8]: ((<matplotlib.image.AxesImage at 0x218ccbc7fa0>,
<matplotlib.image.AxesImage at 0x218d0f32730>),
None,
None)



So, the difference in the Fourier encoding for two very similar characters or alphabets lies not so much in the position-space, as it does in the phase-space. This "hidden" phase-space information can be used to enable better machine encodings for Character Recognition software.

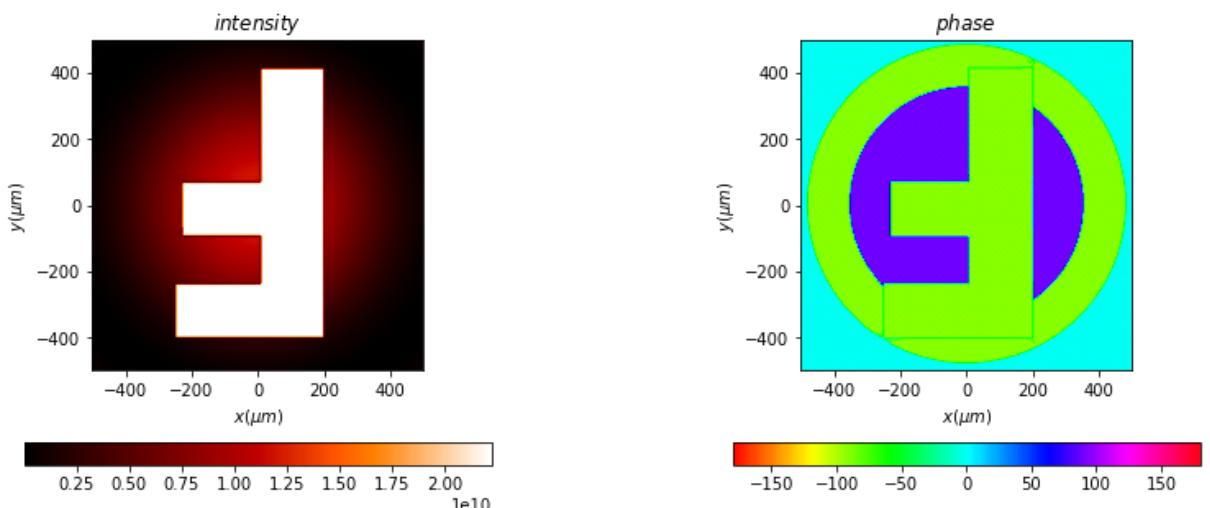
In [9]: # This is how, it'd look without any filter, at the Observation screen
E_a_L2 = E_a_L1.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
E_a_L2.draw(kind='field', logarithm=False)

Out[9]: ((<matplotlib.image.AxesImage at 0x218d0bf7130>,
<matplotlib.image.AxesImage at 0x218d0c8c370>),
None,
None)



```
In [10]: # This is how, it'd look without any filter, at the Observation screen
F_a_L2 = F_a_L1.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
F_a_L2.draw(kind='field', logarithm=False)
```

```
Out[10]: (<matplotlib.image.AxesImage at 0x218d15767f0>,
<matplotlib.image.AxesImage at 0x218d1604a60>,
None,
None)
```

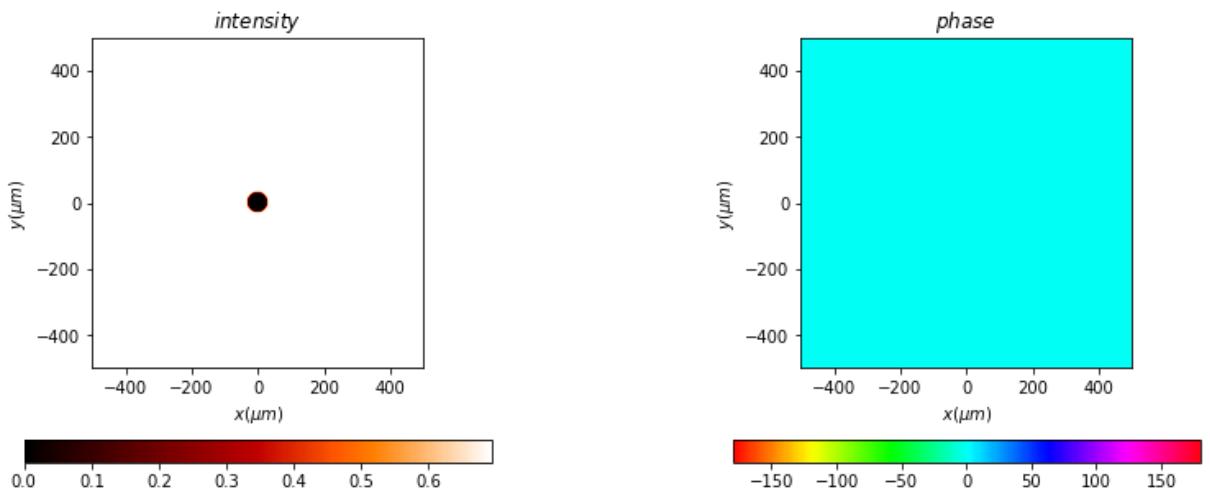


Some Masks / Filters

- Center Dot - High Pass
- Square - Low Pass
- Square + Center Dot -
- Vertical Slit
- Horizontal Slit
- Angled Slit
- Variable Slits
- Mesh

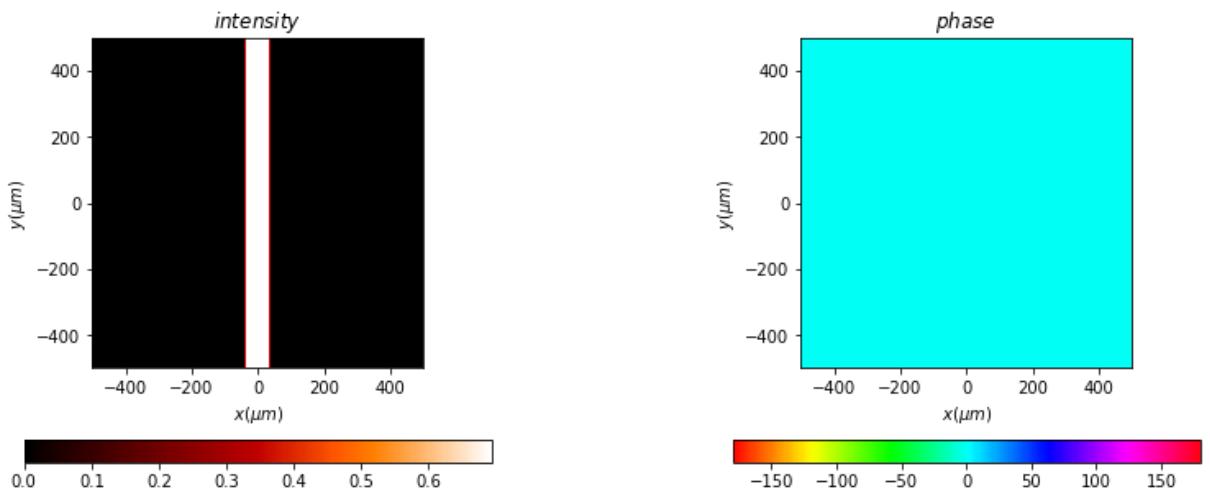
```
In [11]: cDot = Scalar_mask_XY(x0, y0, wavelength)
cDot.ring(
    r0=(0 * um, 0 * um),
    radius1=(30 * um, 30 * um),
    radius2=(1000 * um, 1000 * um)
)
cDot.draw(kind='field', logarithm=True)
```

```
Out[11]: ((<matplotlib.image.AxesImage at 0x218d15a4190>,
    <matplotlib.image.AxesImage at 0x218d0dc1100>),
None,
None)
```



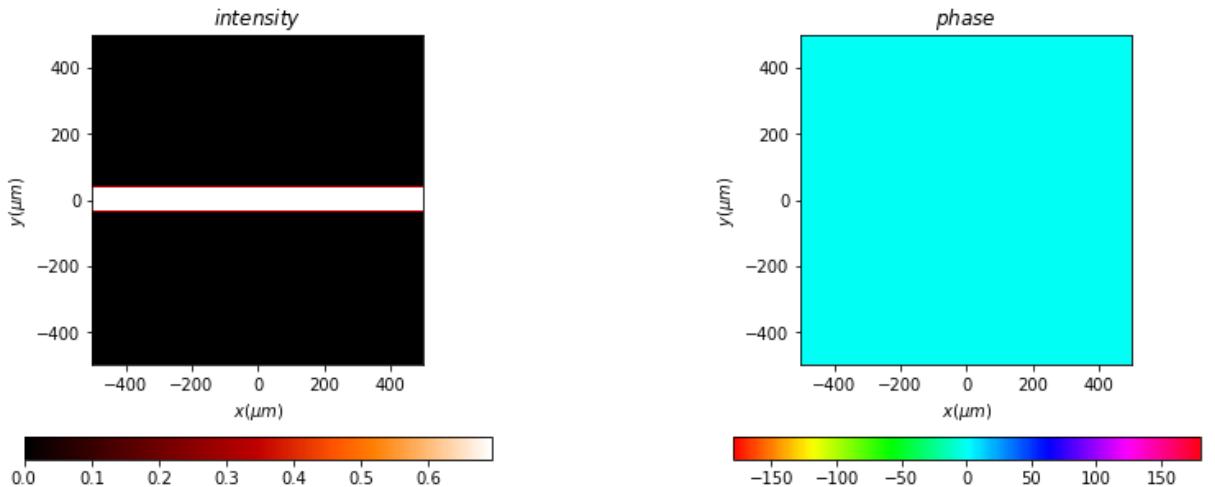
```
In [12]: vert = Scalar_mask_XY(x0, y0, wavelength)
vert.slit(
    x0=0 * um,
    size=75 * um
)
vert.draw(kind='field', logarithm=True)
```

```
Out[12]: ((<matplotlib.image.AxesImage at 0x218d1fbb910>,
    <matplotlib.image.AxesImage at 0x218d20430d0>),
None,
None)
```



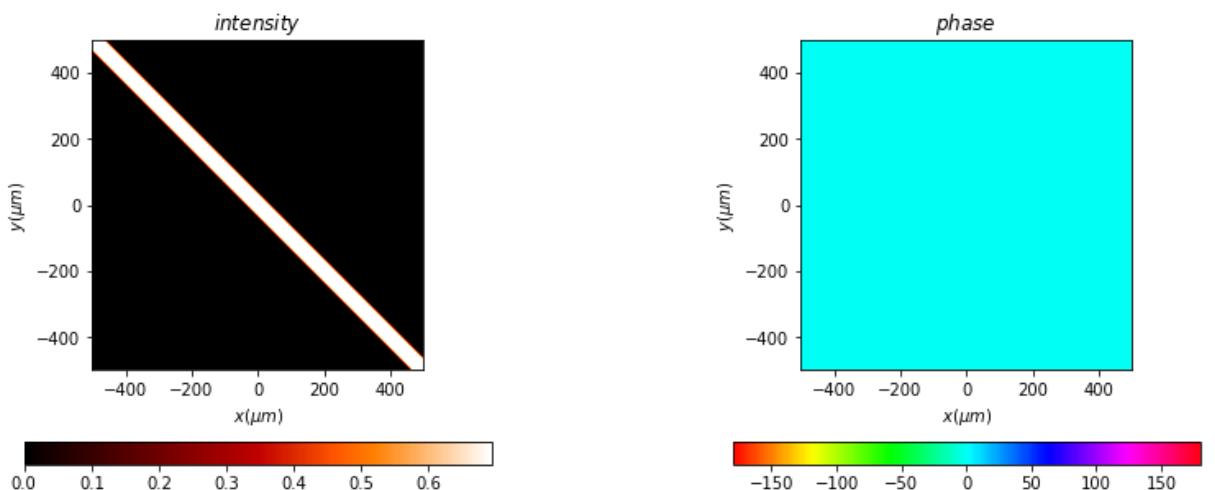
```
In [13]: horiz = Scalar_mask_XY(x0, y0, wavelength)
horiz.slit(
    x0=0 * um,
    size=75 * um,
    angle=np.pi / 2
)
horiz.draw(kind='field', logarithm=True)
```

```
Out[13]: ((<matplotlib.image.AxesImage at 0x218d2108370>,
    <matplotlib.image.AxesImage at 0x218d2184b50>),
None,
None)
```



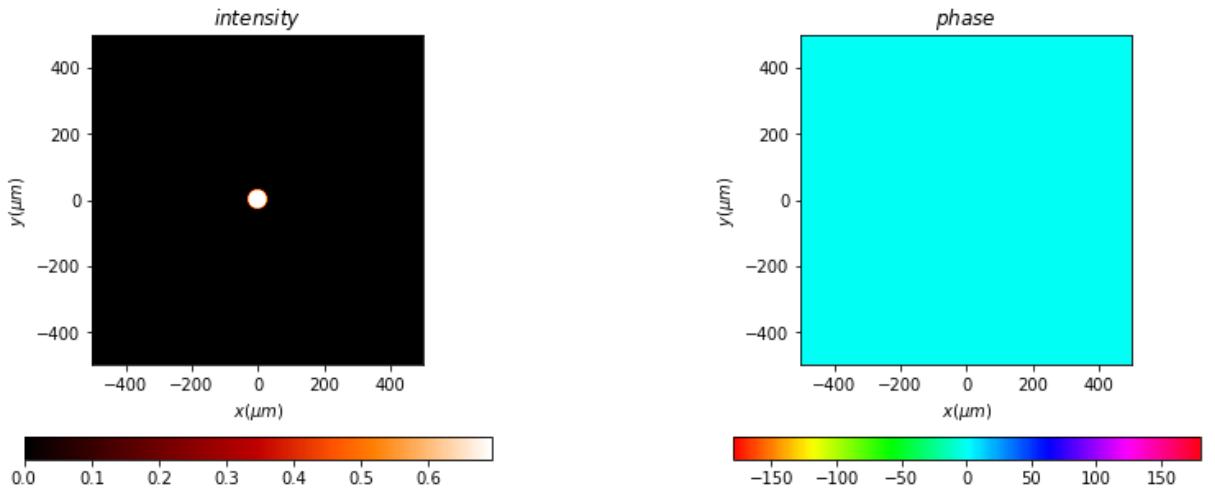
```
In [14]: angled = Scalar_mask_XY(x0, y0, wavelength)
angled.slit(
    x0=0 * um,
    size=50 * um,
    angle=np.pi / 4
)
angled.draw(kind='field', logarithm=True)
```

```
Out[14]: (<matplotlib.image.AxesImage at 0x218d30abdf0>,
<matplotlib.image.AxesImage at 0x218d312d5e0>),
None,
None)
```



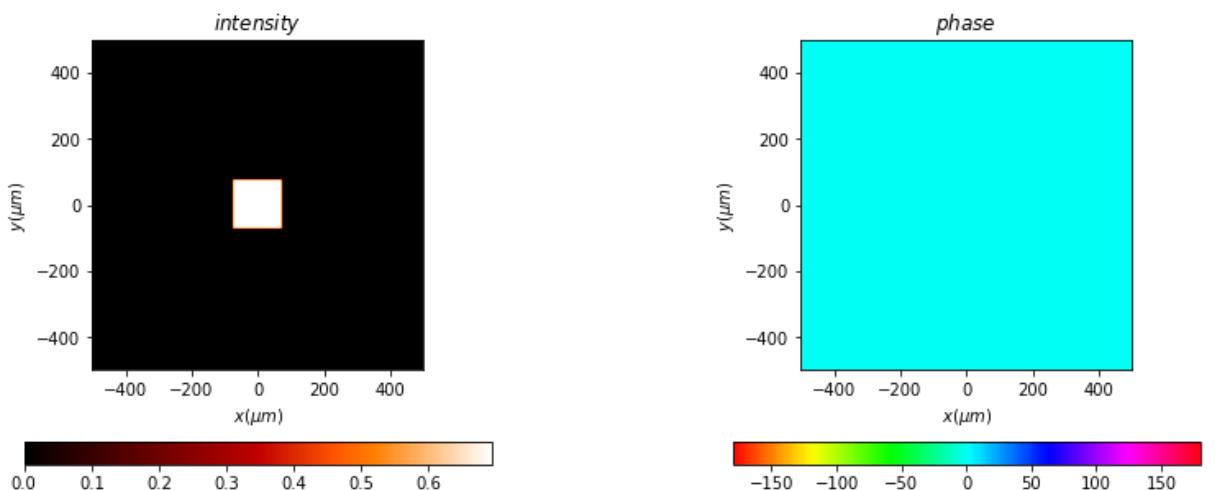
```
In [15]: circ = Scalar_mask_XY(x0, y0, wavelength)
circ.circle(
    r0=(0 * um, 0 * um),
    radius=(30 * um, 30 * um),
    angle=0
)
circ.draw(kind='field', logarithm=True)
```

```
Out[15]: (<matplotlib.image.AxesImage at 0x218d31d6ca0>,
<matplotlib.image.AxesImage at 0x218d4aeeef70>),
None,
None)
```



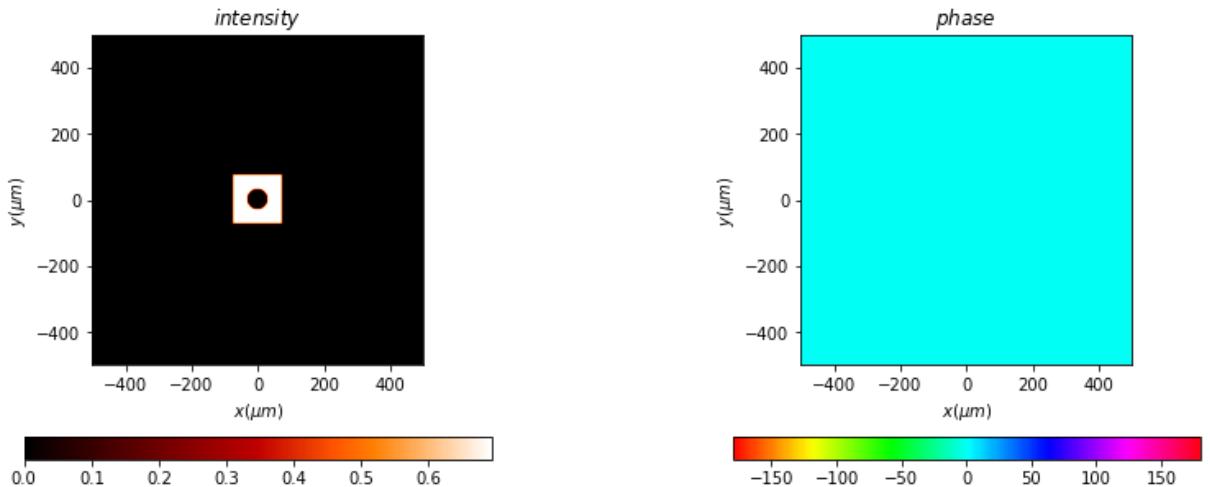
```
In [16]: sq = Scalar_mask_XY(x0, y0, wavelength)
sq.square(
    r0=(0 * um, 0 * um),
    size=(150 * um, 150 * um),
    angle=0,
)
sq.draw(kind='field', logarithm=True)
```

```
Out[16]: (<matplotlib.image.AxesImage at 0x218d4ba1520>,
<matplotlib.image.AxesImage at 0x218d4c357c0>),
None,
None)
```



```
In [17]: # Adding two filters
sqCirc = sq * cDot
sqCirc.draw(kind="field", logarithm=True)
```

```
Out[17]: (<matplotlib.image.AxesImage at 0x218d4bb70d0>,
<matplotlib.image.AxesImage at 0x218d17567f0>),
None,
None)
```



Returns wave after encountering filter and then L2

```
In [18]: def sim(a_L1, mask):
    """
    a_L1: Wave after passing through Lens 1
    mask: Mask or Filter to apply

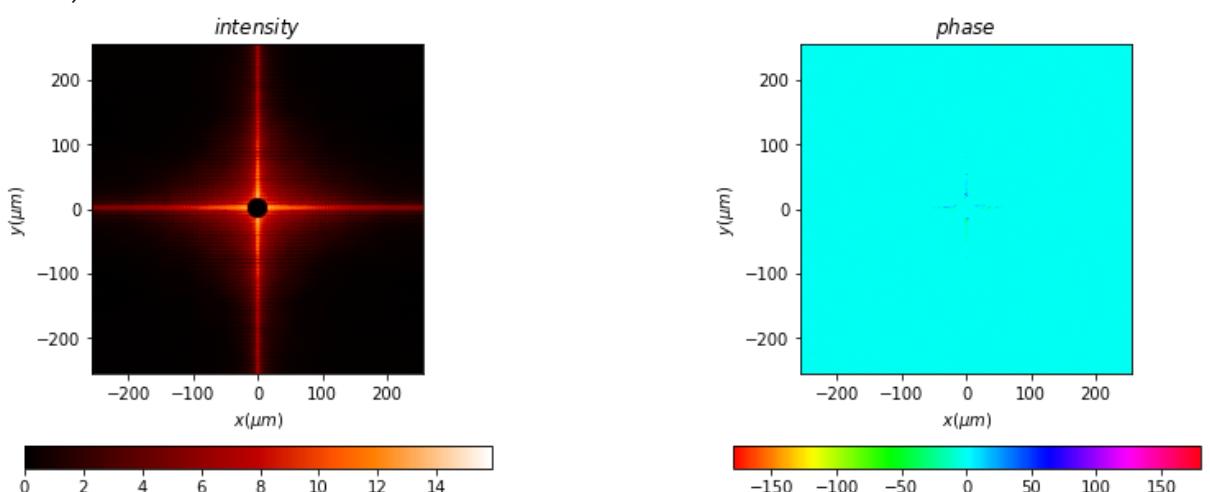
    """
    a_L1_Mask = a_L1 * mask
    a_L1_Mask_L2 = a_L1_Mask.fft(z=1 * mm, shift=False, remove0=False, new_field=True)

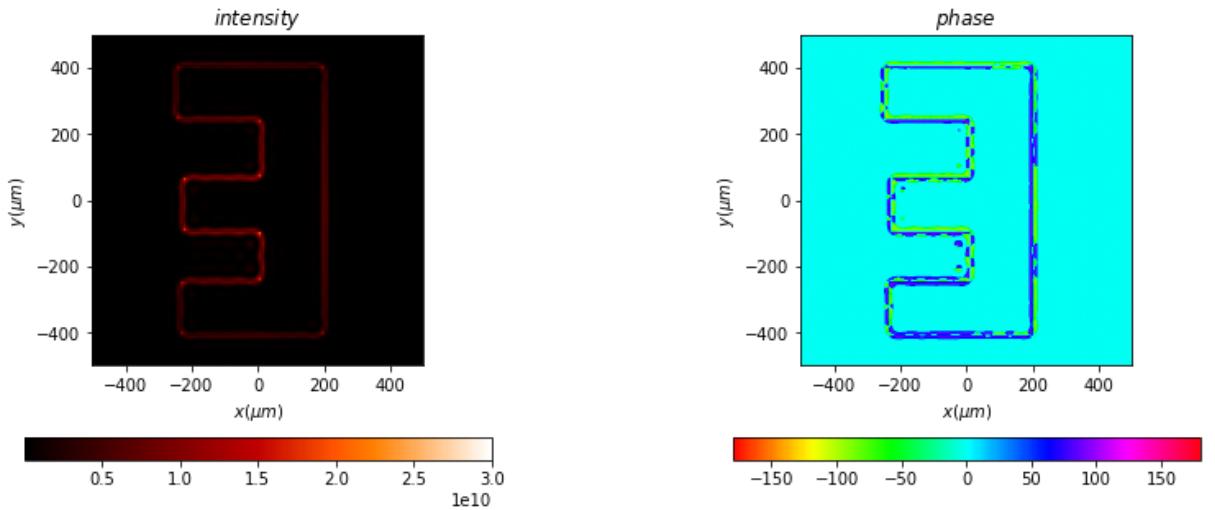
    return a_L1_Mask, a_L1_Mask_L2
```

Center Dot - High Pass - HT Structure Visible - Dark-Field Illumination / Edge Enhancement

```
In [19]: E_a_L1_cD, E_a_L1_cD_L2 = sim(E_a_L1, cDot)
E_a_L1_cD.draw(kind='field', logarithm=True)
E_a_L1_cD_L2.draw(kind='field', logarithm=False)
```

```
Out[19]: (<matplotlib.image.AxesImage at 0x218d5f0c7c0>,
<matplotlib.image.AxesImage at 0x218d7787f40>,
None,
None)
```

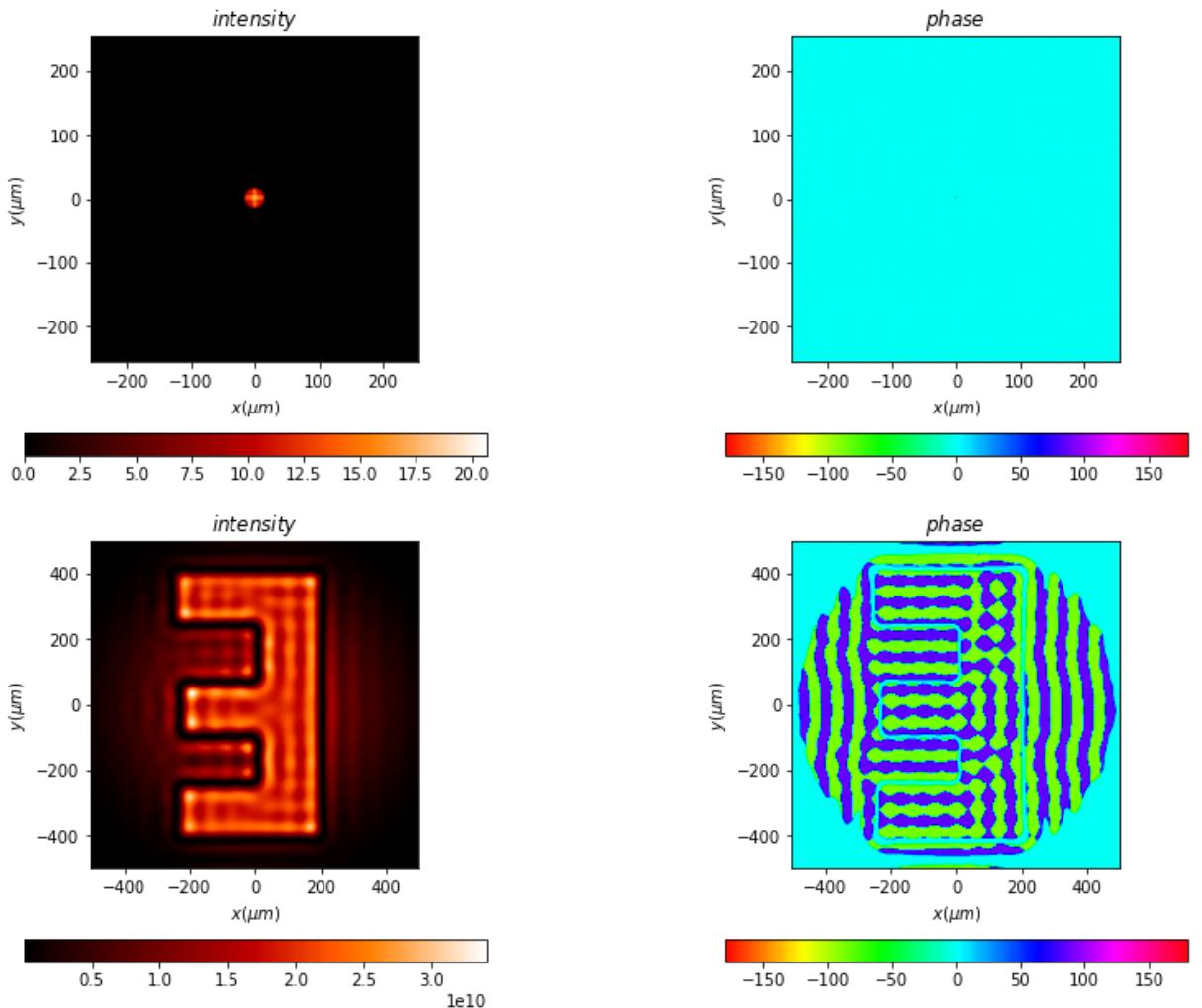




Circle - Low Pass - Blurred Output

```
In [20]: E_a_L1_Circ, E_a_L1_Circ_L2 = sim(E_a_L1, circ)
E_a_L1_Circ.draw(kind='field', logarithm=True)
E_a_L1_Circ_L2.draw(kind='field', logarithm=False)
```

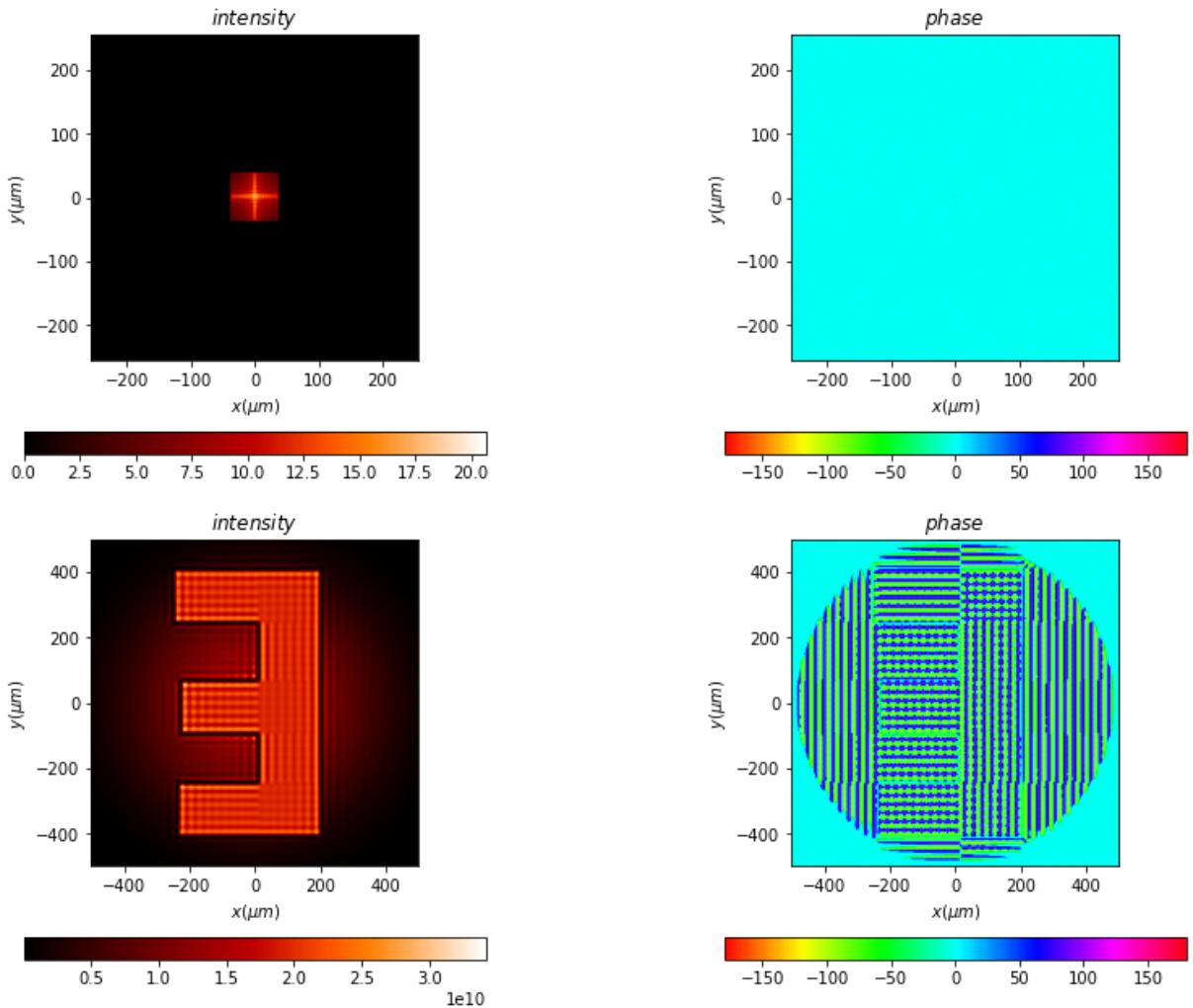
```
Out[20]: (<matplotlib.image.AxesImage at 0x218d8423370>,
<matplotlib.image.AxesImage at 0x218d848e5e0>,
None,
None)
```



Square

```
In [21]: E_a_L1_Sq, E_a_L1_Sq_L2 = sim(E_a_L1, sq)
E_a_L1_Sq.draw(kind='field', logarithm=True)
E_a_L1_Sq_L2.draw(kind='field', logarithm=False)
```

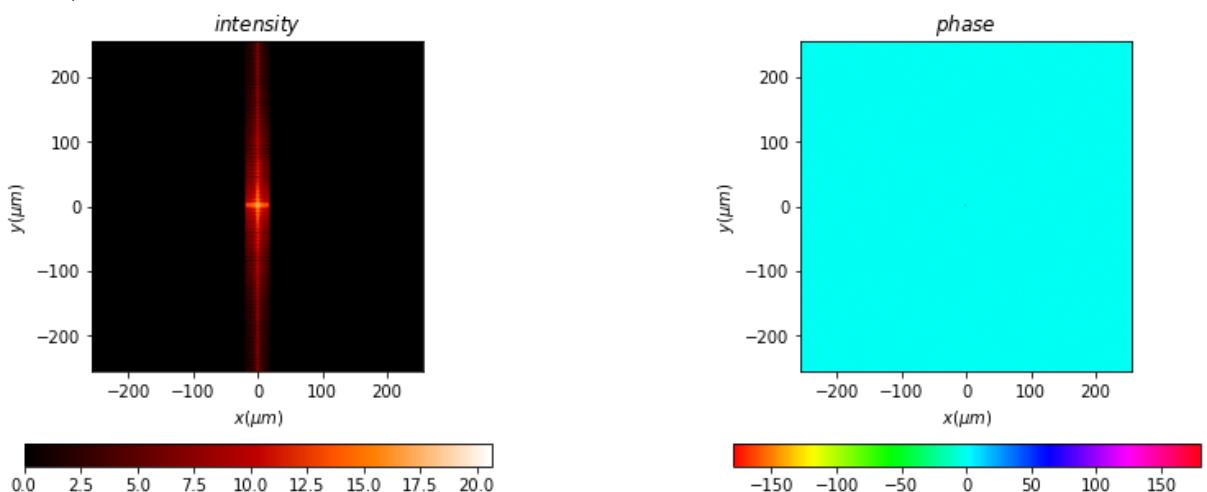
```
Out[21]: ((<matplotlib.image.AxesImage at 0x218d910f580>,
    <matplotlib.image.AxesImage at 0x218d91797f0>),
None,
None)
```

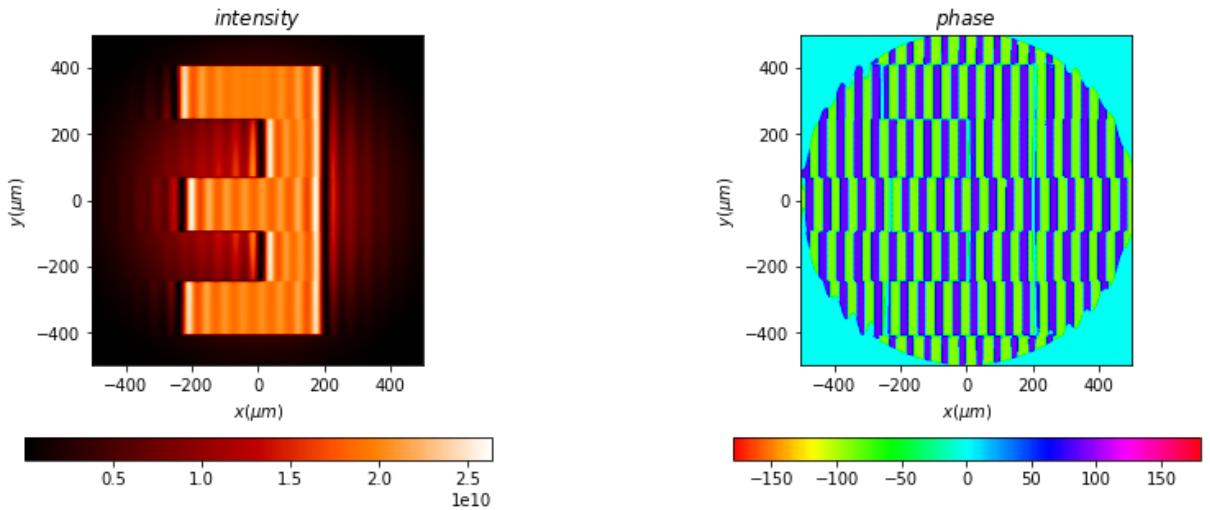


Vertical Slit

```
In [22]: E_a_L1_Vert, E_a_L1_Vert_L2 = sim(E_a_L1, vert)
E_a_L1_Vert.draw(kind='field', logarithm=True)
E_a_L1_Vert_L2.draw(kind='field', logarithm=False)
```

```
Out[22]: ((<matplotlib.image.AxesImage at 0x218d4c9ba00>,
    <matplotlib.image.AxesImage at 0x218d83cf100>),
None,
None)
```

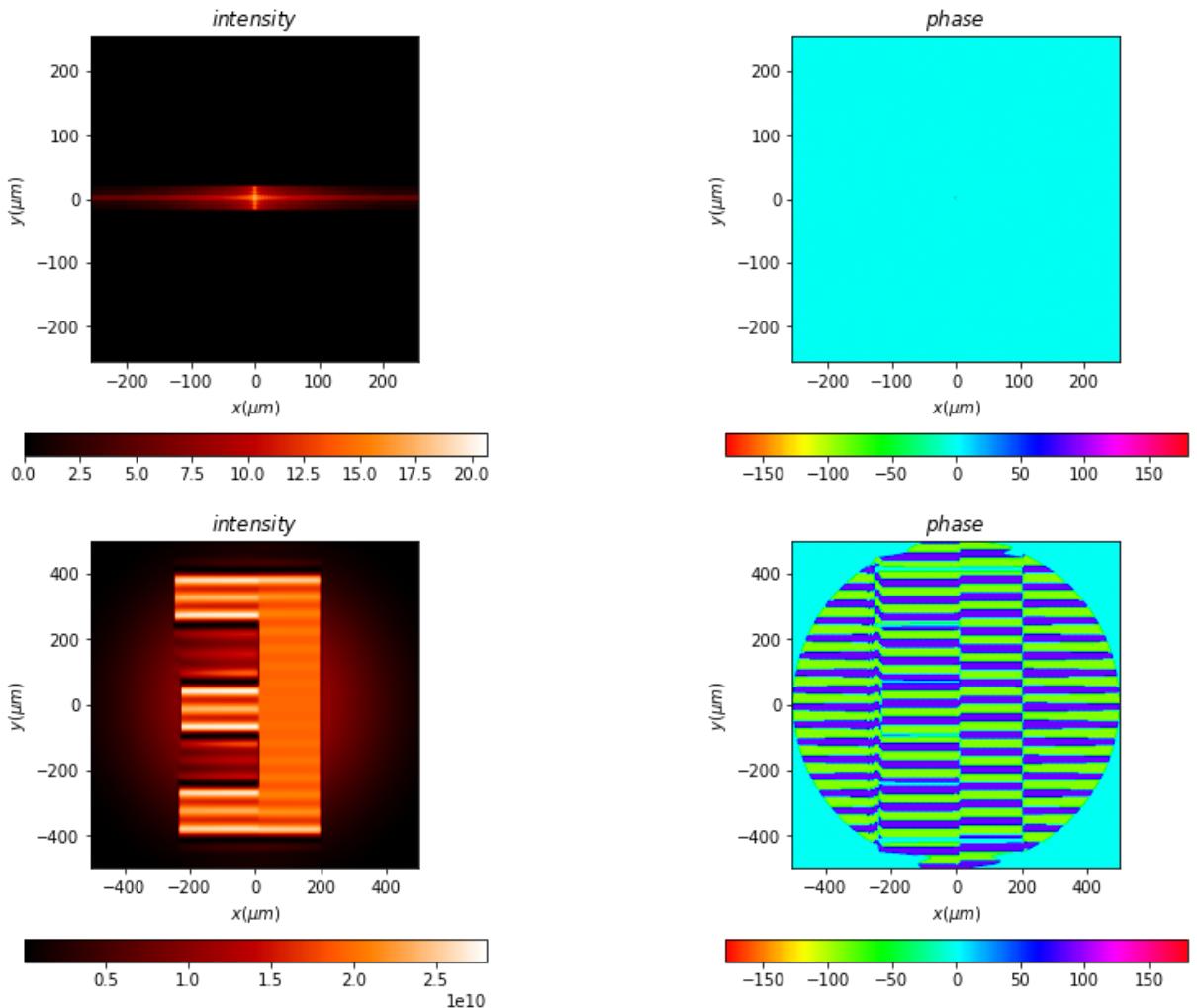




Horizontal Slit

```
In [23]: E_a_L1_Horiz, E_a_L1_Horiz_L2 = sim(E_a_L1, horiz)
E_a_L1_Horiz.draw(kind='field', logarithm=True)
E_a_L1_Horiz_L2.draw(kind='field', logarithm=False)
```

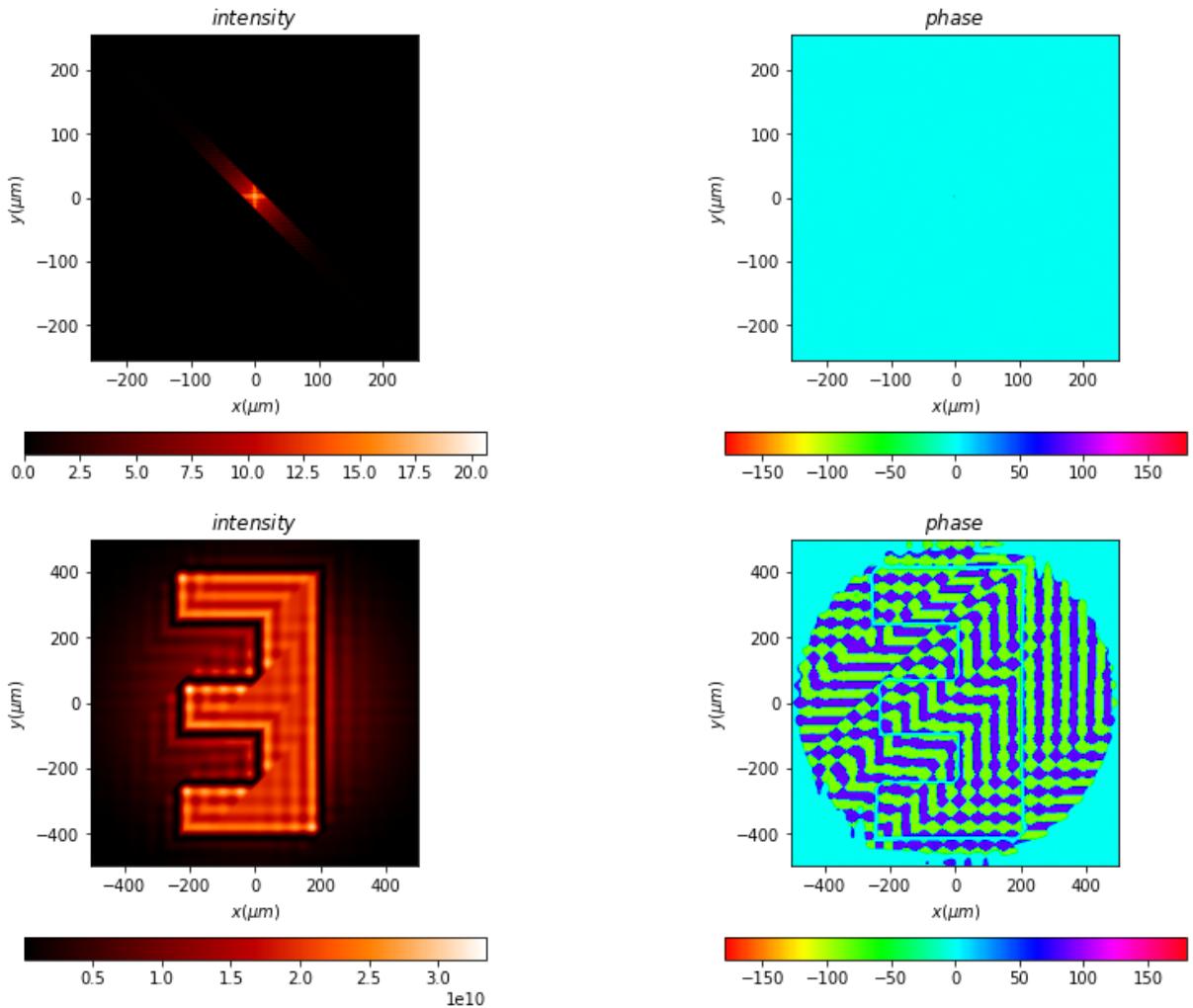
```
Out[23]: (<matplotlib.image.AxesImage at 0x218d9d892b0>,
<matplotlib.image.AxesImage at 0x218d9ded8e0>,
None,
None)
```



Angled Slit

```
In [24]: E_a_L1_Angled, E_a_L1_Angled_L2 = sim(E_a_L1, angled)
E_a_L1_Angled.draw(kind='field', logarithm=True)
E_a_L1_Angled_L2.draw(kind='field', logarithm=False)
```

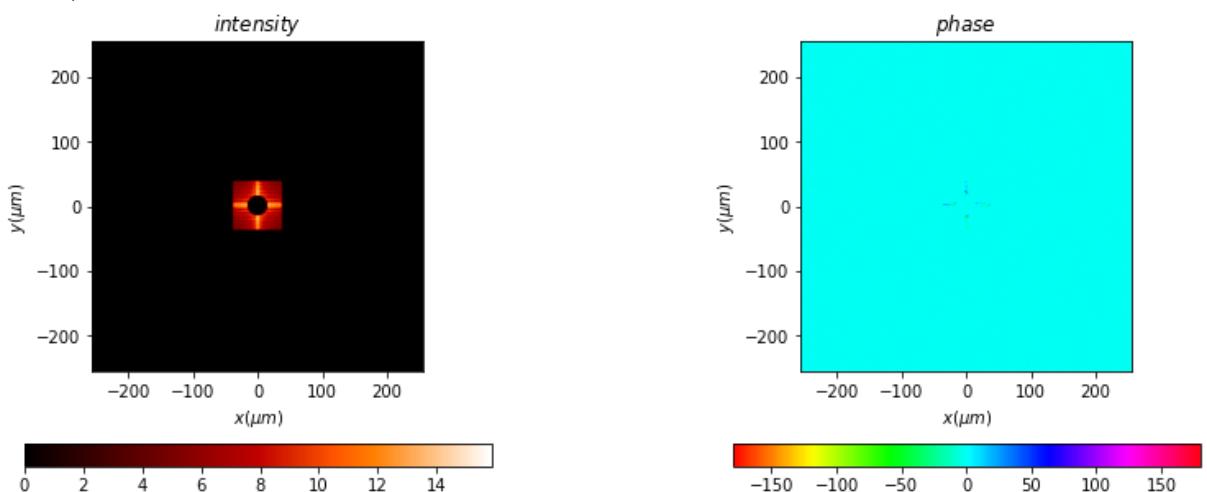
```
Out[24]: ((<matplotlib.image.AxesImage at 0x218da856a30>,
    <matplotlib.image.AxesImage at 0x218dc584ca0>),
None,
None)
```

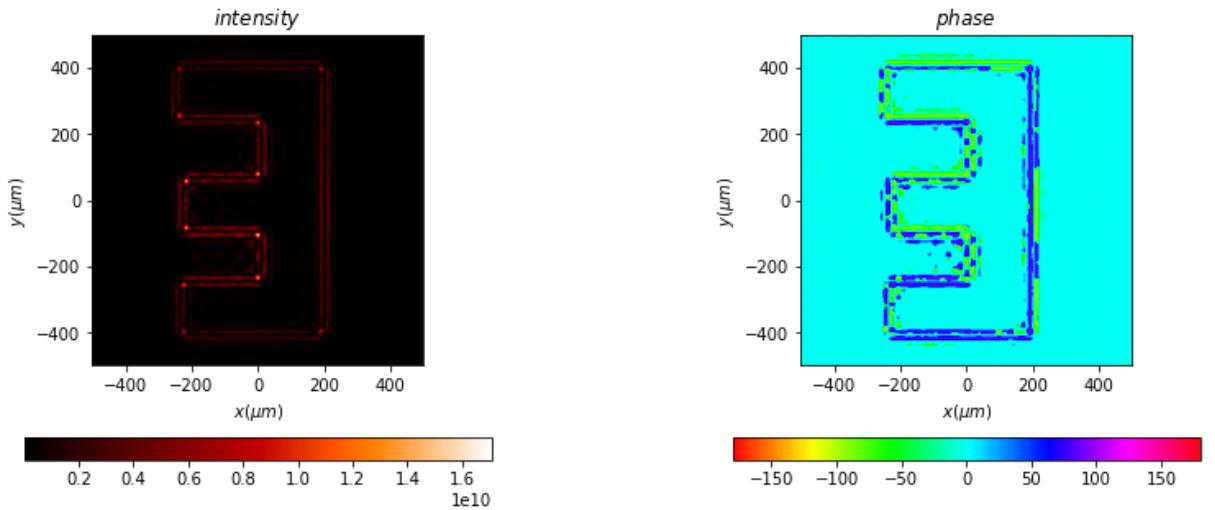


Square + Circle

```
In [25]: E_a_L1_SqCirc, E_a_L1_SqCirc_L2 = sim(E_a_L1, sqCirc)
E_a_L1_SqCirc.draw(kind='field', logarithm=True)
E_a_L1_SqCirc_L2.draw(kind='field', logarithm=False)
```

```
Out[25]: ((<matplotlib.image.AxesImage at 0x218df855e80>,
    <matplotlib.image.AxesImage at 0x218dc5e2970>),
None,
None)
```

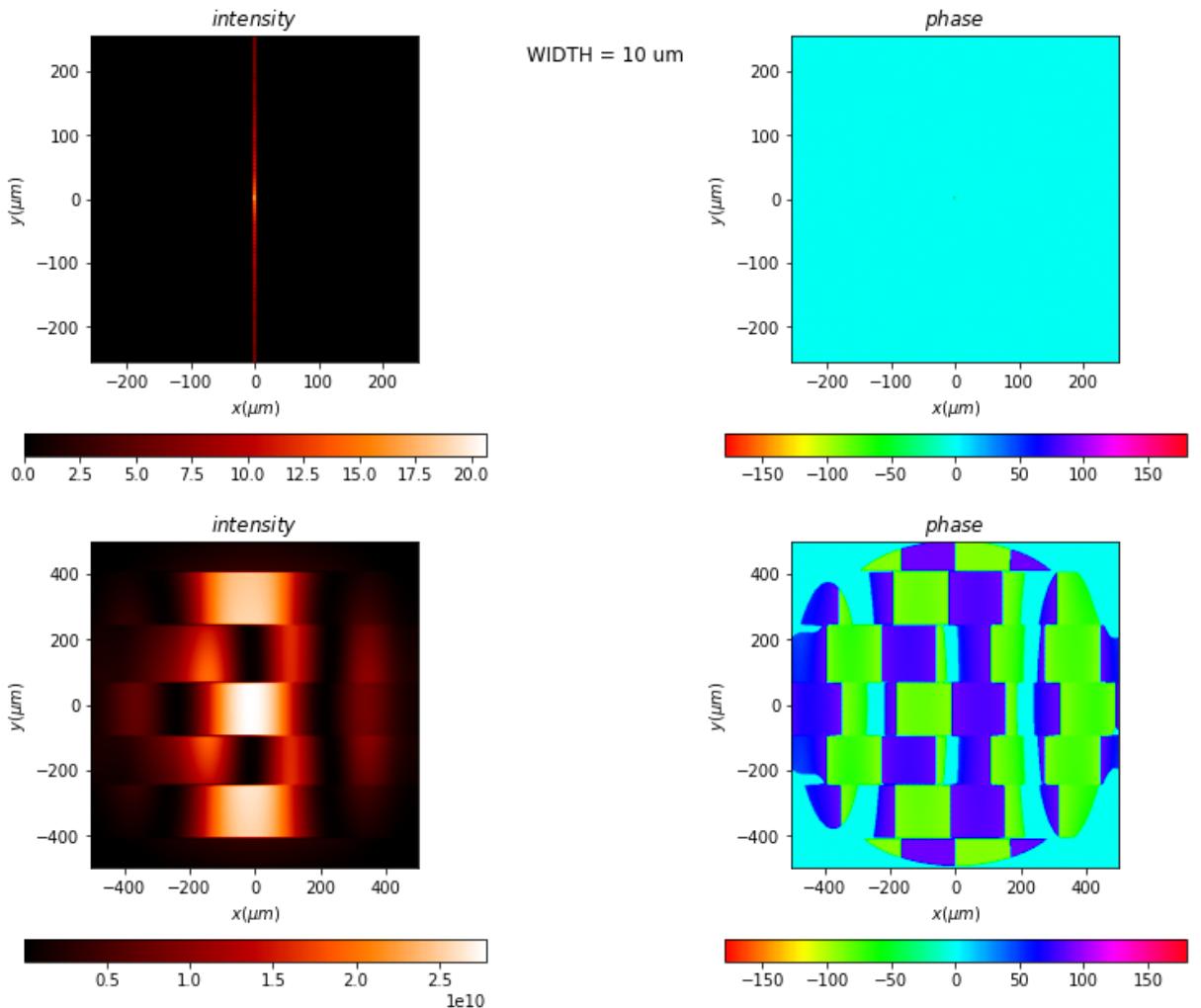


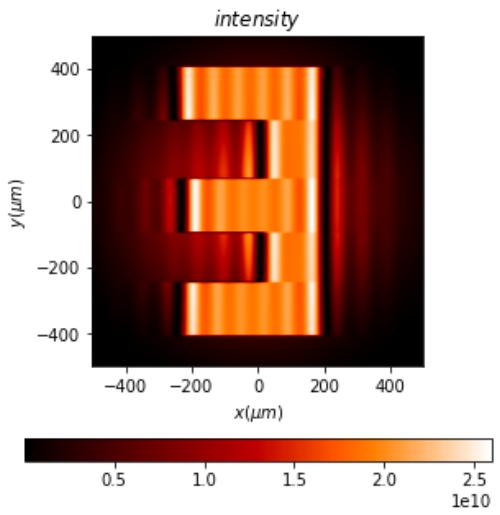
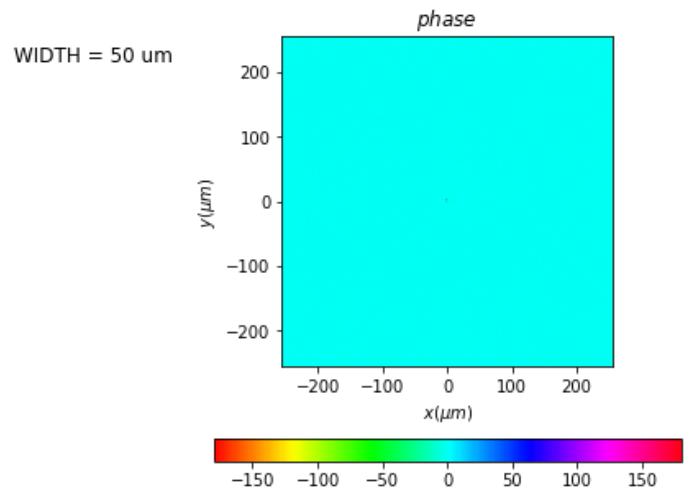
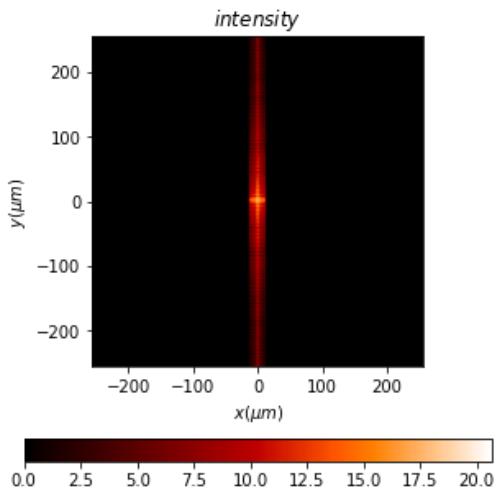
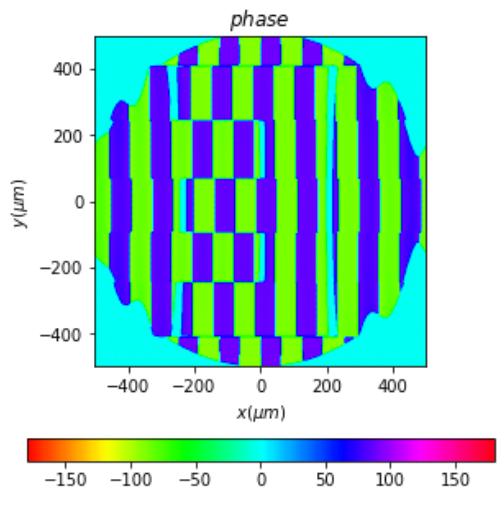
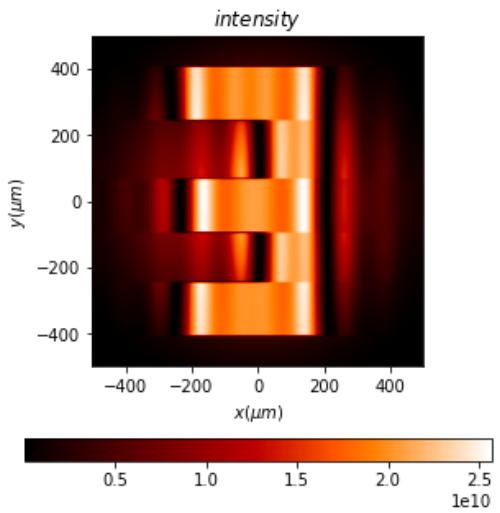
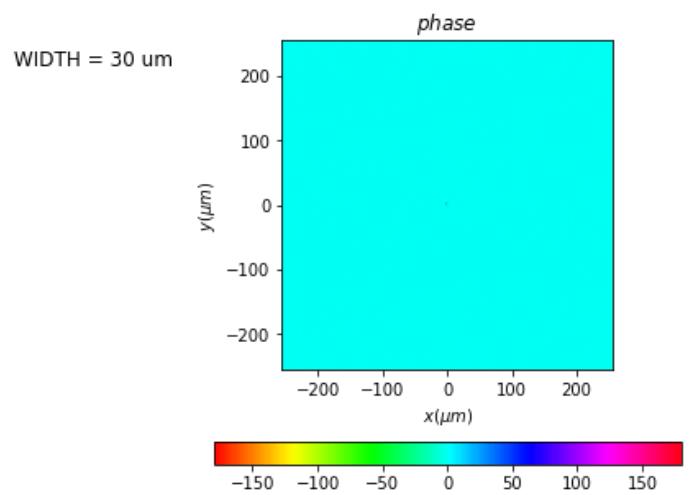
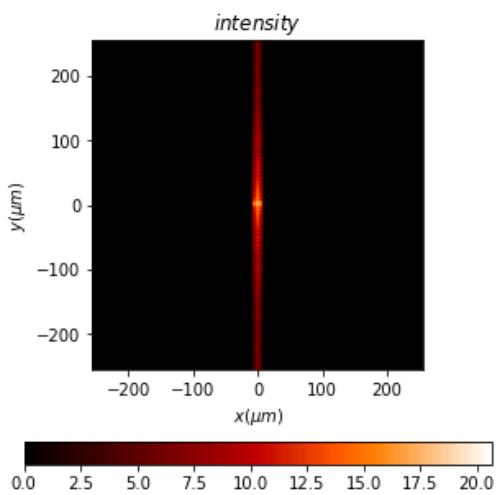


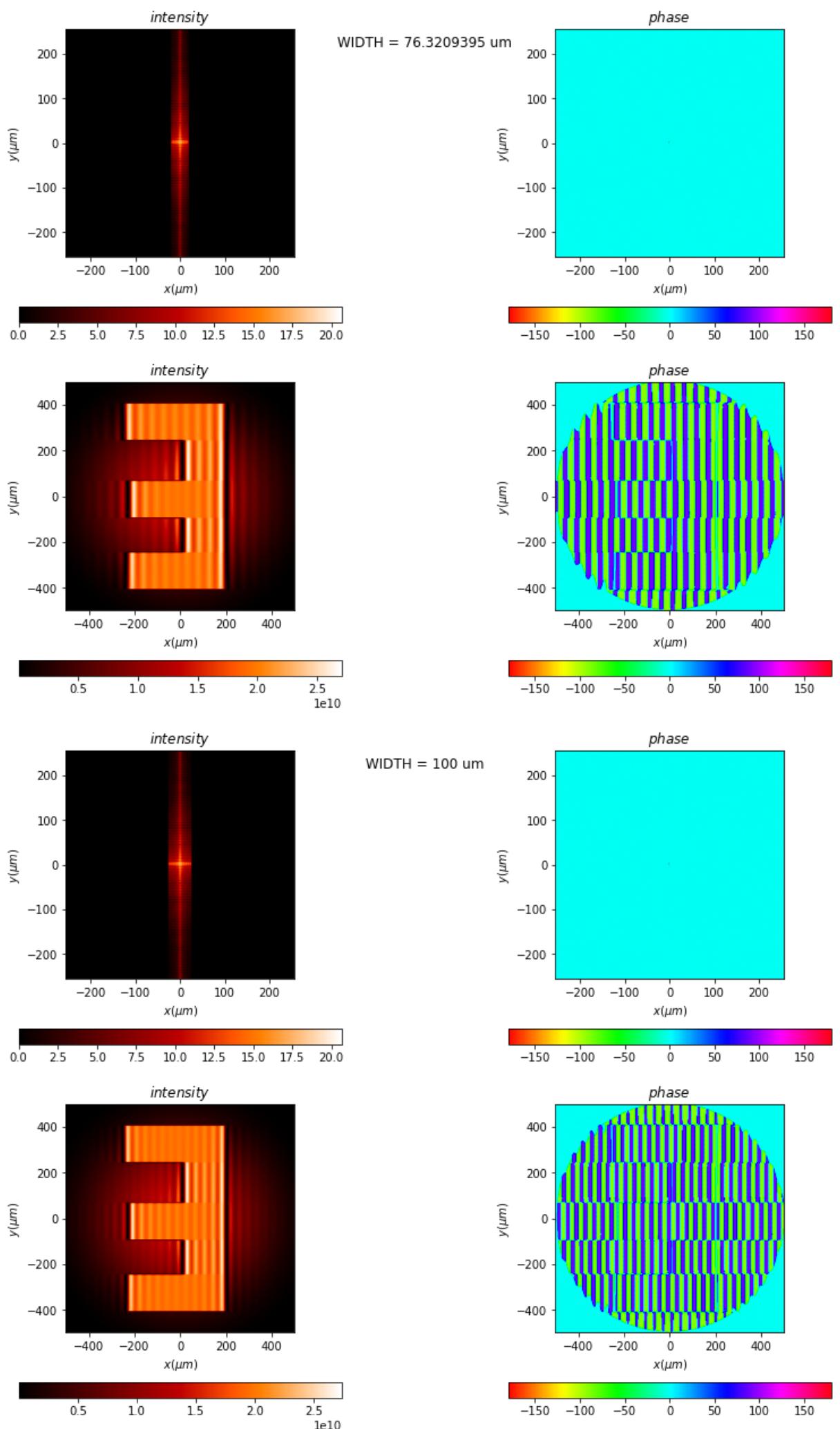
Variable Slit Widths

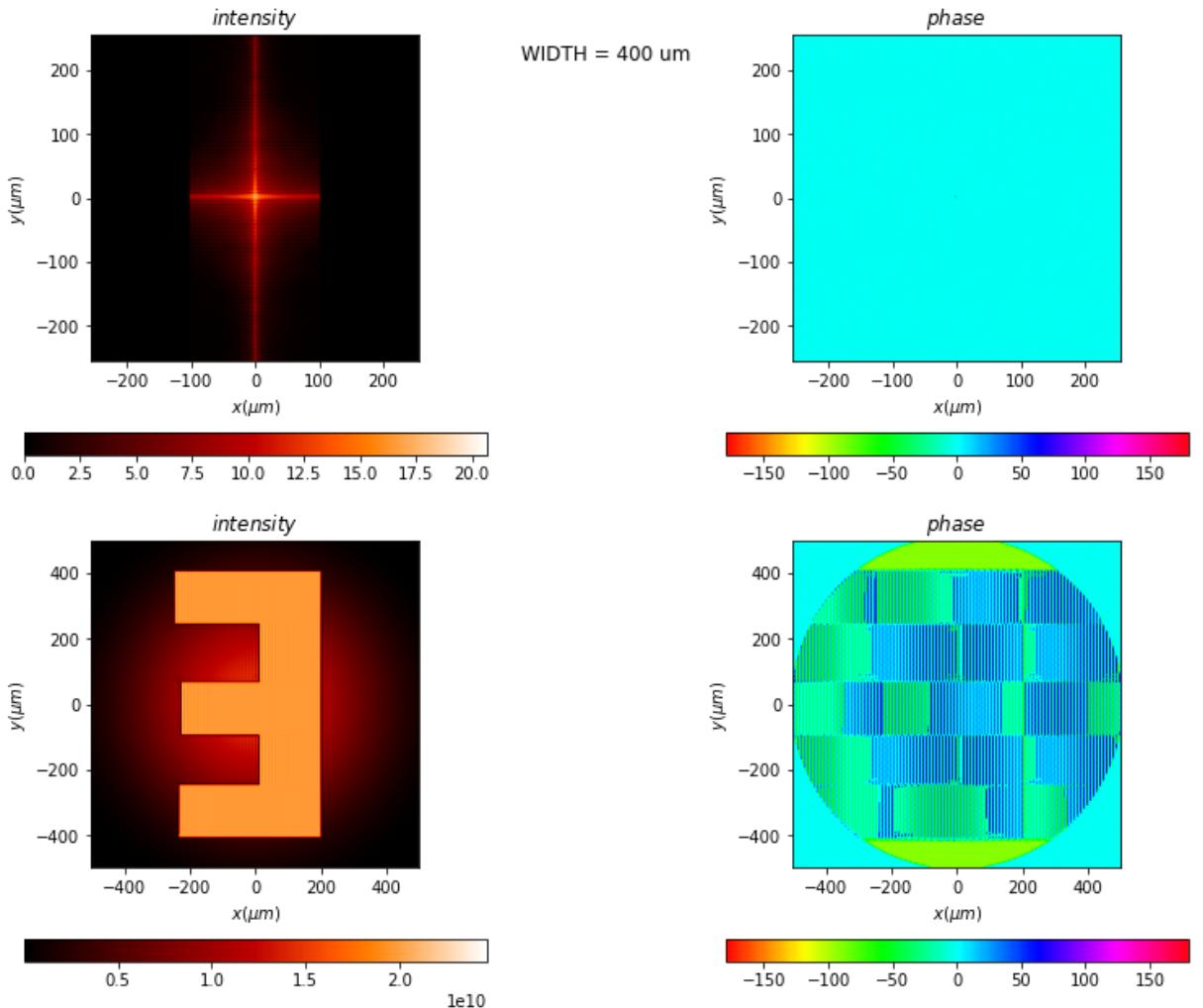
```
In [26]: widths = [10, 30, 50, 76.3209395, 100, 400] # in um
for width in widths:
    varSlit = Scalar_mask_XY(x0, y0, wavelength)
    varSlit.slit(
        x0=0 * um,
        size=width * um
    )

    E_a_L1_VarSlit, E_a_L1_VarSlit_L2 = sim(E_a_L1, varSlit)
    E_a_L1_VarSlit.draw(title=f" WIDTH = {width} um ", kind='field', logarithm=True)
    E_a_L1_VarSlit_L2.draw(kind='field', logarithm=False)
```









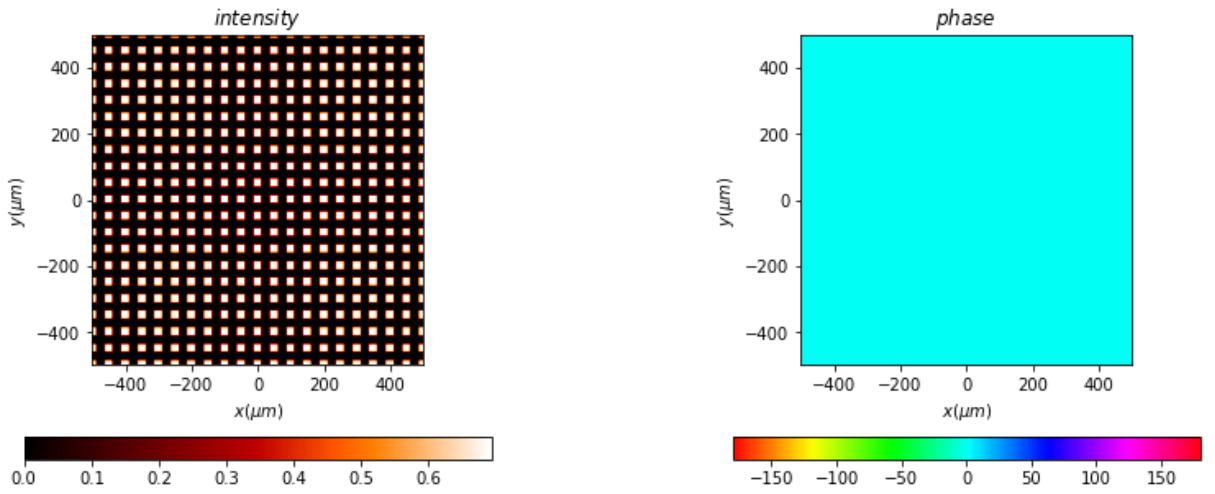
We can observe the "letter being assembled" from various modes, as higher frequencies are allowed to pass through.

Mesh

```
In [27]: mesh = Scalar_mask_XY(x0, y0, wavelength)
mesh.grating_2D(
    period=50 * um,
    fill_factor=0.5,
    angle=0 * degrees
)

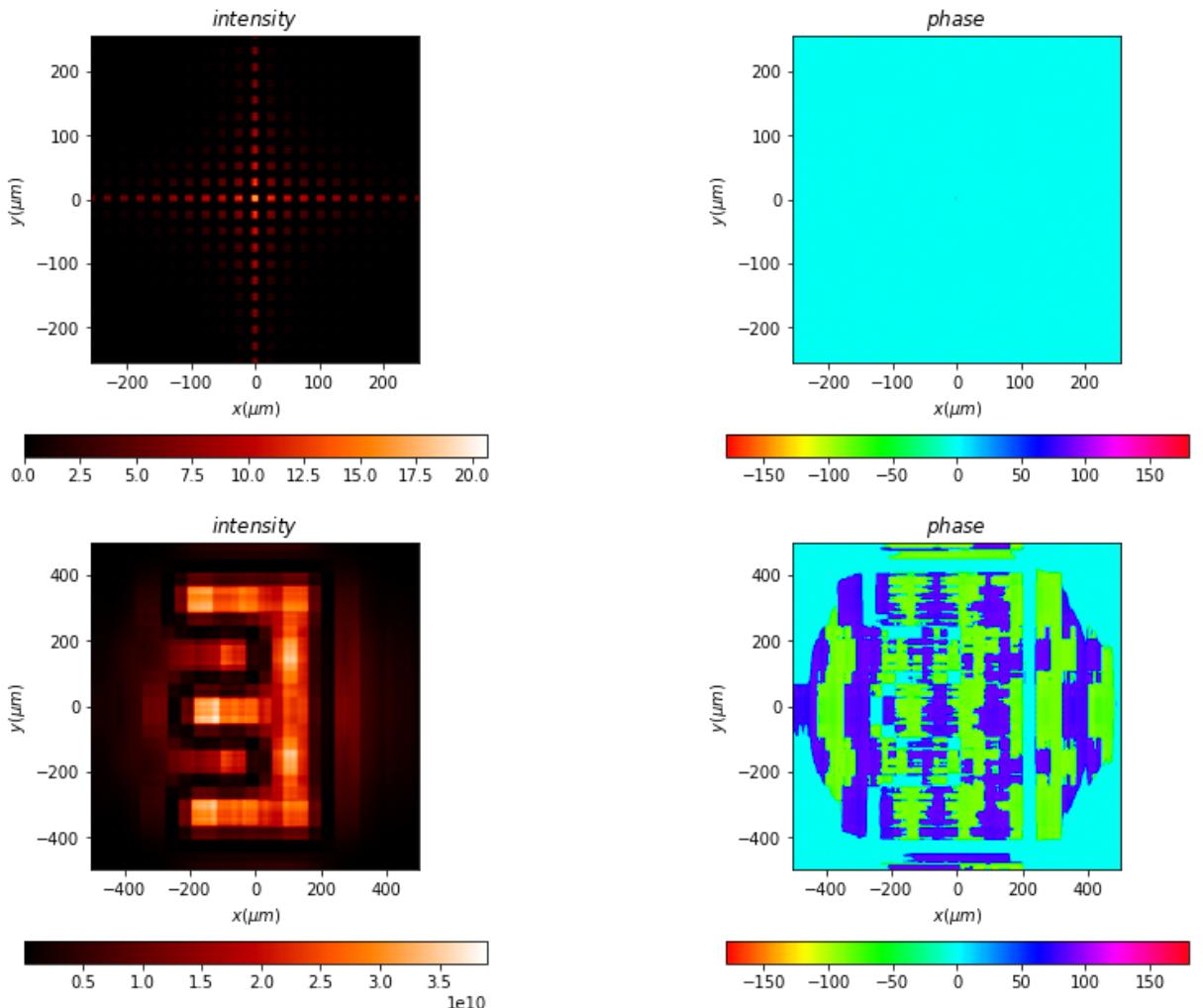
mesh.draw(kind='field', logarithm=True)
```

```
Out[27]: ((<matplotlib.image.AxesImage at 0x218e78d8fd0>,
 <matplotlib.image.AxesImage at 0x218e7b4e8b0>),
None,
None)
```



```
In [28]: E_a_L1_Mesh, E_a_L1_Mesh_L2 = sim(E_a_L1, mesh)
E_a_L1_Mesh.draw(kind='field', logarithm=True)
E_a_L1_Mesh_L2.draw(kind='field', logarithm=False)
```

```
Out[28]: (<matplotlib.image.AxesImage at 0x218e91c9c70>,
<matplotlib.image.AxesImage at 0x218e9234ee0>),
None,
None)
```



One can obtain similar results with the "F" alphabet-mask.

Phase Contrast Imaging - Using phase information to filter overlapped images

```
In [1]: import numpy as np
from diffraction import mm, um, degrees
from diffraction.scalar_sources_XY import Scalar_source_XY
from diffraction.scalar_masks_XY import Scalar_mask_XY

# Setting up
length = 1 * mm
num_data = 512
x0 = np.linspace(-length / 2, length / 2, num_data)
y0 = np.linspace(-length / 2, length / 2, num_data)
wavelength = 0.633 * um
```

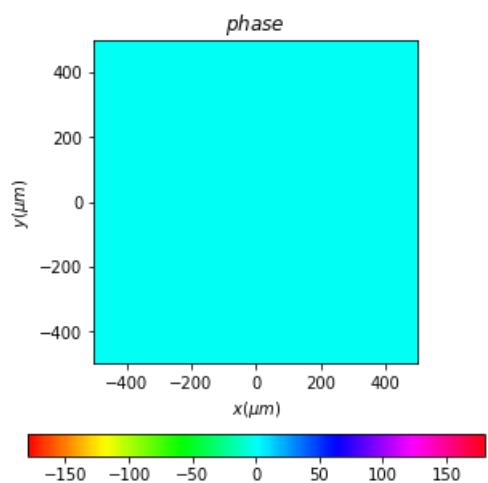
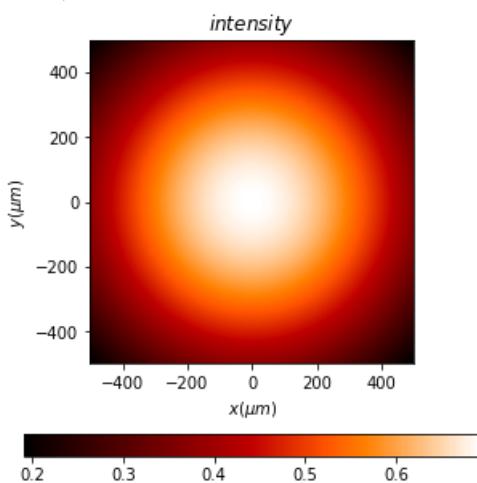
number of processors: 12

Setting up source

- Gaussian Beam (LASER)

```
In [2]: # Gaussian Beam Source - like a LASER
u0 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
u0.gauss_beam(r0=(0, 0), w0=(800 * um, 800 * um), z0=0.0)
u0.draw(kind='field', logarithm=True)
```

```
Out[2]: ((<matplotlib.image.AxesImage at 0x14e0a72da60>,
 <matplotlib.image.AxesImage at 0x14e0a9cc220>),
None,
None)
```



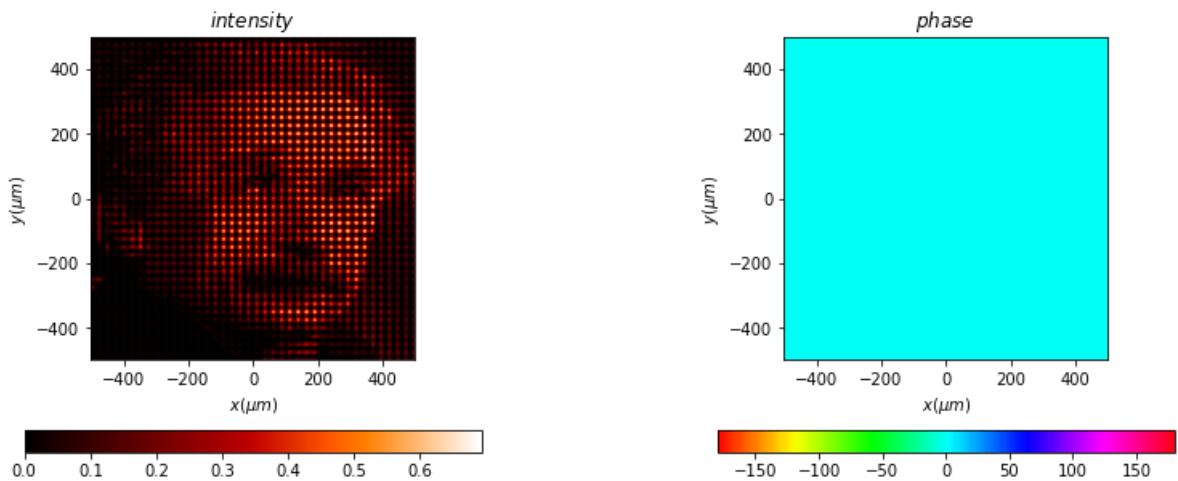
```
In [3]: # Plane Wave Source - Just an experiment
# u1 = Scalar_source_XY(x=x0, y=y0, wavelength=wavelength)
# u1.plane_wave()
# u1.draw(kind='field', logarithm=True)
```

Image - Phase Contrast

Composition of Horizontal and Vertical Lines

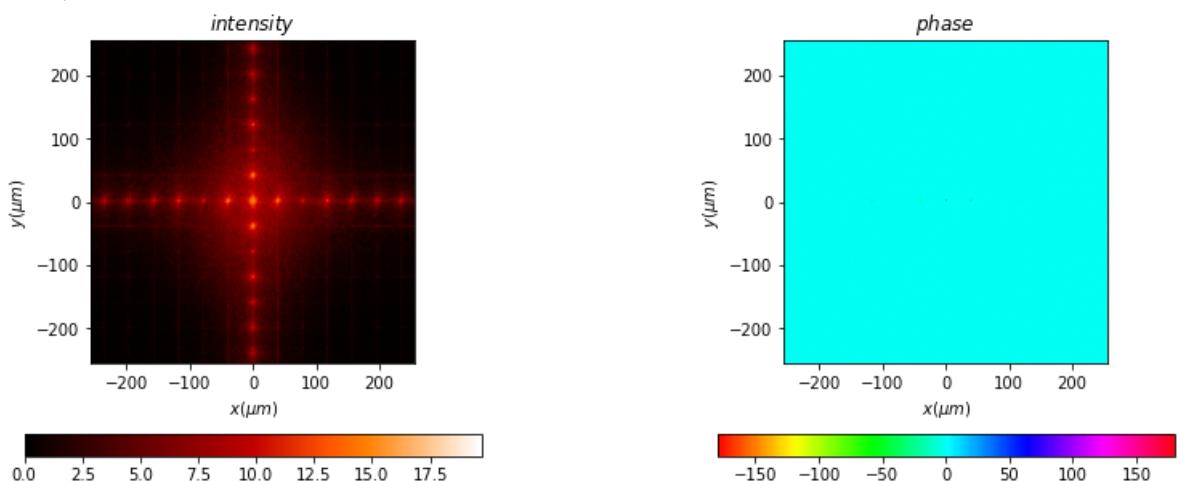
```
In [4]: compLines = Scalar_mask_XY(x0, y0, wavelength)
compLines.image(
    filename="complines-4.png",
    normalize=True,
    canal=2,
)
compLines.draw(kind='field', logarithm=True)
# compLines.draw(kind='real_field', logarithm=True)
# compLines.draw(kind='amplitude', logarithm=True)
```

```
Out[4]: ((<matplotlib.image.AxesImage at 0x14e0b1f11c0>,
 <matplotlib.image.AxesImage at 0x14e0b452940>),
None,
None)
```



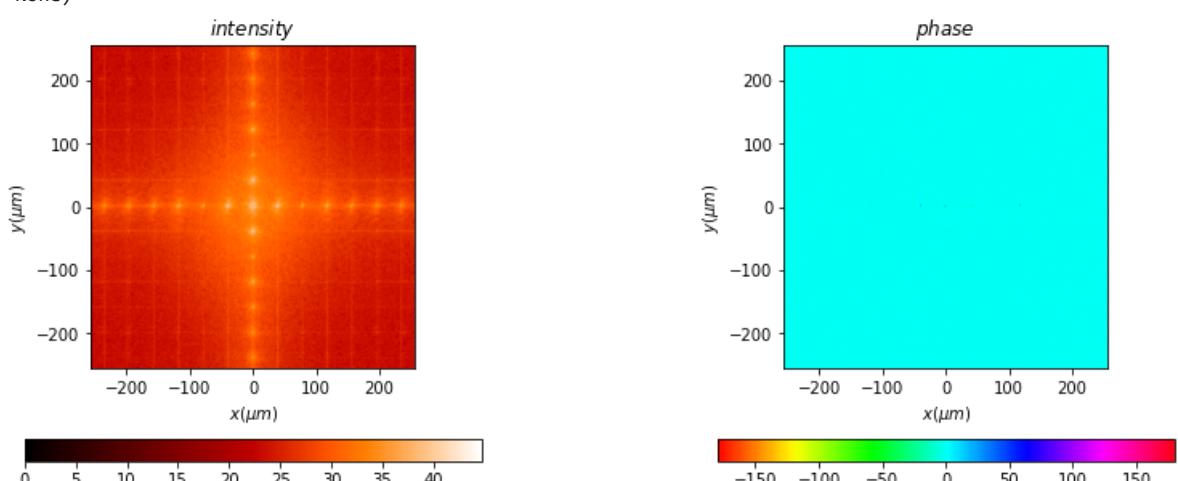
```
In [5]: a_L1 = (u0 * compLines).fft(z=1 * mm, new_field=True)
a_L1.draw(kind='field', logarithm=True)
# a_L1.draw(kind='amplitude', Logarithm=False)
```

```
Out[5]: (<matplotlib.image.AxesImage at 0x14e0b06c880>,
<matplotlib.image.AxesImage at 0x14e0b111070>),
None,
None)
```



```
In [6]: a_L2_NF = (a_L1.fft(z=1 * mm, shift=False, remove0=False, new_field=True)).fft(z=1 * mm, shift=False, remove0=False)
a_L2_NF.draw(kind='field', logarithm=True)
# a_L2_NF.draw(kind='real_field', logarithm=True)
```

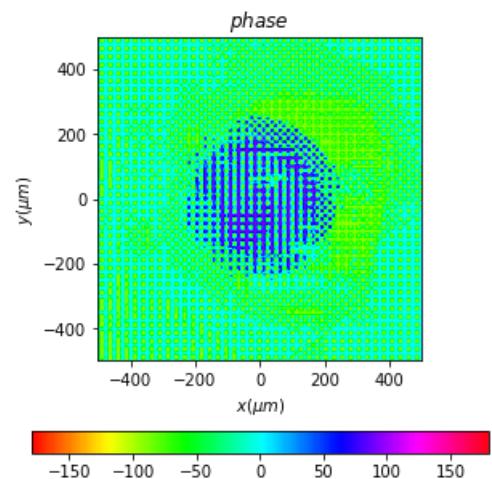
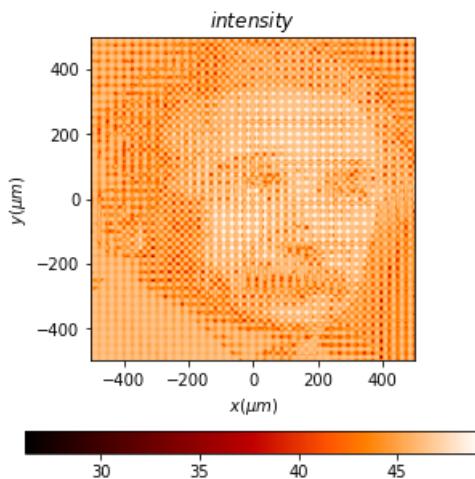
```
Out[6]: (<matplotlib.image.AxesImage at 0x14e0b8b3c70>,
<matplotlib.image.AxesImage at 0x14e0fd98460>),
None,
None)
```



```
In [7]: IFFT_NF = a_L2_NF.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
IFFT_NF.draw(kind='field', logarithm=True)
```

```
Out[7]: (<matplotlib.image.AxesImage at 0x14e0fe49fd0>,
```

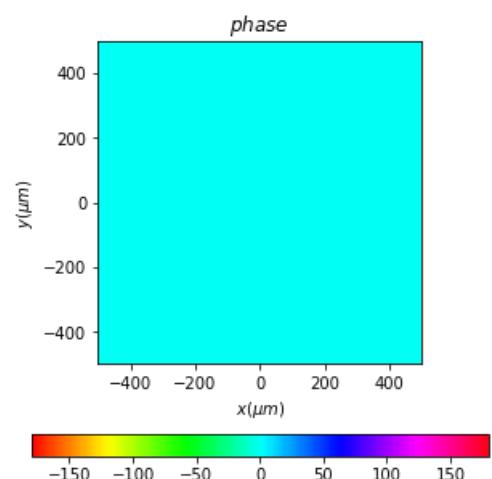
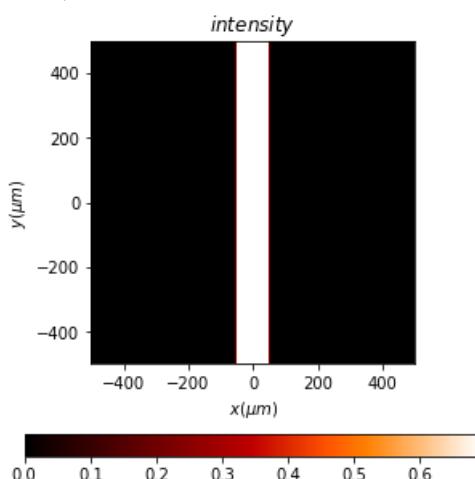
```
<matplotlib.image.AxesImage at 0x14e10712790>),
None,
None)
```



```
In [8]: csize = 100 # Size of slit
```

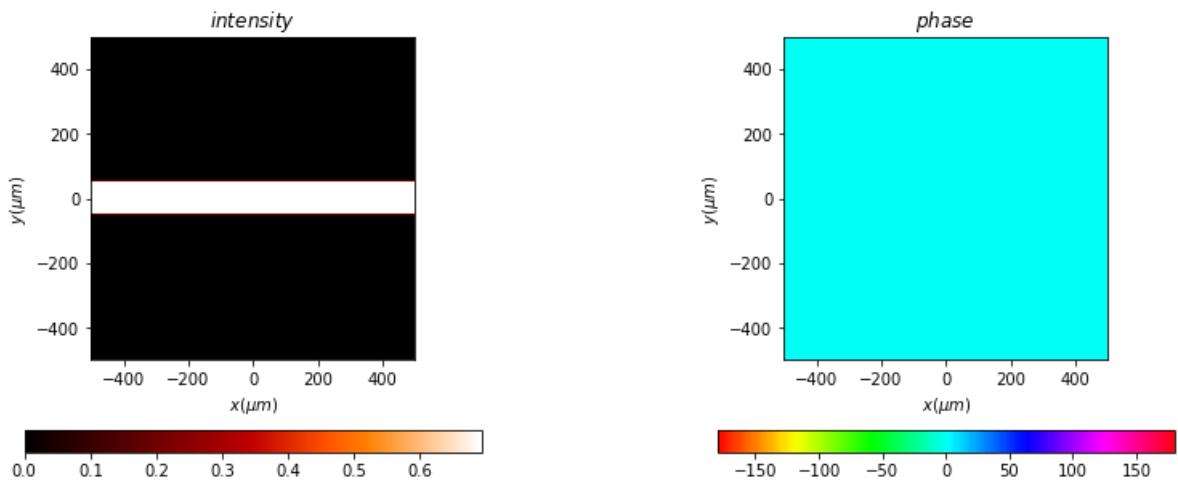
```
In [9]: vertSlit = Scalar_mask_XY(x0, y0, wavelength)
vertSlit.slit(
    x0=0 * um,
    size=csize * um
)
vertSlit.draw(kind='field', logarithm=True)
```

```
Out[9]: (<matplotlib.image.AxesImage at 0x14e0b45e340>,
<matplotlib.image.AxesImage at 0x14e0b0aa970>),
None,
None)
```



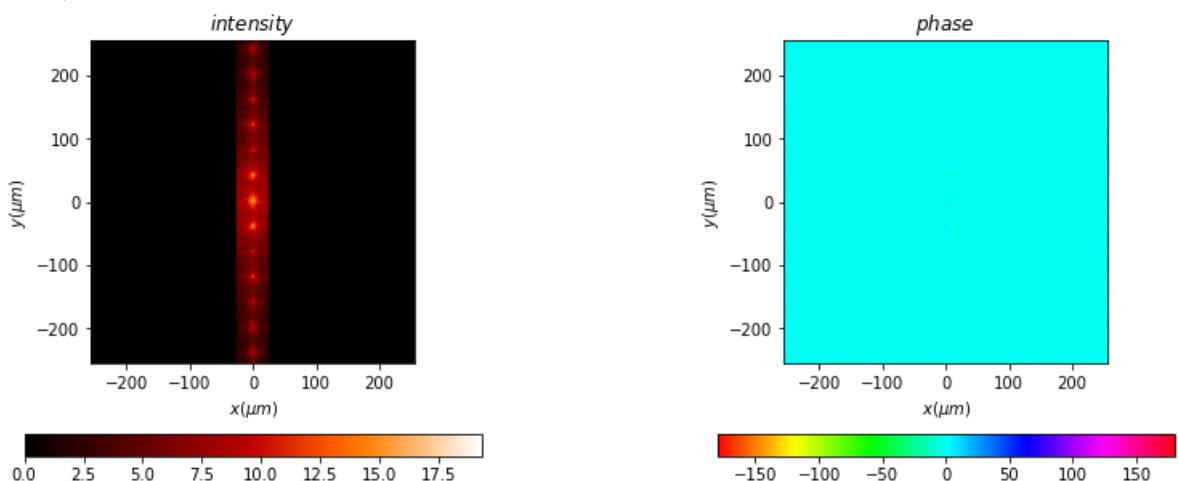
```
In [10]: horizSlit = Scalar_mask_XY(x0, y0, wavelength)
horizSlit.slit(
    x0=0 * um,
    size=csize * um,
    angle=np.pi / 2
)
horizSlit.draw(kind='field', logarithm=True)
```

```
Out[10]: (<matplotlib.image.AxesImage at 0x14e112b4eb0>,
<matplotlib.image.AxesImage at 0x14e1136b670>),
None,
None)
```



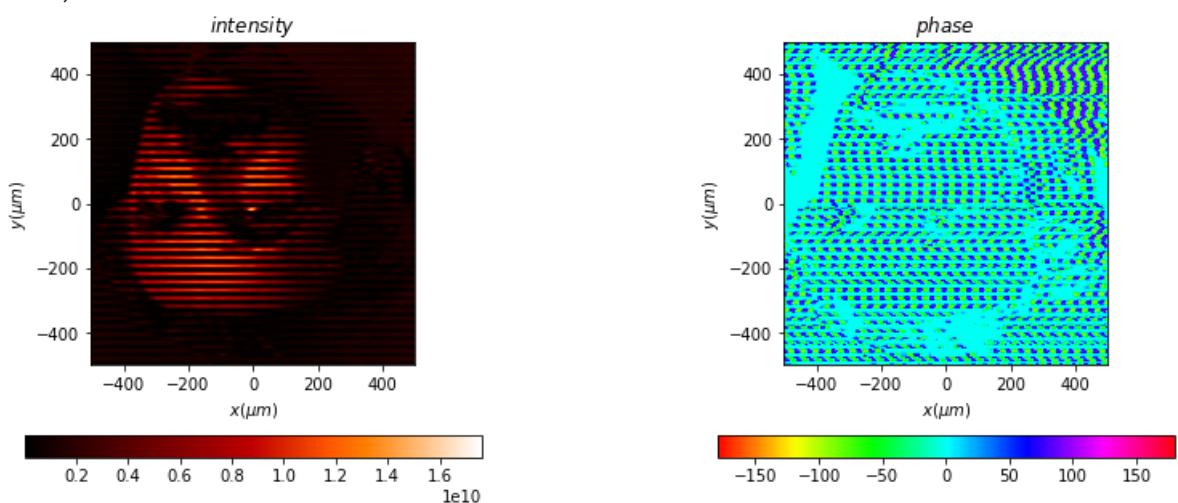
```
In [11]: b_L2_a_vS = a_L1 * vertSlit
b_L2_a_vS.draw(kind='field', logarithm=True)
# b_L2_a_vS.draw(kind='amplitude', logarithm=True)
```

```
Out[11]: (<matplotlib.image.AxesImage at 0x14e12921490>,
<matplotlib.image.AxesImage at 0x14e12983c40>),
None,
None)
```



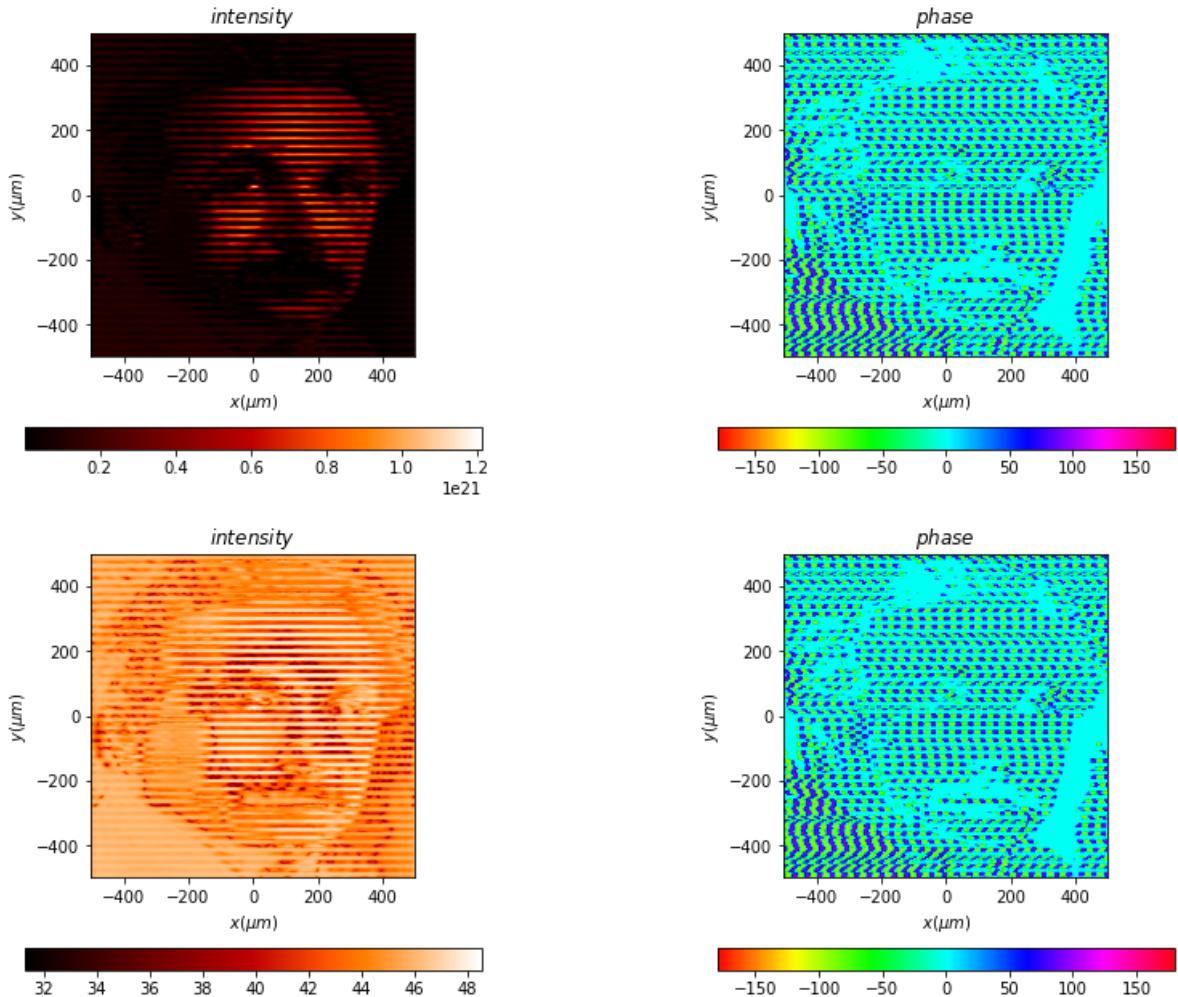
```
In [12]: a_L2_vS = b_L2_a_vS.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
a_L2_vS.draw(kind='field', logarithm=False)
# a_L2_vS.draw(kind='intensity', logarithm=True)
```

```
Out[12]: (<matplotlib.image.AxesImage at 0x14e12a45760>,
<matplotlib.image.AxesImage at 0x14e1331b7c0>),
None,
None)
```



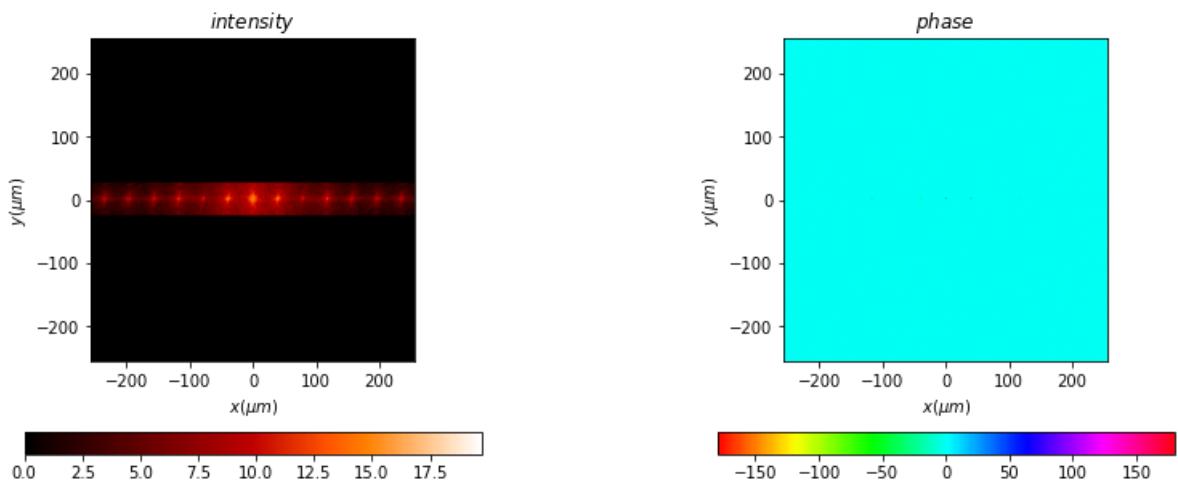
```
In [13]: IFFT_vS = (a_L2_vS.fft(z=1 * mm, shift=False, remove0=False, new_field=True)).fft(z=1 * mm, shift=False, remove0=False, new_field=True)
IFFT_vS.draw(kind='field', logarithm=False)
IFFT_vS.draw(kind='field', logarithm=True)
```

```
Out[13]: ((<matplotlib.image.AxesImage at 0x14e0b0c38e0>,
    <matplotlib.image.AxesImage at 0x14e128b60d0>),
None,
None)
```



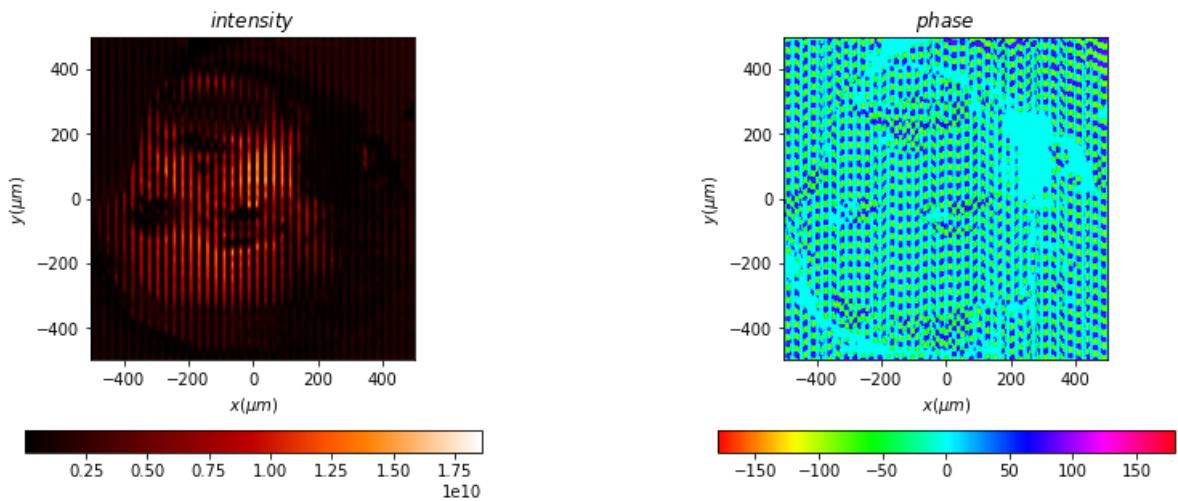
```
In [14]: b_L2_a_hS = a_L1 * horizSlit
b_L2_a_hS.draw(kind='field', logarithm=True)
# b_L2_a_hS.draw(kind='amplitude', Logarithm=True)
```

```
Out[14]: ((<matplotlib.image.AxesImage at 0x14e14874a00>,
    <matplotlib.image.AxesImage at 0x14e148ff220>),
None,
None)
```



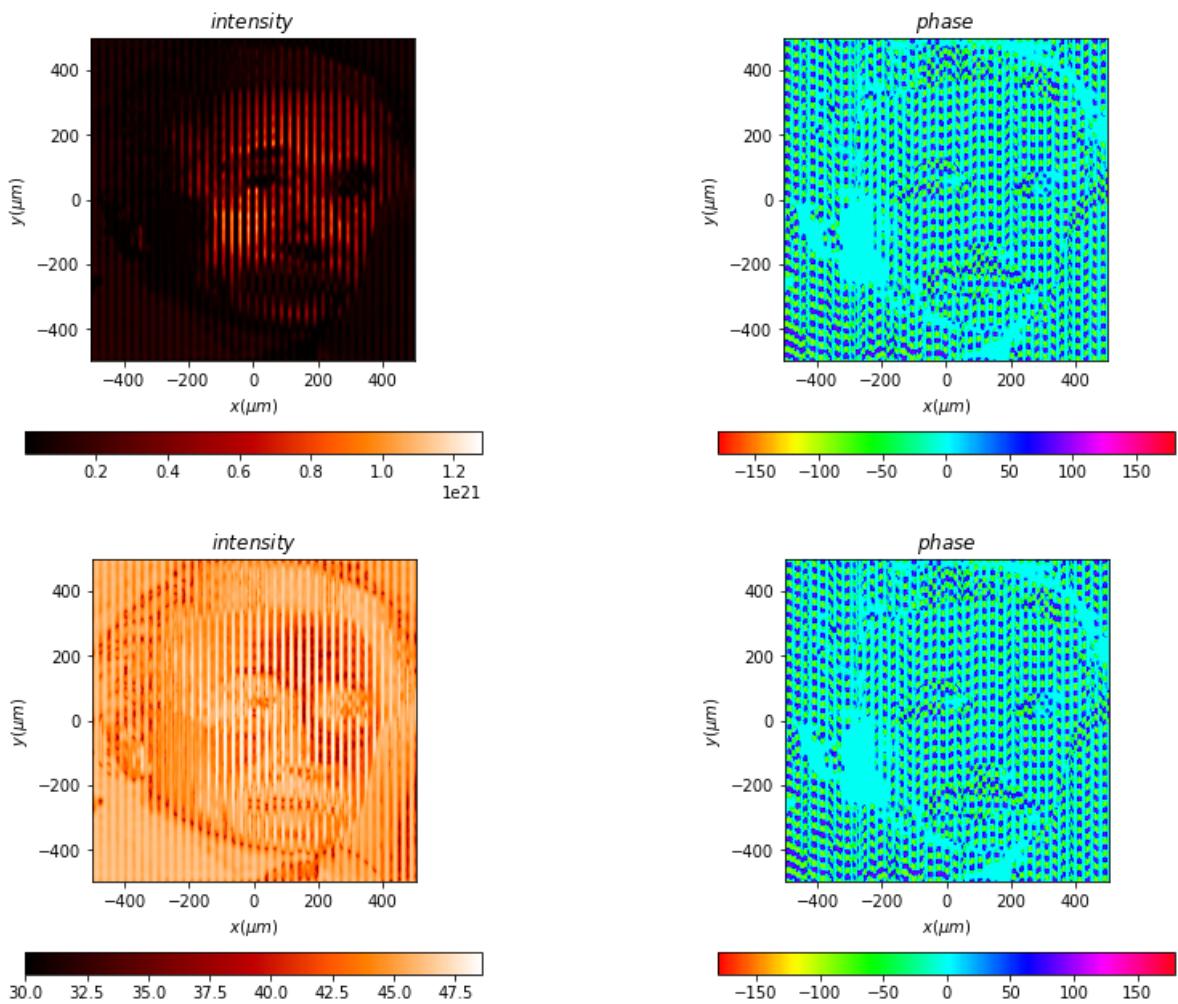
```
In [15]: a_L2_hS = b_L2_a_hS.fft(z=1 * mm, shift=False, remove0=False, new_field=True)
a_L2_hS.draw(kind='field', logarithm=False)
# a_L2_hS.draw(kind='intensity', Logarithm=True)
```

```
Out[15]: ((<matplotlib.image.AxesImage at 0x14e16c12c40>,
    <matplotlib.image.AxesImage at 0x14e16c98400>),
None,
None)
```



```
In [16]: IFFT_hS = (a_L2_hS.fft(z=1 * mm, shift=False, remove0=False, new_field=True)).fft(z=1 * mm, shift=False, remove0=False, new_field=True)
IFFT_hS.draw(kind='field', logarithm=False)
IFFT_hS.draw(kind='field', logarithm=True)
```

```
Out[16]: (<matplotlib.image.AxesImage at 0x14e182461f0>,
<matplotlib.image.AxesImage at 0x14e182b04f0>),
None,
None)
```



```
In [ ]:
```