PROBLEM SET 3

16825 LEARNING FOR 3D VISION (SPRING 2024) https://piazza.com/cmu/spring2024/16825

OUT: Feb. 21, 2024 DUE: Mar. 13, 2024 11:59 PM Instructor: Shubham Tulsiani

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1. [10 pts]

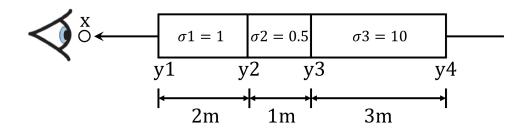
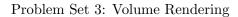


Figure 1: A ray through a non-homogeneous medium. The medium is composed of 3 segments (y1y2, y2y3, y3y4). Each segment has a different absorption coefficient, shown as $\sigma_1, \sigma_2, \sigma_3$ in the figure. The length of each segment is also annotated in the figure (1m means 1 meter).

As shown in Figure 1, we observe a ray going through a non-homogeneous medium. Please compute the following transmittance:

- T(y1, y2)
- T(y2, y4)
- T(x, y4)
- T(x, y3)





Solution

$$\begin{split} \mathbf{T}(\mathbf{x},\,\mathbf{x}_{t_i}) &= T(x,x_{t_{i-1}}) \cdot e^{-\sigma_{t_{i-1}} \cdot \Delta t_{i-1}} \\ \mathbf{T}(\mathbf{y}1,\,\mathbf{y}2) &= \mathbf{e}^{-2} = 0.135 \\ \mathbf{T}(\mathbf{y}2,\,\mathbf{y}4) &= \mathbf{T}(\mathbf{y}2,\,\mathbf{y}3) \cdot T(\mathbf{y}3,\,\mathbf{y}4) = e^{-0.5} \cdot e^{-30} = 5.6756852 \mathbf{e}\text{-}14 \\ \mathbf{T}(\mathbf{x},\,\mathbf{y}4) &= \mathbf{T}(\mathbf{x},\,\mathbf{y}1) \cdot T(\mathbf{y}1,\,\mathbf{y}2) \cdot T(\mathbf{y}2,\,\mathbf{y}3) \cdot T(\mathbf{y}3,\,\mathbf{y}4) = e^0 \cdot e^{-2} \cdot e^{-0.5} \cdot e^{-30} = 7.6812047 \mathbf{e}\text{-}15 \\ \mathbf{T}(\mathbf{x},\,\mathbf{y}3) &= \mathbf{e}^0 \cdot e^{-2} \cdot e^{-0.5} = 0.082 \end{split}$$