A cube of edge length a in free space is charged with a volume charge density

$$\rho_u = \rho_0 \sin(\pi x/a) \,, \quad 0 \le x \le a \,,$$

where ρ_0 is a constant. Find the total charge in the cube.

Solution:

$$Q = \int_0^a \int_0^a \int_0^a \rho_u \, dx \, dy \, dz$$
$$= \rho_0 a^2 \int_0^a \sin(\pi x/a) \, dx$$
$$= \frac{2\rho_0 a^3}{\pi}$$

Answer:

$$Q = \frac{2\rho_0 a^3}{\pi}$$