

P.6-2 $\frac{\partial \mathbf{u}}{\partial t} = -\frac{e}{m}(\bar{\mathbf{E}} + \bar{\mathbf{u}} \times \bar{\mathbf{B}}).$

a) $\bar{\mathbf{E}} = \bar{a}_z E_0, \quad \bar{\mathbf{B}} = \bar{a}_x B_0.$

$$\begin{aligned} \frac{\partial u_x}{\partial t} &= 0, \\ \frac{\partial u_y}{\partial t} &= -\frac{e}{m} B_0 u_x, \\ \frac{\partial u_z}{\partial t} &= -\frac{e}{m} (E_0 - B_0 u_y). \end{aligned} \quad \rightarrow \quad \begin{cases} u_x = 0, \\ u_y = (u_0 - \frac{E_0}{B_0}) \cos \omega_0 t + \frac{E_0}{B_0}, \\ u_z = (\frac{E_0}{B_0} - u_0) \sin \omega_0 t; \quad \omega_0 = \frac{e}{m} B_0. \end{cases}$$

If the electron is injected at the origin ($x=y=z=0$) at $t=0$:

$$x=0, \quad y = \frac{c_2}{\omega_0} \sin \omega_0 t + \frac{E_0}{B_0} t, \quad z = -\frac{c_2}{\omega_0} (1 - \cos \omega_0 t); \quad c_2 = u_0 - \frac{E_0}{B_0}.$$

Eq. of motion: $(y - \frac{E_0}{B_0} t)^2 + (z + \frac{c_2}{\omega_0})^2 = (\frac{c_2}{\omega_0})^2.$

If $\frac{E_0}{B_0} = u_0, \quad u_x = u_z = 0, \quad u_y = u_0;$

$x = z = 0, \text{ and } y = u_0 t$