

# Optimization of Nested Queries using the $NF^2$ Algebra

**Jürgen Hölsch, Michael Grossniklaus, and Marc H. Scholl**

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## Motivation

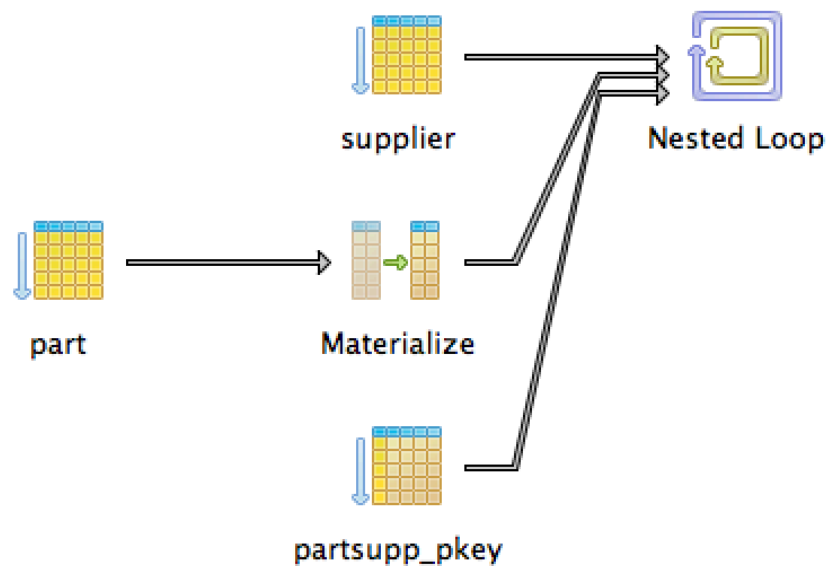
### Example

*“All Parts offered by a supplier”*

```
SELECT p_name, s_name
FROM Part, Supplier
WHERE p_partkey IN (SELECT ps_partkey
                    FROM PartSupp
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```

## Motivation

- Execution plan in PostgreSQL 9.4.2:



- Execution time on a 10 GB TPC-H DB: > 24 h

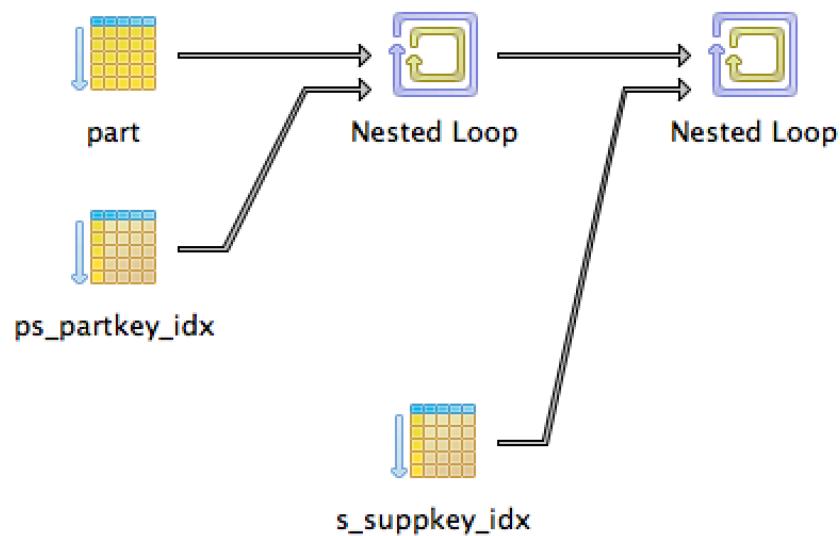
## Motivation

### Alternative formulation

```
SELECT p_name, s_name  
FROM Part, Supplier, PartSupp  
WHERE p_partkey = ps_partkey AND ps_suppkey = s_suppkey
```

## Motivation

- Execution plan in PostgreSQL 9.4.2:



- Execution time on a 10 GB TPC-H DB:  $\approx 32$  s

## Techniques for optimizing nested queries

- Transformations at the level of SQL
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- Transformations at the level of SQL  
⇒ Separates nested query optimization from other optimization steps
  - Different formalisms (e.g. comprehension calculus)  
⇒ Not used in real world optimizers
- Ideally, handle nested query optimization **algebraically**

## How can we optimize this query algebraically?

### Example

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**Nestings cannot be represented by the relational algebra**

How can we optimize this query algebraically?

⇒ Representation with NF<sup>2</sup> algebra

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NF<sup>2</sup> representation:

$$\pi[p\_name, s\_name](\sigma[p\_partkey \in \pi[ps\_partkey](\sigma[ps\_suppkey = s\_suppkey](PartSupp))](Part \times Supplier))$$



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⇒ Representation with NF<sup>2</sup> algebra

No NF<sup>2</sup> backend  
is needed

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- We define  $NF^2$  equivalences that formalize existing optimization techniques
- We introduce new optimization techniques, which are made possible by the  $NF^2$  approach
- We discuss the necessary changes to an optimizer based on Cascades framework
- We quantify the performance benefits of our approach

# Equivalences for existing optimization techniques



Won Kim, *On Optimizing an SQL-like Nested Query*. ACM Transactions on Database Systems (TODS), 1982.

## Unnesting of Type J and N queries

$$\sigma[A \in \pi[B](\sigma[F](Inner))](Outer) \equiv \pi[attr(Outer)](Inner \bowtie_{A=B \wedge F} Outer)$$

## Unnesting of Type A queries

$$\begin{aligned} & \sigma[A \theta f(\pi[B](Inner))](Outer) \\ & \equiv \pi[attr(Outer)](\sigma[A \theta agg](Outer \times (agg := f(\pi[B](Inner)))) \end{aligned}$$

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If  $F$  has inequality predicates:

$$\begin{aligned} & \sigma[A \theta f(\pi[B](\sigma[F](Inner)))](Outer) \\ & \equiv \pi[attr(Outer)](\sigma[A \theta agg](Outer \bowtie \gamma[G; agg := f(B)](Outer \bowtie_F Inner))) \end{aligned}$$

If  $f$  is COUNT:

$$\begin{aligned} & \sigma[A \theta COUNT(\pi[B](\sigma[F](Inner)))](Outer) \\ & \equiv \pi[attr(Outer)](\sigma[A \theta agg](Outer \bowtie \gamma[G; agg := COUNT(B)](Outer \bowtie Inner))) \end{aligned}$$



## Example: Type J and N unnesting rule

### Type J and N unnesting rule

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### Query from the introduction

$$\begin{aligned} & \pi[p\_name, s\_name](\sigma[p\_partkey \in \pi[ps\_partkey]( \\ & \quad \sigma[ps\_supkey = s\_supkey](PartSupp))](Part \times Supplier)) \\ \equiv & \pi[p\_name, s\_name]( \\ & \quad PartSupp \bowtie_{p\_partkey=ps\_partkey \wedge ps\_supkey=s\_supkey} (Part \times Supplier)) \end{aligned}$$



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Existing relational algebra equivalences remain valid

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## More equivalences for existing optimization techniques



Bellamkonda et al., *Enhanced Subquery Optimizations in Oracle*. In PVLDB, 2009.

### Subquery coalescing rule I

$$\begin{aligned} & \sigma[(A \theta_1 \theta_3(\pi[B](\sigma[F_1](Inner)))) \theta_2 (A \theta_1 \theta_3(\pi[B](\sigma[F_2](Inner))))](Outer) \\ & \equiv \sigma[A \theta_1 \theta_3(\pi[B](\sigma[F_1 \vee F_2](Inner)))](Outer) \end{aligned}$$

### Subquery coalescing rule II

$$\begin{aligned} & \sigma[(A \theta_1 \theta_3(\pi[A](\sigma[F_1](Inner)))) \theta_2 (A \theta_1 \theta_3(\pi[A](\sigma[F_2](Inner))))](Outer) \\ & \equiv \sigma[A \theta_1 \theta_3(\pi[A](\sigma[F_1](Inner)))](Outer) \end{aligned}$$

### Subquery coalescing rule III

$$\begin{aligned} & \sigma[(A \theta_1 \theta_3(\pi[A](\sigma[F_1](Inner)))) \theta_2 (A \theta_1 \theta_3(\pi[A](\sigma[F_2](Inner))))](Outer) \\ & \equiv \sigma[A \theta_1 \theta_3(\pi[A](\sigma[F_2](Inner)))](Outer) \end{aligned}$$

## Example: Subquery coalescing

### Example

```
SELECT *  
FROM Orders  
WHERE o_totalprice >= (SELECT MAX(o_totalprice)  
                        FROM Orders  
                        WHERE o_orderpriority = '2-HIGH')  
AND o_totalprice >= (SELECT MAX(o_totalprice)  
                      FROM Orders  
                      WHERE o_orderpriority = '3-MEDIUM')
```



```
SELECT *  
FROM Orders  
WHERE o_totalprice >= (SELECT MAX(o_totalprice)  
                        FROM Orders  
                        WHERE o_orderpriority = '2-HIGH'  
                        OR o_orderpriority = '3-MEDIUM')
```

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 $\sigma[o\_totalprice \geq \text{MAX}(\pi[o\_totalprice]($   
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## Example: Subquery coalescing

### Equivalence rule

$$\begin{aligned} & \sigma[A \geq \text{MAX}(\pi[B](\sigma[F_1](Inner))) \wedge \\ & \quad A \geq \text{MAX}(\pi[B](\sigma[F_2](Inner)))](Outer) \\ \equiv & \sigma[A \geq \text{MAX}(\pi[B](\sigma[F_1 \vee F_2](Inner)))](Outer) \end{aligned}$$

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$\sigma[o\_totalprice \geq \text{MAX}(\pi[o\_totalprice'](\sigma[o\_orderpriority = '2-HIGH'](Orders')))) \wedge$   
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## Example: Subquery coalescing

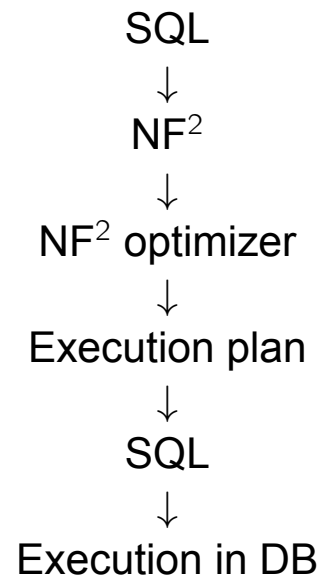
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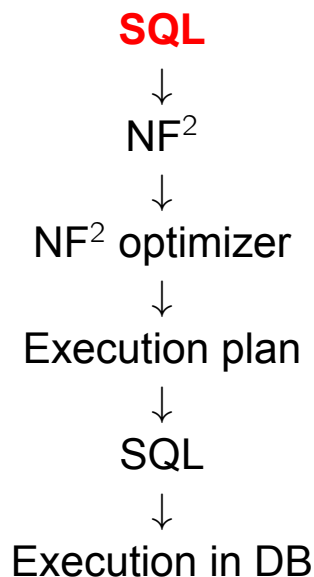
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# Evaluation





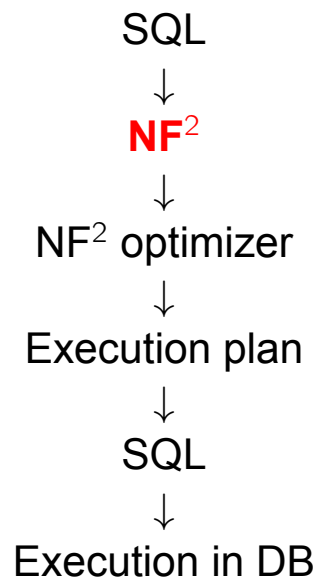
# Evaluation



Set of 11 nested queries

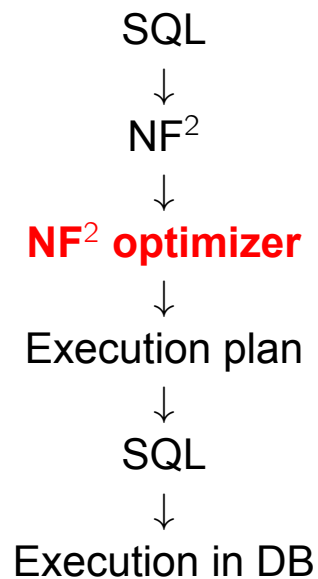
- ▶ Subqueries in SELECT, FROM and WHERE clause
- ▶ Subqueries with multiple nestings
- ▶ Subqueries with redundancy

# Evaluation



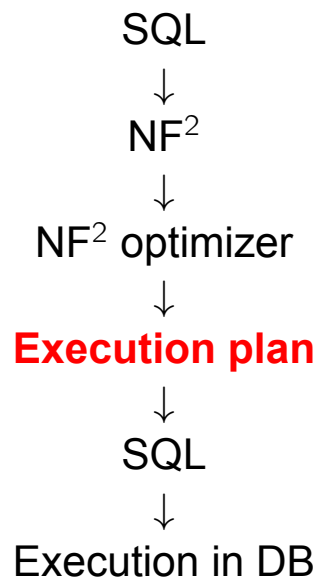
► 1:1 translation from SQL

# Evaluation



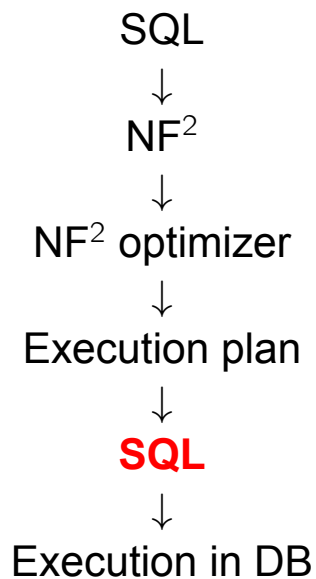
- Optimize each query **with** and **without** NF<sup>2</sup> rules

## Evaluation



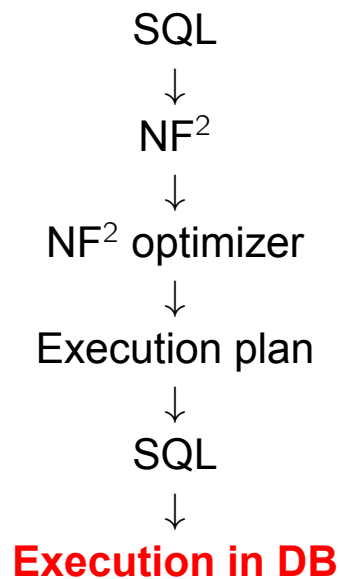
► Generated by the NF<sup>2</sup> optimizer

# Evaluation



► Derived from execution plan

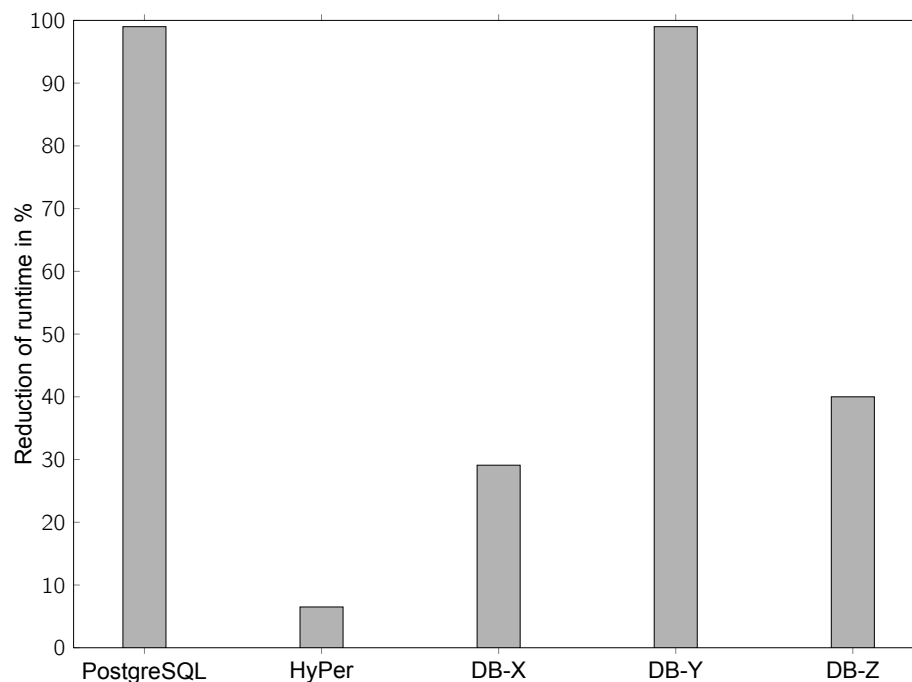
# Evaluation



## Systems:

- ▶ Postgres 9.4.2
- ▶ HyPer
- ▶ Three commercial database systems

## Evaluation: Runtime reduction over all queries

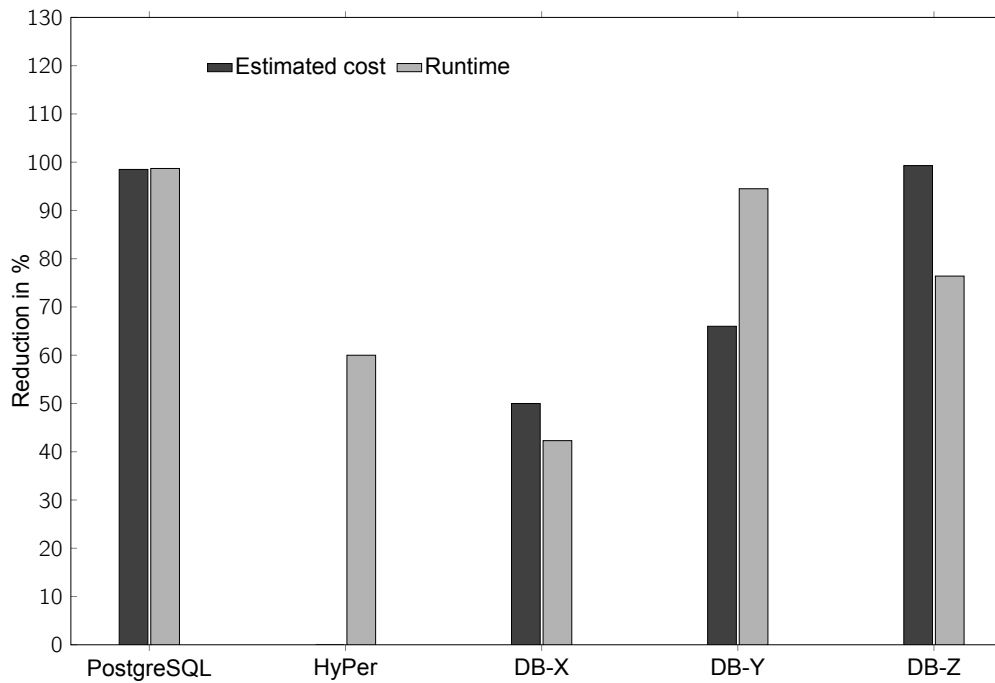


↑  
Larger is better

Formula to compute the runtime reduction:

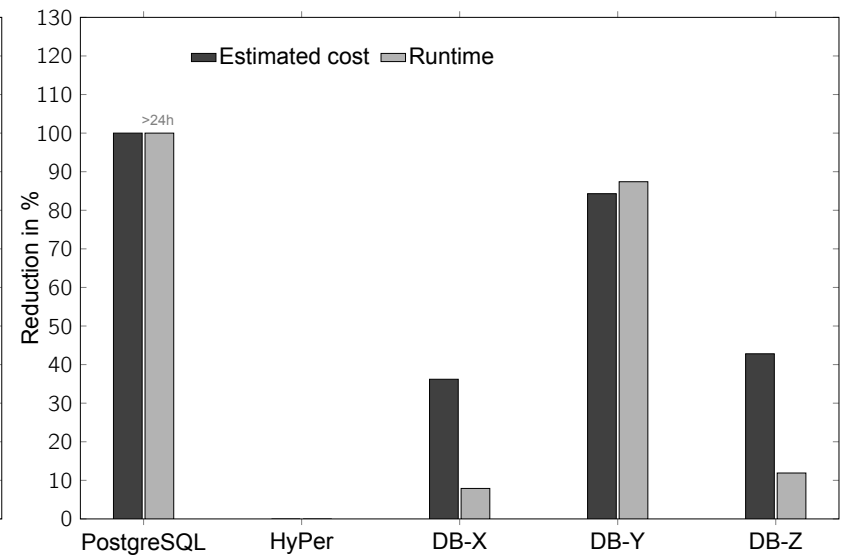
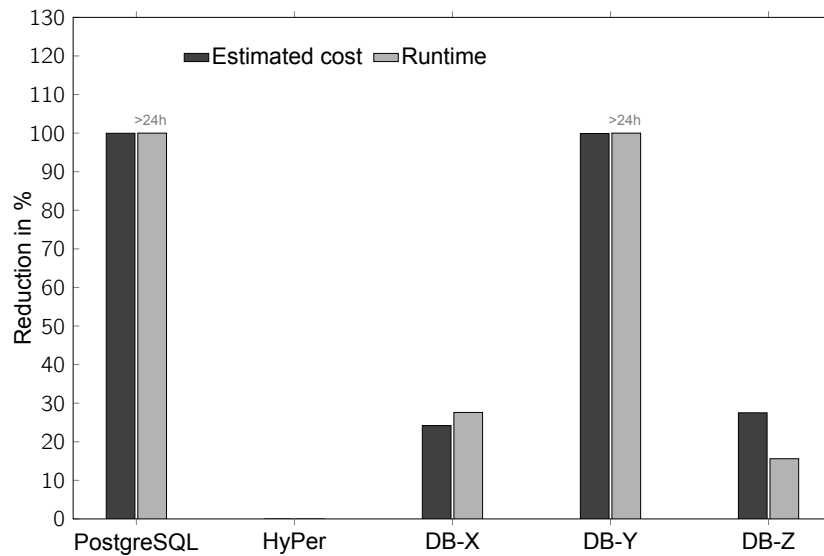
$$\frac{(\text{runtime original query} - \text{runtime transformed query})}{\text{runtime original query}} * 100$$

## Evaluation: Subquery in Select Clause

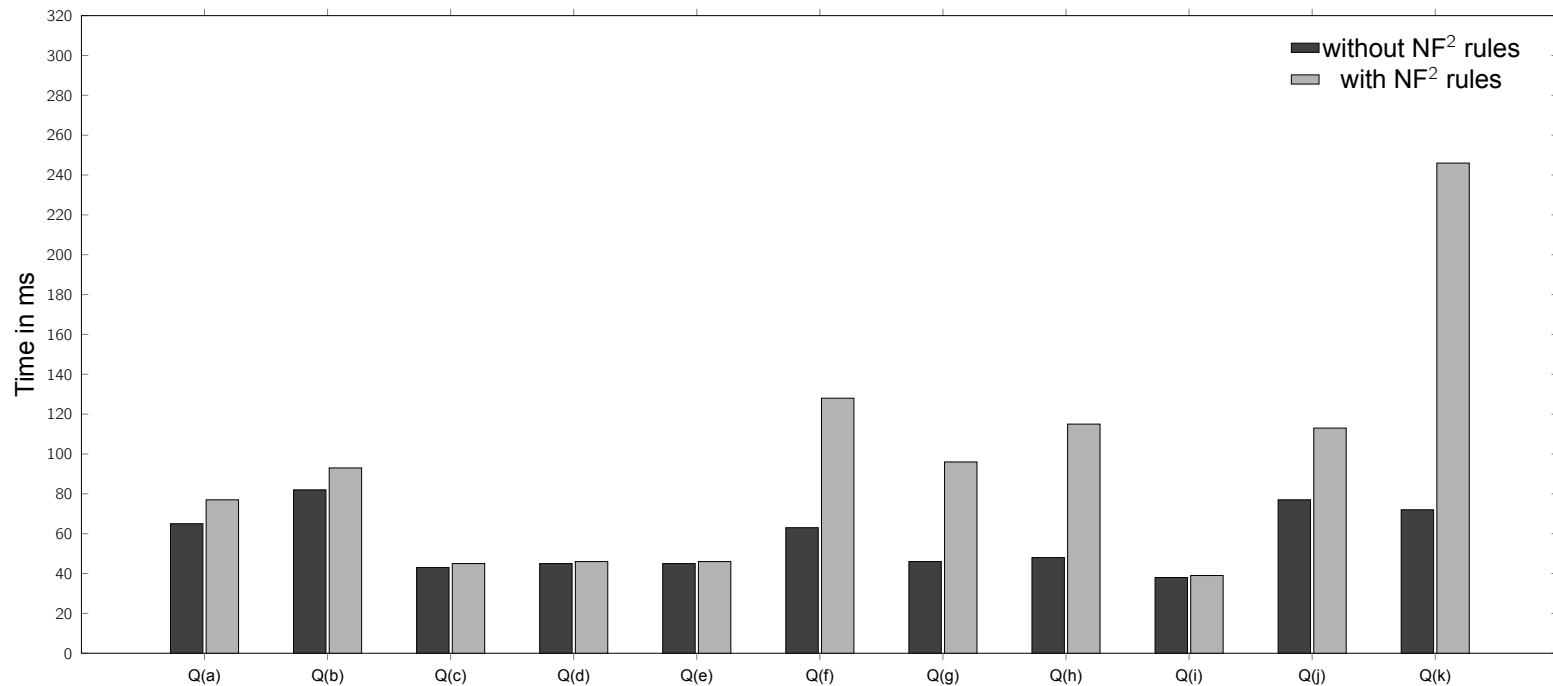




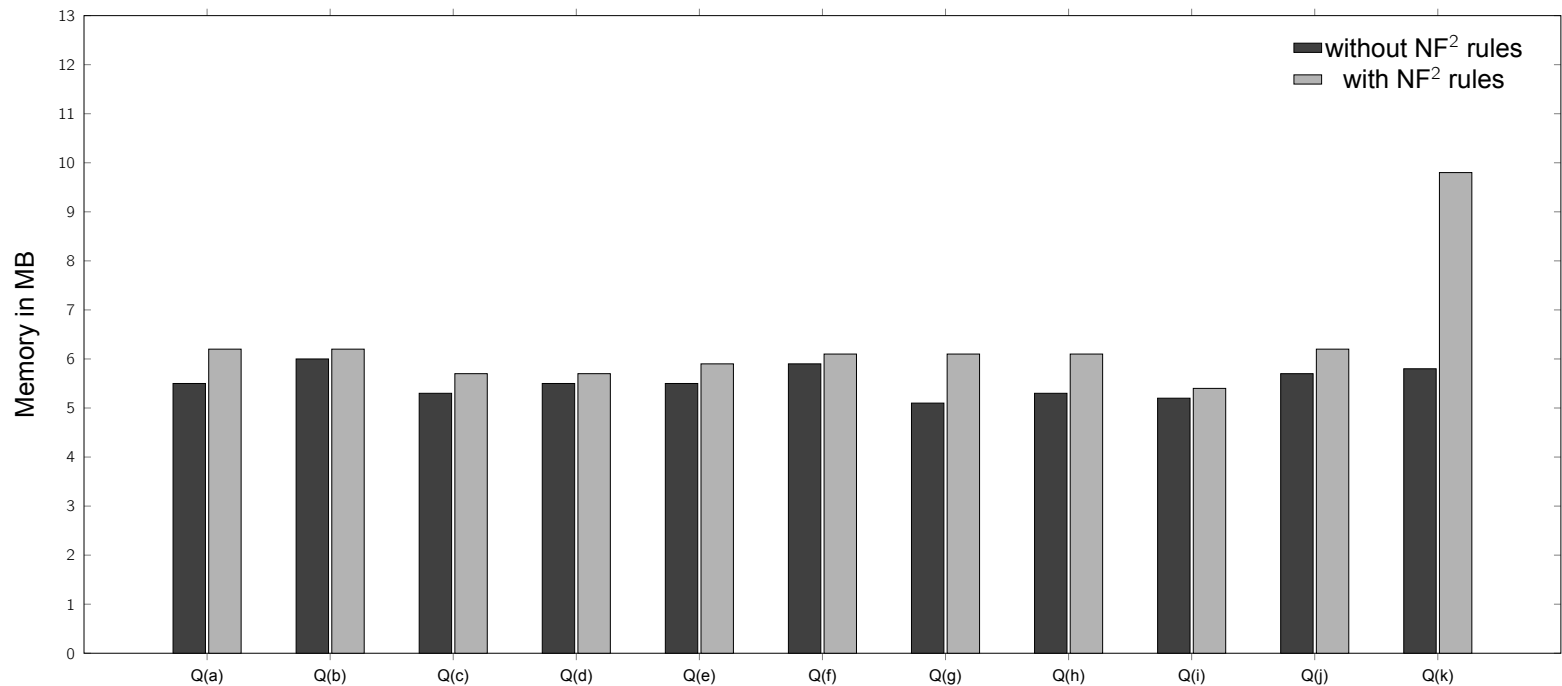
## Evaluation: Subqueries with Multiple Nestings



## Evaluation: NF<sup>2</sup> Optimizer (Runtime)



## Evaluation: NF<sup>2</sup> Optimizer (Memory)



## Summary

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NF<sup>2</sup> algebra for optimizing nested queries

- Can represent all types of nested queries
- Extension of the relational algebra  
⇒ Existing equivalences remain valid
- Can be integrated into a transformation-based optimizer with little effort
- No NF<sup>2</sup> backend is needed