

Tutorial #6. Sorting

Theoretical part

Sorting allows us to do multiple tasks:

- Sorted elements can be found in $O(\log(n))$ for search using binary/interpolation search (or even a place they should be inserted)
- They allow us to select linked areas of data in $O(n)$ time (SELECT * FROM T where C1 > V1).
- They allow us to make cool math (Principal Component Analysis include sorts, create a polygon of points, compression with loss algorithms involve sorting)
- They allow us to represent data for humans.

Faster sorts

There's a class of sorts that allow us to do it in $T(n \cdot \log(n))$ time: **quick sort**, that involves recursive strategy, **heap sort** and **merge sort**. Some of them provide $O(n \cdot \log(n))$, some – $\Omega(n \cdot \log(n))$.

$O(n)$ -sorts

Unlike bubble and insertion sort, there's a class of algorithms that does not involve comparison. All $O(n)$ sorts are non-comparative, because it is proven, that comparative sorts cannot perform better than $\Omega(n \cdot \log(n))$. We already know **counting sort**, it takes $O(n+k)$. There are also two well-known non-comparative sorts:

- **Bucket sort (Explain)**. Idea is to
 - o Split the range of values into buckets [1-50, 51-100, ...].
 - o Then **Scatter**: place items in the buckets according to the value (value / N_{buckets}).
 - o Sort each non-empty bucket.
 - o Then **Gather**: collect values back into array
 - Worst case: $O(n^2)$,
 - best/average case $E(n+k)$ (use count sort inside the bucket)
 - o Study this sort and try to implement it for integers.
- **Radix sort (Just mention)**. Similar idea: use digits as buckets.

Practical part (for Students)

- 1) Implement **insertion sort** using **Comparator** object for case insensitive string sorting.
- 2) Embed your implementation into **MyFramework.sort(...)** method, reuse the *Comparable.compareTo(...)* in comparator object.
- 3) Run tests in **MyFramework** class. See the output.
- 4) Uncomment line 22 in **Tests**. Measure **select** operation speed before and after this operation.
- 5) ***Try to implement $O(n)$ sort**