ITS202: Algorithms and Data Structure Graphs

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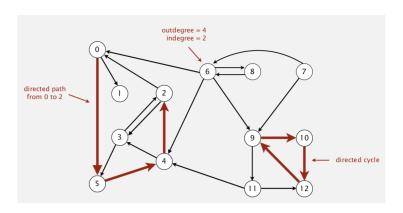
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Graphs: Digraph

Directed Graph

Digraph. Set of vertices connected pairwise by directed edges.



Graphs: Digraph Application: Road Network

digraph	vertex	directed edge
transportation	street intersection	one-way street
web	web page	hyperlink
food web	species	predator-prey relationship
WordNet	synset	hypernym
scheduling	task	precedence constraint
financial	bank	transaction
cell phone	person	placed call
infectious disease	person	infection
game	board position	legal move
citation	journal article	citation
object graph	object	pointer
inheritance hierarchy	class	inherits from
control flow	code block	jump

Graphs: Some digraph problems

problem	description
s→t path	Is there a path from s to t?
shortest s→t path	What is the shortest path from s to t?
directed cycle	Is there a directed cycle in the graph?

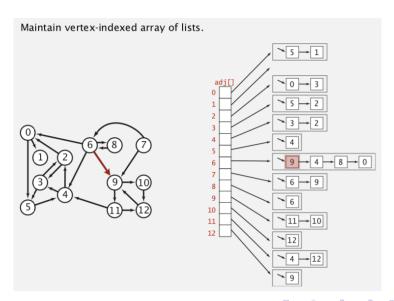
Digraph API

Digraph(int V) create an empty digraph with V vertices Digraph(In in) create a digraph from input stream void addEdge(int v, int w) add a directed edge v→w Iterable <integer> adj(int v) vertices pointing from v number of vertices int E() number of edges Digraph reverse() reverse of this digraph</integer>	public class	Digraph	
void addEdge(int v, int w) add a directed edge v→w Iterable <integer> adj(int v) vertices pointing from v int V() number of vertices int E() number of edges</integer>		Digraph(int V)	create an empty digraph with V vertices
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int E() number of edges	Iterable <integer></integer>	adj(int v)	vertices pointing from v
	int	VO	number of vertices
Digraph reverse() reverse of this digraph	int	E()	number of edges
	Digraph	reverse()	reverse of this digraph
String toString() string representation	String	toString()	string representation

Digraph API

```
% java Digraph tinyDG.txt
 tinyDG.txt
                                             0 -> 5
                                             0 -> 1
                                             2->0
                                             2->3
                                             3->5
      0
   0 1 2 0
                                             3->2
                                             4->3
   11 12
                                             4->2
  12 9
    9 10
                                             5->4
    9 11
    7 9
  10 12
                                             11 -> 4
  11 4
                                            11 -> 12
                                            12->9
In in = new In(args[0]);
                                                     read digraph from
Digraph G = new Digraph(in);
                                                       input stream
for (int v = 0; v < G.V(); v++)
                                                      print out each
    for (int w : G.adj(v))
                                                       edge (once)
       StdOut.println(v + "->" + w);
```

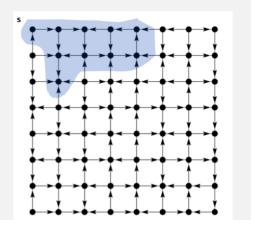
Digraph representation: adjacency lists



Digraph Search

Reachability

Problem. Find all vertices reachable from *s* along a directed path.



Digraph Search: Depth-first search

Same method as for undirected graphs.

- Every undirected graph is a digraph (with edges in both directions).
- DFS is a digraph algorithm.

DFS (to visit a vertex v)

Mark v as visited.

Recursively visit all unmarked

vertices w pointing from v.

Digraph Search: Depth-first search

4→2 To visit a vertex v: $2\rightarrow3$ Mark vertex v as visited. 3→2 • Recursively visit all unmarked vertices pointing from v. 6→0 $0 \rightarrow 1$ 2→0 11→12 12→9 9→10 9→11 8→9 10→12 $11\rightarrow4$ 4→3 3→5

a directed graph

7→6

Digraph Search: Depth-first search

reachable from 0

To visit a vertex v: Mark vertex v as visited. • Recursively visit all unmarked vertices pointing from v. marked[] edgeTo[] reachable from vertex 0

Digraph Search: Breadth-first search

Same method as for undirected graphs.

- Every undirected graph is a digraph (with edges in both directions).
- BFS is a digraph algorithm.

BFS (from source vertex s)

Put s onto a FIFO queue, and mark s as visited. Repeat until the queue is empty:

- remove the least recently added vertex v
- for each unmarked vertex pointing from v: add to queue and mark as visited.

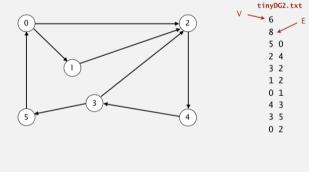
Digraph Search: Breadth-first search

Repeat until queue is empty:

graph G



- Remove vertex v from queue.
- Add to queue all unmarked vertices pointing from v and mark them.

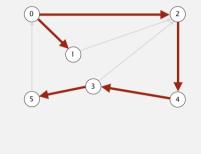


Digraph Search: Breadth-first search

Repeat until queue is empty:

done

- Remove vertex v from queue.
- Add to queue all unmarked vertices pointing from v and mark them.



v	edgeTo[]	distTo[]	
0	-	0	
1	0	1	
2	0	1	
3	4	3	
4	2	2	
5	3	4	