

Chapter 2: Introduction to Relational Model

Database System Concepts, 7th Ed.

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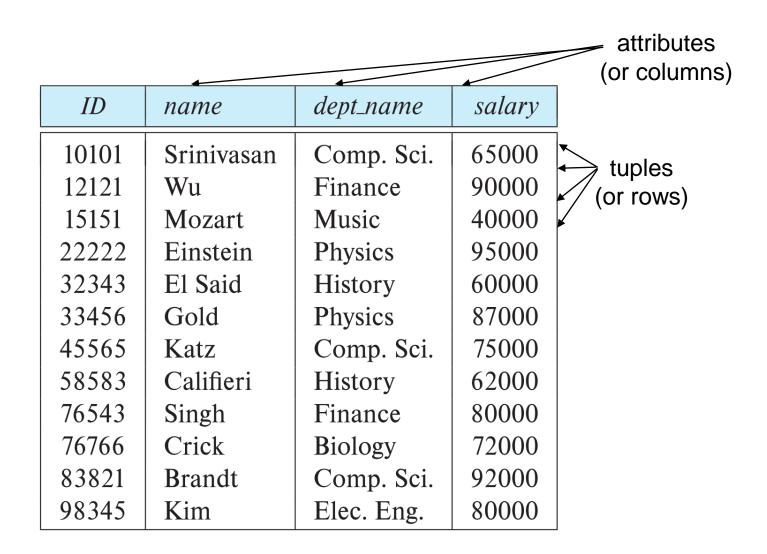


Outline

- □ Structure of Relational Databases
- □ Database Schema
- □ Keys
- □ Schema Diagrams
- □ Relational Query Languages
- ☐ The Relational Algebra



Example of a Instructor Relation





Relation Schema and Instance

- \square $A_1, A_2, ..., A_n$ are attributes
- \square $R = (A_1, A_2, ..., A_n)$ is a relation schema Example:

instructor = (ID, name, dept_name, salary)

- \square A relation instance *r* defined over schema *R* is denoted by r(R).
- The current values a relation are specified by a table
- ☐ An element *t* of relation *r* is called a *tuple* and is represented by a *row* in a table



Attributes

- The set of allowed values for each attribute is called the domain of the attribute
- ☐ Attribute values are (normally) required to be **atomic**; that is, indivisible
- ☐ The special value *null* is a member of every domain. Indicated that the value is "unknown"
- The null value causes complications in the definition of many operations



Relation Schema and Instance

- \Box $A_1, A_2, ..., A_n$ are attributes
- $R = (A_1, A_2, ..., A_n)$ is a relation schema Example:

instructor = (ID, name, dept_name, salary)

- Formally, given sets D₁, D₂, Dₙ a relation r is a subset of D₁ x D₂ x ... x Dₙ
 Thus, a relation is a set of n-tuples (a₁, a₂, ..., aₙ) where each aᵢ ∈ Dᵢ
- The current values (relation instance) of a relation are specified by a table
- □ An element *t* of *r* is a *tuple*, represented by a *row* in a table



Relations are Unordered

- Order of tuples is irrelevant (tuples may be stored in an arbitrary order)
- □ Example: instructor relation with unordered tuples

ID	name	dept_name	salary
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000



Database Schema

- □ Database schema -- is the logical structure of the database.
- Database instance -- is a snapshot of the data in the database at a given instant in time.
- Example:
 - □ schema: instructor (ID, name, dept_name, salary)
 - Instance:

ID	name	dept_name	salary
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000

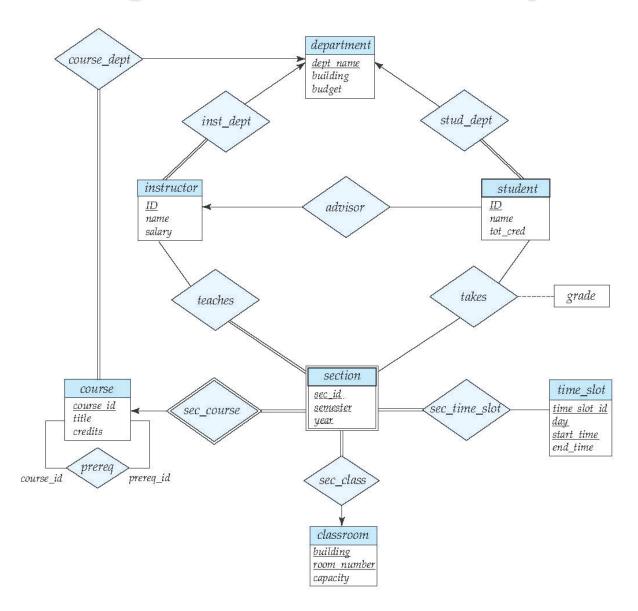


Keys

- \square Let $K \subset R$
- \square K is a **superkey** of R if values for K are sufficient to identify a unique tuple of each possible relation r(R)
 - □ Example: {*ID*} and {ID,name} are both superkeys of *instructor*.
- ☐ Superkey *K* is a **candidate key** if *K* is minimal Example: {*ID*} is a candidate key for *Instructor*
- ☐ One of the candidate keys is selected to be the **primary key**.
 - Which one?
- ☐ Foreign key constraint: Value in one relation must appear in another
 - Referencing relation
 - Referenced relation
 - Example: dept_name in instructor is a foreign key from instructor referencing department

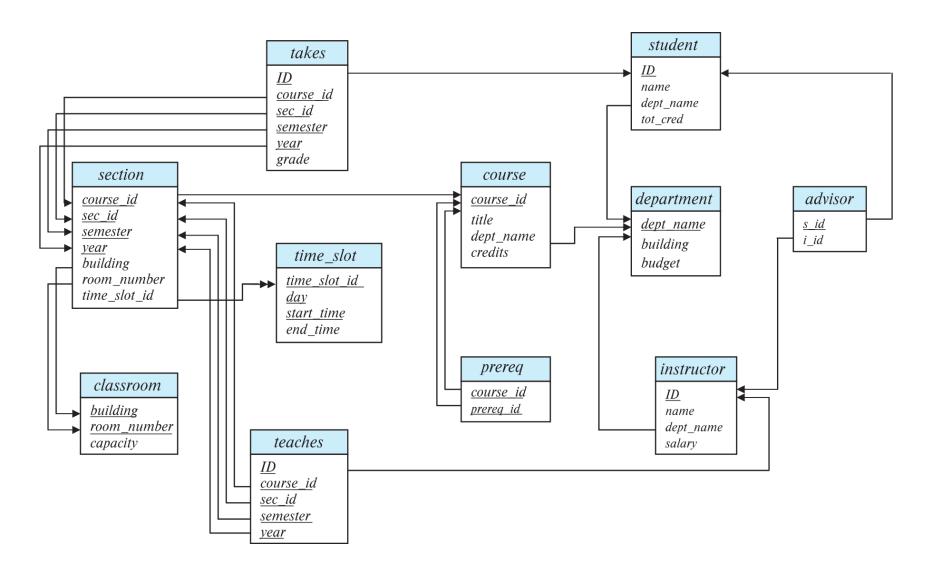


E-R Diagram for a University Enterprise





Schema Diagram for University Database





Relational Query Languages

- ☐ Procedural versus non-procedural, or declarative
- □ "Pure" languages:
 - Relational algebra
 - Tuple relational calculus
 - Domain relational calculus
- □ The above 3 pure languages are equivalent in computing power
- We will concentrate in this chapter on relational algebra
 - Not Turing-machine equivalent
 - Consists of 6 basic operations



Relational Algebra

- ☐ A procedural language consisting of a set of operations that take one or two relations as input and produce a new relation as their result.
- ☐ Six basic operators
 - select: σ
 - □ project: ∏
 - □ union: ∪
 - set difference: –
 - Cartesian product: x
 - \square rename: ρ



Select Operation

- ☐ The **selec**t operation selects tuples that satisfy a given predicate.
- \square Notation: $\sigma_p(r)$
- \Box p is called the **selection predicate**
- Example: select those tuples of the instructor relation where the instructor is in the "Physics" department.
 - Query

$$\sigma_{dept_name="Physics"}(instructor)$$

Result

ID	name	dept_name	salary
22222	Einstein	Physics	95000
33456	Gold	Physics	87000



Select Operation (Cont.)

☐ We allow comparisons using

in the selection predicate.

We can combine several predicates into a larger predicate by using the connectives:

$$\land$$
 (and), \lor (or), \neg (not)

Example: Find the instructors in Physics with a salary greater \$90,000, we write:

$$\sigma_{dept_name="Physics"} \land salary > 90,000 (instructor)$$

- The select predicate may include comparisons between two attributes.
 - Example, find all departments whose name is the same as their building name:
 - \Box $\sigma_{dept_name=building}$ (department)



Project Operation

- ☐ A unary operation that returns its argument relation, with certain attributes left out.
- Notation:

$$\prod_{A_1,A_2,A_3...A_k} (r)$$

where A_1, A_2, \dots, A_k are attribute names and r is a relation name.

- ☐ The result is defined as the relation of *k* columns obtained by erasing the columns that are not listed
- Duplicate rows removed from result, since relations are sets



Project Operation Example

☐ Example: eliminate the *dept_name* attribute of *instructor*

□ Query:

 $\prod_{ID, name, salary}$ (instructor)

Result:

ID	пате	salary
10101	Srinivasan	65000
12121	Wu	90000
15151	Mozart	40000
22222	Einstein	95000
32343	El Said	60000
33456	Gold	87000
45565	Katz	75000
58583	Califieri	62000
76543	Singh	80000
76766	Crick	72000
83821	Brandt	92000
98345	Kim	80000



Composition of Relational Operations

- ☐ The result of a relational-algebra operation is relation and therefore of relational-algebra operations can be composed together into a **relational-algebra expression**.
- ☐ Consider the query -- Find the names of all instructors in the Physics department.

$$\prod_{name} (\sigma_{dept_name = "Physics"} (instructor))$$

☐ Instead of giving the name of a relation as the argument of the projection operation, we give an expression that evaluates to a relation.



Cartesian-Product Operation

The Cartesian-product operation (denoted by X) allows us to combine information from any two relations.

□ Example: the Cartesian product of the relations *instructor* and teaches is written as:

instructor X teaches

- We construct a tuple of the result out of each possible pair of tuples: one from the *instructor* relation and one from the *teaches* relation (see next slide)
- ☐ Since the instructor *ID* appears in both relations we distinguish between these attribute by attaching to the attribute the name of the relation from which the attribute originally came.
 - instructor.ID
 - teaches.ID



The instructor X teaches table

instructor.ID	name	dept_name	salary	teaches.ID	course_id	sec_id	semester	year
10101	Srinivasan	Comp. Sci.	65000	10101	CS-101	1	Fall	2017
10101	Srinivasan	Comp. Sci.	65000	10101	CS-315	1	Spring	2018
10101	Srinivasan	Comp. Sci.	65000	10101	CS-347	1	Fall	2017
10101	Srinivasan	Comp. Sci.	65000	12121	FIN-201	1	Spring	2018
10101	Srinivasan	Comp. Sci.	65000	15151	MU-199	1	Spring	2018
10101	Srinivasan	Comp. Sci.	65000	22222	PHY-101	1	Fall	2017
					•••			
12121	Wu	Finance	90000	10101	CS-101	1	Fall	2017
12121	Wu	Finance	90000	10101	CS-315	1	Spring	2018
12121	Wu	Finance	90000	10101	CS-347	1	Fall	2017
12121	Wu	Finance	90000	12121	FIN-201	1	Spring	2018
12121	Wu	Finance	90000	15151	MU-199	1	Spring	2018
12121	Wu	Finance	90000	22222	PHY-101	1	Fall	2017
•••								
15151	Mozart	Music	40000	10101	CS-101	1	Fall	2017
15151	Mozart	Music	40000	10101	CS-315	1	Spring	2018
15151	Mozart	Music	40000	10101	CS-347	1	Fall	2017
15151	Mozart	Music	40000	12121	FIN-201	1	Spring	2018
15151	Mozart	Music	40000	15151	MU-199	1	Spring	2018
15151	Mozart	Music	40000	22222	PHY-101	1	Fall	2017
•••								
22222	Einstein	Physics	95000	10101	CS-101	1	Fall	2017
22222	Einstein	Physics	95000	10101	CS-315	1	Spring	2018
22222	Einstein	Physics	95000	10101	CS-347	1	Fall	2017
22222	Einstein	Physics	95000	12121	FIN-201	1	Spring	2018
22222	Einstein	Physics	95000	15151	MU-199	1	Spring	2018
22222	Einstein	Physics	95000	22222	PHY-101	1	Fall	2017
•••								
•••			•••		•••		•••	



Join Operation

The Cartesian-Product

instructor X teaches

associates every tuple of instructor with every tuple of teaches.

- Most of the resulting rows have information about instructors who did NOT teach a particular course.
- ☐ To get only those tuples of "instructor X teaches" that pertain to instructors and the courses that they taught, we write:

```
\sigma_{instructor.id = teaches.id} (instructor x teaches))
```

- □ We get only those tuples of "instructor X teaches" that pertain to instructors and the courses that they taught.
- ☐ The result of this expression, shown in the next slide



Join Operation (Cont.)

☐ The table corresponding to:

 $\sigma_{instructor.id = teaches.id}$ (instructor x teaches))

instructor.ID	name	dept_name	salary	teaches.ID	course_id	sec_id	semester	year
10101	Srinivasan	Comp. Sci.	65000	10101	CS-101	1	Fall	2017
10101	Srinivasan	Comp. Sci.	65000	10101	CS-315	1	Spring	2018
10101	Srinivasan	Comp. Sci.	65000	10101	CS-347	1	Fall	2017
12121	Wu	Finance	90000	12121	FIN-201	1	Spring	2018
15151	Mozart	Music	40000	15151	MU-199	1	Spring	2018
22222	Einstein	Physics	95000	22222	PHY-101	1	Fall	2017
32343	El Said	History	60000	32343	HIS-351	1	Spring	2018
45565	Katz	Comp. Sci.	75000	45565	CS-101	1	Spring	2018
45565	Katz	Comp. Sci.	75000	45565	CS-319	1	Spring	2018
76766	Crick	Biology	72000	76766	BIO-101	1	Summer	2017
76766	Crick	Biology	72000	76766	BIO-301	1	Summer	2018
83821	Brandt	Comp. Sci.	92000	83821	CS-190	1	Spring	2017
83821	Brandt	Comp. Sci.	92000	83821	CS-190	2	Spring	2017
83821	Brandt	Comp. Sci.	92000	83821	CS-319	2	Spring	2018
98345	Kim	Elec. Eng.	80000	98345	EE-181	1	Spring	2017



Join Operation (Cont.)

- ☐ The **join** operation allows us to combine a select operation and a Cartesian-Product operation into a single operation.
- \square Consider relations r(R) and s(S)
- Let "theta" be a predicate on attributes in the schema R "union" S. The join operation r

 simple size is defined as follows:

Thus

 $\sigma_{instructor.id = teaches.id}$ (instructor x teaches))

☐ Can equivalently be written as

instructor

Instructor.id = teaches.id teaches.



Union Operation

- ☐ The union operation allows us to combine two relations
- \square Notation: $r \cup s$
- \square For $r \cup s$ to be valid.
 - 1. *r*, *s* must have the *same* **arity** (same number of attributes)
 - 2. The attribute domains must be **compatible** (example: 2^{nd} column of r deals with the same type of values as does the 2^{nd} column of s)
- □ Example: to find all courses taught in the Fall 2017 semester, or in the Spring 2018 semester, or in both

$$\prod_{course_id} (\sigma_{semester="Fall" \land year=2017}(section)) \cup \prod_{course_id} (\sigma_{semester="Spring" \land year=2018}(section))$$



Union Operation (Cont.)

☐ Result of:

$$\prod_{course_id} (\sigma_{semester="Fall" \land year=2017}(section)) \cup \prod_{course_id} (\sigma_{semester="Spring" \land year=2018}(section))$$

course_id

CS-101 CS-315 CS-319 CS-347 FIN-201 HIS-351 MU-199 PHY-101



Set-Intersection Operation

- ☐ The set-intersection operation allows us to find tuples that are in both the input relations.
- □ Notation: $r \cap s$
- Assume:
 - \square r, s have the same arity
 - attributes of r and s are compatible
- □ Example: Find the set of all courses taught in both the Fall 2017 and the Spring 2018 semesters.

$$\prod_{course_id} (\sigma_{semester="Fall" \land year=2017}(section)) \cap \prod_{course_id} (\sigma_{semester="Spring" \land year=2018}(section))$$

Result

course_id
CS-101



Set Difference Operation

- ☐ The set-difference operation allows us to find tuples that are in one relation but are not in another.
- \square Notation r-s
- ☐ Set differences must be taken between **compatible** relations.
 - r and s must have the same arity
 - attribute domains of r and s must be compatible
- Example: to find all courses taught in the Fall 2017 semester,
 but not in the Spring 2018 semester

$$\Pi_{course_id}$$
 ($\sigma_{semester="Fall" \land year=2017}$ (section)) - Π_{course_id} ($\sigma_{semester="Spring" \land year=2018}$ (section))

course_id

CS-347

PHY-101



The Assignment Operation

- ☐ It is convenient at times to write a relational-algebra expression by assigning parts of it to temporary relation variables.
- □ The assignment operation is denoted by ← and works like assignment in a programming language.
- □ Example: Find all instructor in the "Physics" and Music department.

Physics
$$\leftarrow \sigma_{dept_name="Physics"}(instructor)$$
Music $\leftarrow \sigma_{dept_name="Music"}(instructor)$
Physics \cup Music

☐ With the assignment operation, a query can be written as a sequential program consisting of a series of assignments followed by an expression whose value is displayed as the result of the query.



The Rename Operation

- \square The results of relational-algebra expressions do not have a name that we can use to refer to them. The rename operator, ρ , is provided for that purpose
- ☐ The expression:

$$\rho_{x}(E)$$

returns the result of expression *E* under the name *x*

☐ Another form of the rename operation:

$$\rho_{x(A1,A2,..An)}(E)$$



Equivalent Queries

- There is more than one way to write a query in relational algebra.
- Example: Find information about courses taught by instructors in the Physics department with salary greater than 90,000
- Query 1

```
\sigma_{dept\_name="Physics"} \land salary > 90,000 (instructor)
```

Query 2

```
\sigma_{dept\_name="Physics"}(\sigma_{salary>90.000}(instructor))
```

☐ The two queries are not identical; they are, however, equivalent -- they give the same result on any database.



Equivalent Queries

- There is more than one way to write a query in relational algebra.
- Example: Find information about courses taught by instructors in the Physics department
- □ Query 1

```
\sigma_{dept\_name="Physics"} (instructor instructor.ID = teaches.ID teaches)
```

☐ Query 2

```
(\sigma_{dept\_name="Physics"}(instructor))_{instructor.ID=teaches.ID} teaches
```

☐ The two queries are not identical; they are, however, equivalent -- they give the same result on any database.



Select Operation – selection of rows (tuples)

Relation r

A	В	C	D
α	α	1	7
α	β	5	7
β	β	12	3
β	β	23	10

$$\bullet$$
 $\sigma_{A=B \land D > 5}(r)$

A	В	C	D
α	α	1	7
β	β	23	10



Project Operation – selection of columns (Attributes)

□ Relation *r*.

\boldsymbol{A}	В	C
α	10	1
α	20	1
β	30	1
β	40	2

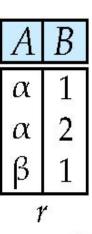
 $\square \prod_{A,C} (r)$

\boldsymbol{A}	C	A	C
α	1	α	1
α	1	β	1
β	1	β	2
β	2		



Union of two relations

□ Relations *r*, *s*:

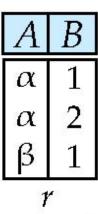


 \square $r \cup s$:



Set difference of two relations

□ Relations *r*, *s*:



A	В
α	2
β	3

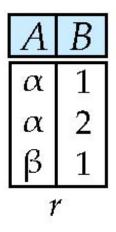
 \square r-s:

A	В
α	1
β	1



Set intersection of two relations

□ Relation *r*, *s*:



$$egin{array}{c|c} A & B \\ \hline $lpha$ & 2 \\ eta & 3 \\ \hline s & \end{array}$$

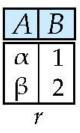
$$\square$$
 $r \cap s$

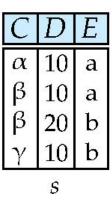
Note:
$$r \cap s = r - (r - s)$$



joining two relations -- Cartesian-product

Relations *r*, *s*:





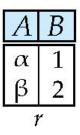
 \square $r \times s$:

A	В	C	D	Ε
α	1	α	10	a
α	1	β	10	a
α	1	β	20	b
α	1	γ	10	b
β	2	α	10	a
β	2	β	10	a
β	2	β	20	b
β	2	γ	10	b



Cartesian-product – naming issue

Relations *r*, *s*:



$$B$$
 D
 E
 α
 10
 a

 β
 10
 a

 β
 20
 b

 γ
 10
 b

 \square $r \times s$:

A	r.B	s.B	D	Ε
α	1	α	10	a
α	1	β	10	a
α	1	β	20	b
α	1	γ	10	b
β	2	α	10	a
β	2	β	10	a
β	2	β	20	b
β	2	γ	10	b



Renaming a Table

☐ Allows us to refer to a relation, (say E) by more than one name.

$$\rho_x(E)$$

returns the expression E under the name X

□ Relations *r*

A	В
α	1
β	2
1	y

 \Box $r \times \rho_s(r)$

r.A	r.B	s.A	s.B
α	1	α	1
α	1	β	2
β	2	α	1
β	2	β	2



Composition of Operations

- Can build expressions using multiple operations
- □ Example: $\sigma_{A=C}(rxs)$
- \square rxs

A	В	C	D	E
α	1	α	10	a
α	1	β	10	a
α	1	β	20	b
α	1	γ	10	b
β	2	α	10	a
β	2	β	10	a
β	2	β	20	b
β	2	γ	10	b

 \Box $\sigma_{A=C}(rxs)$

A	В	C	D	Ε
α	1	α	10	a
β	2	β	10	a
β	2	β	20	b



Joining two relations – Natural Join

- Let r and s be relations on schemas R and S respectively. Then, the "natural join" of relations r and s is a relation on schema $R \cup S$ obtained as follows:
 - Consider each pair of tuples t_r from r and t_s from s.
 - If t_r and t_s have the same value on each of the attributes in $R \cap S$, add a tuple t to the result, where
 - t has the same value as t_r on r
 - t has the same value as t_S on s



Natural Join Example

□ Relations r, s:

A	В	C	D
α	1	α	a
β	2	γ	a
γ	4	β	b
α	1	γ	a
δ	2	β	b
		r	

В	D	Ε
1	a	α
3	a	β
1	a	γ
2	b	δ
3	b	3
	s	

- Natural Join
 - \square r \bowtie s

A	В	C	D	E
α	1	α	a	α
α	1	α	a	γ
α	1	γ	a	α
α	1	γ	a	γ
δ	2	β	b	δ

$$\prod_{A, r.B, C, r.D, E} (\sigma_{r.B = s.B \land r.D = s.D} (r \times s)))$$



Notes about Relational Languages

- Each Query input is a table (or set of tables)
- Each query output is a table
- All data in the output table appears in one of the input tables
- ☐ Can we compute:
 - SUM
 - AVG
 - MAX
 - MIN
 - □ → Using Relational Algebra extensions (Refer to Chapter 6 of the book)



Summary of Relational Algebra Operators

Symbol (Name)	Example of Use
σ (Selection)	σ salary $>$ = 85000 (instructor)
	Return rows of the input relation that satisfy the predicate.
П (Projection)	П ID, salary ^(instructor)
	Output specified attributes from all rows of the input relation. Remove duplicate tuples from the output.
X (Cartesian Product)	instructor x department
	Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.
∪ (Union)	Π name $(instructor) \cup \Pi$ name $(student)$
	Output the union of tuples from the <i>two</i> input relations.
- (Set Difference)	П name (instructor) П name (student)
	Output the set difference of tuples from the two input relations.
⋈ (Natural Join)	instructor ⋈ department
	Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.



End of Chapter 2