# Classification

Boston University CS 506 - Lance Galletti

age	Tumor size	malignant?
20	9	no
30	16	yes
40	18	no
50	28	yes

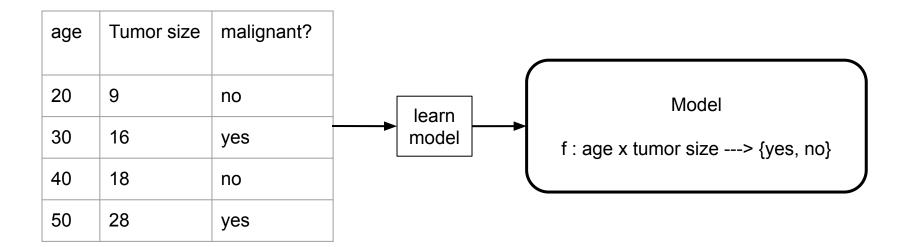
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CLASS

PREDICTORS / FEATURES / ATTRIBUTES



age	Tumor size	malignant?
20	9	no
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40	18	no
50	28	yes

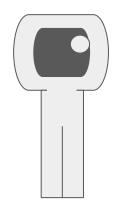
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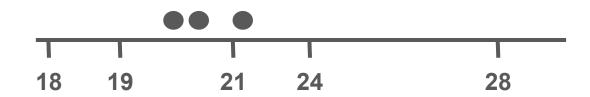
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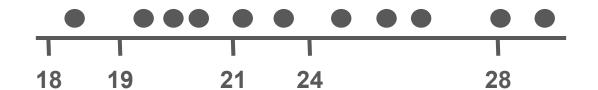
What property / combination of age and tumor size is unique to malignant tumors?





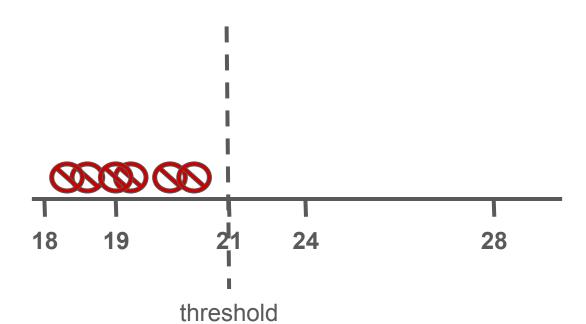


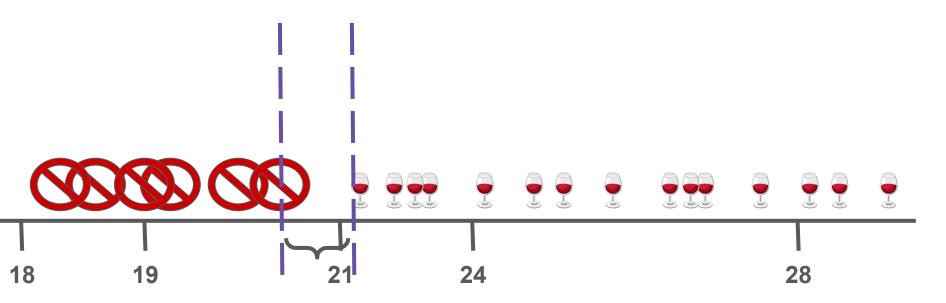








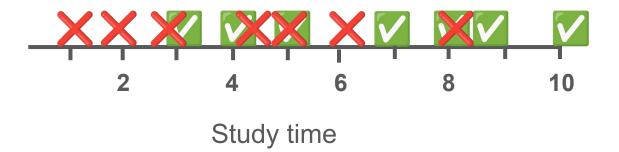




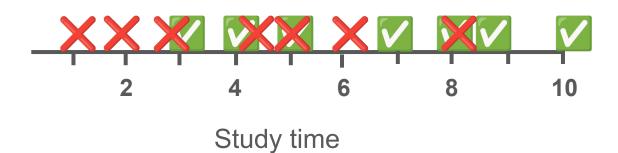


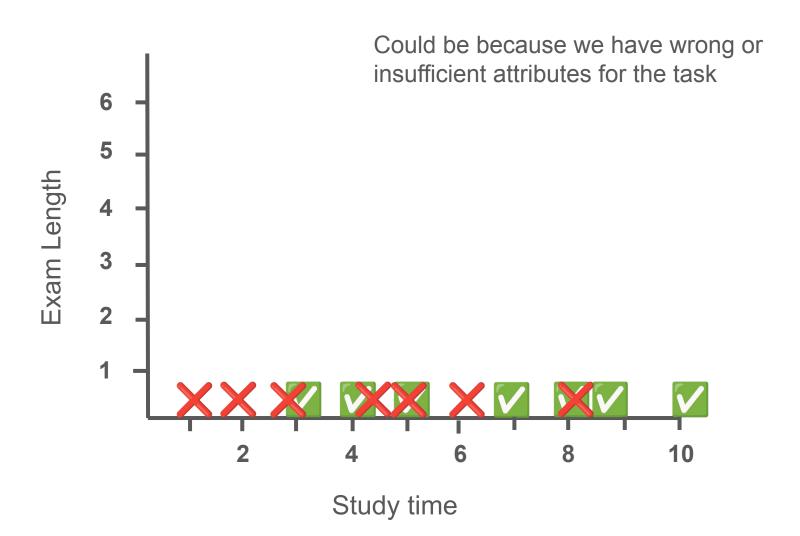


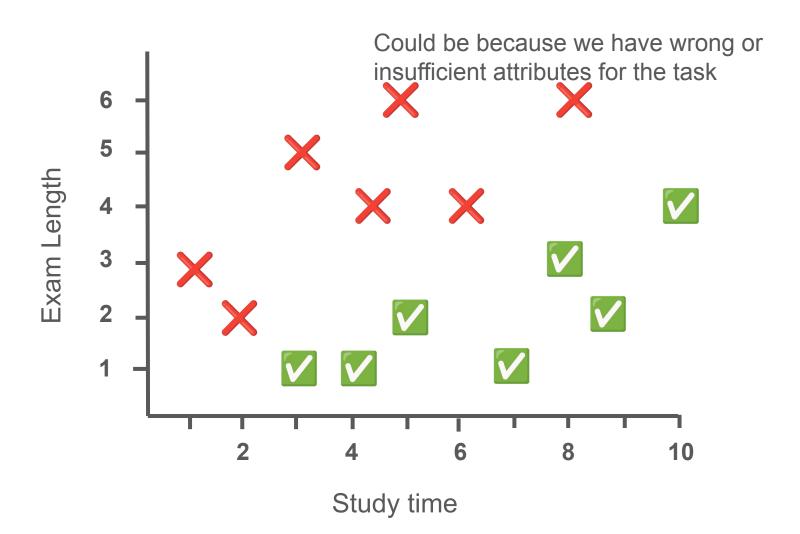


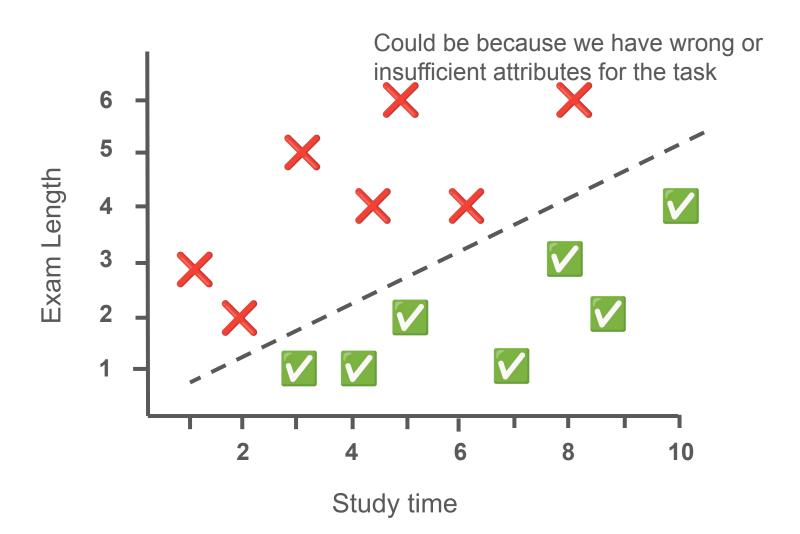


# Could be because we have wrong or insufficient attributes for the task

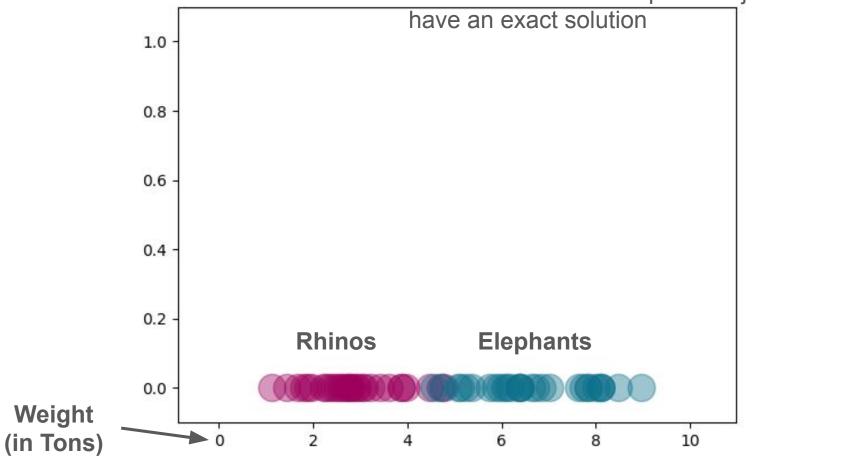




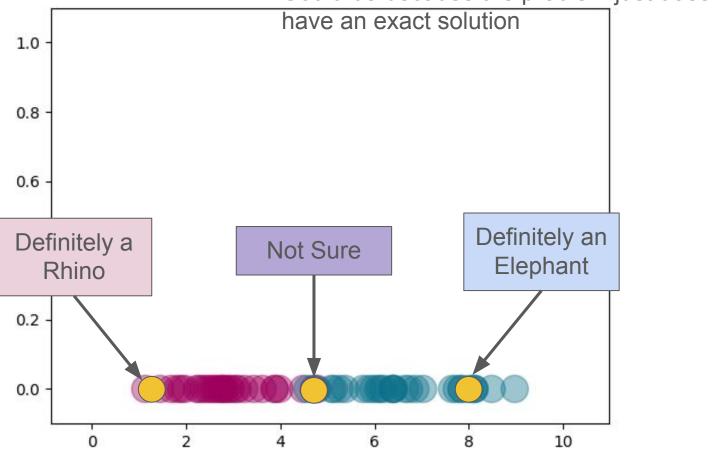




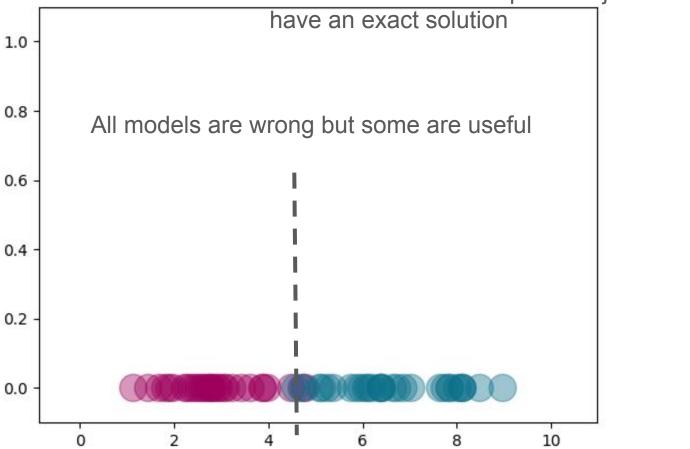
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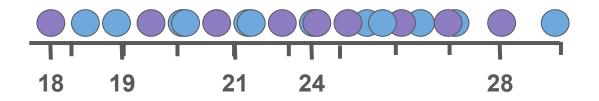


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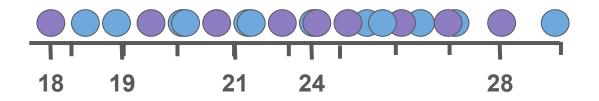


The feasibility of classification task completely depends on the relationship between the attributes predictors) and the class.

For example if we used age instead of weight for elephants and rhinos



Age cannot distinguish rhinos and elephants



# **Takeaways**

- There could be many correct answers
- There could be no correct answers
  - And maybe that's ok no relationship is interesting information too
  - But the model could **still be useful** if it's more or less correct most of the time
- Whether a task is feasible depends on:
  - The relationship between the predictors and the class

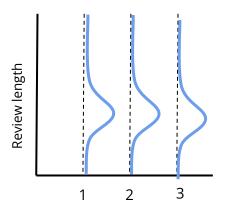
# **Lots of Questions**

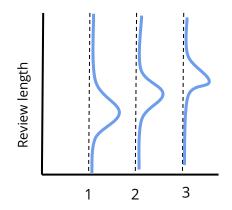
- How do we know if we have good predictors for a task?
- How do we know we have done a good job at classification?

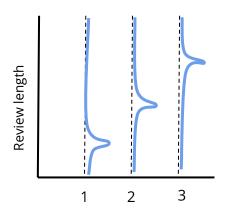
## **Lots of Questions**

- How do we know if we have good predictors for a task?
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What constitutes a good feature/predictor?

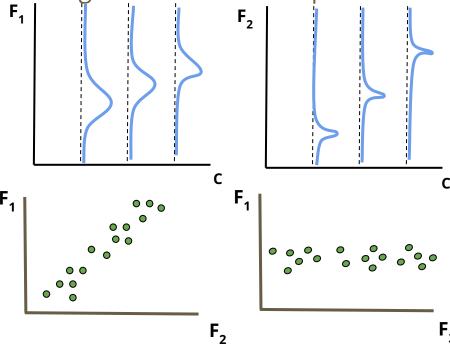






What constitutes a good feature/predictor?

What constitutes a good set of features/predictors?



- What constitutes a good feature/predictor?
- What constitutes a good set of features/predictors?

We want features that are related to the target but not to each other. How do we know if features are related?

Correlation

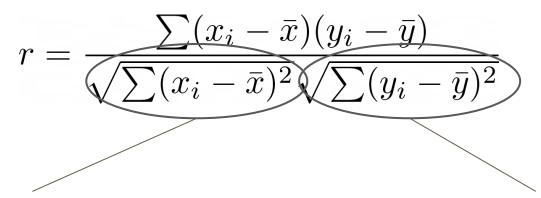
Correlation between X and Y (continuous variables) can be measured as:

$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2} \sqrt{\sum (y_i - \bar{y})^2}}$$

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 Covariance

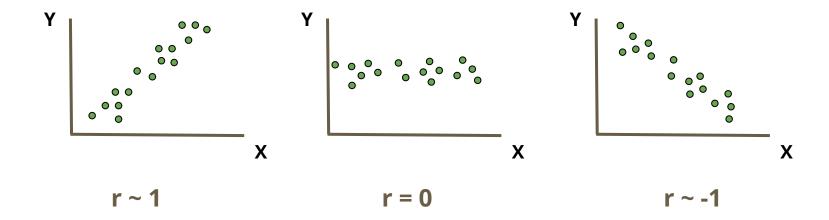
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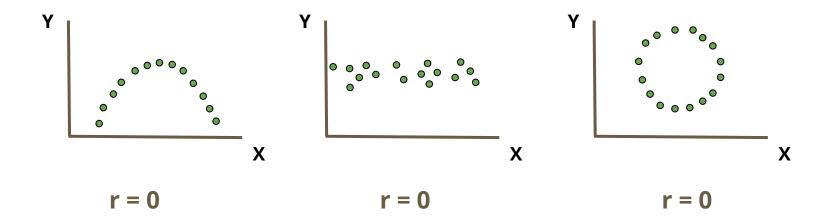
**Standard Deviation of X** 

**Standard Deviation of Y** 

#### **Correlation**



No correlation doesn't mean there isn't a relationship



What if X is continuous and Y is a class?

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- Y is {Yes, No}, Colors, Cities etc
- Y is {Terrible, Bad, Ok, Good, Great}

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**Nominal** 

**Ordinal** 

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No order, need to look at the means of X and how they differ across each Nominal Value of Y

**Nominal** 

**Ordinal** 

There is a natural Order and we can assign numbers to each category like {0, 1, 2, 3, 4}. BUT it's not clear if the difference between Terrible and Bad is the same as between OK and Good...

#### **Correlation**

What if X is continuous and Y is a class?

- Y is {Yes, No}, Colors, Cities etc

Y is {Terrible, Bad, Ok, Good, Great}

No order, need to look at the means of X and how they differ across each Nominal Value of Y

Nominal Ordinal

Instead of using the exact numbers assigned we can compare their rank / position in the data. So it doesn't matter how far Bad is from Ok it just matters that Ok comes after Bad.

X	Υ
10	1
20	0
30	2
40	3
50	4

X	Υ
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R(X)	R(Y)
1	2
2	1
3	3
4	4
5	5

$$\rho = 1 - \frac{6\sum d_i^2}{n(n^2 - 1)}$$

X	Υ
10	1
20	0
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40	3
50	4

R(X)	R(Y)	d
1	2	-1
2	1	1
3	3	0
4	4	0
5	5	0

$$\rho = 1 - \frac{6\sum d_i^2}{n(n^2 - 1)}$$

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$$p = .9$$

- What constitutes a good feature/predictor?
- What constitutes a good set of features/predictors?

We want features that are related to the target but not to each other. How do we know if features are related? **Correlation (Pearson or Spearman)** 

BUT...

Correlation is not causation.

#### **Correlation VS Causation**

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  - a. Temperature increases seem to cause ice cream sales to spike
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- Sleeping with shoes on is strongly correlated with waking up with a headache.
  - a. But neither causes the other...
  - b. There's a third common factor causing this correlation: going to bed drunk.

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But it's very hard to show that things are causally linked through observational data... Especially if the relationship isn't deterministic.

Not everyone who smokes will get lung cancer

Hard to say what would have happened if you hadn't smoked cause you can't rewrite the past.

Testing for causality requires specific testing / experimentation with a control group

Ethical considerations when testing effects of new drugs

	applied	accepted	rate	applied	accepted	rate	
TOTAL	1184	274	23%	2470	584	24%	

	applied	accepted	rate	applied	accepted	rate
Computer science	26	7	27%	228	58	25%
Economics	240	63	26%	512	112	22%
Engineering	164	52	32%	972	252	26%
Medicine	416	99	24%	578	140	24%
Veterinary Med	338	53	16%	180	22	12%
TOTAL	1184	274	23%	2470	584	24%

Simpson's Paradox

When the relationship is reversed when data is aggregated.

Bob is diagnosed with lung cancer. He thinks it's because of exposure to asbestos while working and decides to sue his previous employer.

It cannot be proven that the cancer would not have occurred without exposure to asbestos. So how does Bob go about this?

Bob is diagnosed with lung cancer. He thinks it's because of exposure to asbestos while working and decides to sue his previous employer.

- Out of 1000 people like Bob, 10 are expected to develop lung cancer
- Exposure to asbestos more than doubles the expected development of lung cancer. So out of 1000 people exposed to asbestos like Bob, let's say about 25 would get lung cancer.
- So of those exposed to asbestos that go on to develop lung cancer, less than half developed lung cancer if they had no been exposed.
- So it's more likely than not that the asbestos caused the cancer.

#### **Bob** wins

Forensic epidemiology

## **Lots of Questions**

- How do we know if we have good predictors for a task?
- How do we know we have done a good job at classification?

### How do we know we've done well at classification?

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Testing without cheating. Learning not memorizing.

- Testing without cheating. Learning not memorizing.
  - Split up our data into a training set and a separate testing set
  - Use the training set to find patterns and create a model
  - Use the testing set to evaluate the model on data it has not seen before

train

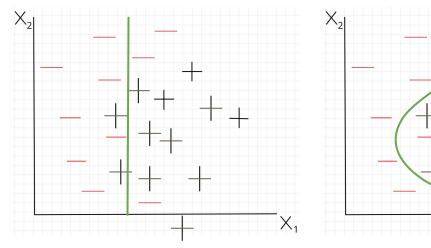
test

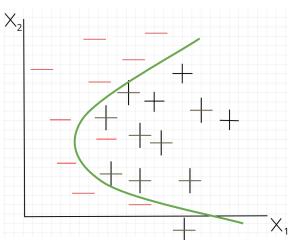
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  - Overfitting vs underfitting

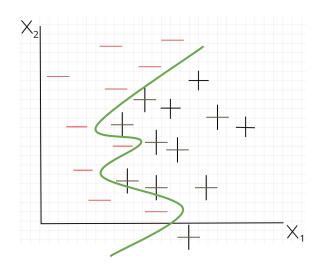
train

test

## **Underfitting VS Overfitting**

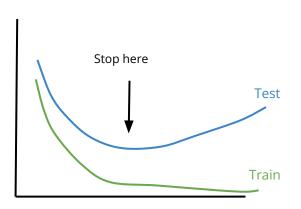






### **Underfitting VS Overfitting**

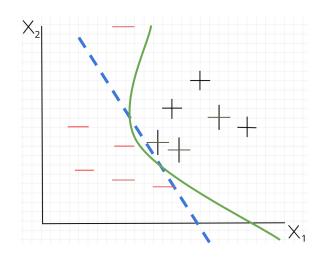
# mistakes made by the model

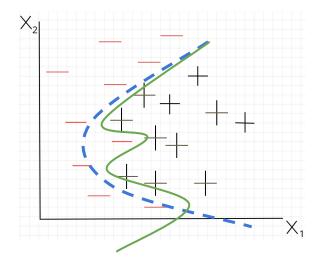


Complexity of the model

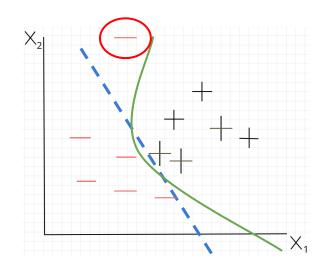
- Testing without cheating:
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  - Overfitting vs underfitting
  - Goal is to capture general trends
    - Watch out for outliers and noise

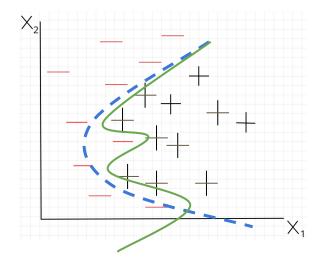
### **Outliers and Noise**



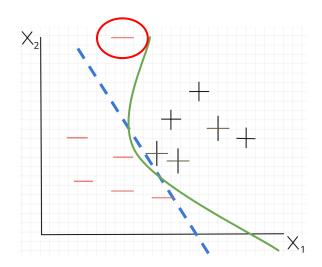


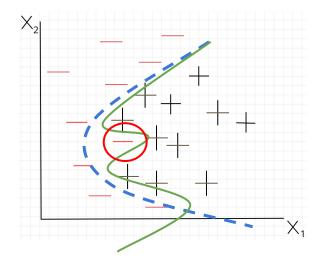
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  - Overfitting vs underfitting
  - Goal is to capture general trends
    - Watch out for outliers and noise
- The types of mistakes made matters

### Types of mistakes

- Testing for a rare disease
  - Out of 1000 data points, only 10 have this rare disease. A model that simply tells folks they don't have the disease will have an accuracy of 99%.

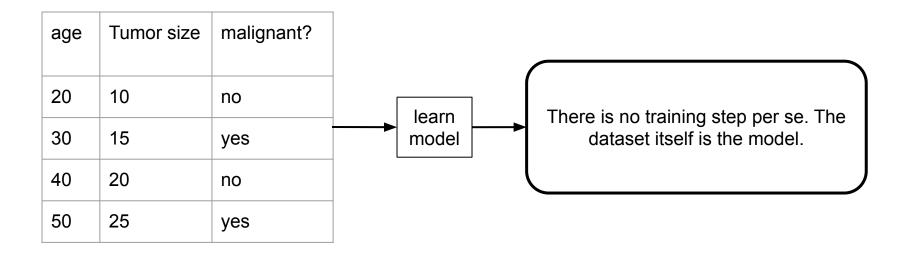
## **Classification**

- Training Step
  - Create the model based on the examples / data points in the training set
- Testing Step
  - Use the model to fill in the blanks of the testing set
  - Compare the result of the model to the true values

## **Instance-Based Classifiers**

- Use the stored training records to predict the class label of unseen cases
- Rote-learners:
  - Perform classification only if the attributes of the unseen record exactly match a record in our training set

# **Instance-Based Classifiers: Training Step**



# Instance-Based Classifiers: Applying the model

age	Tumor size	malignant?			
20	10	no	200	Tumor size	malignant?
30	15	yes	age	Turrior Size	malignant?
40	20	no	20	10	?
50	25	yes			

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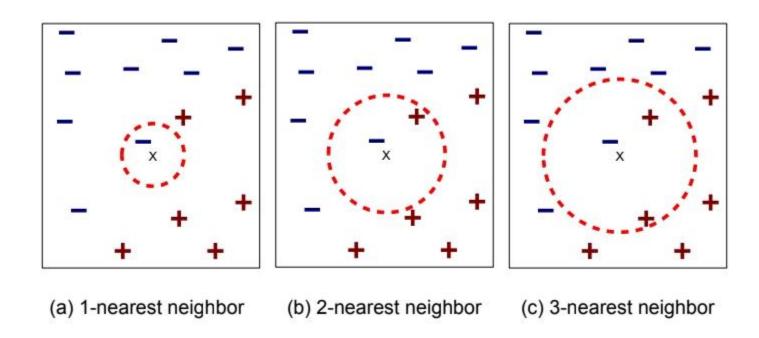
Use **SIMILAR** records to perform classification

### Requires:

- Training set
- Distance function
- Value for k

### How to classify an unseen record:

- 1. Compute distance of unseen record to all training records
- 2. Identify the k nearest neighbors
- 3. Aggregate the labels of these k neighbors to predict the unseen record class (ex: majority rule)



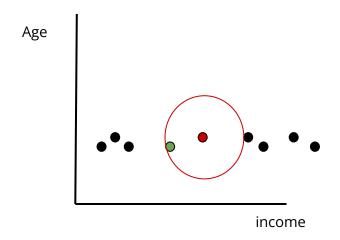
### Aggregation methods:

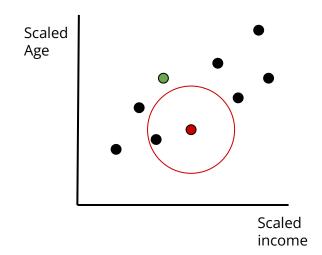
- Majority rule
- Weighted majority based on distance ( $w = 1/d^2$ )

### Scaling issues:

- Attributes should be scaled to prevent distance measures from being dominated by one attribute. Example:
  - o Age: 0 -> 100
  - o Income: 10k -> 1million

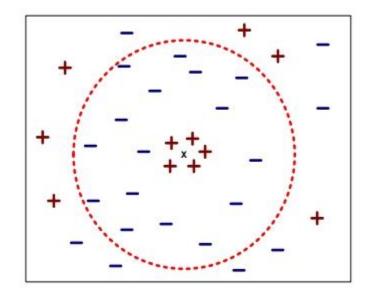
# **Scaling Attributes**

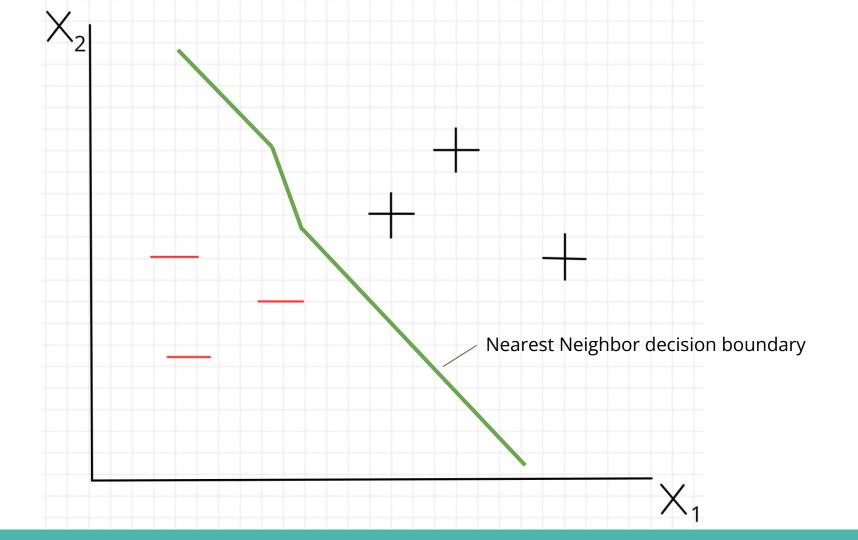




### Choosing the value of k:

- If k is too small ->
  - sensitive to noise points + doesn't generalize well
- If k is too big ->
  - neighborhood may include points from other classes





#### Pros:

Simple to understand why a given unseen record was given a particular class

#### Cons:

- Expensive to classify new points
- KNN can be problematic in high dimensions (curse of dimensionality)

