

1.

- b) Antecedent: "The moon is made of cheese"
Consequent: "8 is an irrational number"
- c) Antecedent: " b divides 3"
Consequent: " b divides 9"
- e) Antecedent: " a is convergent"
Consequent: "A sequence a is bounded"
- g) Antecedent: " $1 + 1 = 2$ "
Consequent: " $1 + 2 = 3$ "
- h) Antecedent: "The fish bite"
Consequent: "The moon is full"

2.

- b) Converse: "If 8 is an irrational number, then the moon is made of cheese"
Contrapositive: "If 8 is not an irrational number, then the moon is not made of cheese"
- c) Converse: " b divides 9 only if b divides 3"
Contrapositive: " b does not divide 9 only if b does not divide 3"
- e) Converse: "A sequence a is convergent whenever a is bounded"
Contrapositive: "A sequence a is not convergent whenever a is unbounded"
- g) Converse: " $1 + 1 = 2$ is necessary for $1 + 2 = 3$ "
Contrapositive: " $1 + 1 \neq 2$ is necessary for $1 + 2 \neq 3$ "
- h) Converse: "The moon is full only when the fish bite"
Contrapositive: "The moon is not full only when the fish don't bite"

5.

- b) “Hexagons have size sides” \rightarrow true
“The moon is made of cheese” \rightarrow false
 $T \rightarrow F \equiv F$, so this statement is false.
- d) “The Nile River flows east” \rightarrow false
“64 is a perfect square” \rightarrow true
 $F \rightarrow T \equiv T$, so this statement is true.
- e) “Earth has one moon” \rightarrow true
“The Amazon River flows into the North Sea” \rightarrow false
 $T \rightarrow F \equiv F$, so this statement is false.
- f) “Euclid’s birthday was April 2” \rightarrow ?
“Rectangles have four sides” \rightarrow true
The antecedent is true, so this statement is true.
- g) “ $\sqrt{2}$ is not irrational” \rightarrow false
“5 is prime” \rightarrow true
 $F \rightarrow T \equiv T$, so this statement is true.
- h) “ $1 + 1 = 2$ ” \rightarrow true
“ $3 > 6$ ” \rightarrow false
 $T \rightarrow F \equiv F$, so this statement is false.

14.

- a) “If 3 is an integer, then this class does not have a textbook.”
- b) This is not possible, since if a conditional is false it’s converse will always be true. This is because all other combinations of truth values for P and Q in a conditional statement lead to a true statement.
- c) “If earth is a planet, then this sentence does not exist.”
- d) This is not possible, since the contrapositive of a conditional always has the same truth value of the original conditional statement. Thus a false conditional can never have a true contrapositive.