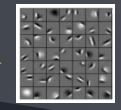
Place Category Prediction using Graph Convolutional Model

Soojung Hong

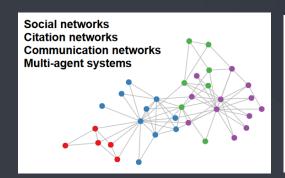
September 27. 2019

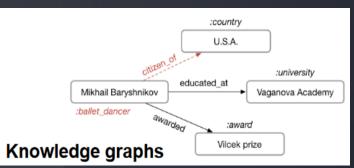


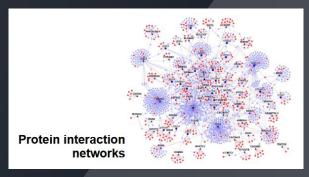
Why Graph Model in Deep Learning?



- A lot of real-world data does not "live" on grids (Thomas Kipf)
- Learn representations that encode structural information
- Standard DNN, CNN model didn't handle structure
- Mapping the geometric relationship in the learned space



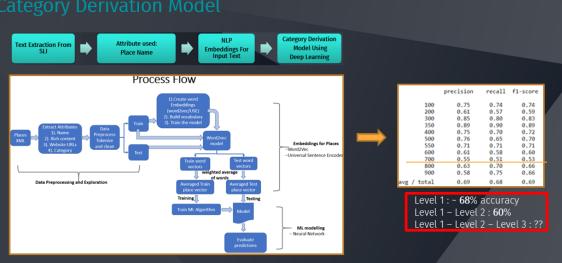






Why Graph Model in HERE Category Prediction problem?

Lack of features about places



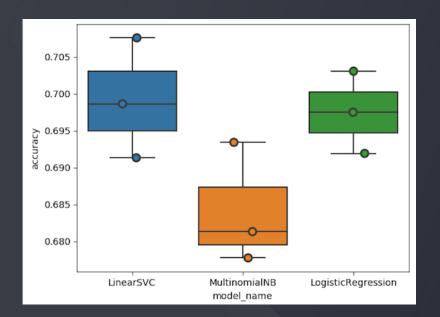
- Training data: 88,000 samples per category
- Test data: 15,000 samples per category
- Neural network with 3 hidden layers, <u>adam</u> optimizer, <u>softmax</u> output layer <u>Credit</u>: Charitha H.



Limit: Category Prediction using only Place name

Q: Can we predict place category based on place (POI) name?

A: Yes, With approximately 70% accuracy. But,,,



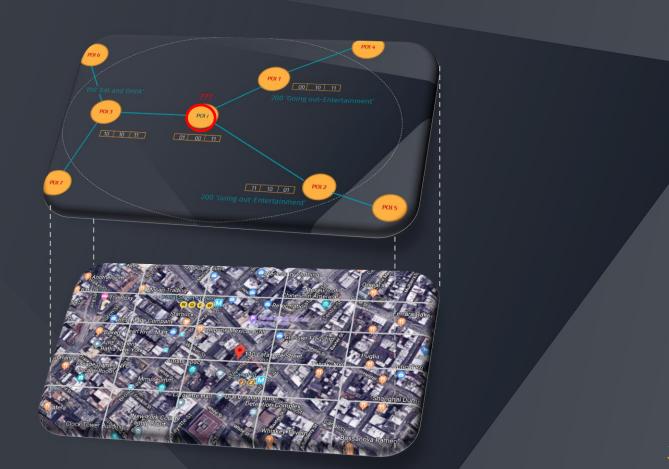
Category	Precision	Recall	
restaurant	64%	62%	
coffee shop	84%	59%	
nightlife-entertainment	34%	56%	
theatre,music,culture	50%	46%	
museum	86%	78%	
church / reglious place	92%	85%	
hotel/motel	71%	67%	
lodging	60%	54%	
drugstore / pharmacy	98%	92%	
hardware/house/garden	78%	78%	
bookstore	81%	70%	
hair and beauty	92%	80%	
car repair	88%	83%	
sports facility-venue	58%	72%	
Average values	74%	70%	



HERE Category Prediction in a long run



Place Graph



Graph Neural Network

$$G = (A, X)$$

Preprocessed Adjacency matrix $A \in R^{N \times N}$ Feature matrix $X \in R^{N \times F}$

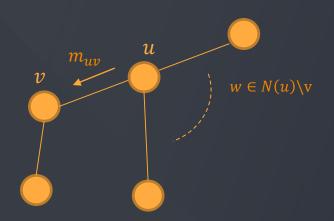
$$egin{aligned} h_v &= f\left(X_v, X_{co[v]}, h_{ne[v]}, X_{ne[v]}
ight) \ o_v &= \operatorname{g}\left(h_v, X_v
ight) \end{aligned}$$

- f : Transition function that projects inputs onto a d-dimensional space
 - h_{ν} : State embedding of Node (d-dim vector contains information of its neighborhood)
 - $X_{co[v]}$: Features of the Edges connect to v
 - $X_{ne[v]}$: Features of neighboring nodes of v
- $h_{ne[v]}$: Embedding of the neighboring nodes of v
- $oldsymbol{o_v}$: output of node v computed by state h_v and node feature x_v
 - g: feed-forward fully connected neural network



GNN: Nodes and Edges embedding in the graph

Main idea: Pass messages between pairs of nodes & agglomerate



* Graph is bidirectional in this presentation

- Each node has feature vector: $X_v = [0, 0, 1]$
- Each edge has feature vector: $X_{uv} = [0, 1, 1]$
- Embedding of node u:

$$h_u = \tanh(U_1 X_u + U_2 * \sum_{w \in N(u)} m_{wu})$$

Message from node u to node v:

$$m_{uv} = \tanh(W_1 X_u + W_2 X_{uv} + W_3 * \sum_{w \in N(u) \setminus v} m_{wu})$$

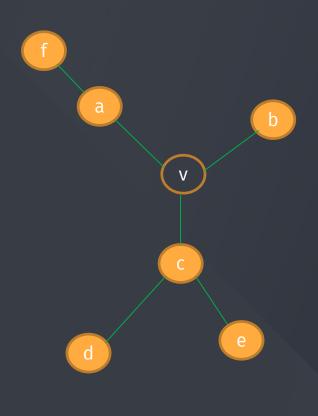
Iterative Neighbor Aggregation (Message passing)

-simple forward NN

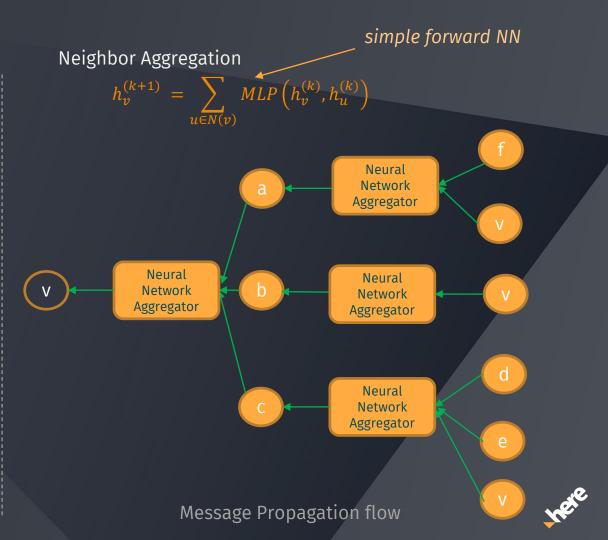
$$h_v^{(k+1)} = \sum_{u \in N(v)} MLP(h_v^{(k)}, h_u^{(k)})$$



Graph Readout



Graph structure



Neighborhood Aggregation

Algorithm 1: Neighborhood-aggregation encoder algorithm. Adapted from [28].

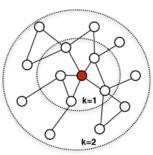
Input: Graph $\mathcal{G}(\mathcal{V}, \mathcal{E})$; input features $\{\mathbf{x}_v, \forall v \in \mathcal{V}\}$; depth K; weight matrices $\{\mathbf{W}^k, \forall k \in [1, K]\}$; non-linearity σ ; differentiable aggregator functions {AGGREGATE_k, $\forall k \in [1, K]$ }; neighborhood function $\mathcal{N}: v \to 2^{\mathcal{V}}$

Output: Vector representations \mathbf{z}_v for all $v \in \mathcal{V}$

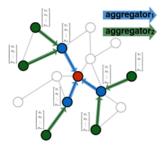
```
\mathbf{1} \ \mathbf{h}_v^0 \leftarrow \mathbf{x}_v, \forall v \in \mathcal{V};
2 for k = 1...K do
              for v \in \mathcal{V} do
                   \mathbf{h}_{\mathcal{N}(v)}^k \leftarrow \text{AGGREGATE}_k(\{\mathbf{h}_u^{k-1}, \forall u \in \mathcal{N}(v)\});
                  \mathbf{h}_v^k \leftarrow \sigma\left(\mathbf{W}^k \cdot \text{combine}(\mathbf{h}_v^{k-1}, \mathbf{h}_{\mathcal{N}(v)}^k)\right)
              end
            \mathbf{h}_v^k \leftarrow \text{NORMALIZE}(\mathbf{h}_v^k), \forall v \in \mathcal{V}
```



8 end 9 $\mathbf{z}_v \leftarrow \mathbf{h}_v^K, \forall v \in \mathcal{V}$



1. Collect neighbors



2. Aggregate feature information from neighbors



Aggregation types

Mean aggregator

$$h_v^k \leftarrow \sigma(W \cdot mean(\{h_v^{k-1}\} \cup \{h_u^{k-1}, \forall u \in N(v)\}))$$

LSTM aggregator

- Advantage of larger expressive capability
- But not inherently symmetric (i.e. not permutation invariant)

Pooling aggregator

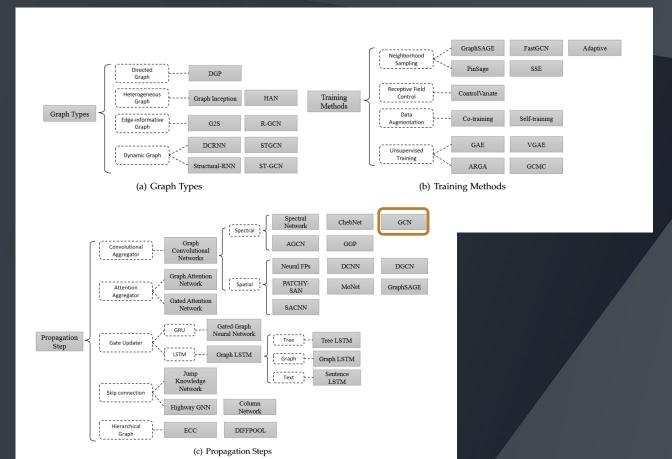
$$Aggregate_k^{pool} \leftarrow \max(\{\sigma(W_{pool}h_{u_i}^k + b), \forall u \in N(v)\})$$

→ idea : differentiate the relevance of neighbor?



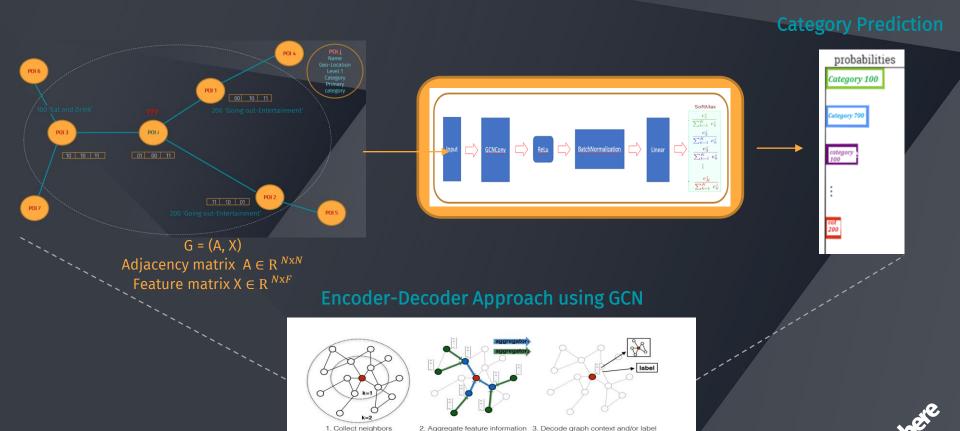
Variant Graph Network

* Graph Neural Networks : A Review of Methods and Applications

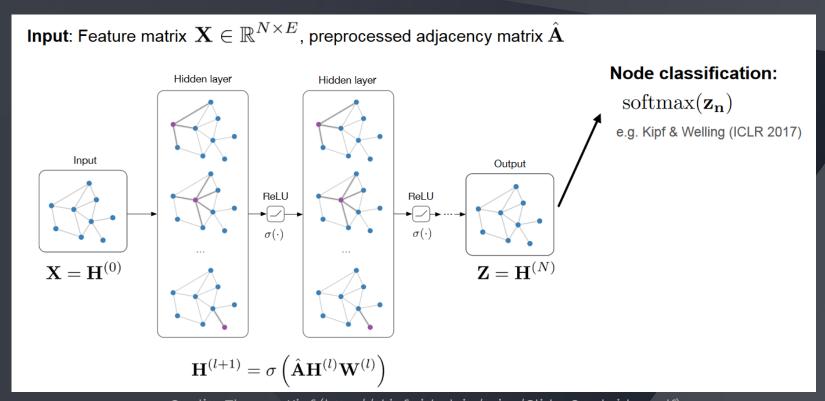




Place Graph Embedding and Category Prediction with GCN



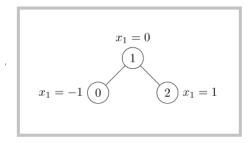
Node classification with GNN/GCN



Credit: Thomas Kipf (http://tkipf.github.io/misc/SlidesCambridge.pdf)



Graph Representation using Adjacency Matrix





1. Adjacency Matrix Represenatation

	0		
0	0	1	0
1	1	0	0
2	0	1	0

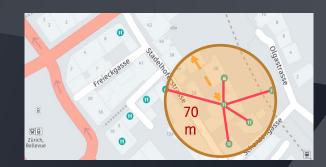
Adjacency Matrix representation of Undirected Graph



2. Develop using PyTorch GCN

New York Place Graph

Neighboring places: Distance within 70m Number of nodes (places) in New York: 806,830 Number of edges in New York graph: 4,033,104



data	size	elapsed time to create
New York place data (806,830 places)	119 MB	
New York data place name and label embedding generation (using BERT)	10.2 GB	35 hour in 125 GB memory GPU machine
New York Adjacency matrix size	86.3 MB	9 hour to generate
Number of edges in adjmatrix	4,033,105 (4 million edges)	

Place data analysis on New York and Chicago

city	number of places	bounding box
New York	806,830	{'left_lon':-74.2591, 'bottom_lat':40.4774, 'right_lon':-73.7002, 'top_lat':40.9162}
Chicago	248,024	{'left_lon':-88.133, 'bottom_lat':41.6062, 'right_lon':-87.4656, 'top_lat':42.1603}



Chicago Place Graph

- Neighboring places : Distance within 70m
- Number of nodes (places) in Chicago: 248,024
- Number of edges in Chicago graph: 2,442,558



The number of places in Chicago is 248,024 and each place contains pid, geo-location.

The data frame that contains pid, place name, level 1 category, full category, category name, place name vector (with 768 dimension), Label encoding

data	size	time to create
Chicago place data (248,024 places)	18.42 MB	
Chicago place adjacency matrix	50.8 MB	~ 4 hours in GPU machine (with 125 GB memory)
Number of edges (connections between places)	2,442,558 (2 million edges)	
Chicago dataframe contains place name vectors using BERT	3.13 GB	~ 8 hours to generate dataframe
NYC dataframe contains place name vectors using BERT	10.2 GB	~ 1 day to generate dataframe



Graph Convolutional Model Architecture

x = self.linearl(x)

return F.log softmax(x, dim=1)

```
class Net(torch.nn.Module):
    def init (self):
        super (Net7, self). init ()
        self.conv1 = GCNConv(dataset.num_node_features, 256)
        self.conv2 = GCNConv(126, 62)
        self.linear1 = torch.nn.Linear(256, 11)
        self.linear2 = torch.nn.Linear(126, 11)
        self.pool1 = TopKPooling(512, ratio=0.5)
        self.pool2 = TopKPooling(62, ratio=0.5)
        self.bn1 = torch.nn.BatchNorm1d(256)
                                                                                                                    BatchNormalization
                                                                   Input
                                                                                  GCNConv
        self.bn2 = torch.nn.BatchNormld(62)
    def forward(self, data):
        x, edge index = data.x, data.edge index
        x = self.convl(x, edge index)
        x = F.relu(x)
        x = self.bnl(x)
```

Model Architecture - Forward Pass

Chicago Graph Model Accuracy

Number of Places: 248,024

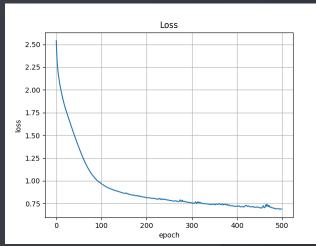
Neighboring distance : 70m

Number of edges in graph : 2,442,558 (2.4 M edges)

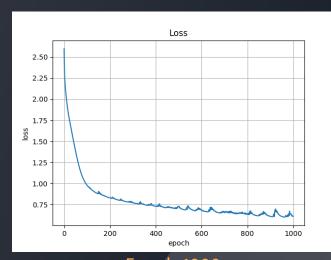
Learning Rate: 0.001

Optimizer : Adam

Loss function : Cross Entropy Loss



Epoch 500 Accuracy : **0.7**5

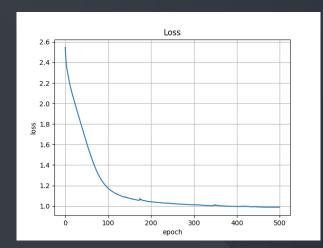


Epoch 1000 Accuracy : **0.7846**

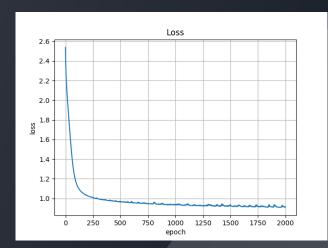


New York Graph Model Accuracy

- Number of Places: 806,830
- Neighboring distance : 70m
- Number of edges in graph: 4,033,105 (4.03 M edges)
- Learning Rate : 0.001
- Optimizer : Adam
- Loss function : Cross Entropy Loss



Epoch 500 Accuracy : **0.63**



Epoch 2000 Accuracy: **0.67**



New York (very small) Graph Model Accuracy

Number of places : 1000

Neighboring distance: 50m

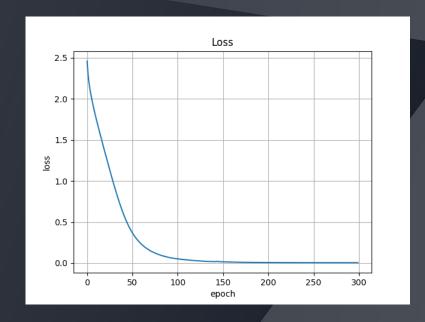
Accuracy: 0.87

Epochs: 300

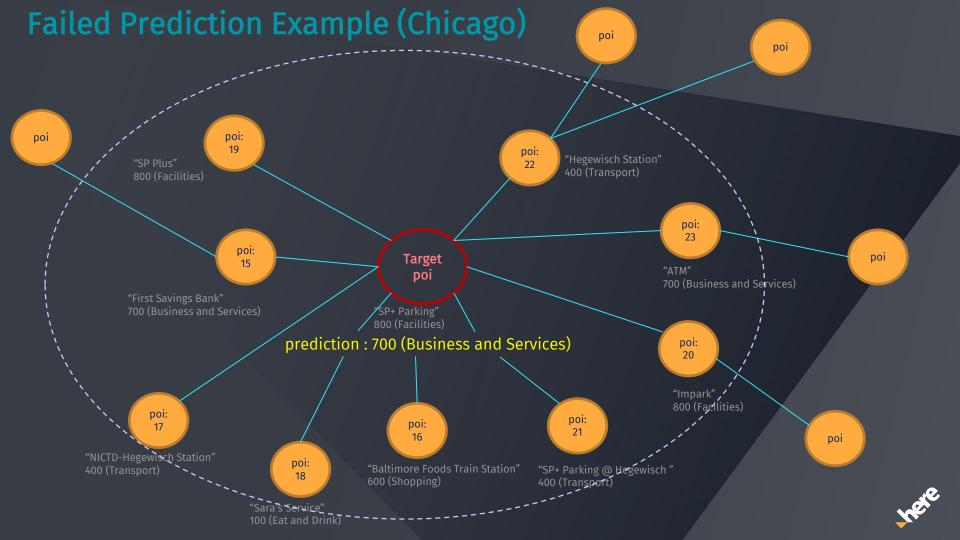
Learning Rate: 0.001

Optimizer : Adam

Loss function : Cross Entropy Loss

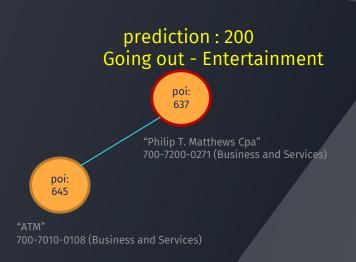






Failed Prediction Example (New York)







Open problems

In general

- Scalability: Graph can be extremely big!
- Interpretability

In HERE place prediction

- Effect of different Aggregator
- Graph size matters for better prediction?
- Encoding with probability of category distribution

