Objective(s):

You are to run benchmark on isPrime0, isPrime1, and isPrime2 mentioned in lectures.

For computing numPrime(n), we can use the following program:

```
public class L2 CountPrimeNum {
  private static boolean isPrimeO(int n) {
    if (n == 1) return false;
    if (n <= 3) return true;
    int m = n/2;
    for (int i = 2; i \le m; i++) {
      if (n % i == 0) return false;
    return true;
  private static void testIsPrime012() {
    int N = 100;
    int count = 0;
    for (int n = 1; n < N; n++) {
      if (isPrimeO(n)) count++;
    println("Pi ("+ N + ") = " + count);
    count = 0;
    for (int n = 1; n < N; n++) {
      if (isPrime1(n)) count++;
    println("Pi ("+ N + ") = " + count);
    count = 0;
    for (int n = 1; n < N; n++) {
      if (isPrime2(n)) count++;
    println("Pi ("+ N + ") = " + count);
  }
  public static void main(String [] args) {
    int count = 0;
    int N = 100;
    testIsPrime012();
  }
}
```

The method isPrimeO(n) takes any positive integer and returns true if it is a prime, false otherwise. The method run through all integer from 2 to n/2 and check if n is divisible by any of them.

There are two more methods, isPrime1(n) and isPrime2(n). The method isPrime1(n) is similar to isPrime0(n) but only run from 2 to \sqrt{n} . The method isPrime2(n) improves upon isPrime1(n) by take out anything divisible by 2 and 3 and not going to test divisibility of number that are multiple of 2 and 3.

```
private static boolean isPrime1(int n) {
  if (n == 1) return false;
  if (n <= 3) return true;
  int m = (int) Math.sqrt(n);
  for (int i = 2; i <= m; i++) {
    if (n % i == 0) return false;
  return true;
private static boolean isPrime2(int n) {
  if (n == 1) return false;
  if (n <= 3) return true;
  if ((n%2 == 0) || (n%3 == 0)) return false;
  int m = (int) Math.sqrt(n);
  for (int i = 5; i \le m; i += 6) {
    if (n % i == 0) return false;
    if (n % (i+2) == 0) return false;
                                                      java CountPiN
  return true;
                                                     Pi (100)= 25
                                                        (100) = 25
```

The output would look like this.

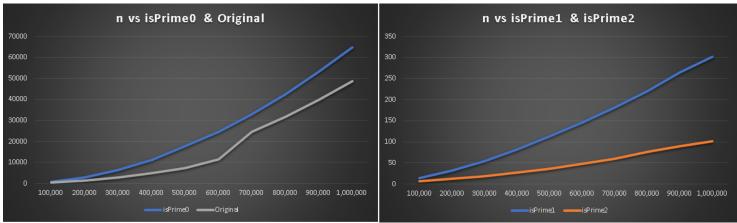
To measure efficiency of these methods, modify the main method as follows.

```
public static void main(String [] args) {
     int count = 0;
     int N = 100;
     // testIsPrime012();
     for (N = 100\ 000;\ N <= 1\ 000\ 000;\ N+=\ 100\ 000) {
        long start = System.currentTimeMillis();
        for (int n = 1; n < N; n++) {
          if (isPrimeO(n)) count++;
        long time = (System.currentTimeMillis() - start);
        println(N + "\t" + count + "\t" + time);
                                                                    9592
                                                                          353
                                                              200000
     }
                                                              300000
   }
                                                              400000
                                                              500000
                                                              600000
                                                                          15580
The result of running with isPrimeO(n) should be
                                                              900000 369837
                                                                         39964
```

Task 1: run the program with isPrime0, isPrime1, and isPrime2. Record your result into the following table.

| Running-time table | | | | | |
|--------------------|----------------|-----------------------|--------------------|----------|----------|
| | | | time(milliseconds) | | |
| n | noPrime(n) | Original | isPrime0 | isPrime1 | isPrime2 |
| 100,000 | 9592 | 353 | 801 | 14 | 7 |
| 200,000 | 27576 | 1283 | 2968 | 32 | 12 |
| 300,000 | 53573 | 2792 | 6432 | 54 | 18 |
| 400,000 | 87433 | 482 0 | 11214 | 82 | 27 |
| 500,000 | 128971 | 7 3 7 0 | 17609 | 113 | 37 |
| 600,000 | 178 069 | 11580 | 24577 | 146 | 48 |
| 700,000 | 234612 | 24557 | 32878 | 181 | 60 |
| 800,000 | 298563 | 31716 | 42452 | 220 | 77 |
| 900,000 | 369837 | 39964 | 53240 | 265 | 90 |
| 1,000,000 | 448335 | 48785 | 64801 | 302 | 101 |

Task 2: Plot two graphs, A --> n vs. lab's result isPrime0's time and your isPrime0's and B --> n vs. lab's isPrime1's time and isPrime2's time. And your isPrime1's and isPrime2's



Taks 3: In your own words, describe trend of isPrime0, isPrime1, and isPrime2. Are your recorded times differ to the recorded time given? Why?

The graphs isPrime0, isPrime1, isPrime2, Original are exponentially increasing as we increase the number of n. My recorded time was a bit slower than the original time, this might be due to the difference in cpu's performance.

Due Date: TBA