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1  """
2  Movement along z-axis (normal to surface)
3   $dz(t)/dt = v(t)$ 
4   $dv(t)/dt = -g - (A*v(t) + B*v(t)^3)/m$ 
5  """
6
7  import numpy as np
8  from scipy.integrate import odeint
9  import matplotlib.pyplot as plt
10
11  z0 = 0.0          # m
12  v0 = 500.0        # m/sec
13  m = 0.009         # kg
14  g = 9.8           # m/sec^2
15  A = 1.e-5         # N*sec/m
16  B = 1.e-8         # N*sec^3/m^3
17  tm = 110.0        # sec
18
19
```

```
20 def system(f, t):
21     global m, g, A, B
22     z = f[0]
23     v = f[1]
24     dzdt = v
25     dvdt = -g - (A*v + B*v**3)/m
26     return [dzdt, dvdt]
27
28 nt = 1000
29 t = np.linspace(0., tm, nt)
30 sol = odeint(system, [z0, v0], t)
31 z = sol[:, 0]
32 v = sol[:, 1]
33
34 print("len(z)=", len(z))
35
36 # Simple calculation of Tflight
37 for i in range(len(z)):
38     if z[i] < 0.0:
```

```
39     Tflight = (t[i]+t[i-1])/2.0
40     print("Node of landing:", i)
41     print("Tflight=", Tflight)
42     break
43
44     plt.plot(t, v, 'r-', linewidth=3)
45     plt.plot(t, [0.0]*nt, 'g-', linewidth=1)
46     plt.axis([0, Tflight+1, -250., 500.])
47     plt.grid(True)
48     plt.xlabel("t")
49     plt.ylabel("v(t)")
50     plt.savefig("v.pdf", dpi=300)
51     plt.show()
52
53     plt.plot(t, z, 'b-', linewidth=3)
54     plt.axis([0, Tflight+1, 0., 3500.])
55     plt.grid(True)
56     plt.xlabel("t")
57     plt.ylabel("z(t)")
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```
58 plt.savefig("z.pdf", dpi=300)
59 plt.show()
```