

Zhejiang University
Department of Physics

General Physics (H)

Problem Set #11

1. At 20.0°C , an aluminum ring has an inner diameter of $5.000\ 0\ \text{cm}$ and a brass rod has a diameter of $5.050\ 0\ \text{cm}$. (a) To what temperature must the ring be heated so that it will just slip over the rod? (b) To what common temperature must the two be heated so that the ring just slips over the rod? Would this latter process work?
2. In state-of-the-art vacuum systems, pressures as low as $10^{-9}\ \text{Pa}$ are being attained. Calculate the number of molecules in a 1.00-m^3 vessel at this pressure if the temperature is 27°C .
3. At $25.0\ \text{m}$ below the surface of the sea (density = $1\ 025\ \text{kg/m}^3$), where the temperature is 5.00°C , a diver exhales an air bubble having a volume of $1.00\ \text{cm}^3$. If the surface temperature of the sea is 20.0°C , what is the volume of the bubble right before it breaks the surface?
4. The rms speed of a helium atom at a certain temperature is $1\ 350\ \text{m/s}$. Find by proportion the rms speed of an oxygen molecule at this temperature. (The molar mass of O_2 is $32.0\ \text{g/mol}$, and the molar mass of He is $4.00\ \text{g/mol}$.)

5. In class we calculated the root-mean-square speed of the water molecules at room temperature. Following the same line of thinking in Question 4, we realize that the root-mean-square speed of molecules in air (mostly N_2) should be comparable to the speed of sound in air (or in an ideal gas). This should not be too surprising to you with the knowledge now you have.

(a) Using the equation of state of an ideal gas, calculate the bulk modulus (at temperature T), which is defined as

$$B = \frac{\text{volume stress}}{\text{volume strain}} = -\frac{\Delta F/A}{\Delta V/V} = -\frac{\Delta P}{\Delta V/V}$$

(b) Recall that the speed of sound in a fluid $v = \sqrt{B/\rho}$ depends on the elastic and inertial properties of the fluid, where B is the bulk modulus and ρ is the density of air. Express the speed of sound waves in terms of molecular mass m , temperature T , as well as the Boltzmann's constant k_B .

(c) Compute the result in (b) at room temperature. The result was first obtained by Isaac Newton, but it is lower than the measured value due to the failure to include the effect of fluctuating temperature.

(d) Pierre-Simon Laplace later pointed out that as a sound wave passes through a gas, the compressions are so rapid or so far apart that energy flow by heat is prevented by lack of time or by insulation. The compressions and rarefactions are adiabatic. As a result, the speed of sound has an additional factor of $\sqrt{\gamma}$, where γ is the adiabatic index ($\gamma = 7/5 = 1.400$ for diatomic molecules at room temperature). Please evaluate Laplace's result for the speed of sound and compare it to the numerical value that you know or you find elsewhere.

(e) Compare your result with the root-mean-square molecular speed.