

Minimization of Weighted Automata

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Introduction

In the last presentation . . .

- two models for stochastic dynamical systems were considered:
Weighted Automata (WA) and Differential Equations (DE)
- an example for modelling a CRN's dynamics in both models was given:
 - DE Solving Chemical Master Equation
 - WA Monte Carlo CTMC

Goals specified

1. Implement minimization algorithm for weighted automata [1]. ✓
2. Implement model reduction algorithm for ODEs [2].
3. Develop reproducible benchmarks
4. Write report including

What has been done so far

- Software Requirement Specification & Software Design Document
- Random Basis Minimal WA Construction Algorithm by Kiefer/Schützenberger [1]
- Execution of example by Matlab script and hand
- Implementation of minimization & equivalence algorithm, interfaces, TUI, CLI, tests

The Weighted Automaton Minimization Algorithm

Weighted Automaton $A = (n, \Sigma, \alpha, \mu, \eta)$, where

- n the number of states
- Σ the input alphabet
- α the initial vector with a non-zero value for all starting states
- μ the set of transition matrices, one per input character

Intuition:

1. Generate $|\text{states}|$ many random matrices r_i with $|\Sigma|$ rows and $|\text{states}|$ columns with values between 1 and r

The Weighted Automaton Minimization Algorithm: Pseudo Code

b

The Weighted Automaton Minimization Algorithm: Example

C



Implementation Details

d

Up Next

e

Bibliography

-  S. Kiefer, A. S. Murawski, J. Ouaknine, B. Wachter, and J. Worrell, “On the complexity of equivalence and minimisation for q-weighted automata”, *Logical Methods in Computer Science*, vol. 9, 2013.
-  L. Cardelli, M. Tribastone, M. Tschaikowski, and A. Vandin, “Maximal aggregation of polynomial dynamical systems”, *Proceedings of the National Academy of Sciences of the United States of America*, vol. 114 38, pp. 10 029–10 034, 2017.