

t 2-7

$$f(n) = 3n^2 - n + 4$$

$$g(n) = n \log n + 5$$

$$f(n) + g(n) = O(n^2)$$

$$3n^2 - n + 4 + n \log n + 5 \leq Cn^2$$

$$3n^2 - n + n \log n + 9 \leq Cn^2$$

$$3n^2 + n(\log n - 1) + 9 \leq Cn^2$$

$$C = 4 \quad n \log n \leq \frac{n^2}{2}$$

$$n \log n - n + 9 \leq n^2$$

$$\frac{n^2}{2} - n + 9 \leq n^2$$

$$9 \leq n^2 - \frac{n^2}{2} + n$$

$$\frac{n^2}{2} + n - 9 > 0$$

$$n \left(\frac{n}{2} + 1 \right) - 9 \geq 0$$

• $\forall n \geq 4$: $f(n) + g(n) = O(n^2)$