

Homework 7, by Somesh Srivastava, Mar 09, 2018

Executive Summary

As part of this project, Fama-Macbeth type of regression analysis has been conducted with stock returns as dependent variable and firm-marketcap, price-normalized accruals, the earnings-price ratio, and 1/price as independent variables.

Details

For data preparation, annual data for price, market cap, Earning per share has been taken from CRSP/Compustat database. Also to calculate price normalized accruals data has been taken from annual fundamental table for account payable(AP), receivable total (rect), tax payable (txp) and accrued expense (xacc).

Price Normalized Accruals = $(ap-rect+txp+xacc)/MarketCap$

Period of data is starting 1980 till 2016. Only those stocks have been filtered which have complete records in the specified period. As a first step, Time series regression has been run with Annual holding period return of stocks vs independent lagged variables viz. Market Cap, Price-normalized-accruals, earning-price ratio, 1/price for each stock. In the second steps, cross-sectional regression has been run for each year to calculate the risk premium of each factor loading(Lambda). Finally mean of each Lambda has been calculated as final estimated value of each risk premium.

From Time series regression -

$$\text{Annual Stock Ret} = \alpha + \beta_{\text{marketcap}} * \text{MarketCap} + \beta_{\text{(price-normalized-earnings)}} * \text{Price_normalized_Earnings} + \beta_{\text{(earning-price-ratio)}} * \text{EarningPriceRatio} + \beta_{\text{(price-inverse)}} * (1/\text{price}) + \epsilon$$

From cross-sectional regression -

$$\text{Annual Stock Ret} = \alpha' + \beta_{\text{marketcap}} * \lambda_{\text{marketcap}} + \beta_{\text{(price-normalized-earnings)}} * \lambda_{\text{(price-normalized-earnings)}} + \beta_{\text{(earning-price-ratio)}} * \lambda_{\text{(earning-price-ratio)}} + \beta_{\text{(price-inverse)}} * \lambda_{\text{(price-inverse)}} + \epsilon'$$

Tables and Figures

Sample Data for One stock:

| year | PERMNO | AnnualRet | MarketCap | price_norm_accrual | EPRatio | Price | lag_MarketCap | lag_price_norm_accrual | lag_EPRatio | lag_Price |
|------|--------|------------|------------|--------------------|------------|-------|---------------|------------------------|-------------|-----------|
| 1982 | 10145 | -0.2110357 | 1141218.8 | 0.00034787 | 0.1921236 | 32.38 | 1791661.5 | 0.0001948 | 0.152336 | 53.50 |
| 1983 | 10145 | 0.8104779 | 2980339.3 | 0.00027648 | 0.1239462 | 55.75 | 1480518.0 | 0.0002459 | 0.209003 | 43.88 |
| 1984 | 10145 | -0.0224920 | 2864500.5 | 0.00031000 | 0.1455072 | 34.50 | 1141218.8 | 0.0003479 | 0.192124 | 32.38 |
| 1985 | 10145 | 0.4143333 | 8190319.5 | 0.00014358 | -0.0701604 | 46.75 | 2980339.3 | 0.0002765 | 0.123946 | 55.75 |
| 1986 | 10145 | -0.0034831 | 6995874.0 | 0.00018983 | 0.0812461 | 40.13 | 2864500.5 | 0.0003100 | 0.145507 | 34.50 |
| 1987 | 10145 | -0.2628861 | 4269450.8 | 0.00033892 | 0.1086726 | 28.25 | 8190319.5 | 0.0001436 | -0.070160 | 46.75 |
| 1988 | 10145 | 0.2142041 | 4834245.0 | 0.00028877 | 0.0953846 | 32.50 | 6995874.0 | 0.0001898 | 0.081246 | 40.13 |
| 1989 | 10145 | 0.1275422 | 5231494.1 | 0.00027086 | 0.1017921 | 34.88 | 4269450.8 | 0.0003389 | 0.108673 | 28.25 |
| 1990 | 10145 | -0.1816399 | 3639465.0 | 0.00031049 | 0.1240741 | 27.00 | 4834245.0 | 0.0002888 | 0.095385 | 32.50 |
| 1991 | 10145 | 0.7049566 | 6029741.3 | 0.00018475 | -0.0455840 | 43.88 | 5231494.1 | 0.0002709 | 0.101792 | 34.88 |
| 1992 | 10145 | 0.4046008 | 8569038.5 | 0.00017622 | 0.0628099 | 60.50 | 3639465.0 | 0.0003105 | 0.124074 | 27.00 |
| 1993 | 10145 | 0.3277328 | 11192483.0 | 0.00013795 | 0.0584810 | 79.00 | 6029741.3 | 0.0001848 | -0.045584 | 43.88 |
| 1994 | 10145 | -0.1234848 | 9621558.0 | 0.00012430 | 0.0788235 | 34.00 | 8569038.5 | 0.0001762 | 0.062810 | 60.50 |
| 1995 | 10145 | 0.4230697 | 13435517.5 | 0.00009133 | 0.0650526 | 47.50 | 11192483.0 | 0.0001379 | 0.058481 | 79.00 |
| 1996 | 10145 | 0.4316193 | 18947667.0 | 0.00006829 | 0.0538806 | 67.00 | 9621558.0 | 0.0001243 | 0.078824 | 34.00 |
| 1997 | 10145 | 0.1744621 | 21894237.3 | 0.00006084 | 0.0520458 | 38.81 | 13435517.5 | 0.0000913 | 0.065053 | 47.50 |

| | | | | | | | | | | |
|------|-------|------------|------------|------------|------------|--------|------------|-----------|-----------|-------|
| 1998 | 10145 | 0.1587137 | 24817215.6 | 0.00004251 | 0.0523554 | 44.31 | 18947667.0 | 0.0000683 | 0.053881 | 67.00 |
| 1999 | 10145 | 0.3183616 | 45528878.7 | 0.00002759 | 0.0329361 | 57.69 | 21894237.3 | 0.0000608 | 0.052046 | 38.81 |
| 2000 | 10145 | -0.1666203 | 38083534.5 | 0.00001197 | 0.0433289 | 47.31 | 24817215.6 | 0.0000425 | 0.052355 | 44.31 |
| 2001 | 10145 | -0.2709287 | 27502052.0 | 0.00005716 | -0.0035482 | 33.82 | 45528878.7 | 0.0000276 | 0.032936 | 57.69 |
| 2002 | 10145 | -0.2737764 | 19705224.0 | 0.00012596 | -0.0112500 | 24.00 | 38083534.5 | 0.0000120 | 0.043329 | 47.31 |
| 2003 | 10145 | 0.4325132 | 28818364.9 | 0.00008415 | 0.0466647 | 33.43 | 27502052.0 | 0.0000572 | -0.003548 | 33.82 |
| 2004 | 10145 | 0.0821139 | 30458548.9 | 0.00009019 | 0.0420785 | 35.41 | 19705224.0 | 0.0001260 | -0.011250 | 24.00 |
| 2005 | 10145 | 0.0754672 | 31392772.8 | 0.00007314 | 0.0499329 | 37.25 | 28818364.9 | 0.0000841 | 0.046665 | 33.43 |
| 2006 | 10145 | 0.2416667 | 36938912.4 | 0.00005864 | 0.0554819 | 45.24 | 30458548.9 | 0.0000902 | 0.042079 | 35.41 |
| 2007 | 10145 | 0.3864151 | 45978628.9 | 0.00004474 | 0.0513237 | 61.57 | 31392772.8 | 0.0000731 | 0.049933 | 37.25 |
| 2008 | 10145 | -0.4534744 | 23844002.2 | 0.00010447 | 0.1145294 | 32.83 | 36938912.4 | 0.0000586 | 0.055482 | 45.24 |
| 2009 | 10145 | 0.2381948 | 29911324.8 | 0.00007495 | 0.0727041 | 39.20 | 45978628.9 | 0.0000447 | 0.051324 | 61.57 |
| 2010 | 10145 | 0.3950954 | 41473996.7 | 0.00004960 | 0.0487208 | 53.16 | 23844002.2 | 0.0001045 | 0.114529 | 32.83 |
| 2011 | 10145 | 0.0483500 | 42039562.0 | 0.00005849 | 0.0432383 | 54.35 | 29911324.8 | 0.0000750 | 0.072704 | 39.20 |
| 2012 | 10145 | 0.1984656 | 49720620.8 | 0.00004803 | 0.0581377 | 63.47 | 41473996.7 | 0.0000496 | 0.048721 | 53.16 |
| 2013 | 10145 | 0.4705048 | 71695572.0 | 0.00002755 | 0.0538470 | 91.37 | 42039562.0 | 0.0000585 | 0.043238 | 54.35 |
| 2014 | 10145 | 0.1151062 | 78218375.2 | 0.00002622 | 0.0533427 | 99.92 | 49720620.8 | 0.0000480 | 0.058138 | 63.47 |
| 2015 | 10145 | 0.0584036 | 79820466.9 | 0.00002375 | 0.0583180 | 103.57 | 71695572.0 | 0.0000275 | 0.053847 | 91.37 |
| 2016 | 10145 | 0.1498829 | 88292181.3 | 0.00001978 | 0.0535175 | 115.85 | 78218375.2 | 0.0000262 | 0.053343 | 99.92 |

Time Series Regression Output:

| PERMNO | alpha | beta1 | beta2 | beta3 | beta4 |
|---------------|--------------|--------------|--------------|--------------|--------------|
| 10145 | 0.136747514 | -1.70E-09 | -75.25452949 | 0.98800913 | 0.196442535 |
| 10656 | 0.059838645 | -4.55E-07 | -2792.539481 | -0.244173882 | 0.282147331 |
| 10866 | 0.356856275 | -4.59E-07 | 108.4222691 | 0.320337772 | 0.217782414 |
| 10890 | 0.425826754 | -1.13E-07 | 146.361354 | -0.100391075 | 0.247739192 |
| 11790 | 0.433159201 | -1.22E-06 | -151.7256897 | -2.869282296 | 0.204171002 |
| 13303 | 0.430157182 | -3.16E-07 | -851.3706477 | -0.282446205 | 0.19115951 |
| 13901 | 0.527716361 | -1.81E-09 | 609.0189532 | -2.797688614 | 0.289125426 |
| 13928 | 0.098598573 | -1.13E-10 | 789.5386756 | -1.081804804 | 0.091103731 |
| 14198 | 0.127503325 | -8.96E-08 | 2673.594301 | 3.293437502 | 0.277548051 |
| 14277 | -0.039551558 | 1.28E-09 | 3634.498397 | 0.731181045 | 0.165586702 |
| 14526 | 0.346440752 | -2.52E-07 | 516.7614622 | -0.469886463 | 0.245751034 |
| 14541 | 0.149961323 | 7.99E-11 | 472.3228925 | -0.828457906 | 0.096193622 |
| 14702 | 0.398320272 | -1.32E-08 | 3259.647727 | 2.462295251 | 0.201063715 |
| 14816 | -0.160330667 | -5.66E-08 | 2702.302426 | 6.769448085 | 0.266273781 |
| 15203 | 0.193731564 | -2.98E-06 | 1066.706498 | -0.537209085 | 0.239583544 |
| 15721 | 0.254582768 | -2.88E-08 | 1593.003997 | -0.197730284 | 0.16365365 |
| 16126 | -0.023512523 | 1.42E-07 | -2646.523926 | 0.126742194 | 0.152118932 |

| | | | | | |
|-------|-------------|-----------|-------------|-------------|-------------|
| 16600 | 0.133758972 | -1.15E-08 | 1973.197211 | 0.168384811 | 0.123481653 |
|-------|-------------|-----------|-------------|-------------|-------------|

Fama-Macbeth coefficients (Lambda's) :

$\lambda_{\text{marketcap}} = 7.898767\text{e}+03$
 $\lambda_{\text{(price-normalized-earnings)}} = -1.429522\text{e}-06$
 $\lambda_{\text{(earning-price-ratio)}} = 1.515075\text{e}-03$
 $\lambda_{\text{(price-inverse)}} = 3.316640\text{e}-01$

Computer Code

```
## Loading required libraries

if (!require("data.table")) install.packages("data.table")
if (!require("xts")) install.packages("xts")
if (!require("ggplot2")) install.packages("ggplot2")
if (!require("plyr")) install.packages("plyr")

setwd("D:/MFE/Curriculum/Winter 2018/404-Corporate Finance and Risk Management - WELCH/Homework/HW7")

#Data collection (1980 to 2016) and cleaning

stocks <- fread("./stock_daily.CSV", header = TRUE)
stocks$date <- as.Date(as.character(stocks$date), "%Y%m%d")
stocks$RET <- as.numeric(as.character(stocks$RET))
stocks[is.na(stocks)] = 0
ticker <- data.table(PERMNO=stocks$PERMNO, TICKER=stocks$TICKER, key="PERMNO")
ticker = unique(ticker[!ticker$TICKER==""])
stocks$grossRet <- stocks$RET+1
stocks[, grossRet := lapply(.SD, prod), by=list(stocks$PERMNO, year(stocks$date)), .SDcols=c("grossRet")]
yearend <- stocks[, .(max(date)), by=year(stocks$date)]
colnames(yearend) <- c("year", "date")
stocks <- stocks[date %in% yearend$date]
stocks$AnnualRet = stocks$grossRet-1
stocks$year = year(stocks$date)
stocks$TICKER=ticker$TICKER[match(stocks$PERMNO, ticker$PERMNO)]

fundamental <- fread("./Fundamental_Annual.CSV", header = TRUE)
colnames(fundamental)[2] = "PERMNO"
colnames(fundamental)[20] = "Price"
mastertable <- merge(fundamental, stocks, by=c("fyear", "PERMNO"))
mastertable$EPRatio <- mastertable$epsfx/mastertable$Price
mastertable$price_norm_accrual <- mastertable[, .(price_norm_accrual = (ap-rect+txp+xacc)/(Price*SHROUT))]
mastertable <- mastertable[, .(fyear, PERMNO, AnnualRet, MarketCap = SHROUT*Price, price_norm_accrual, EPRatio, Price)]
mastertable <- mastertable[complete.cases(mastertable)]
YearData <- mastertable[, .(Count = .N), by = "PERMNO"]
YearData <- YearData[YearData$Count==37] #complete 37 year data (1980 to 2016)
mastertable <- mastertable[mastertable$PERMNO %in% YearData$PERMNO]

## regression should be dependent_var_t~independent_var_(t-2). Shifting by 2
setorder(mastertable, PERMNO, fyear)

cols = c("MarketCap", "price_norm_accrual", "EPRatio", "Price")
anscols = paste("lag", cols, sep="_")
mastertable[, (anscols) := shift(.SD, 2, NA, "lag"), .SDcol=cols, by=PERMNO]
mastertable <- mastertable[complete.cases(mastertable)]

#to find beta
regression <- mastertable[,
{
  summary <- summary(lm(AnnualRet ~ lag_MarketCap + lag_price_norm_accrual + lag_EPRatio + 1/lag_Price))
  out <- data.table(
    alpha=summary$coefficients[1],
    beta1=summary$coefficients[2],
    beta2=summary$coefficients[3],
    beta3=summary$coefficients[4],
    beta4=summary$coefficients[5]
  )
  out
},
by=PERMNO]

## Fama MacBeth
YearlyLambda <- mastertable[, {
  summary <- summary(lm(AnnualRet~regression$beta1+regression$beta2+regression$beta3+regression$beta4))
  out <- data.table(
    lambda0=summary$coefficients[1],
    lambda1=summary$coefficients[2],
    lambda2=summary$coefficients[3],
    lambda3=summary$coefficients[4],
    lambda4=summary$coefficients[5])
  out
}, by=fyear]
```

```
FamaMLambda <- colMeans(YearlyLambda[, -1])
```

References

- [Wharton Research Data Services \(WRDS\)](#) CRSP data taken on Mar 09, 2018.