Regression

APAM E4990
Modeling Social Data

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Definition

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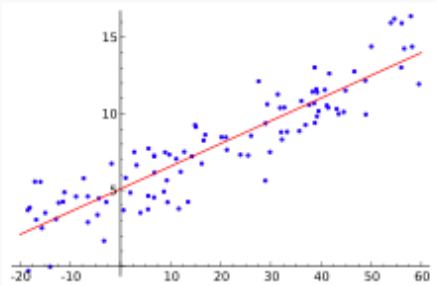
Regression analysis



Models

Linear regression · Simple regression · Ordinary least squares · Polynomial regression · General linear model

Generalized linear model · Discrete choice · Logistic regression · Multinomial logit · Mixed logit · Probit · Multinomial probit · Ordered logit · Ordered probit · Poisson

Multilevel model · Fixed effects · Random effects · Mixed model

Nonlinear regression · Nonparametric · Semiparametric · Robust · Quantile · Isotonic · Principal components · Least angle · Local · Segmented

Errors-in-variables

Estimation

Least squares · Ordinary least squares · Linear (math) · Partial · Total · Generalized · Weighted · Non-linear · Iteratively reweighted · Ridge regression · LASSO

Least absolute deviations · Bayesian · Bayesian multivariate

Background

Regression model validation · Mean and predicted response · Errors and residuals · Goodness of fit · Studentized residual · Gauss–Markov theorem

Definition

"The primary goal in a regression analysis is to **understand**, *as far as possible* **with the available data**, *how the conditional distribution of the* **response varies across subpopulations** *determined by the possible values of the predictor or* **predictors**."

-"Applied Regression Including Computing and Graphics"
Cook & Weisberg (1999)

Goals

Describe

Provide a compact summary of outcomes under different conditions

Predict

Make forecasts for future outcomes or unobserved conditions

Explain

Account for associations between predictors and outcomes

Goals

Describe

Provide a compact summary of outcomes under different conditions

Never "false", but may be wasteful or misleading

Predict

Make forecasts for future outcomes or unobserved conditions

Varying degrees of success, often room for improvement

Explain

Account for associations between predictors and outcomes

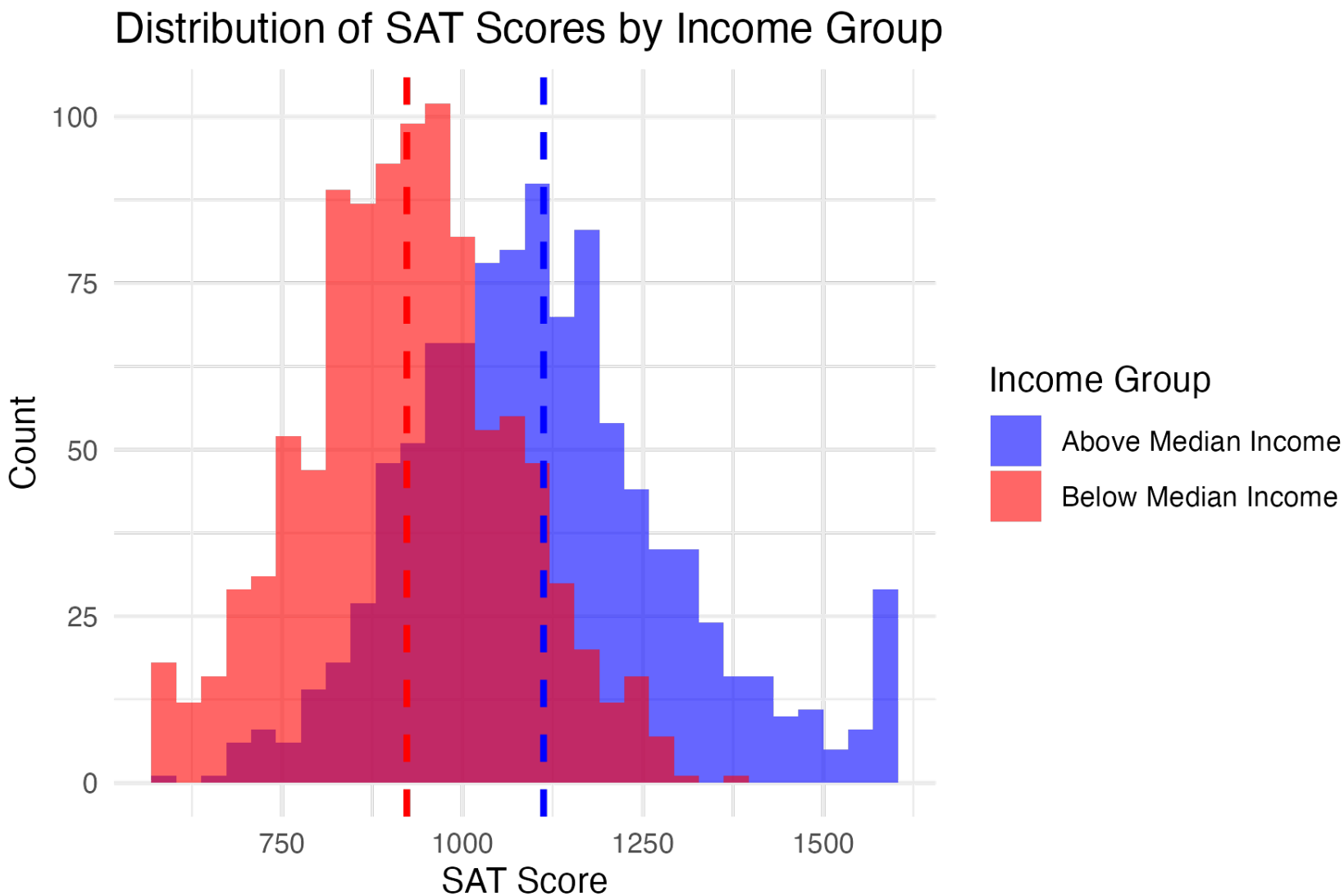
Difficult to establish causality in observational studies

See "Regression Analysis: A Constructive Critique", Berk (2004)

Goals

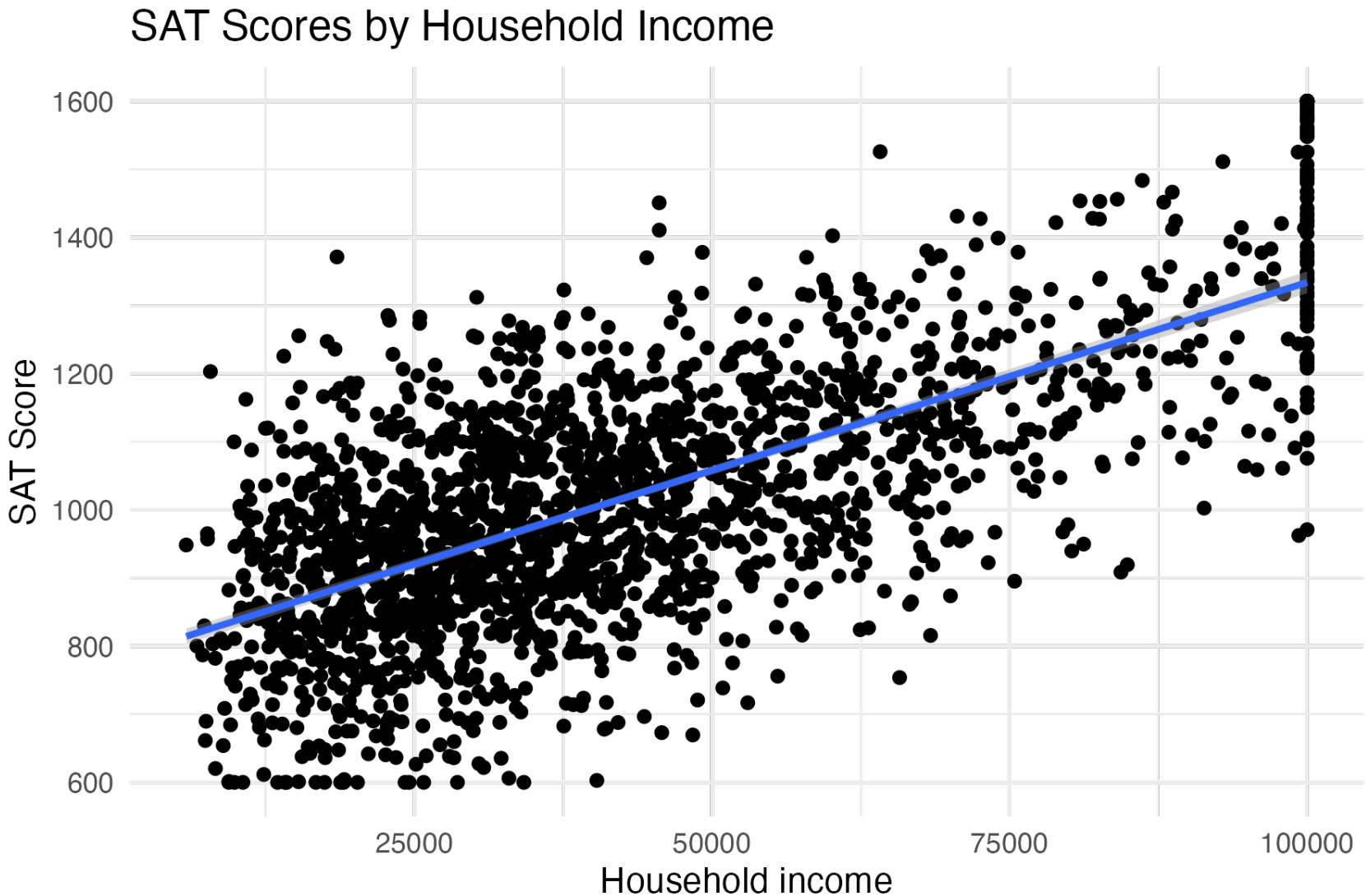
Models should be flexible enough to describe observed phenomena but simple enough to generalize to future observations

Examples[1]



[1] "Statistical Learning from a Regression Perspective", Berk (2008)

Examples[1]



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Framework

- Specify the outcome and predictors, along with the form of the model relating them
- Define a loss function that quantifies how close a model's predictions are to observed outcomes
- Develop an algorithm to fit the model to the observations by minimizing this loss
- Assess model performance and interpret results.