



# Midterm Exam Info

- ◆ Time: Oct. 23, during class time, 45 minutes
- ◆ Closed book, written exam
- ◆ Coverage: Weeks 0-5
- ◆ Types of questions: Multiple choices, True/false, short answer, open-ended questions.
  - More details on practice and sample questions
- ◆ How to prepare
  - Lecture content, Assignments, Labs
  - Practice questions coming one week before the midterm
  - Oct. 21 lecture, review and sample questions



# Midterm Exam Info

- ◆ Makeup midterm
  - Oct. 28 (Mon.) class time
  - Requests must be sent to the course email **before** the midterm
  - No other makeup exam offered. If missed, the weight of midterm will be shifted to final. (Note: your final will have a 60% of the total grade)



# Plans for Week of Oct. 14 - 28

## ◆ Week 6 (Oct. 14-18)

- No class on Oct. 14 (holiday)
- No labs and office hours on Oct 14&15
- Classes, labs, and office hours are as usual on Oct. 16-18.

## ◆ Week 7 (Oct. 21-25)

- Review lecture on Oct. 21
- Midterm on Oct. 23
- Labs and office hours are as usual on Oct. 21-23
- No classes, labs, and office hours on Oct. 24&25



# Plans for Week of Oct. 14 - 28

- ◆ Week 8 (Oct. 28 - Nov. 1)
  - Oct. 28 (Mon.) makeup midterm
  - Course lecture on Oct. 28 will be uploaded as videos.
  - No labs and office hours on Oct. 28&29
  - Classes, labs, and office hours are as usual on Oct. 30 – Nov. 1.

# Resources on CourseLink

- ◆ Garbage Collection





A collection of objects is arranged on a light-colored, textured surface. On the left, a portion of a chessboard with a blue and brown checkered pattern is visible, featuring several chess pieces. Below the chessboard, there are two medals: one with a red ribbon and a white star, and another with a blue ribbon and a white star. A small, round, silver compass is located at the bottom left. A pair of glasses with thin, gold-colored frames and dark lenses is positioned diagonally across the center. A small, red, star-shaped object is also visible near the top left.

# Stacks

**Notes from Charlie Obimbo  
and revised by Yan Yan.**



# Contents

1. Definition of Stacks
2. Stacks Applications
3. Implementation



# Learning Objectives

1. Define the data structure of the Stack ADT
2. Implement the operations of the Stack ADT.
3. Describe the advantages and disadvantages of linked list implementation and array implementation of the stack.



# Stacks & Queues

## ◆ Stacks & Queues

– Stacks: Last in First Out



- Queues: First in First Out





# Stack: Definition

- ◆ **Stack**: A stack is an ADT in which items are only inserted on or removed from the top of a stack.
- ◆ **Push** operation inserts an item on the top of the stack.
- ◆ **Pop** operation removes and returns the item at the top of the stack.
- ◆ A *linear* data structure, in which elements are accessed using the LIFO (Last in First Out) Order.



# Stack: Some Applications

- ◆ Page-visited history in a Web browser
- ◆ Undo and Redo mechanism in a text editor
- ◆ Backtracking, i.e., to check parenthesis matching in an expression.
- ◆ Saving local variables when one function calls another, and this one calls another, and so on.
- ◆ String Reversal

# Queue: Definition

- ◆ **Queue**: A queue is an ADT in which items are inserted at the end of the queue and removed from the front of the queue.
- ◆ **Enqueue** operation inserts an item at the end of the queue.
- ◆ **Dequeue** operation removes and returns the item at the front of the queue.
- ◆ **FIFO** (First in First Out) ADT.





# Queue: Some Applications

- ◆ Waiting lines
- ◆ Access to shared resources (e.g., printer)
- ◆ Maintaining the playlist in media players.



# Stacks: Operations

- ◆ Mainly the following basic operations are performed in the stack:
  - **Push (stack, X)**
  - **Pop (stack)**
  - **Peek (stack)**
  - **isEmpty (stack)**





# Push

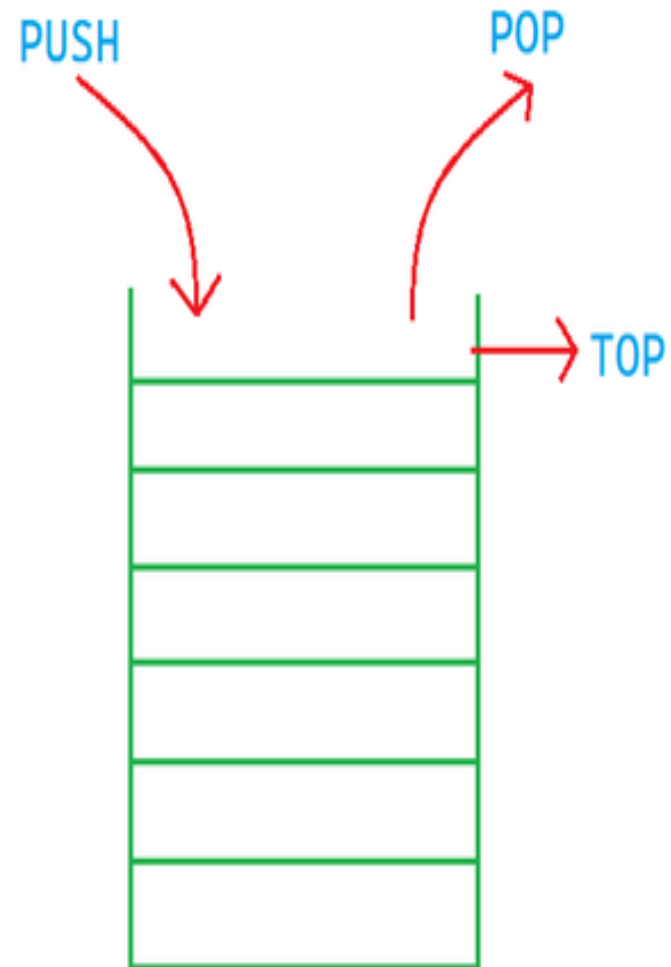
- ◆ Push: Adds an item to the stack. If the stack is full, then it is said to be an **overflow** condition.

## Algorithm for push:

```
begin
  if stack is full
    return
  endif
  else
    increment top
    stack[top] assign value
  end else
end procedure
```

# Stack

Insertion & Deletion  
happens on the same end.





# Pop

- ◆ Pop: Removes an item from the stack. The items are popped in the reversed order in which they are pushed. If the stack is empty, then it is said to be an **underflow** condition.

## Algorithm for pop:

```
begin
  if stack is empty
    return
  endif
  else
    store value of stack[top]
    decrement top
    return value
  end else
end procedure
```



# isEmpty

- ◆ **isEmpty**: Returns true if the stack is empty, else false.

Algorithm for isEmpty:

begin

if  $\text{top} < 1$

    return true

else

    return false

end procedure

# Peek

- ◆ **Peek** or **Top**: Returns the top element of the stack.

Algorithm for peek:

begin

if  $top == null$  // (or if **isEmpty**)

return “stack is empty”

else

return  $stack[top]$

end procedure





# Time Complexities

- ◆ What are the time complexities of the operations on the stack?
- ◆ `push()`, `pop()`, `isEmpty()` and `peek()` all take  $O(1)$  time. We do not run any loop in any of these operations.





# Stacks: Exercise - 1

Given numStack: 5, 9, 1 (top is 5)

- ◆ What is the stack after a pop operation  
Pop(numStack) ?
- ◆ Following the previous operation, what is the stack after a push operation  
Push(numStack, 8) ?

What operation determines if the stack contains no items?



# Stacks: Exercise - 1 Solution

Given numStack: 5, 9, 1 (top is 5)

- ◆ What is the stack after a pop operation  
Pop(numStack) ? 9,1
- ◆ Following the previous operation, what is the stack after a push operation  
Push(numStack, 8) ? 8, 9,1

What operation determines if the stack contains no items? **IsEmpty**



## Stacks: Exercise - 2

- ◆ What are the output of the following operations?

route = new Stack

Push(route, Tokyo)

Push(route, Osaka)

Push(route, Nara)

print Pop(route)

print Pop(route)

- ◆ What is the route stack after the above operations?



## Stacks: Exercise - 3

- ◆ What are the output of the following operations?

route = new Stack

Push(route, Tokyo)

Push(route, Osaka)

Push(route, Nara)

print **Peek**(route)

print Pop(route)

- ◆ What is the route stack after the above operations?




# Stacks

## ◆ Implementation:

- Using array
- Using linked list





// A structure to represent a stack

**struct** Stack {

**int** top;

**unsigned** capacity;

**int**\* array;

};

//

---

// function creates a stack of given capacity. It initializes size to 0

**struct** Stack\* createStack(**unsigned** capacity){

**struct** Stack\* stack = (**struct** Stack\*)**malloc**(**sizeof**(**struct** Stack));

    stack->capacity = capacity;

    stack->top = -1;

    stack->array = (**int**\*)**malloc**(stack->capacity \* **sizeof**(**int**));

**return** stack;

}

//


---

// Stack is full when top is equal to the last index

**int** isFull(**struct** Stack\* stack){

**return** stack->top == stack->capacity - 1;

}



// Stack is empty when top is equal to -1

```
int isEmpty(struct Stack* stack){  
    return stack->top == -1;  
}
```

// Function to add an item to stack. It increases top by 1

```
void push(struct Stack* stack, int item){  
    if (isFull(stack))  
        printf("Overflow\n");  
        return;  
    stack->array[++stack->top] = item;  
    printf("%d pushed to stack\n", item);  
}
```

// Function to remove an item from stack. It decreases top by 1

```
int pop(struct Stack* stack){  
    if (isEmpty(stack))  
        return INT_MIN;  
    return stack->array[stack->top--];  
}
```



```
// Function to return the top from stack without removing it
```

```
int peek(struct Stack* stack){  
    if (isEmpty(stack))  
        return INT_MIN;  
    return stack->array[stack->top];  
}
```

```
// Driver program to test above functions
```

```
int main() {  
    struct Stack* stack = createStack(100);  
  
    push(stack, 10);  
    push(stack, 20);  
    push(stack, 30);  
  
    printf("%d popped from stack\n", pop(stack));  
    printf("Top element is: %d\n", peek(stack));  
  
    return 0;  
}
```

### Output :

```
10 pushed into stack  
20 pushed into stack  
30 pushed into stack  
30 Popped from stack  
Top element is : 20
```





# Pros & Cons of Array Implementation

- ◆ **Pros:** Easy to implement. No additional pointer for each element is needed (save memory).
- ◆ **Cons:** It is not dynamic. It doesn't grow and shrink depending on needs at runtime.



# Stack Linked List Implementation

- ◆ **Head** of the list is the **top** of the stack.
- ◆ Push/Pop: update the top of the stack.  
Similar to adding/deleting the first node in a linked list.



# Knowledge Prep: pointer to the pointer

- ◆ **Pointer (\*p)** stores the information of an address (can be null)
- ◆ Pointer to the pointer (\*\*p) stores the address of that pointer (\*p)
- ◆ Use \*\* when you want to preserve (or retain change in) the memory-allocation or assignment even outside of a function call



# Knowledge Prep: pointer to the pointer -- Example

```
#include <stdio.h>
```

```
int main () {  
    int c = 1;  
    int d = 2;  
    int e = 3;  
    int * a = &c;  
    int * b = &d;  
    int * f = &e;  
    int ** pp = &a; // pointer to  
                     // pointer 'a'  
  
    a = b; // a stores d' address  
    cant_change(a, f);  
    change(pp, f);  
    return 0;  
}
```

```
void cant_change(int * x, int * z){
```

```
    x = z;
```

```
    printf("\n ----> value of 'a' is: %x inside  
    function, same as 'f', BUT NOT the same  
    outside of this function \n", x);
```

```
}
```

```
void change(int ** x, int * z){
```

```
    *x = z;
```

```
    printf("\n ----> value of 'a' is: %x inside  
    function, same as 'f', and the same outside  
    of this function\n", *x);
```

```
}
```





```
// C program for linked list implementation of stack
```

```
#include <limits.h>
```

```
#include <stdio.h>
```

```
#include <stdlib.h>
```

```
// A structure to represent a stack
```

```
struct StackNode {
```

```
    int data;
```

```
    struct StackNode* next;
```

```
};
```

```
// create a new node in the stack (implemented by linked list)
```

```
struct StackNode* newNode(int data) {
```

```
    struct StackNode* stackNode =
```

```
        (struct StackNode*)
```


```
        malloc(sizeof(struct StackNode));
```

```
    stackNode->data = data;
```


```
    stackNode->next = NULL;
```

```
    return stackNode;
```

```
}
```



```
int isEmpty(struct StackNode* top) {  
    return !top;  
}  
  
void push(struct StackNode** top, int data) {  
    struct StackNode* stackNode = newNode(data);  
    stackNode->next = *top;  
    *top = stackNode;  
    printf("%d pushed to stack\n", data);  
}  
  
int pop(struct StackNode** top) {  
    if (isEmpty(*top))  
        return INT_MIN;  
    struct StackNode* temp = *top;  
    *top = (*top)->next;  
    int popped = temp->data;  
    free(temp);  
    return popped;  
}
```



```
int peek(struct StackNode* top) {  
    if (isEmpty(top))  
        return INT_MIN;  
    return top->data;  
}
```

```
int main() {  
    struct StackNode* top = NULL;  
  
    push(&top, 10);  
    push(&top, 20);  
    push(&top, 30);  
    printf("%d popped from stack\n", pop(&top));  
  
    printf("Top element is %d\n", peek(top));  
  
    return 0;  
}
```



# Pros & Cons of LL Implementation

- ◆ **Pros:** The linked list implementation of a stack can grow and shrink according to the needs at runtime.
- ◆ **Cons:** Requires extra memory due to involvement of pointers.





# Exercise - 1

- ◆ An empty stack is indicated by a list head pointer value of \_\_\_\_\_.

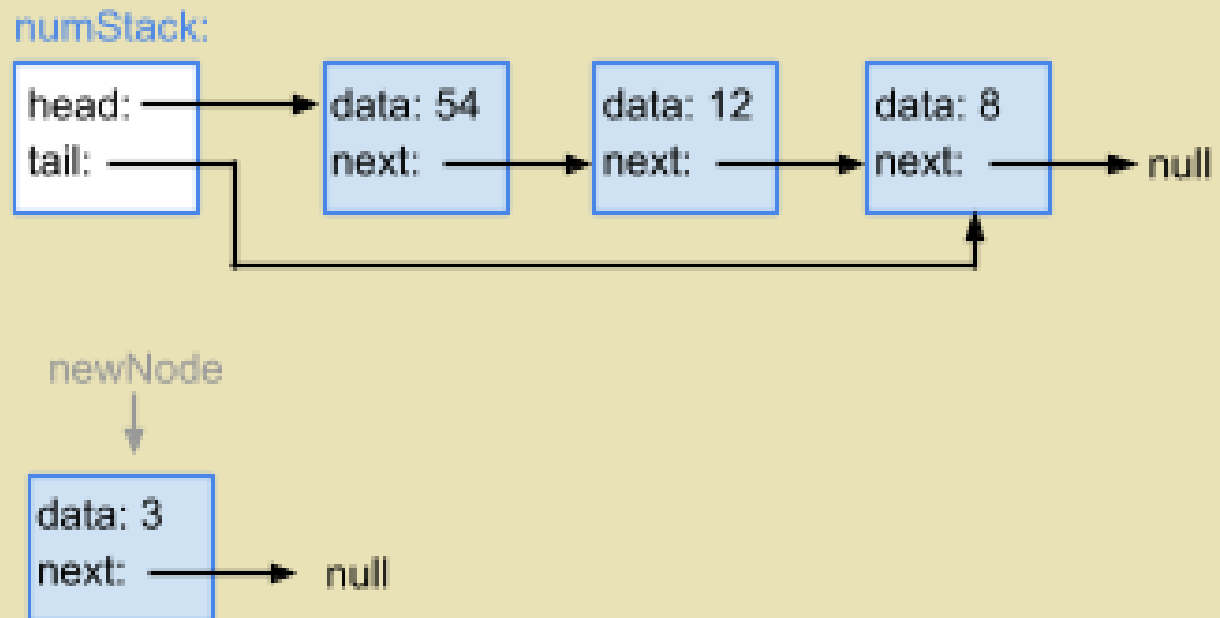
A. newNode

B. null

C. Unknown

# Exercise - 2

- ◆ For StackPush(numStack, 3), newNode's next pointer is pointed to? **54**





# References and Useful Resources

- ◆ Zybook Data Structures 5) Stacks and Queues
- ◆ Signed and unsigned in Type Define
  - [https://www.cs.yale.edu/homes/aspnes/pinewiki/C\(2f\)IntegerTypes.html#:~:text=Unsigned%20variables%2C%20which%20can%20be,the%20whim%20of%20the%20compiler.](https://www.cs.yale.edu/homes/aspnes/pinewiki/C(2f)IntegerTypes.html#:~:text=Unsigned%20variables%2C%20which%20can%20be,the%20whim%20of%20the%20compiler.)
  - <https://ece.uwaterloo.ca/~dwharder/icsrts/C/07/>
- ◆ Array implementation of Stacks
  - <https://www.geeksforgeeks.org/array-implementation-of-stack-in-c/>

That's  
about this  
lecture!

