

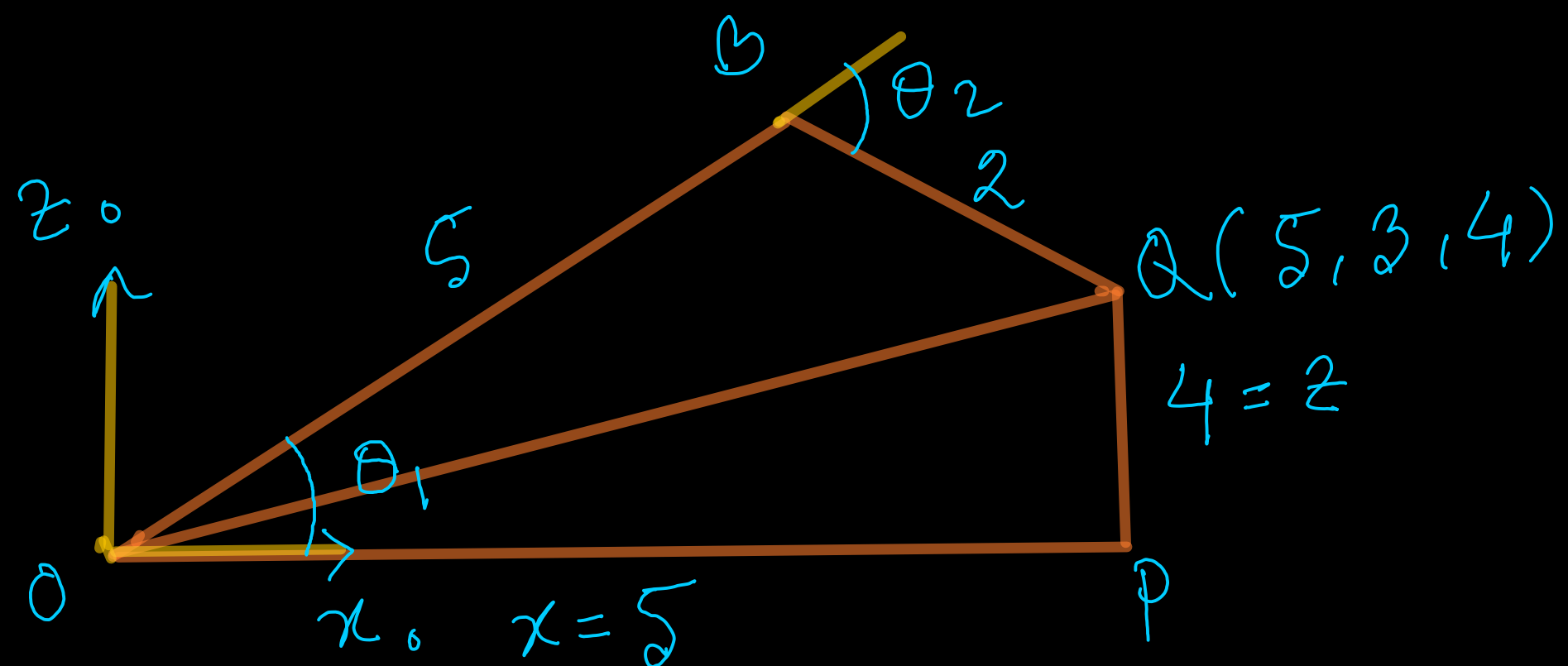
Given that, position of end effector  $(x, y, z) = (5, 3, 4)$

length of arm 1 (OB) = 5 cm

" " arm 2 (BQ) = 2 cm

we need to calculate joint angles  $\theta_0 = ?$ ,  $\theta_1 = ?$ ,  $\theta_2 = ?$

lets redraw the structure,



$$\begin{aligned} \therefore \Delta OQP &\rightarrow OQ^2 = OP^2 + PQ^2 \\ \therefore OQ &= \sqrt{OP^2 + PQ^2} \\ &= \sqrt{5^2 + 4^2} \\ &= \sqrt{25 + 16} \\ &= \sqrt{41} \end{aligned}$$



Now, from  $\triangle OBQ$ ,

according to cosine rule,

$$\begin{aligned}\cos \angle OBQ &= \frac{5^2 + 2^2 - (\sqrt{41})^2}{2 \cdot 5 \cdot 2} \\ &= \frac{25 + 4 - 41}{20} \\ &= \frac{-12}{20} = -0.6 \\ \therefore \angle OBQ &= \cos^{-1}(-0.6) \\ &= 126.87^\circ\end{aligned}$$

$$\begin{aligned}\therefore \theta_2 &= 180^\circ - \angle OBQ = 180^\circ - 126.87^\circ \\ &= 53.13^\circ\end{aligned}$$

Again, from  $\triangle OBQ$

according to cosine rule,

$$\begin{aligned}\cos \angle BOQ &= \frac{5^2 + (\sqrt{41})^2 - 2^2}{2 \cdot 5 \cdot \sqrt{41}} \\ &= \frac{25 + 41 - 4}{10 \cdot \sqrt{41}} = 0.968\end{aligned}$$

$$\therefore \angle BOQ = \cos^{-1}(0.968) = 14.53^\circ$$

And again from  $\triangle OQP$ ,

$$\begin{aligned}\therefore \tan \angle QOP &= \frac{PQ}{OP} \\ &= \frac{4}{5} \\ \therefore \angle QOP &= \tan^{-1}\left(\frac{4}{5}\right) \\ &= 38.66^\circ\end{aligned}$$

$$\begin{aligned}\therefore \theta_1 &= \angle QOP + \angle BOQ = 38.66 + 14.33 \\ &= 52.99^\circ\end{aligned}$$

Lastly, from the figure,

we can see,

$$\tan \theta_0 = \frac{y}{x}$$

$$\therefore \theta_0 = \tan^{-1}\left(\frac{y}{x}\right) = \tan^{-1}\left(\frac{3}{5}\right)$$

$$\therefore \theta_0 = 30.96^\circ$$

