

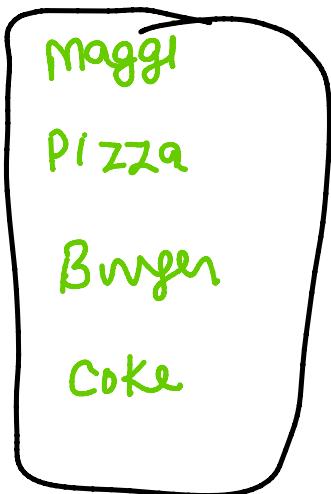
## Hashmap

25 September 2022 13:07

store key value pair.

unique

food item  
<String>,



price  
<Int>

40

100

60

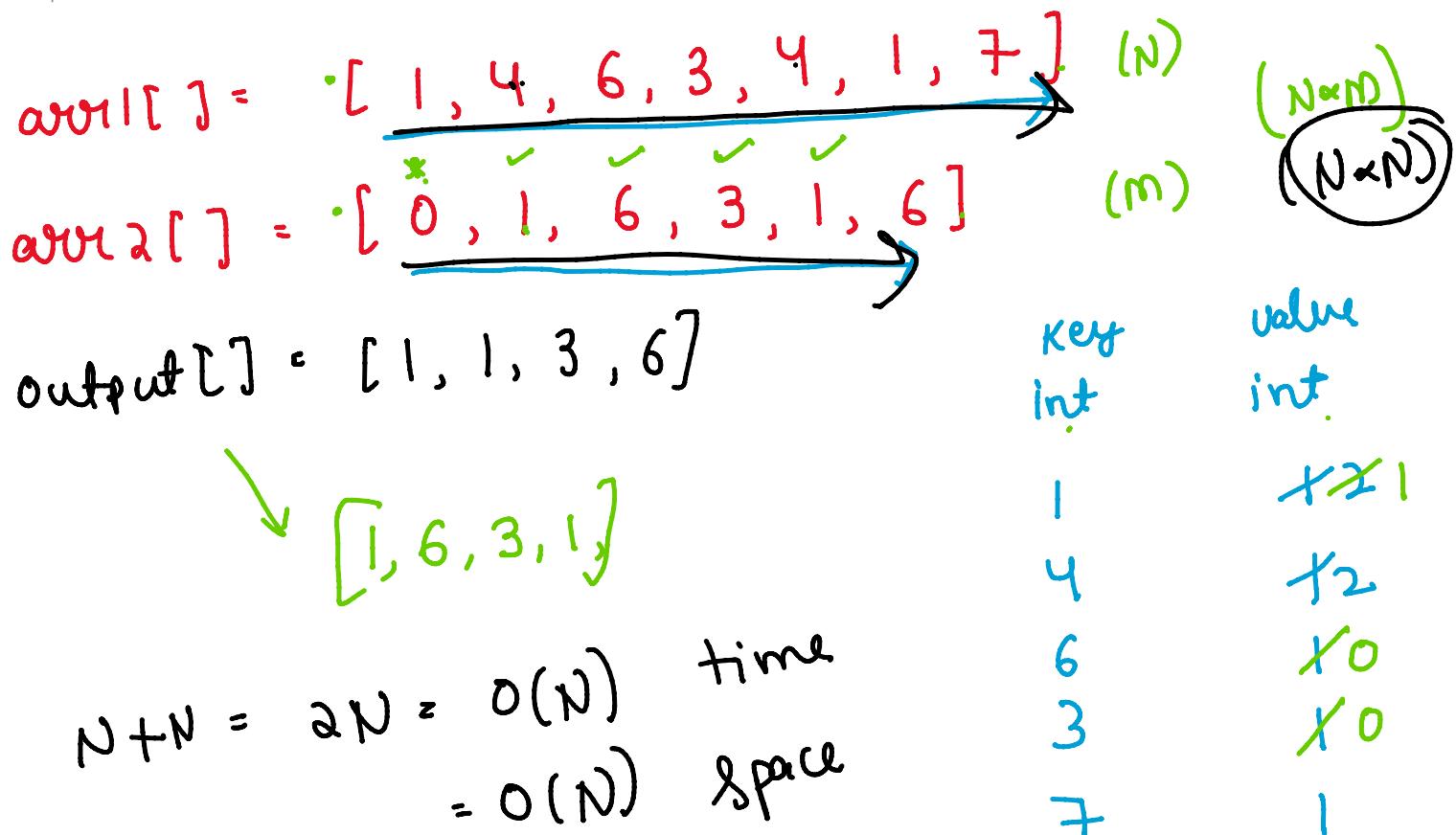
40

Roll no.	Name
<u>&lt;Int&gt;</u>	<u>&lt;String&gt;</u>
1	Rahul
2	Sangav
5	Manish
10	

O(1)

## Intersection of two arrays

25 September 2022 13:15



[2, 3, 3, 4, 5, 5] sorted.

output [2, 4]

## First non repeating character

25 September 2022 13:37

0 1 2 3 4 5 6 7 8 9

leet~~c~~ode~~l~~t

$O(N^2)$

output = 4

$O(N)$

~~$O(N)$~~

$O(1)$

26

map  
pair  
int

char

\* 2

\* 2 3

\* 2

l

e

t

c

o

d

X [Java → linked hashmap]



ordered



alphabetical

unordered



random

$O(1)$

$O(\log N)$

## Subarray with sum 0

25 September 2022 13:55

1, 2, 5, 2, 3, 1

set  
unique elements  
set int  
1, 2, 5, 3

3 -2 [5 1 4 -7 -3] 8 true

-3 -2 6 1 7 -1 false

5 -4 8 [3 2 -5] 4 true  
 Prefix sum: 5 1 9 12 14 9 =

using set.  
 $O(N)$   
 $O(N)$

5, 1, 9,  
12, 14

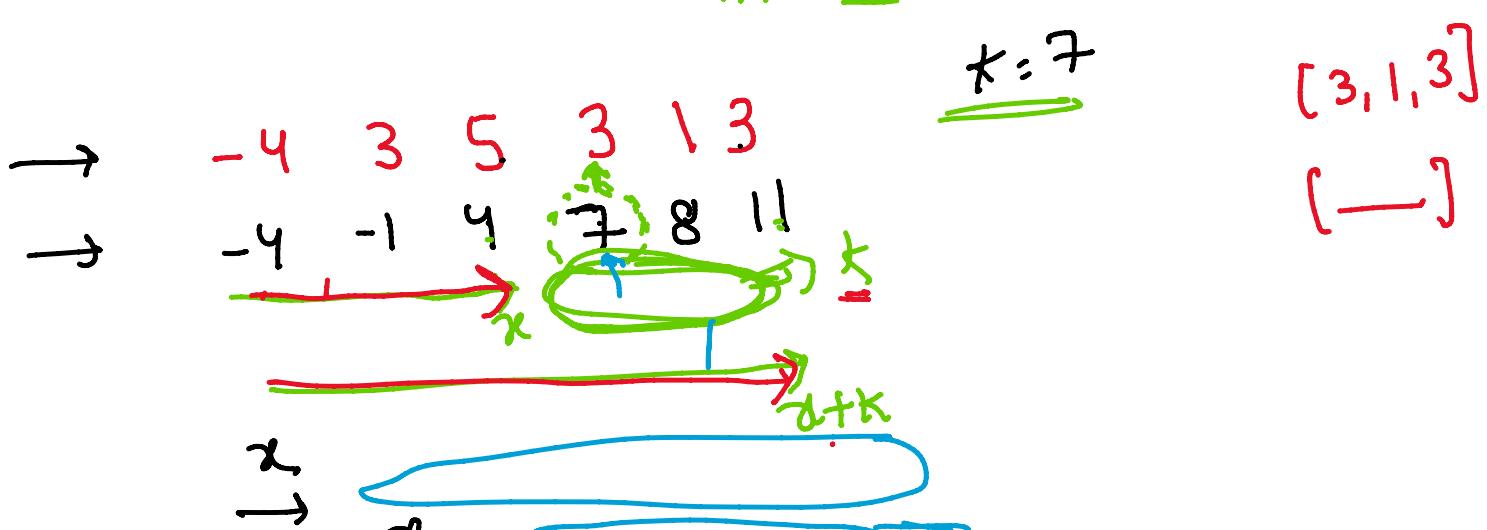
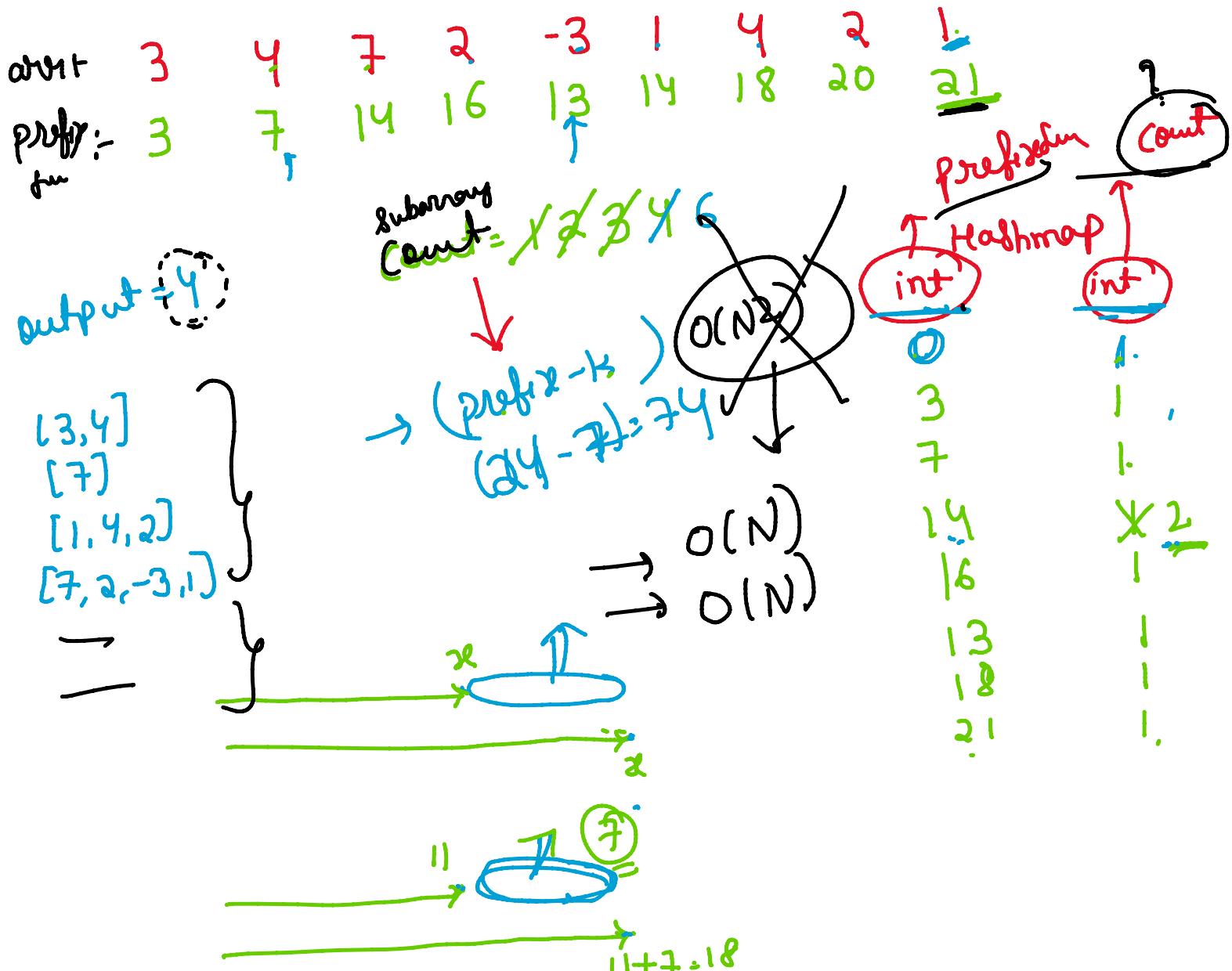
3 4 -2 [8 3 -11]  
 → 3 7 5 13 16 5  
 $O(N^2)$

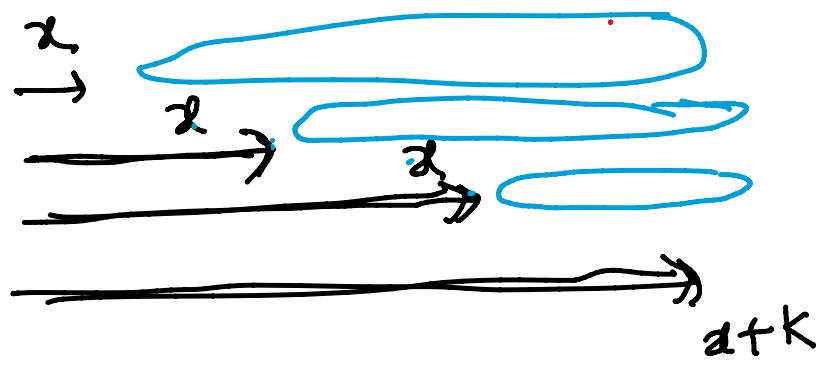
arr 3 4 - 7 8  
prefix 3 7 0 8  
arr

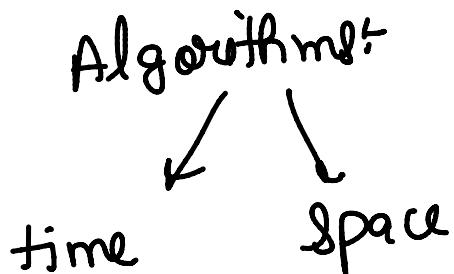
## Subarray sum equals k

25 September 2022 14:14

K = 7







→ decrease time.

$$O(N^2), O(1)$$

$\downarrow$

$O(N)$        $O(N)$

$$3n^2 + 2n \rightarrow O(N^2)$$

$$\frac{n}{5} + \log N \rightarrow O(N)$$

$O(1)$ ,  $O(\log n)$ ,  $O(n)$ ,  $O(n \log n)$ ,  $O(n^2)$ ,  $O(n^3)$ , -

$O(2^n)$ ,  $O(n!)$

$$2n + 100 \log N \rightarrow O(n)$$

→ Bubble sort

→ Binary search

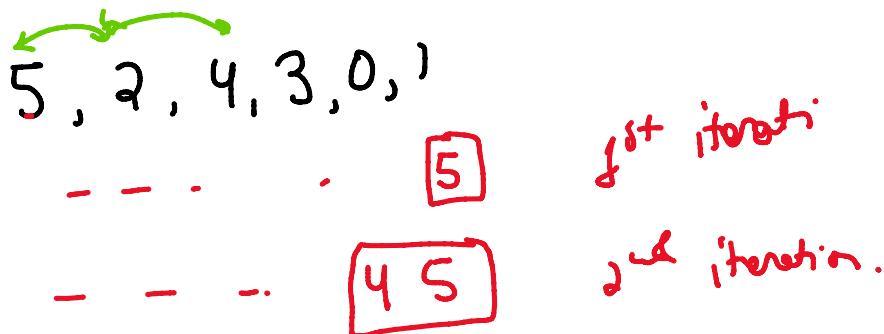
→ Recursive



- Recusive
- Merge sort

J

Bubble Sort  $O(N^2)$



$$N-1 + N-2 + N-3 + N-4 + \dots + 1$$

↓  
1 + 2 + 3 + 4 + \dots + (N-1)

$$\frac{N(N-1)}{2} \times k$$

$$\frac{N^2}{2}k - \frac{N}{2}k \Rightarrow O(N^2)$$

Recurrence

$$T(n) = k \cdot n + T(n-1)$$

$$T(n-1) = k(n-1) + T(n-2)$$

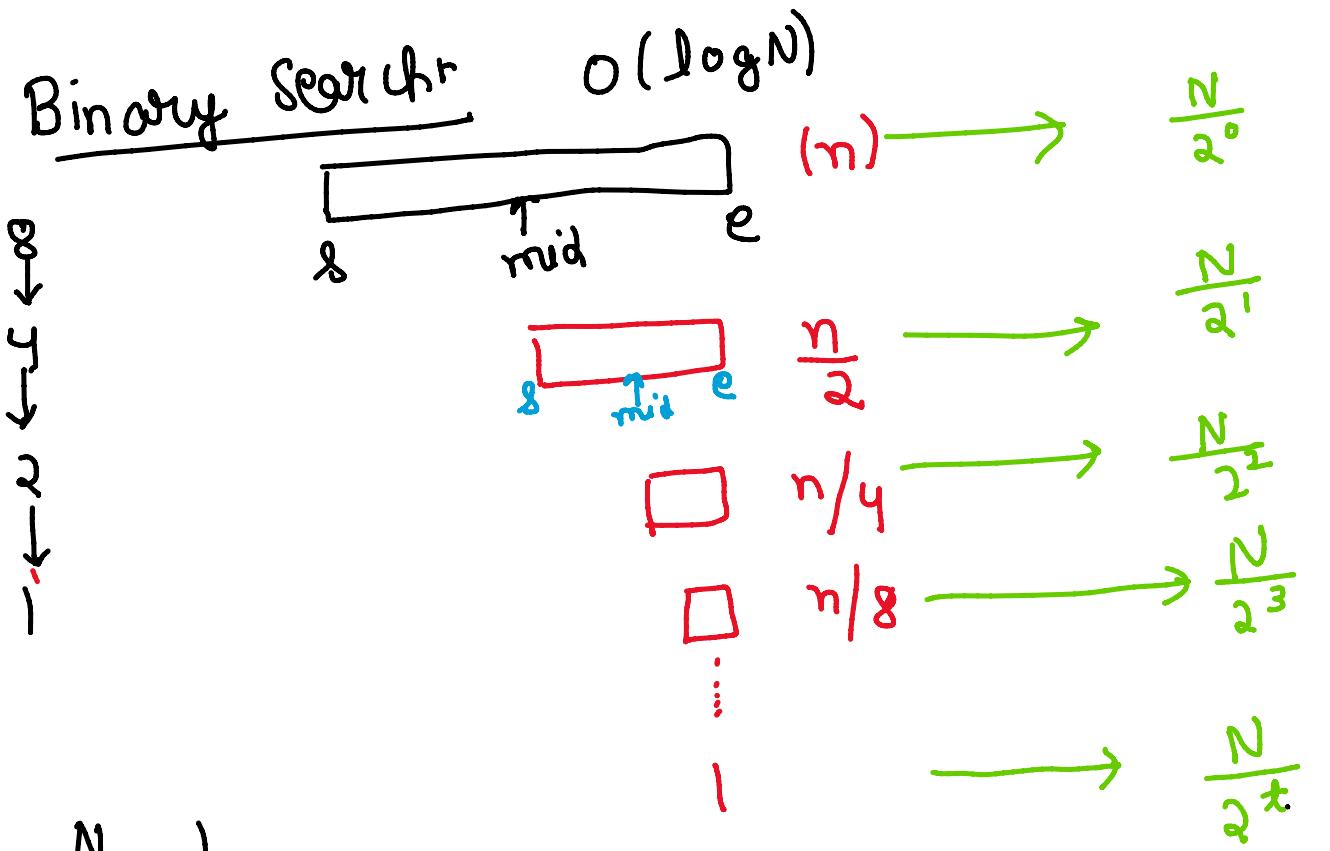
$$T(n-2) = k(n-2) + T(n-3)$$

⋮

$$T(1) = k(1) + 0$$

$$\underline{+ (n-1) + (n-2) + \dots + 1}$$

$$\begin{aligned}
 T(n) &= k(n + (n-1) + (n-2) + \dots + 1) \\
 &= k \frac{(n)(n-1)}{2} \\
 &= O(N^2)
 \end{aligned}$$



$$\frac{N}{2^t} = 1$$

$$N = 2^t$$

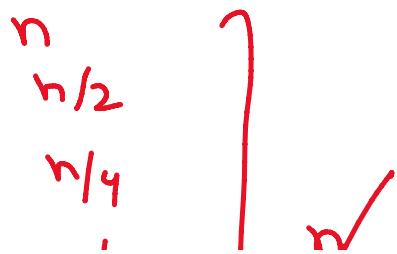
$$\log_2 N = \log_2 2^t$$

$O(\log N)$

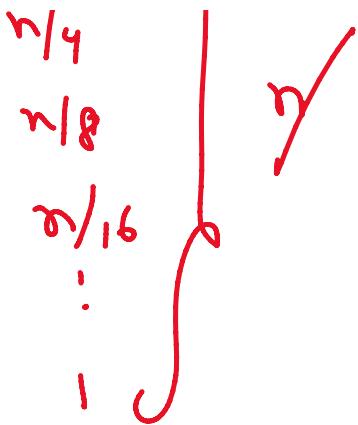
$$\log_2 N = t$$

Recurrence

$$T(n) = k + T\left(\frac{n}{2}\right) + T\left(\frac{n}{4}\right)$$



$$\begin{aligned}
 T(n) &= k + \cancel{T(\dots)} \\
 \cancel{T(n/2)} &= k + \cancel{T(n/4)} \\
 \cancel{T(n/4)} &= k + \cancel{T(n/8)} \\
 \vdots & \\
 \cancel{\vdots} &= k + 0
 \end{aligned}$$

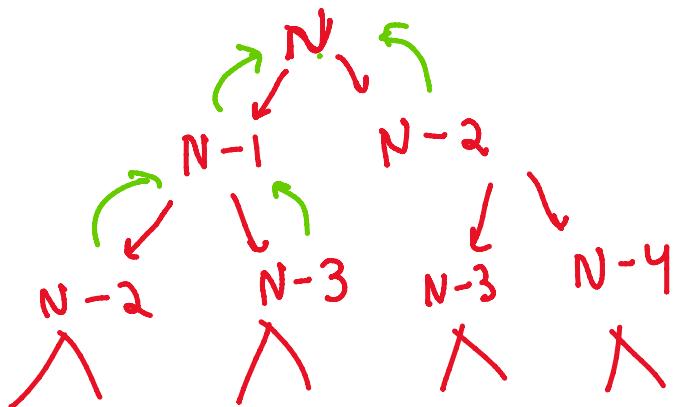


$$\begin{aligned}
 T(n) &= \sum_{i=0}^{\log n} k = \log n \cdot k \\
 &= O(\log N)
 \end{aligned}$$

Fibonacci Series

$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$

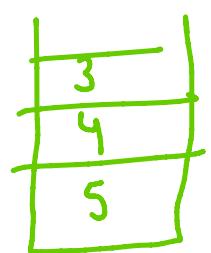
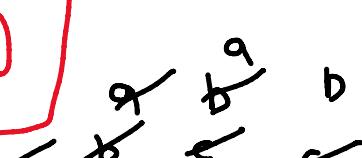
$$0 \ 1 \ 1 \ 2 \ 3 \ 5 \ 8 \ \dots$$



$$\begin{array}{c}
 2^0 \\
 2^1 \\
 2^2 \\
 2^3 \\
 \vdots \\
 2^{N-1}
 \end{array}$$

$$k(1 + 2 + 4 + 8 + \dots + 2^{N-1})$$

$$k \frac{(2^N - 1)}{2 - 1} = \boxed{O(2^N)}$$



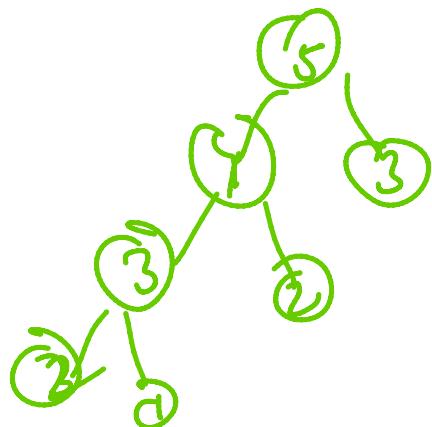
$$K \frac{19}{2-1} = \boxed{U(a)} \quad \begin{matrix} a & b & c & d \\ \swarrow & \searrow & \leftarrow & \leftarrow \end{matrix}$$

3 approaches:

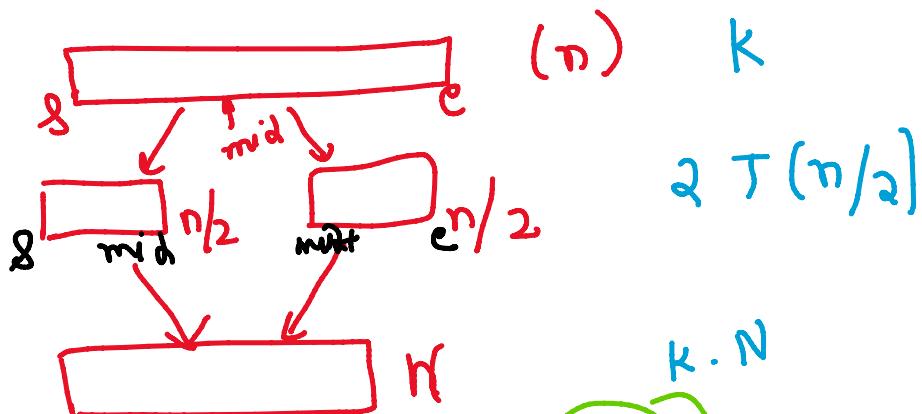
1. 3 variables.
2. dp array
3. Recursion

$$\begin{matrix} O(N), O(1) \\ O(N), O(N) \\ O(2^N), O(N) \end{matrix}$$

$$dp[i] = dp[i-1] + dp[i-2]$$



merge sort  $O(N \log N)$



$$T(n) = K + 2T(n/2) + \boxed{k \cdot N}$$

~~$$T(n) = \cancel{NK'} + 2T(n/2)$$~~

~~$$2T(n/2) = \cancel{\frac{N}{2} K'} + \cancel{4T(n/4)}$$~~

~~$$\dots = \cancel{n \cdot N' + 8T(n/8)}$$~~

$$\cancel{4T(n/4)} = \cancel{N} \cancel{k'} + \cancel{8T(n/8)}$$

$$T(1) = k' + 0$$

$$T(n) = \sum_{j=1}^{\log n} NK$$

$$= N \log N K. = O(N \log N)$$

## Two Sum

25 September 2022 15:53

