

Given position, velocity and acceleration,  $\mathbf{p}, \mathbf{v}, \mathbf{a} \in \mathbb{R}^2$ , where  $\mathbf{a} \neq \mathbf{0}$  Dishonored's movement system works as follows:

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**Algorithm 1** MOVEMENT( $\Delta t, s, f$ )

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1: MaxSpeed = 400 · s
2: MaxAccel = 2000 · s
3:  $\mathbf{d} = \mathbf{a} / |\mathbf{a}|$ 
4: if  $|\mathbf{a}| > \text{MaxAccel}$  then
5:    $\mathbf{a} = \text{MaxAccel} \cdot \mathbf{d}$  // Limit acceleration to MaxAccel
6:  $\mathbf{v} -= \Delta t \cdot f \cdot (\mathbf{v} - |\mathbf{v}| \cdot \mathbf{d})$  // Friction
7:  $\mathbf{v} += \Delta t \cdot \mathbf{a}$  // Acceleration
8: if  $|\mathbf{v}| > \text{MaxSpeed}$  then
9:    $\mathbf{v} = \text{MaxSpeed} \cdot \mathbf{v} / |\mathbf{v}|$  // Limit velocity to MaxSpeed
10:  $\mathbf{p} += \Delta t \cdot \mathbf{v}$  // Movement

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Here  $\Delta t, s, f \in \mathbb{R}$  represent respectively the delta time (in seconds), the speed scale, and friction constant. The friction constant  $f = 8$ , and the speed scale  $s$  depends on the type of movement. Some relevant values are  $s = 1$  when walking,  $s = 1.5$  when sprinting, and  $s = 1.95$  when agility sprinting. We can generally assume  $|\mathbf{a}| = 2000 \leq \text{MaxAccel}$ .

Note that when  $\Delta t = \frac{1}{f} = \frac{1}{8}$ , they cancel each other out during the friction step (Line 6), where we simply get  $\mathbf{v} -= \mathbf{v} - |\mathbf{v}| \cdot \mathbf{d}$ , which is equivalent to  $\mathbf{v} = |\mathbf{v}| \cdot \mathbf{d}$ , i.e., all previous speed gets redirected in the direction we are currently moving. This property is unique to 8 FPS.

It is possible to achieve something similar at other frame rates if we take into account the acceleration step (Line 7), by solving the equation

$$m \cdot \mathbf{u} = \mathbf{v} - \Delta t \cdot f \cdot (\mathbf{v} - |\mathbf{v}| \cdot \mathbf{d}) + \Delta t \cdot 2000 \cdot \mathbf{d},$$

for  $m$  and  $\mathbf{d}$  where  $|\mathbf{d}| = 1$  in order to move in direction  $\mathbf{u}$ .

If we make the simplifying assumption that  $\mathbf{v} = \text{MaxSpeed} \cdot \mathbf{w}$  for some unit vector  $\mathbf{w}$ , we can further simplify the equation to

$$\begin{aligned}
m \cdot \mathbf{u} &= \text{MaxSpeed} \cdot \mathbf{w} - \Delta t \cdot f \cdot \text{MaxSpeed} \cdot (\mathbf{w} - \mathbf{d}) + \Delta t \cdot 2000 \cdot \mathbf{d} \\
&= 400 \cdot s \cdot \mathbf{w} - \Delta t \cdot f \cdot 400 \cdot s \cdot (\mathbf{w} - \mathbf{d}) + \Delta t \cdot 2000 \cdot \mathbf{d} \\
\iff \frac{m}{400 \cdot s} \cdot \mathbf{u} &= \mathbf{w} - \Delta t \cdot f \cdot (\mathbf{w} - \mathbf{d}) + \frac{5}{s} \cdot \Delta t \cdot \mathbf{d}.
\end{aligned}$$

We let  $m' = \frac{m}{400 \cdot s}$  and  $a = \frac{5}{s}$ , and end up with the final equation

$$m' \cdot \mathbf{u} = \mathbf{w} - \Delta t \cdot f \cdot (\mathbf{w} - \mathbf{d}) + a \cdot \Delta t \cdot \mathbf{d}.$$

It is easy to rearrange in order to find

$$\mathbf{d} = \frac{m' \cdot \mathbf{u} + (\Delta t \cdot f - 1) \cdot \mathbf{w}}{\Delta t \cdot (a + f)}.$$

Solving for  $m'$  is harder but yields

$$m' = \sqrt{(\Delta t \cdot (a + f))^2 - ((\Delta t \cdot f - 1) \cdot \mathbf{u} \cdot \mathbf{w}')^2} - (\Delta t \cdot f - 1) \cdot \mathbf{u} \cdot \mathbf{w},$$

where  $\mathbf{w}' = (-w_2, w_1)$ .

If we want to simply turn an absolute amount, we can fix  $\mathbf{w} = (1, 0)$ , which simplifies the above equations to

$$\mathbf{d} = \frac{m' \cdot \mathbf{u} + (\Delta t \cdot f - 1, 0)}{\Delta t \cdot (a + f)},$$

and

$$m' = \sqrt{(\Delta t \cdot (a + f))^2 - ((\Delta t \cdot f - 1) \cdot u_2)^2} - (\Delta t \cdot f - 1) \cdot u_1.$$