

POORNIMA

COLLEGE OF ENGINEERING

DETAILED LECTURE NOTES

Unit-5

Convolutional Code

Convolutional Code generate encoded sequence for input sequence on bit by bit basis. for successive input bits output bits are generated.

It works on the input bit rather than block of input sequence.

A convolutional coding is done by combining the fixed number of input bits. The input bit stored in the fixed length register (shift register) and then combined with the help of mod 2 adders. The operation is equivalent to binary convolution and hence it is called convolutional coding.

Code Rate

$$r = \frac{k}{n}$$

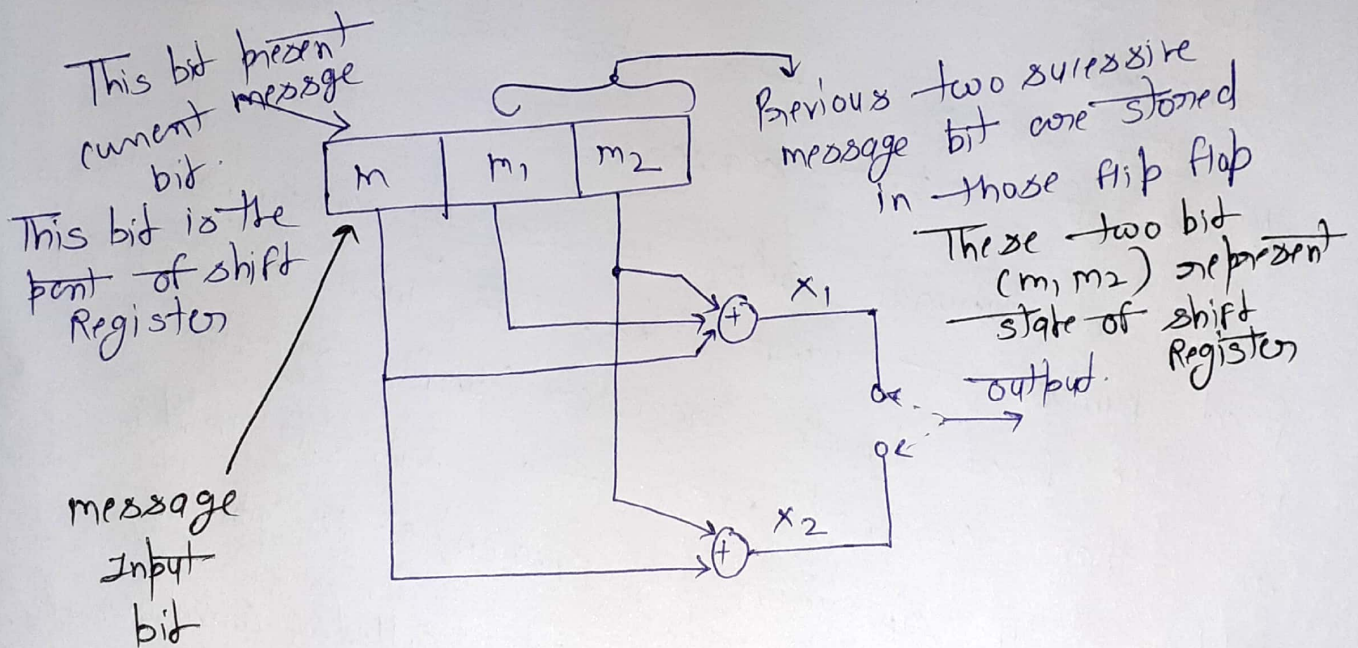
small k
number of
message bit

Constraint length (k)

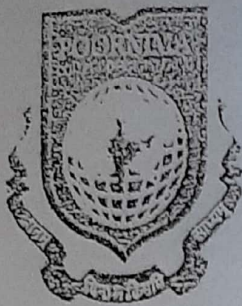
It is defined as the number of shift over which a single message bit can influence the encoder output. It is expressed in terms of message bit.

Dimension of code

It is given by (n, k) . k is the number of message bit taken at the particular time by the encoder, n is the encoded output bit for one message bit.

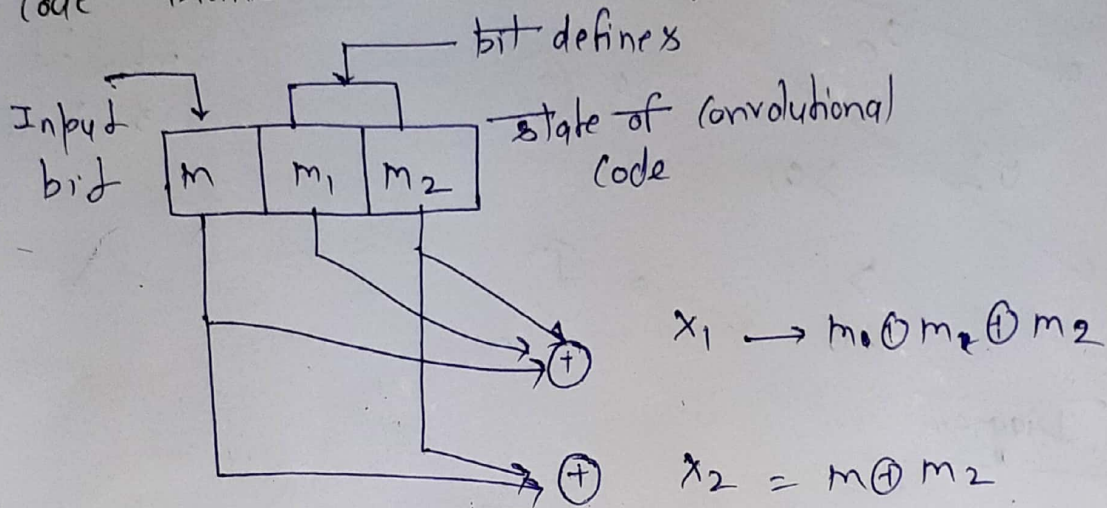


Convolutional Encoder with $k=3$, $k=1$ and $n=2$



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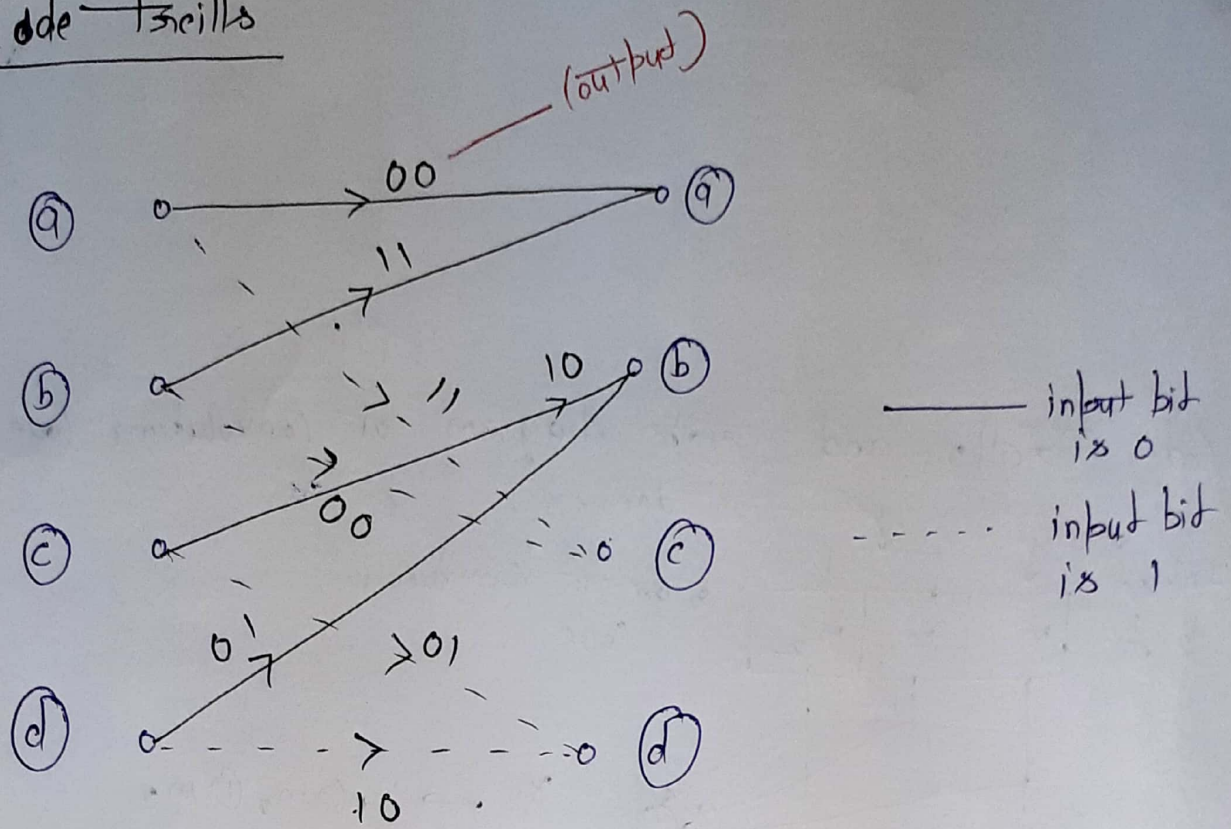
Code Trellis and state diagram of Convolutional code



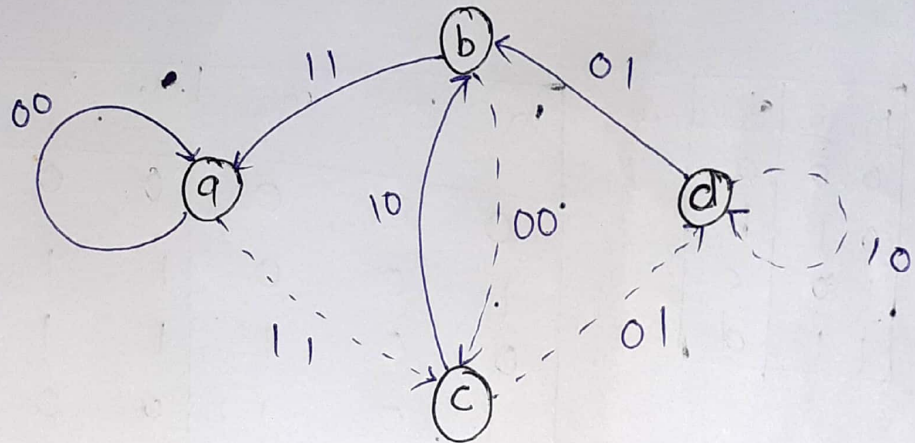
m_1	m_2	state
0	0	a
0	1	b
1	0	c
1	1	d

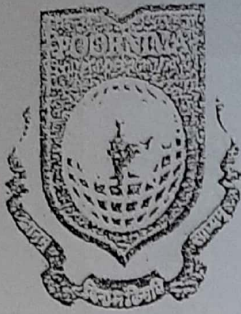
m	m_1	m_2	x_1	x_2	Parent state	Next state
0	0	0	0	0	a	a
1	0	0	1	1	a	c
0	0	1	1	1	b	a
1	0	1	0	0	b	c
0	1	0	1	0	c	b
1	1	0	0	1	c	d
0	1	1	0	1	d	b
1	1	1	1	0	d	d

Code - 13cills



State Diagram.





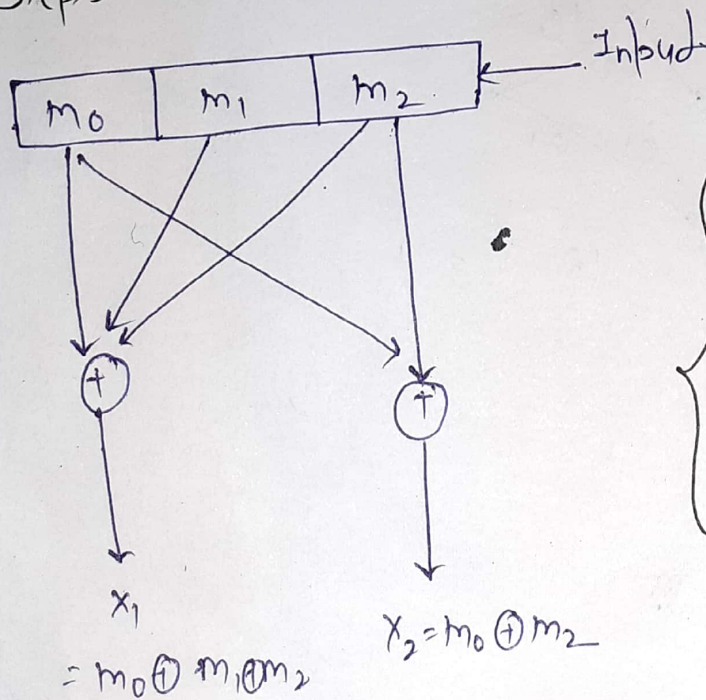
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Viterbi Algorithm. (Maximum Likelihood Decoding)

It is the method for decoding convolution codes.
We use trellis decoder to decode the received data.

Objective: To find the best path through the trellis that is closest using the trellis diagram.

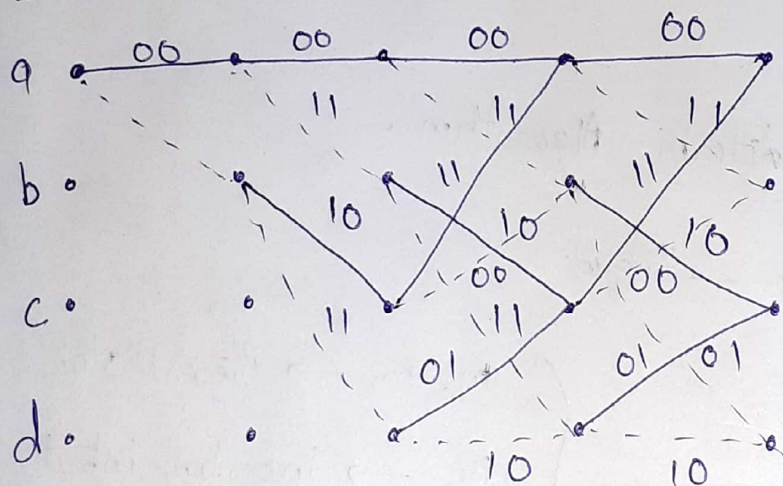
Steps of trellis Viterbi Algorithm.



$m_0 m_1 \rightarrow$ Present state
 $m_2 \rightarrow$ Inserting input
 $m_0 m_1 \rightarrow$ Present state
 $m_1 m_2 \rightarrow$ next state.

m_0	m_1	m_2	x_1	x_2	p_s	M_s
0	0	0	0	0	a	a
0	0	1	1	1	a	b
0	1	0	1	0	b	c
0	1	1	0	1	b	d
1	0	0	1	1	c	a
1	0	1	0	0	c	b
1	1	0	0	1	d	c
1	1	1	1	0	d	d

Truth Diagram



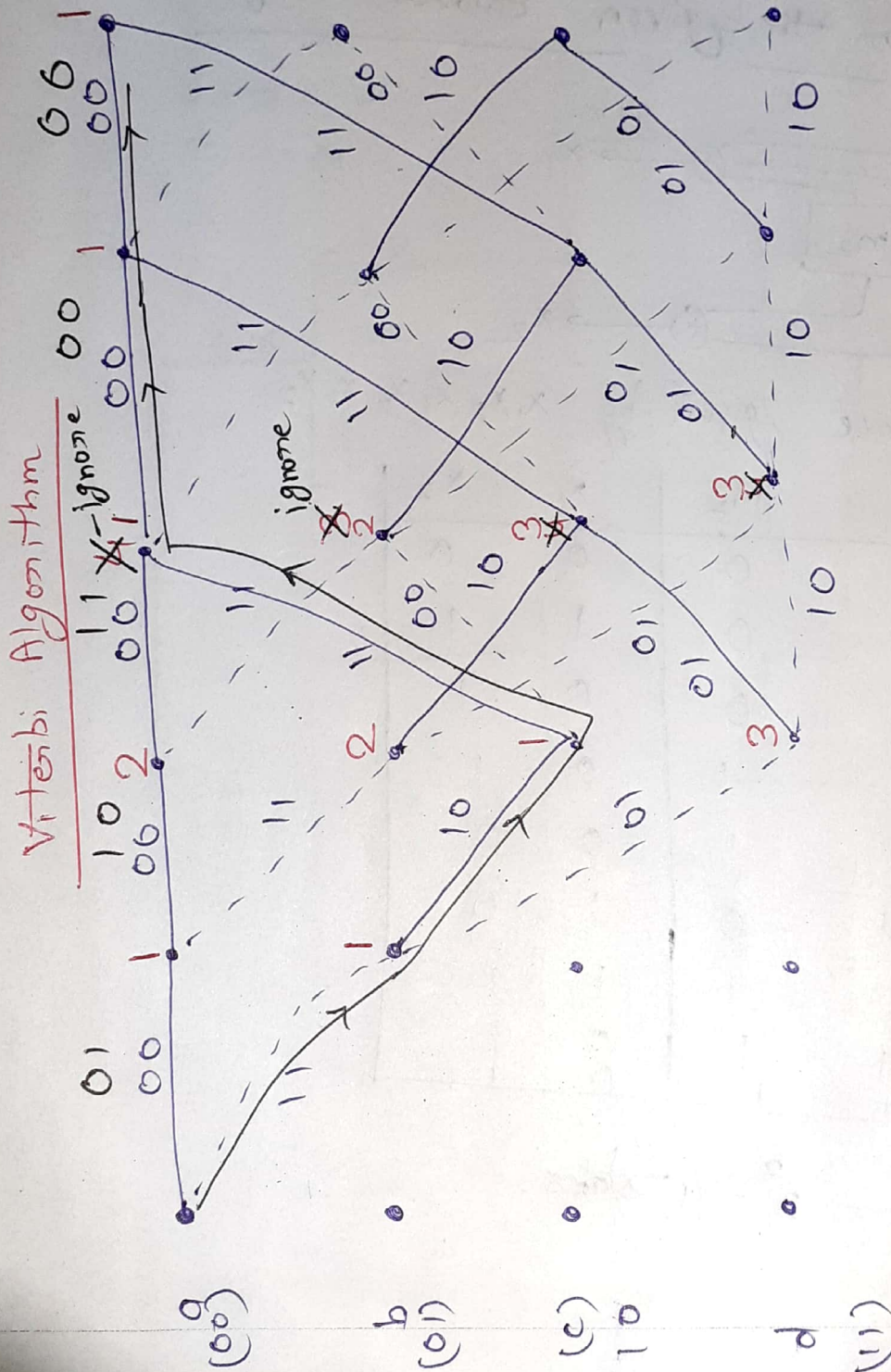


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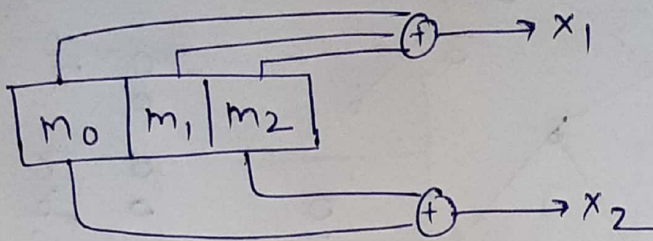


Decoded data sequence of the Viterbi Algorithm by computed Hamming distance = 1

→ 11 10 11 00 00

So there error is the one bit during decoding by the Viterbi Algorithm.

Code Tree for the given encoder Design



Encoded sequence given by $x_1 x_2 x_1 x_2 x_1 x_2$

m_0	m_1	m_2	x_1	x_2
0	0	0	0	0
1	0	0	1	1
1	1	0	0	1
0	1	1	0	1
1	0	1	0	0
0	1	0	1	0
0	0	1	1	1
0	1	1	0	1

$$2^{N-1} = 2^{3-1} = 2^2 = 4 \text{ states}$$



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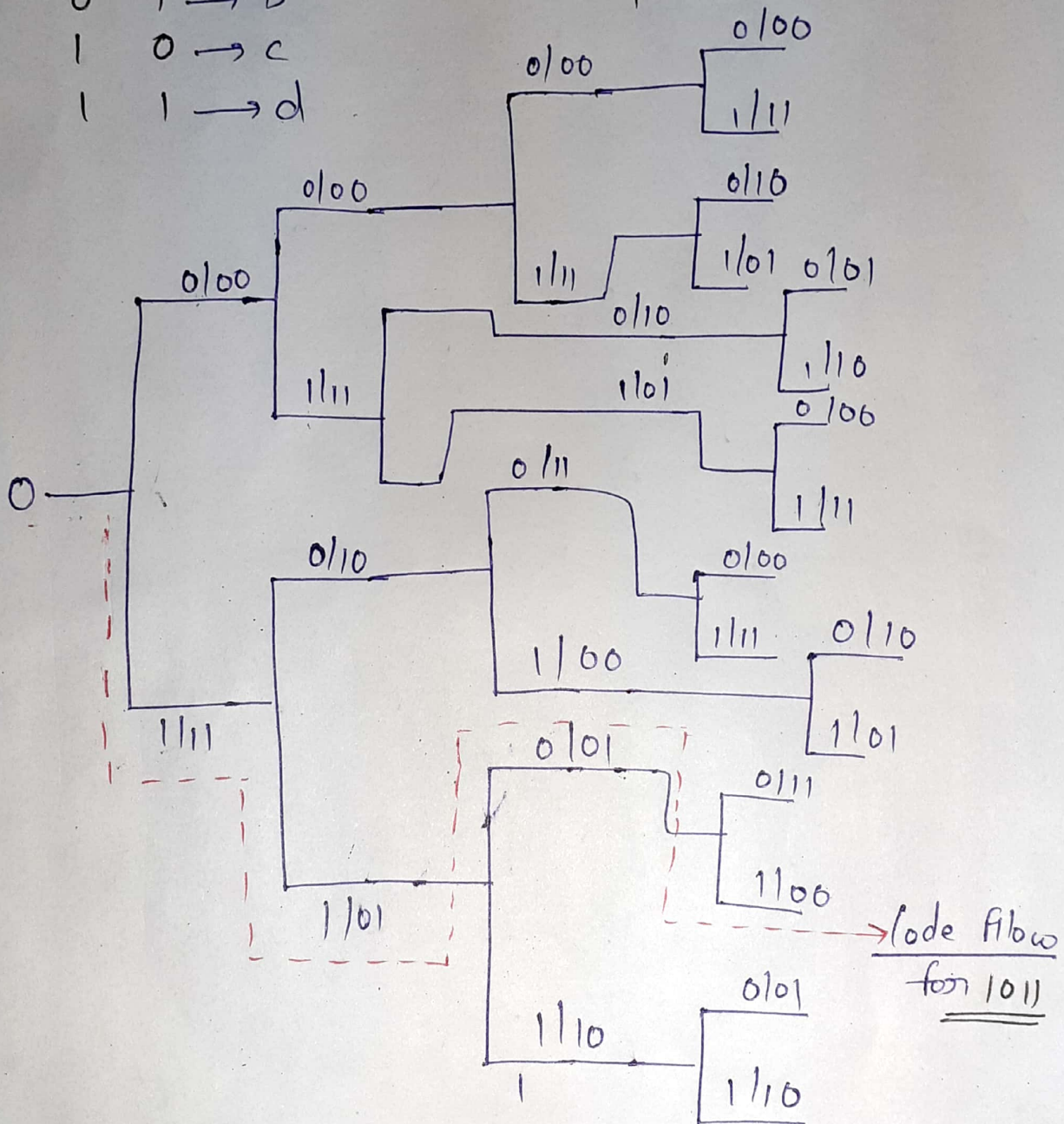
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m_2 m_1
 0 0 \rightarrow a
 0 1 \rightarrow b
 1 0 \rightarrow c
 1 1 \rightarrow d

0 input \rightarrow more upside

1 input \rightarrow more downside



Code tree for Convolution Encoder.