

#### Lecture 1:

Chapter 1: Digital Systems and Binary Numbers

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# Agenda

- What's this course about?
- Course Arrangement:
  - Study Materials
  - Teaching Methods
  - Lab Activities,
  - Grading and Assessment
  - Syllabus (Planned)
  - Instructor Contact

# Logistics

- Lectures
  - Tell & Show you digital logic design concepts
- Tutorial and Lab
  - Exercises and Practical matters
- Assignments
  - Weekly Assignment



# What is this course about? What is Logic Design?

#### What is design?

Given a problem specification, come up with a systematic way of finding the solution, that involves choosing appropriate components while meeting some of the design constraints such as size, cost, power, beauty, elegance, etc.

#### What is logic design?

- Determining the collection of digital logic components and the interconnections between them to perform a specified control and/or data manipulation and/or communication functions
- The design may need to be optimized and/or transformed to meet design constraints



# What is this course about? What is Logic Design?

#### Why study Logic Design

- First step to understand computer architectures from both hardware and computations perspectives
- It is the base of all modern computing/ control devices
- It makes all the following possible
  - Microprocessors
  - Storage so inexpensive and dense
  - Wireless networking
  - New materials



# Study Materials

Notes/slides

- 2. Tutorial / Lab Sheets
- 3. Textbook
  - Digital Design [5th Edition] (M. Morris Mano and Michael Ciletti), <u>Download</u> <u>PDF From Here</u>.



# Teaching Methods

- Interactive Lecture
- Discussions
- Problem Based learning
- Assignments
- Experimental learning: Lab Activities devoted to practice Digital Design concepts through a series of hands-on



# Grading and Assessment

Assessment	Marks
Final Written Exam	50
Midterm	15
Quizzes	5
Lab Activities ,Assignments and Tasks	10
Practical Exam	20



# Syllabus

- I. Digital Systems and Binary Numbers
- 2. Boolean Algebra and Logic Gates
- 3. Gate Level Minimization
- 4. Combinational Logic
- 5. Synchronous Sequential Logic
- 6. Registers and Counters



#### Contact

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#### **Outlines**

- ▶ I.I Digital Systems
- ▶ 1.2 Binary Numbers
- ▶ 1.3 Number-base Conversions
- I.4 Octal and Hexadecimal Numbers
- ▶ 1.9 Binary Logic



# Digital Systems

- One characteristic of digital systems is their ability to represent and manipulate discrete elements of information
  - ▶ 10 decimal digits {0,1,2,3,...,9}
  - ▶ 26 letters of alphabet {A, B, C, ...,Z}
  - ▶ 64 squares of chessboard



# Analog and Digital Signal

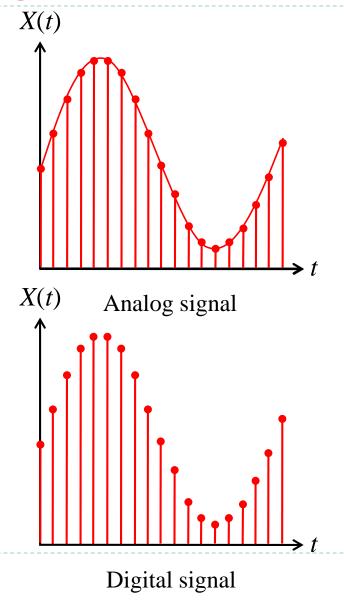
Discrete quantities of information either emerge from the nature of the data being processed or may be quantized from a continuous process.

#### Analog system

The physical quantities or signals may vary continuously over a specified range.

#### Digital system

The physical quantities or signals can assume only discrete values.



#### Why Digital Systems?

#### A World Transformed: What Are the Top 30 Innovations of

Published: February 18, 2009 in Knowledge@Wharlon

the Last 30 Years?



Of these 30 innovations, 10 are directly related to advances in Digital Logic and Solid State Circuits;

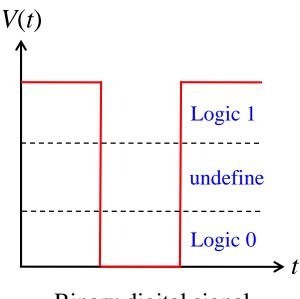
Another 8 are the indirect results of ICs.

- 1. Internet, broadband, WWW (browser and html)
- 2. PC/laptop computers
- Mobile phones
- → 4. E-mail.
  - DNA testing and sequencing/Human genome mapping
  - Magnetic Resonance Imaging (MRI)
  - Microprocessors
    - 8. Fiber optics
    - 9. Office software (spreadsheets, word processors)
  - 10. Non-invasive laser/robotic surgery (laparoscopy)
  - 11. Open source software and services (e.g., Linux, Wikipedia)
  - 12. Light emitting diodes
  - 13. Liquid crystal display (LCD)
    - GPS systems
- 15. Online shopping/ecommerce/auctions (e.g., eBay)
  - Media file compression (jpeg, mpeg, mp3)
    - 17. Microfinance
- 18. Photovoltaic Solar Energy
  - Large scale wind turbines
- 20. Social networking via the Internet
- → 21. Graphic user interface (GUI)
  - 22. Digital photography/videography
  - 23. RFID and applications (e.g., EZ Pass)
    - Genetically modified plants
    - Bio fuels
- 26. Bar codes and scanners
  - 27. ATMs
  - 28. Stents
- 29. SRAM flash memory
  - Anti retroviral treatment for AIDS



# **Binary** Digital Signal

- Binary digital systems, the variable takes on discrete values.
  - Two level, or binary values are the most prevalent values.
- Binary values are represented abstractly by:
  - Digits 0 and I
  - False (F) and True (T)
  - Low (L) and High (H)
  - On and Off



# **Decimal** Number System (base 10)

For solid and deep understanding of binary numbers we recall our understanding of decimal number system with more analysis.

Example: 7392

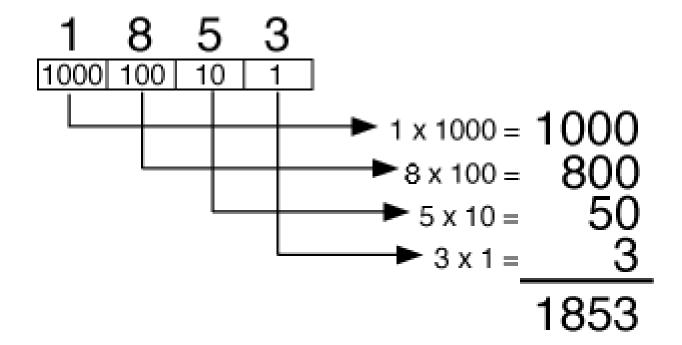
	2	9	3	7
7*10	0	0	0	7
+ 3*1(	0	0	3	0
+ 9*10	0	9	0	0
+ 3*10	2	0	0	0

The power of 10 is implied by the digit (coefficient) position



#### **Decimal** Number System

- For solid and deep understanding of binary numbers we recall our understanding of decimal number system with more analysis.
- Example: 1853





#### **Decimal** Number System

- Base (also called radix) = 10
  - 10 digits { 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 }
  - I 0 possible digits ranges from (0 to r-1)



- Digit Position
  - Integer & fraction
- Digit Weight
  - Weight = (Base=10) Position

5	1	2	-	5	4

10 <sup>2</sup>	10 <sup>1</sup>	10º	•	10 <sup>-1</sup>	10 <sup>-2</sup>
100	10	1	•	0.1	0.01

Weights

- Magnitude
  - Sum of "Digit Value x Weight"

Formal Notation (...)<sub>10</sub>

500 10 2 . 0.5 0.	04
-------------------	----

$$d_2*B^2+d_1*B^1+d_0*B^0+d_{-1}*B^{-1}+d_{-2}*B^{-2}$$
(512.54)10



# Binary Number System (Base 2)

- Base (also called radix) = 2
  - 2 digits { 0, I)
  - 2 possible digits ranges from (0 to r-1)
- Digit Position
  - Integer & fraction
- Digit Weight
  - Weight = (Base=2) Position

1 1 0 1 0 . 1 1
-----------------

<b>2</b> <sup>4</sup>	<b>2</b> <sup>3</sup>	<b>2</b> <sup>2</sup>	<b>2</b> <sup>1</sup>	<b>2</b> <sup>0</sup>	-	<b>2</b> -1	<b>2</b> -2
16	8	4	2	1	-	0.5	0.25

Weights

- Magnitude ( Decimal Equivalent )
  - Sum of "Digit x Weight"

Formal Notation 
$$(...)_2$$

$$16*1 + 8*1 + 4*0 + 2*1 + 1*0 + 1*0.5 + 1*0.25$$
$$= (26.75)_{10}$$

#### Base - 5 Number System

- Base (also called radix) = 5
  - 5 digits { 0, 1,2,3,4)
  - 5 possible digits ranges from (0 to r-1)
- Digit Position
  - Integer & fraction

Digit Weight
--------------

▶ Weight = (Base=5) Position

4 0 2	1		2
-------	---	--	---

<b>5</b> <sup>3</sup>	<b>5</b> <sup>2</sup>	5 <sup>1</sup>	5 <sup>0</sup>	-	<b>5</b> -1
125	25	5	1	•	0.2

Weights

- Magnitude ( Decimal Equivalent )
  - Sum of "Digit x Weight"

Formal Notation  $(...)_5$ 

# Base – 8(**Octal**) Number System

- Base (also called radix) = 8
  - 8 digits { 0, 1,2,3,4,5,6,7)
  - 8 possible digits ranges from (0 to r-1)
- Digit Position
  - Integer & fraction
- Digit Weight
  - Weight = (Base) Position

<b>8</b> <sup>2</sup>	8 <sup>1</sup>	80	-	8-1
64	8	1	•	0.125

Weights

- Magnitude ( Decimal Equivalent )
  - Sum of "Digit x Weight"

#### Base – 16 (**Hexadecimal**) Number System

- Base (also called radix) = 16
  - ▶ 16 digits { 0, 1,2,3,4,5,6,7,8,9,A,B,C,D,E,F)
  - I 6 possible digits ranges from (0 to r-I)
  - The letters of the alphabet are used to supplement the 10 decimal digits when the base of the number is greater than 10.

В

Digit	<b>Position</b>
-------	-----------------

Integer & fraction

16 <sup>3</sup>	16 <sup>2</sup>	16 <sup>1</sup>	16 <sup>0</sup>
			- 0

- Digit Weight
  - Weight = (Base=16) Position
- Magnitude ( Decimal Equivalent )
  - Sum of "Digit x Weight"

$$16^{3}*B + 16^{2}*6 + 16^{1}*5 + 16^{0}*F$$

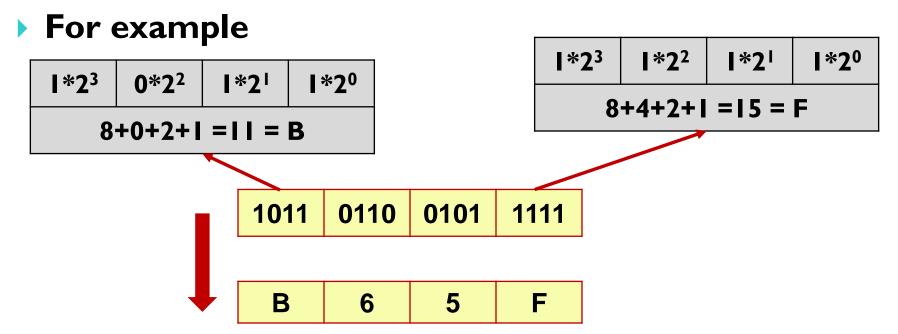
$$16^{3}*(11) + 16^{2}*6 + 16^{1}*5 + 16^{0}*(15)$$

$$= (46,687)_{10}$$



#### **Hexadecimal System**

The hexadecimal system is used commonly by designers to represent long strings of bits in the addresses, instructions, and data in digital systems.





# More about Binary System

The digits in a binary number are called bits.

When a bit is equal to 0, it does not contribute to the sum during the conversion.

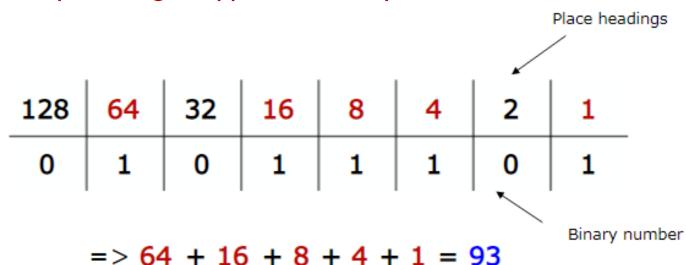
<b>2</b> <sup>4</sup>	<b>2</b> <sup>3</sup>	<b>2</b> <sup>2</sup>	<b>2</b> <sup>1</sup>	<b>2</b> <sup>0</sup>
16	8	4	2	1

Therefore, the conversion from binary to decimal can be obtained by adding only the numbers with powers of two corresponding to the bits that are equal to 1

$$16 + 8 + 2 = (26)_{10}$$

#### More about Binary System

- ▶ The conversion from binary to decimal
  - Write binary number
  - 2. Write place heading
  - Ignore zeros
  - 4. Sum up headings mapped to I's only





# More about Binary System (units)

- In computer work,
- **2**<sup>10</sup> is referred to as K (**kilo**),  $4K = 2^{12} = 4,096$
- **2**<sup>20</sup> as M (mega), and  $16M = 2^{24} = 16,777,216$
- **2**<sup>30</sup> as G (giga), 4G =  $2^{32}$  bytes
- $ightharpoonup 2^{40}$  as T (tera).
- Computer capacity is usually given in bytes. A byte is equal to eight bits and can accommodate



# More about Binary System (units)

 Computer capacity is usually given in bytes. A byte is equal to eight bits and can accommodate

Unit	Bytes
1 Bit	0,1
1 Byte	8 bits
1 Kilobyte (Kb)	2 <sup>10</sup> = 1024 bytes
1 Megabyte (Mb)	2 <sup>20</sup> = 1,048,576 bytes (1024 Kb)
1 Gigabyte (Gb)	2 <sup>30</sup> = 1,073,741,824 bytes (1024 Mb)
1 Terabyte (Tb)	2 <sup>40</sup> = 1,099,511,627,776 bytes (1024 Gb)



# More about Binary System (Range)

These measurements are used to determine the lower and upper limits of the range numbers possible with a given amount of bits (vise versa)

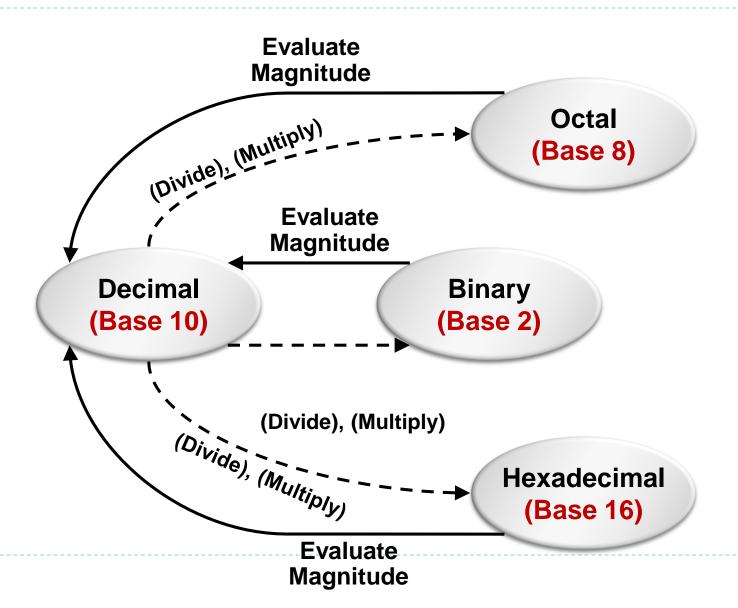
		0	1	0	1	1	1	0	1
Unit	Range					+ 4 +	1 =	93	Binary number
1 Bit	0 to 21 - 1 (0 to 1	)							
8 bits (1 Byte)	0 to 28 - 1 (0 to 2	55)							
16 bits (2 bytes)	tes) 0 to 2 <sup>16</sup> - 1 (0 to 65,535)								
24 bits (3 bytes) 0 to 2 <sup>24</sup> - 1 (0 to 16, 777, 215)									
32 bits (4 bytes)	0 to 2 <sup>32</sup> – 1 (0 to 4	4,29	94,9	967	,29	5)			

Place headings

128 64 32 16 8 4



#### **Number Base Conversions**



# Decimal (*Integer*) to Binary Conversion

- ▶ **Divide** the number by the 'Base' (=2)
- ▶ Take the remainder (either 0 or 1) as a coefficient
- ▶ Take the quotient and repeat the division

#### Example: $(13)_{10}$

Answer: 
$$(13)_{10} = (1101)_2$$



#### Decimal (*Fraction*) to Binary Conversion

- ▶ Multiply the number by the 'Base' (=2)
- Take the integer (either 0 or 1) as a coefficient
- ▶ Take the resultant fraction and repeat the division

#### Example: $(0.625)_{10}$

	I	nteger	Fraction	Coefficient
0.625	* 2 =	ı	. 25	$\mathbf{a}_{-1} = \mathbf{I}$
0.25	* 2 =	0	. 5	$a_{-2} = 0$
0.5	* 2 =		. 0	$a_{-3} = 1$

Answer: 
$$(0.625)_{10} = (0.101)_2$$

**MSB** 





#### **Decimal to Octal Conversion**

Example:  $(175)_{10}$ 

	Quotient	Remainder	Coefficient
175 / 8 =	21	7	$a_0 = 7$
21 /8=	2	5	$a_1 = 5$
2 / 8 =	0	2	$a_2 = 2$

Answer: 
$$(175)_{10} = (a_2 a_1 a_0)_8 = (257)_8$$

Example:  $(0.3125)_{10}$ 

Integer Fraction Coefficient 
$$0.3125 * 8 = 2 . 5$$
  $a_{-1} = 2$   $0.5 * 8 = 4 . 0$   $a_{-2} = 4$ 

Answer: 
$$(0.3125)_{10} = (0.a_{-1} a_{-2} a_{-3})_8 = (0.24)_8$$



#### **Decimal to Hexadecimal Conversion**

Example:  $(175)_{10}$ 

Quotient Remainder Coefficient

175 / 16 = 10 | 15=F | 
$$a_0 = F$$

10 / 16 = 0 | 10=A |  $a_1 = A$ 

Answer: 
$$(175)_{10} = (a_1 a_0)_{16} = (AF)_{16}$$

Example:  $(0.3125)_{10}$ 

Integer Fraction Coefficient 
$$0.3125 * 16 = 5$$
 .  $0$   $a_{-1} = 5$ 

Answer: 
$$(0.3125)_{10} = (0.a_{-1})_{16} = (0.5)_{16}$$



Convert 41 decimal to binary

The arithmetic process can be manipulated more conveniently as follows:

Integer	Remainder	
41		
20	1	
10	0	
5	0	
2	1	
1	0	
0	1  101001 = answer	r



Convert 153 decimal to octal

153
19
1
2
3
0
$$2 = (231)_8$$

Convert 0.6875 decimal to binary

	Integer		Fraction	Coefficient
$0.6875 \times 2 =$	1	+	0.3750	$a_{-1} = 1$
$0.3750 \times 2 =$	0	+	0.7500	$a_{-2} = 0$
$0.7500 \times 2 =$	1	+	0.5000	$a_{-3} = 1$
$0.5000 \times 2 =$	1	+	0.0000	$a_{-4} = 1$

Therefore, the answer is  $(0.6875)_{10} = (0. \ a_{-1} \ a_{-2} \ a_{-3} \ a_{-4})_2 = (0.1011)_2$ .



#### Convert 0.513 to octal

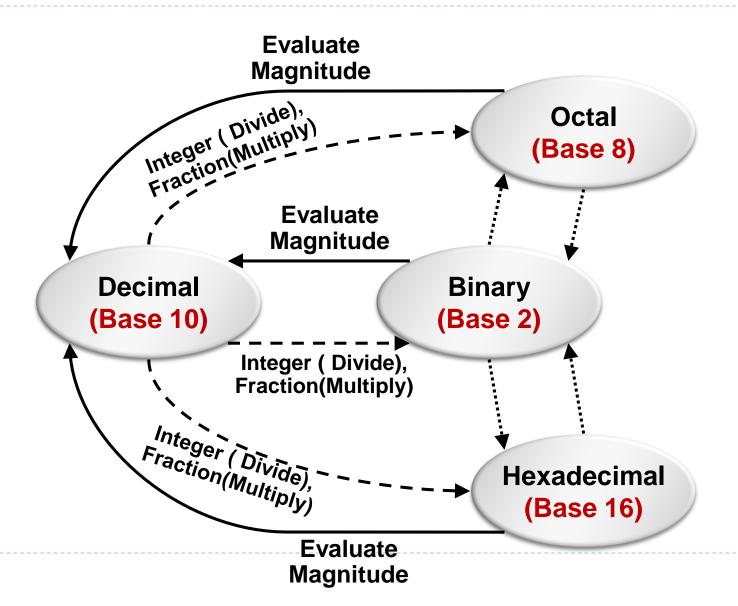
Convert  $(0.513)_{10}$  to octal.

$$0.513 \times 8 = 4.104$$
  
 $0.104 \times 8 = 0.832$   
 $0.832 \times 8 = 6.656$   
 $0.656 \times 8 = 5.248$   
 $0.248 \times 8 = 1.984$   
 $0.984 \times 8 = 7.872$ 

The answer, to seven significant figures, is obtained from the integer part of the products:

$$(0.513)_{10} = (0.406517...)_8$$

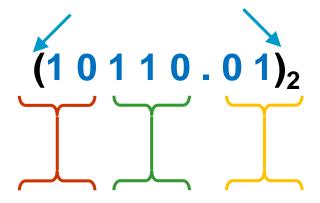
#### **Number Base Conversions**



# **Binary - Octal Conversion**

- $8 = 2^3$
- Each group of 3 bits represents an octal digit

#### **Example:**

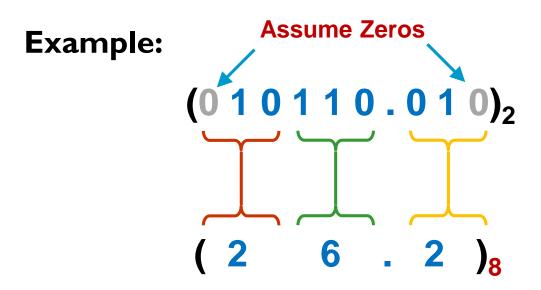


Octal	Binary
0	0 0 0
1	0 0 1
2	010
3	011
4	100
5	101
6	110
7	111



#### **Binary - Octal Conversion**

- $8 = 2^3$
- Each group of 3 bits represents an octal digit



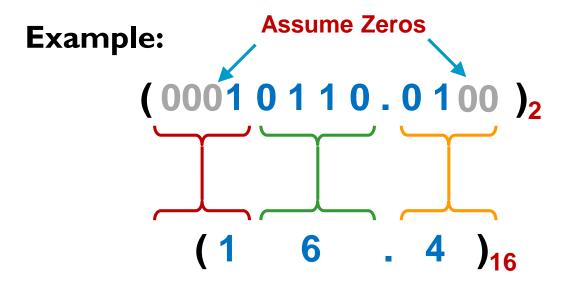
Octal	Binary
0	0 0 0
1	0 0 1
2	010
3	0 1 1
4	100
5	1 0 1
6	110
7	1 1 1

Works both ways (Binary to Octal & Octal to Binary)



#### **Binary - Hexadecimal Conversion**

- $16 = 2^4$
- Each group of 4 bits represents a hexadecimal digit



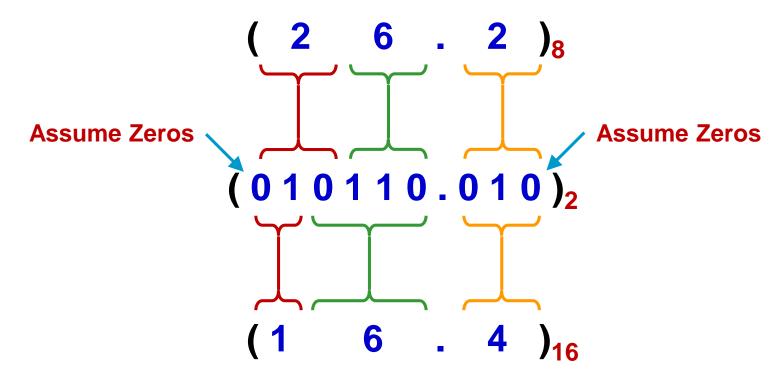
Hex	Binary		
0	0000		
1	0001		
2	0010		
3	0011		
4	0100		
5	0101		
6	0110		
7	0 1 1 1		
8	1000		
9	1001		
A	1010		
В	1011		
С	1100		
D	1 1 0 1		
Е	1110		
F	1111		

Works both ways (Binary to Hex & Hex to Binary)

#### Octal - Hexadecimal Conversion

Convert to Binary as an intermediate step

#### **Example:**



Works both ways (Octal to Hex & Hex to Octal)



#### Decimal, Binary, Octal and Hexadecimal

Decimal	Binary	Octal	Hex
00	0000	00	0
01	0001	01	I
02	0010	02	2
03	0011	03	3
04	0100	04	4
05	0101	05	5
06	0110	06	6
07	0111	07	7
80	08 1000 10		8
09	1001	11	9
10	1010	12	Α
11	1011	13	В
12	1100	14	С
13	13   1101		D
14	1110	16	E
15	1111	17	F



Convert (01101011.111100) binary to octal

01	101	011	-	111	100
1	5	3	•	7	4

Convert (01101011.111100) binary to Hexadecimal

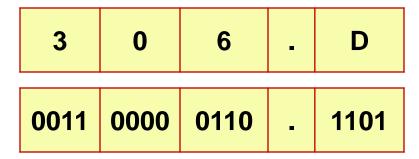
0110	1011	•	1111	00
6	В	-	F	0



Convert (673.12) octal to binary

6	7	3	•	1	2
110	111	011	-	001	010

Convert (306.D) **Hexadecimal** to **binary** 





/hank Mou!