

# Answers to exercises in How To Prove It

Son To  
<[son.trung.to@gmail.com](mailto:son.trung.to@gmail.com)>

*StaffPoint Oy*

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This is to answer all the questions in the books ‘How to prove it’ by Velleman. Comments are appreciated!

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## 1 Introduction

Exercise 1.1. (a)  $a = 3$ ,  $b = 5 \Rightarrow x = 2^5 - 1 = 31$ ,  $y = 1 + 2^5 + 2^{10} = 1057$

(b) Since 32,767 is not a prime,  $2^{32,767} - 1$  is not a prime either. Therefore, there exists a positive integer  $0 < x < 2^{32,767} - 1$  such that  $2^{32,767} - 1$  is divisible by  $x$ . Hence, by (a),  $x = 2^{31} - 1$  satisfies this.

Exercise 1.2.

$n$	$3^n - 1$	$3^n - 2^n$
2	8, not prime	5, prime

## 2 Chapter 1

Exercise 2.1. OK MAN