

1.

- b) Let $x \in$ (All stones)
Let $P(x) = x$ is precious
Let $B(x) = x$ is beautiful
Symbolically, the statement is:
 $(\forall x)(P(x) \Rightarrow \sim B(x))$
- c) Let $x \in$ (All triangles).
Let $R(x) = x$ is a right triangle
Let $I(x) = x$ is an isosceles triangle
Symbolically, the statement is:
 $(\exists x)(P(x) \wedge R(x))$
- d) Note: Using definitions from part c
Symbolically, the statement is:
 $(\forall x)(P(x) \Rightarrow \sim I(x))$
- e) Note: Using definitions from part c
Symbolically, the statement is:
 $(\forall x)(\sim I(x) \Rightarrow R(x))$
- f) Let $x \in$ (All people)
Let $H(x) = x$ is honest.
Symbolically, the statement is:
 $[(\forall x)(H(x))] \vee [(\forall x)(\sim H(x))]$
- g) Note: Using definitions from part f
Let $y \in$ (All people)
Symbolically, the statement is:
 $(\exists x)(H(x)) \wedge (\exists y)(\sim H(y))$
- h) Let $x \in \mathbb{R}$
Symbolically, the statement is:
 $(\forall x)(x \neq 0 \Rightarrow (x > 0 \vee x < 0))$
- j) Let $x, y \in \mathbb{Z}$
Symbolically, the statement is:
 $(\forall x)(\exists y)(x > y)$
- l) Let $x, y \in \mathbb{Z}$, let $m \in \mathbb{R}$
Symbolically, the statement is:
 $(\forall x)(\forall y)(\exists m)[(x \neq y) \Rightarrow (x > m > y) \vee (y > m > x)]$

- o) Let $x, y \in (\text{All people})$
Let $L(x, y) = x \text{ loves } y$
Symbolically, the statement is:
 $(\forall x)(\exists y)(L(x, y))$
- p) Let $x, y \in \mathbb{R}$
Symbolically, the statement is:
 $(\forall x)(\exists! y)((x > 0) \Rightarrow (2^y = x))$

2.

- b)
- c)
- d)
- e)
- f)
- g)
- h)
- j)
- l)
- o)
- p)

6.

- b)
- c)
- d)

7.

a) *Proof:*

b)

8.

a)

c)

d)

f)

g)

i)

j)

k)

l)

12.

b)

c)

d)

e)

f)

g)

h)