



# POORNIMA

## COLLEGE OF ENGINEERING

### DETAILED LECTURE NOTES

①

#### Binary Arithmetic

| Bits |   | sum carry |   | Difference borrow |   | Product a.b |
|------|---|-----------|---|-------------------|---|-------------|
| a    | b | a+b       |   | a-b               |   |             |
| 0    | 0 | 0         | 0 | 0                 | 0 | 0           |
| 0    | 1 | 1         | 0 | 1                 | 1 | 0           |
| 1    | 0 | 1         | 0 | 1                 | 0 | 0           |
| 1    | 1 | 1         | 1 | 0                 | 0 | 1           |

#### Arithmetic Operation

##### (i) Binary Addition

Two binary no can be added in the same way as two decimal number one added. The carry is taken out from least to high significant bit.

##### Addition

$$\begin{aligned}
 0 + 0 &= 0 \\
 0 + 1 &= 1 \\
 1 + 0 &= 1 \\
 1 + 1 &= 10
 \end{aligned}$$

##### Example

$$1010 + 1111 = 1111$$

##### (ii) Binary Subtraction

It done as the same way of the decimal number. It started from the LSB and proceed to the MSB.

| MSB | LSB | Decimal |
|-----|-----|---------|
| 1   | 1   | 13      |
| 1   | 0   | 9       |
| 0   | 1   | 4       |
| 0   | 0   |         |

## Special Case Example

$$\begin{array}{r}
 \phantom{0}1\phantom{0}0\phantom{1} \\
 \phantom{0}1\phantom{0}0\phantom{1} \\
 0\phantom{0}1\phantom{0}1\phantom{0} \\
 \hline
 0010
 \end{array}$$

$$\begin{array}{r}
 \text{Decimal} \\
 9 \\
 7 \\
 \hline
 2
 \end{array}$$

→ In the second column it is not possible to subtract the 1 from 0. So, 1 has to be borrowed from the next msb. So the borrow taken from the 4<sup>th</sup> bit results in 1 and 10 with weight 4 in the 3<sup>rd</sup> column. So the subtraction is performed.  $10 - 1 = 1$

Binary Multiplication: The procedure is the same as the decimal multiplication.

→ In the particular case if bit is 1 the multiplicand is copied as such, and multiplier bit is 0, a 0 is placed at the particular position.

→ When all the terms have been performed the all product should be added.

Example

$$\begin{array}{r}
 \phantom{00}1011 \\
 \phantom{00}1101 \\
 \hline
 \phantom{000}1011 \\
 \phantom{000}0000 \\
 \phantom{000}1011 \\
 \phantom{000}1011 \\
 \hline
 10001111
 \end{array}$$

Example  $1.01 \times 10.1$

$$\begin{array}{r}
 \phantom{00}1.01 \\
 \phantom{00}10.1 \\
 \hline
 \phantom{000}101 \\
 \phantom{000}000 \\
 \phantom{000}101 \\
 \hline
 11.001
 \end{array}$$



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Binary Division Division follows the same process as done for the decimal number.

Example

(i)  $11001 \div 101$

$$\begin{array}{r} 101 \overline{) 11001} \quad (101 \\ \underline{101} \phantom{000} \\ 0101 \phantom{0} \\ \underline{101} \phantom{0} \\ 0000 \end{array}$$

$1000100110 \div 11001$

(ii)  $11001 \overline{) 1000100110} \quad (10110$

$$\begin{array}{r} \phantom{11001} \underline{011001} \phantom{00000} \\ 00100101 \phantom{0000} \\ \phantom{001001} \underline{11001} \phantom{0000} \\ 000011001 \phantom{000} \\ \phantom{000011} \underline{11001} \phantom{000} \\ 000000000 \end{array}$$

So the answer is 10110