

## Noise Level Adaptive Diffusion Model for Robust Reconstruction of Accelerated MRI

Shoujin Huang<sup>1</sup>, Guanxiong Luo<sup>2\*</sup>, Xi Wang<sup>4</sup>, Ziran Chen<sup>1</sup>, Yuwan Wang<sup>1</sup>, Huaishui Yang<sup>1</sup>, Pheng-Ann Heng<sup>4</sup>, Lingyan Zhang<sup>2\*</sup>, and Mengye Lyu<sup>1\*</sup>

1 Shenzhen Technology University, Shenzhen, China

3 The Chinese University of Hong Kong, Hong Kong, China

2 University Medical Center Göttingen, Göttingen, Germany

4 Longgang Central Hospital of Shenzhen, Shenzhen, China

### Introduction

**MRI Acceleration and Reconstruction:** MRI scans are accelerated by using multiple coils for k-space data acquisition, and reconstruction is enhanced by incorporating sparsity and total variation, with deep learning models further improving the process. [1]

**Challenges in Diffusion-Based MRI Reconstruction:** Diffusion models improve MRI reconstruction by integrating k-space data consistency[2], but noise from hardware and thermal fluctuations can disrupt their performance, especially in low-field MRI[3], fMRI, and DWI[4].

**Nila-DC:** The proposed Noise Level Adaptive Data Consistency (Nila-DC) operation addresses noise interference, ensuring robust k-space data guidance and improving diffusion model performance in MRI.

### Methodology

(a) The proposed data consistency (Nila-DC) operation. The computed gradient ( $A^H A x_t - A^H y$ ) can be noisy due to MRI noise in  $y$  (c.f. Eqs. 7 and 8), and is therefore adjusted by a attenuation function (lambda).

$$\nabla \log(y|x_t) = -(A^H A x_t - A^H y)/\sigma_y^2 \quad \text{Eq. 7}$$

$$A^H y = A^H A \bar{x} + A^H \sigma_y \quad \text{Eq. 10}$$

(b) The attenuation function  $\lambda_t$  rescale the DC gradient.  $t$  is the index of the reverse step.

$$\lambda_t = \begin{cases} 1, & A^H \sigma_y < 1 - \sqrt{\bar{a}_{t-1}} \\ kt + b, & \sqrt{\bar{a}_{t-1}} A^H \sigma_y > 1 - \sqrt{\bar{a}_{t-1}} \end{cases}$$

(c) The image reconstruction process, where Gaussian noise initialized  $x_t$  undergoes multi-step reverse diffusion process with the guidance from Nila-DC.

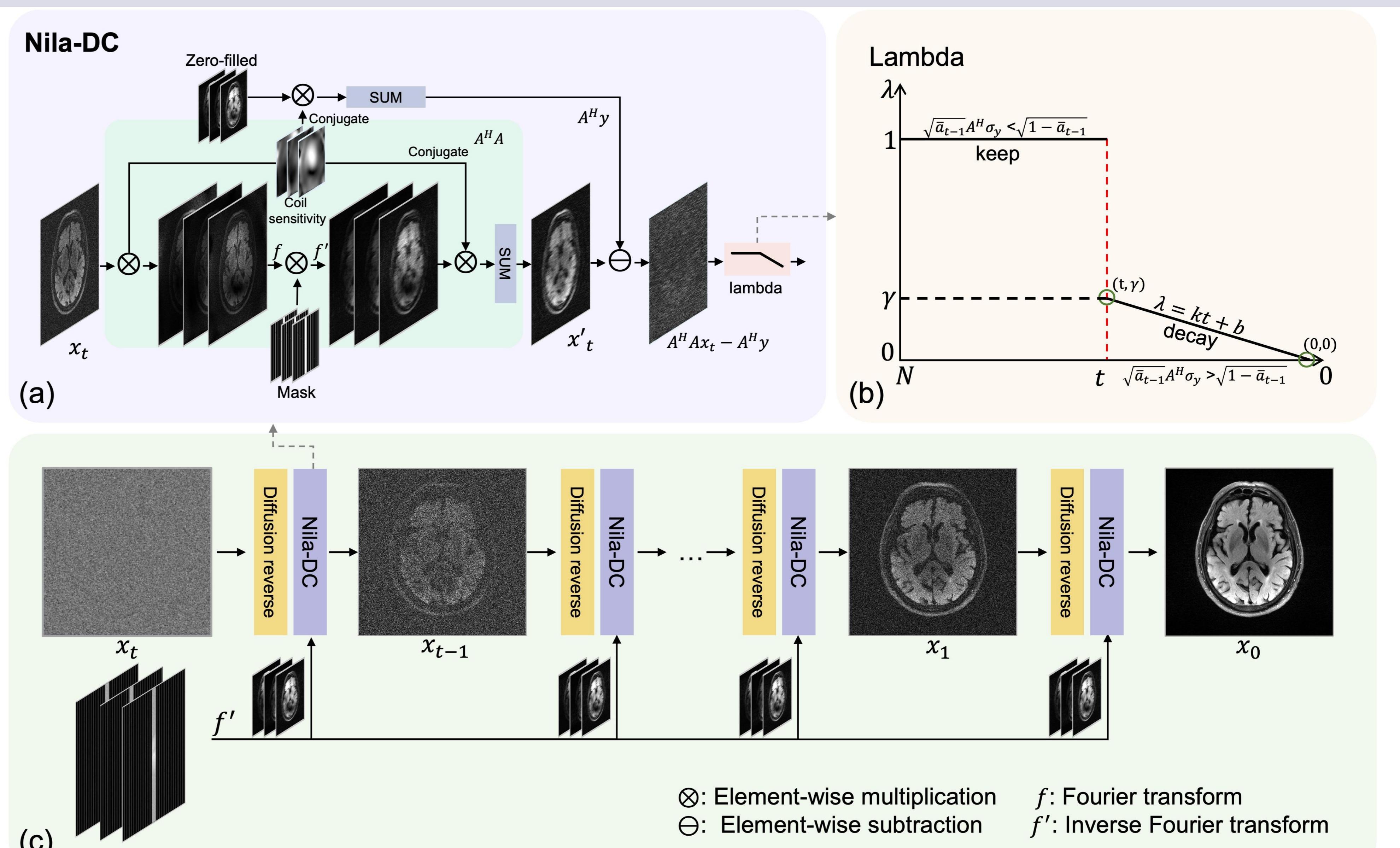


Fig.1 Overview of the proposed method.

### Qualitative Evaluation

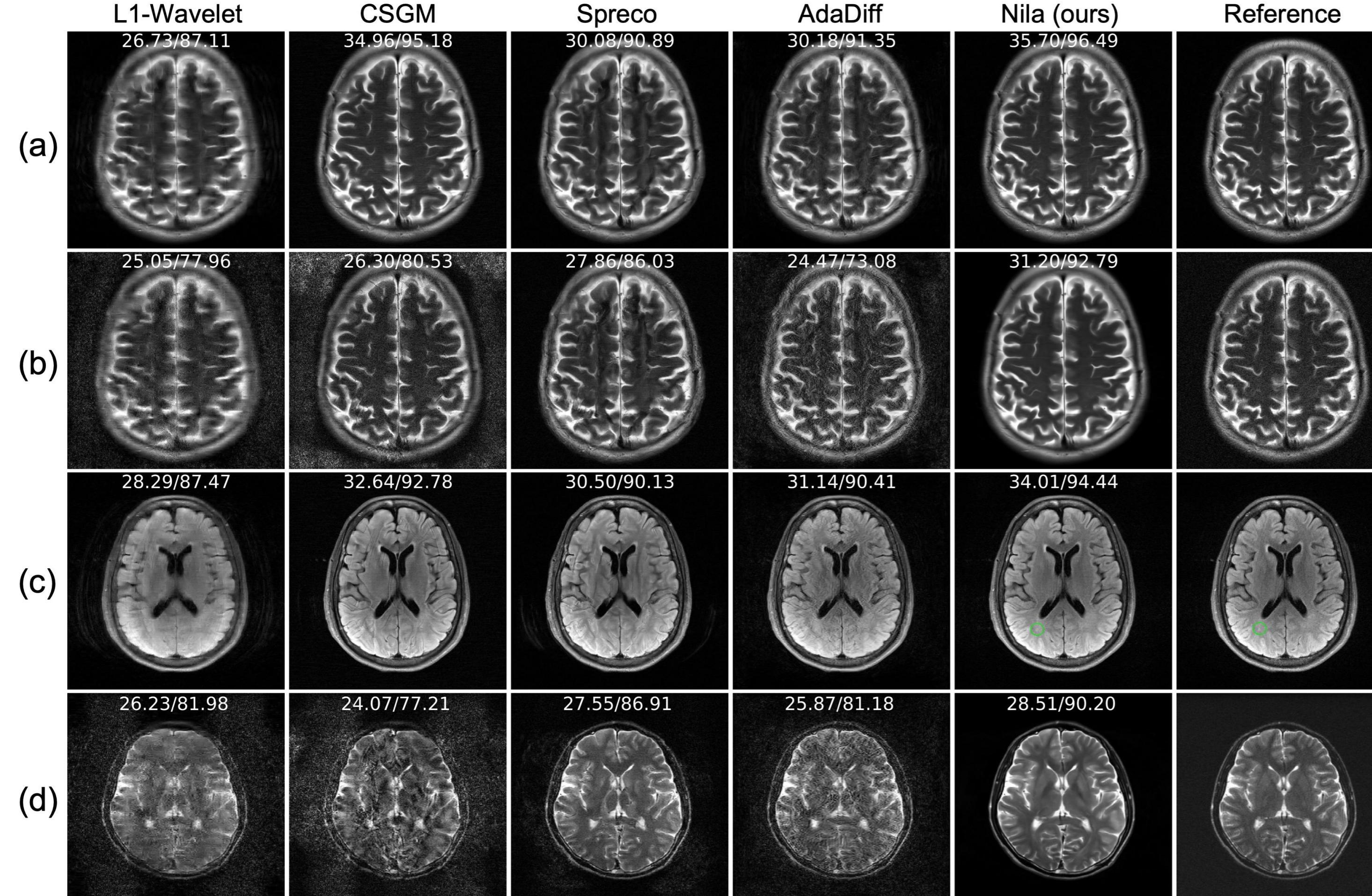


Fig.3 Visual comparison of reconstruction results. (a) 6× acceleration on fastMRI.  
(b) 6× acceleration on fastMRI with added Gaussian noise.

(c) 6× acceleration on the clinical dataset. (d) 4× acceleration on M4Raw.

### Quantitative Results

Table 1. Quantitative assessment for the three test datasets at different acceleration factors. No extra noise was added.

Dataset	fastMRI		Clinical		M4Raw			
	Acceleration factor	6×	8×	6×	8×	3×	4×	
Metric	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
Zero-filled	26.12	82.27	25.41	80.36	27.07	82.40	26.33	80.34
L1-wavelet	30.04	89.43	27.31	84.55	31.27	89.60	28.35	84.59
CSGM	<b>35.04</b>	<b>93.53</b>	<b>32.11</b>	<b>90.78</b>	<b>34.67</b>	<b>92.65</b>	26.73	84.53
Spreco	32.24	90.70	28.65	85.28	32.27	89.84	28.77	84.07
AdaDiff	33.25	91.79	29.62	86.66	32.84	90.81	29.60	85.65
Nila (ours)	<b>37.08</b>	<b>95.74</b>	<b>34.82</b>	<b>94.21</b>	<b>36.10</b>	<b>94.34</b>	<b>33.54</b>	<b>91.55</b>

Table 2. Quantitative assessment under various noise levels at 6x acceleration factor. Note that the sigma values represent the added noise to full sampled data.

Dataset	fastMRI			Clinical		
	noisy level	$\sigma = 0.025$	$\sigma = 0.05$	$\sigma = 0.1$	$\sigma = 0.025$	$\sigma = 0.05$
Metric	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
Zero-filled	26.06	81.40	25.90	79.22	25.32	74.08
L1-wavelet	29.07	85.86	26.78	78.15	21.28	64.98
CSGM	31.15	87.64	25.08	76.16	19.47	61.78
Spreco	<b>31.31</b>	<b>89.03</b>	<b>29.62</b>	<b>84.93</b>	<b>25.89</b>	<b>74.23</b>
AdaDiff	29.29	82.93	25.83	73.8	21.99	64.82
Nila (ours)	<b>34.98</b>	<b>93.96</b>	<b>33.56</b>	<b>92.49</b>	<b>31.86</b>	<b>90.38</b>

### Reference

- [1] Block, K.T., Uecker, M., Frahm, J.: Undersampled radial mri with multiple coils: iterative image reconstruction using a total variation constraint. *Magnetic Resonance in Medicine* 57(6), 1086–1098 (2007)
- [2] Fan, Y., Liao, H., Huang, S., Luo, Y., Fu, H., Qi, H.: A survey of emerging applications of diffusion probabilistic models in mri. *arXiv preprint arXiv:2311.11383*(2023)
- [3] Marques, J.P., Simonis, F.F., Webb, A.G.: Low-field mri: An mr physics perspective. *Journal of magnetic resonance imaging* 49(6), 1528–1542 (2019)
- [4] Biswal, B., Zerrin Yetkin, F., Haughton, V.M., Hyde, J.S.: Functional connectivity in the motor cortex of resting human brain using echo-planar mri. *Magnetic resonance in medicine* 34(4), 537–541 (1995)

### Conclusion

We identify and address the issue that existing diffusion model-based reconstruction methods are sensitive to the MRI noise level by introducing a noise level adaptive data consistency operation for the reverse diffusion process, which permits robust guidance. The proposed method is comprehensively evaluated to demonstrate outstanding performance under various experimental conditions.