ASSIGNMENT 3

SYSTEMS ENGINEERING FOR DEEP LEARNING

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STEP 1

A neural network with the given architecture was trained on the FMNIST dataset. The network weights were initialized with Xavier uniform initialisation. Stochastic Gradient Descend optimizer with momentum was used with a learning rate of 0.001 and with a momentum weightage of 0.9.

Dataset	FMNIST 60000 Training samples 10000 Testing samples
Preprocessing	Normalization
Optimizer	SGD with momentum
Learning Rate	1e-3
Momentum (β)	0.9
Batch Size	32
Network initialization	Weights : Xavier uniform Biases : Zero
Network Architecture	Layer 1 : Conv 3x3, 16 Channels, ReLU Layer 2: Conv 3x3, 16 Channels, ReLU Layer 3: Dense 100 neurons, ReLU Layer 4: Dense 10 neurons, Softmax

Table 1.1: Model and training hyperparameters.

The network was trained in a CPU only instance on Google Colaboratory. With a batch size of 32, I got 90.18 % training accuracy and a test accuracy of 88.33%. The loss vs batches plots and accuracy vs batches plots and the final results are given in the following page.

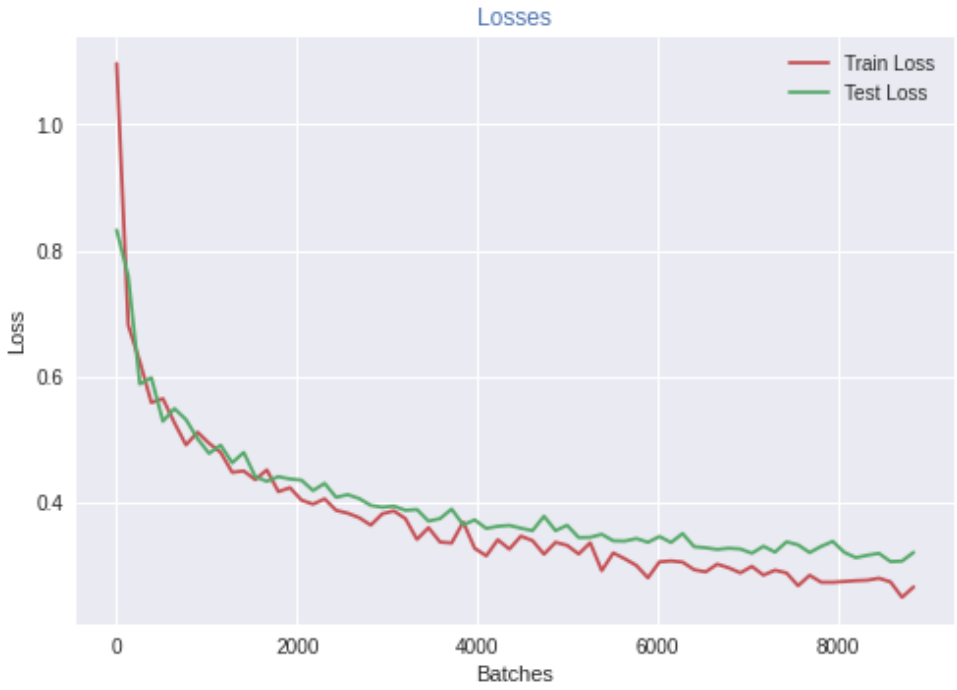


Figure 1.1.a:
Loss vs Batches plot

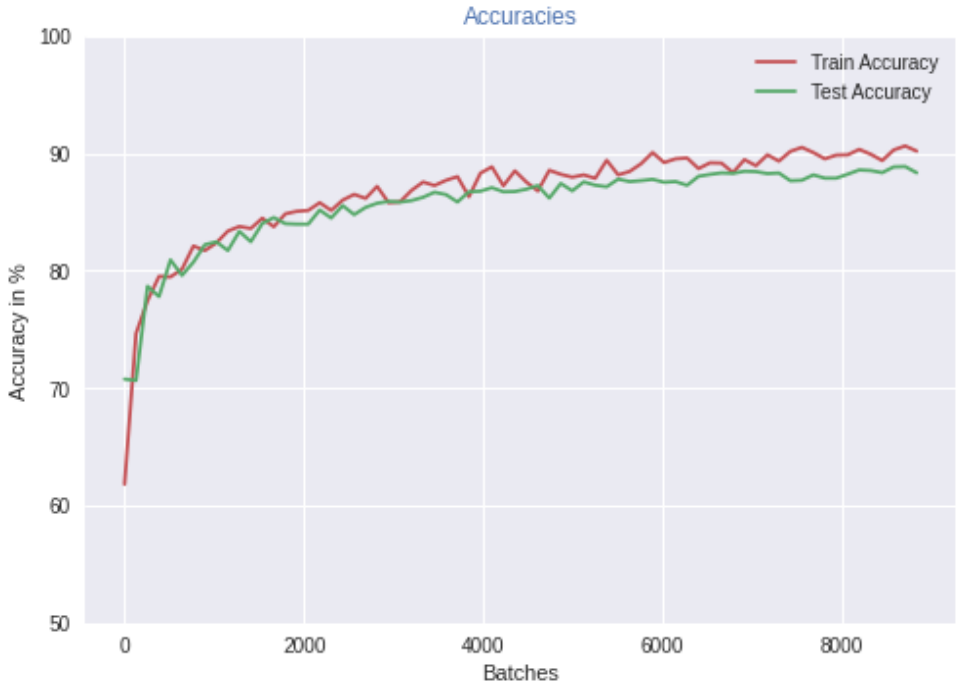


Figure 1.1.b:
Accuracy vs Batches plot

Google Facets was used to analyse the prediction performance of the trained model. Google Facets allow inputs only in CSV format. So the first the model was used to generate predictions for the entire test dataset. Then a CSV file was generated with columns being the True and Predicted labels. This CSV file was uploaded to Google Facets website. Many visualizations like the confusion matrix, distribution of predictions were obtained.

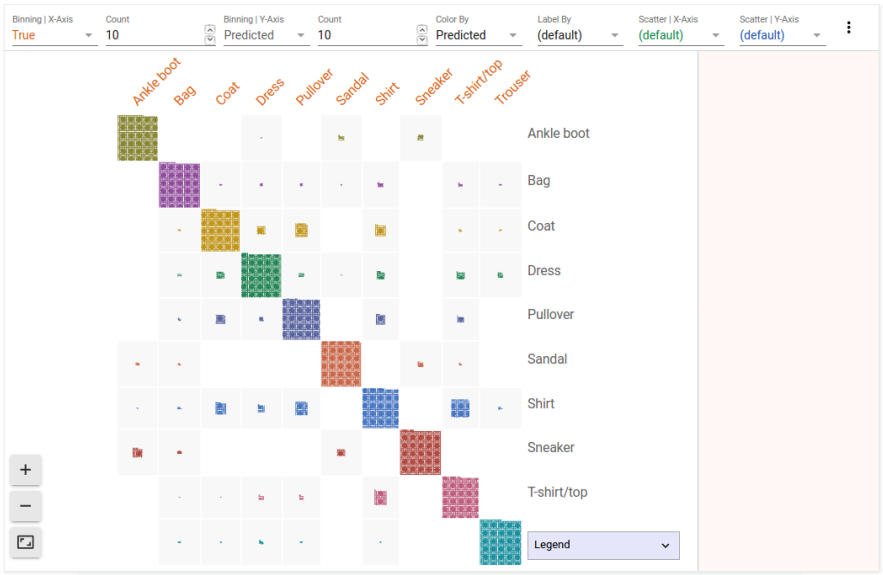


Figure 1.2.a: Confusion Matrix

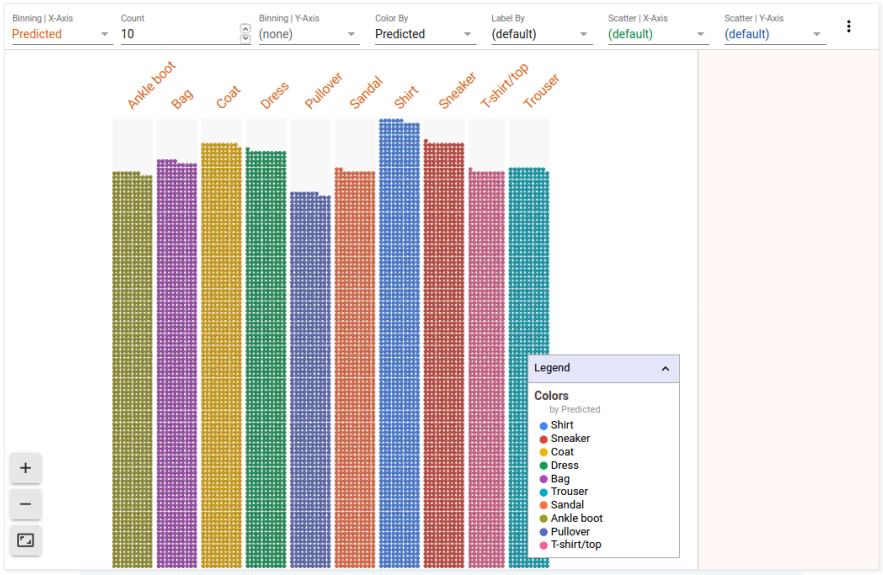


Figure 1.2.b: Distribution of predictions.

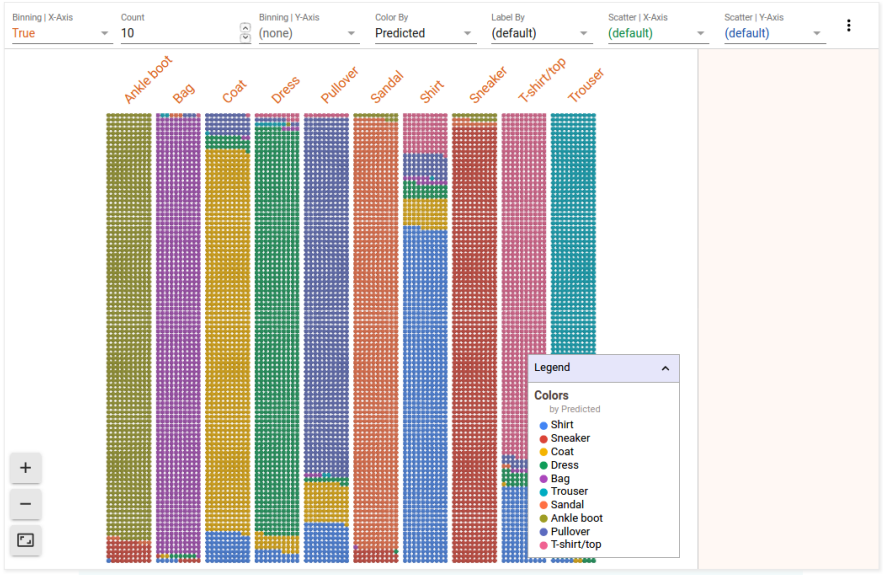


Figure 1.2.c: Predictions for each true label.

These visualizations helps us to understand where out model is failing to perform. For example, in Fig. 1.2.c, we can see that nearly 30% of T-shirts/tops are misclassified as shirts.

¯_(ツ)_/¯	*Loss*	*Accuracy*
Training	0.267	90.186 %
Testing	0.321	88.338 %

Table 1.2: Train and test performances

STEP 2

MLflow was used to conduct grid search to find the optimial hyperparameters for the model. Two experiments were conducted, one to find the right Model Hyperparameters and another one to find the right Training Hyperparameters. These experiments were conducted one by one. The optimal model architecture obtained from the first experiment was used for the second experiment.

The first experiment search space is as follows:

Hyperparameter	*Values*
Conv 1 kernel sizes	3x3, 5x5
Conv 2 kernel sizes	3x3, 5x5
Conv 1 no of filters	8, 16, 32
Conv 2 no of filters	8, 16, 32
Dense 1 no of neurons	64, 100

Table 2.1.a: The search space for experiment 1

Results are as follows.

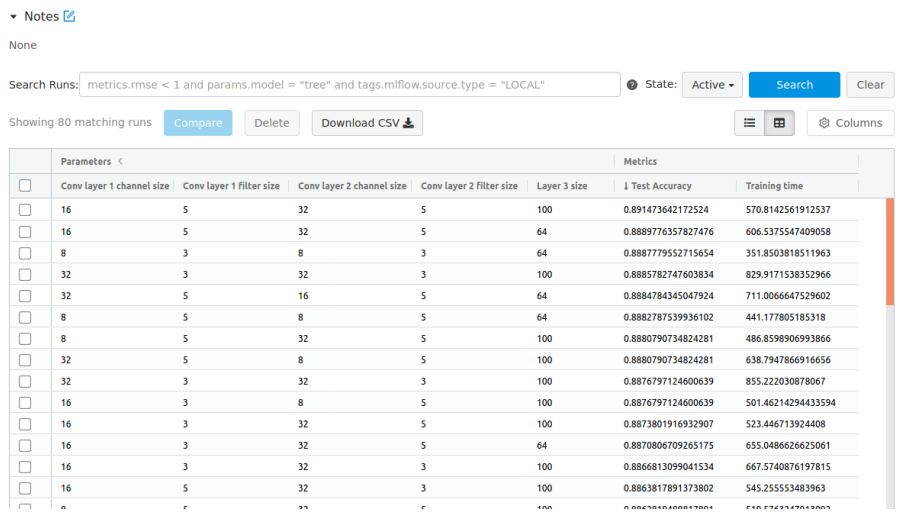


Fig 2.1.a: Experiment results sorted by decreasing accuracy on the test dataset.

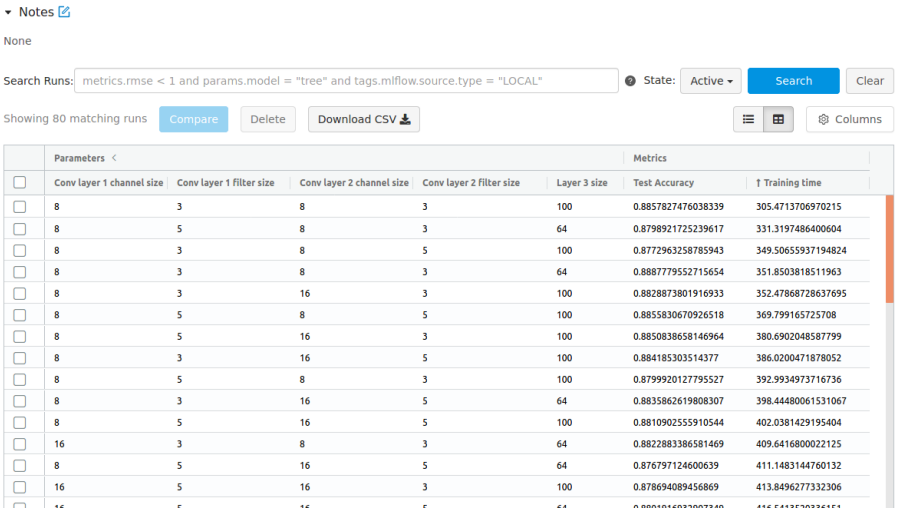


Fig 2.1.b: Experiment results sorted by increasing training time required to reach 90% train accuracy.

Top 3 results are as shown below:

	#1	*#2*	*#3*
Conv 1	5x5, 16 filters	5x5, 16 filters	3x3, 8 filters
Conv 2	5x5, 32 filters	5x5, 32 filters	3x3, 8 filters
Dense 3	100 neurons	64 neurons	64 neurons
Test Accuracy	89.14 %	88.89 %	88.87 %
Training Time	570.81s	606.53s	351.85s

Table 2.1.a: Top 3 results based on test accuracy.

	#1	*#2*	*#3*
Conv 1	3x3, 8 filters	5x5, 8 filters	3x3, 8 filters
Conv 2	3x3, 8 filters	3x3, 8 filters	5x5, 8 filters
Dense 3	100 neurons	64 neurons	100 neurons
Test Accuracy	88.57 %	87.98 %	87.72 %
Training Time	305s	331s	349s

Table 2.1.b: Top 3 results based on training time.

Smaller filter sizes have smaller training time because there are less parameters and less computation involved. But filters with larger receptive field performs better as they have higher representative power. This effect is more profound for shallow networks like the one we experimented with. Also, netoworks with higher number of filters can represent more features and are likely to have higher performance but compromises on training time. When the number of neurons on the dense layer is incresed, it improves the performance but increases the training time.

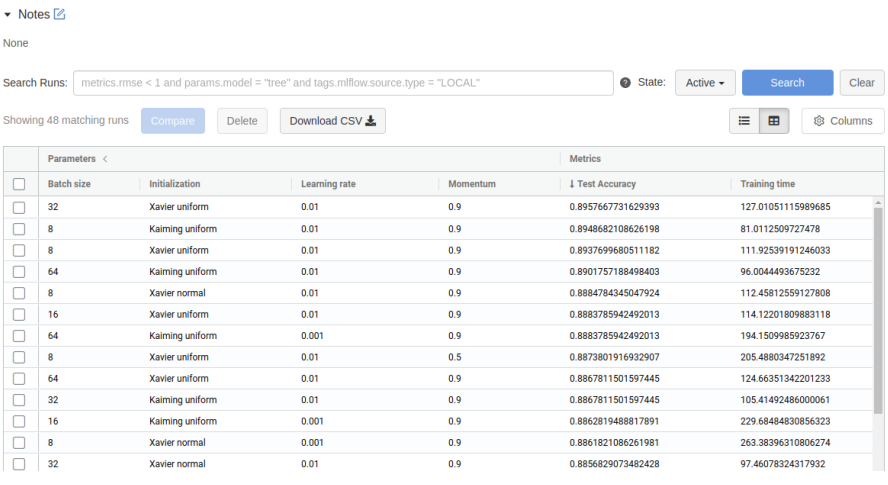
I decided to choose the model with lowest training time for the next experiment because it is acceptable to sacrifice 0.64% of accuracy for 46% reduction in training time.

Experiment 2 was conducted on the model that had the smallest training time.

Hyperparameter	*Values*
Initialisation	Xavier Uniform, Xavier Normal, Kaiming Uniform
Batch sizes	8, 16, 32, 64
Optimizer params	1. Learning rate : 0.001 Momentum : 0.9 2. Learning rate : 0.01 Momentum : 0.9 3. Learning rate : 0.001 Momentum : 0.5 4. Learning rate : 0.01 Momentum : 0.5

Table 2.2:
The search space for experiment 2

Results are as follows.


Notes

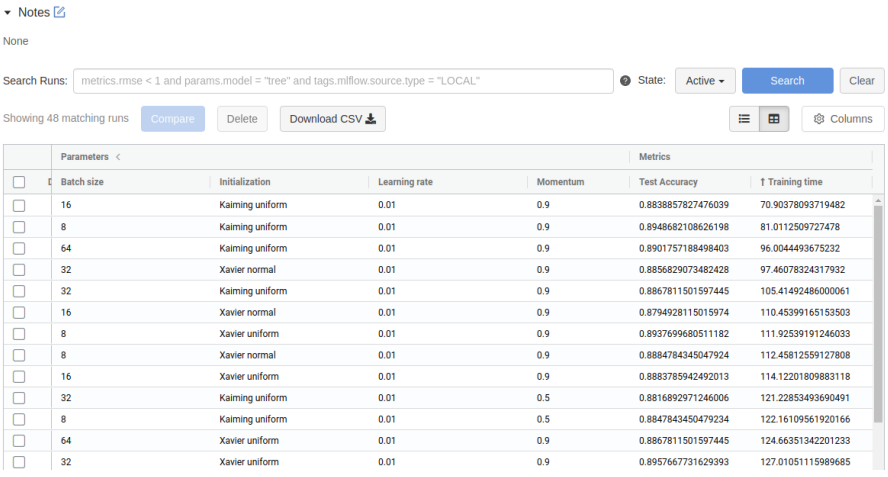
None

Search Runs: metrics.rmse < 1 and params.model = "tree" and tags.mlflow.source.type = "LOCAL" State: Active Search Clear

Showing 48 matching runs Compare Delete Download CSV Columns

	Parameters			Metrics	
Batch size	Initialization	Learning rate	Momentum	↓ Test Accuracy	Training time
32	Xavier uniform	0.01	0.9	0.8957667731629393	127.01051115989685
8	Kaiming uniform	0.01	0.9	0.8948682108626198	81.0112509727478
8	Xavier uniform	0.01	0.9	0.8937699680511182	111.92539191246033
64	Kaiming uniform	0.01	0.9	0.8901757188498403	96.0044493675232
8	Xavier normal	0.01	0.9	0.8884784345047924	112.45812559127808
16	Xavier uniform	0.01	0.9	0.8883785942492013	114.12201809883118
64	Kaiming uniform	0.001	0.9	0.8883785942492013	194.1509985923767
8	Xavier uniform	0.01	0.5	0.8873801916932907	205.4880347251892
64	Xavier uniform	0.01	0.9	0.8867811501597445	124.66351342201233
32	Kaiming uniform	0.01	0.9	0.8867811501597445	105.41492486000061
16	Kaiming uniform	0.001	0.9	0.8862819488817891	229.68484830856323
8	Xavier normal	0.001	0.9	0.8861821086261981	263.38396310806274
32	Xavier normal	0.01	0.9	0.8856829073482428	97.46078324317932

Fig 2.2.a:
Experiment 2 results sorted by decreasing accuracy on the test dataset.


Notes

None

Search Runs: metrics.rmse < 1 and params.model = "tree" and tags.mlflow.source.type = "LOCAL" State: Active Search Clear

Showing 48 matching runs Compare Delete Download CSV Columns

	Parameters			Metrics	
Batch size	Initialization	Learning rate	Momentum	Test Accuracy	↑ Training time
16	Kaiming uniform	0.01	0.9	0.8838857827476039	70.90378093719482
8	Kaiming uniform	0.01	0.9	0.8948682108626198	81.0112509727478
64	Kaiming uniform	0.01	0.9	0.8901757188498403	96.0044493675232
32	Xavier normal	0.01	0.9	0.8856829073482428	97.46078324317932
32	Kaiming uniform	0.01	0.9	0.8867811501597445	105.41492486000061
16	Xavier normal	0.01	0.9	0.8794928115015974	110.45399165153503
8	Xavier uniform	0.01	0.9	0.8937699680511182	111.92539191246033
8	Xavier normal	0.01	0.9	0.8884784345047924	112.45812559127808
16	Xavier uniform	0.01	0.9	0.8883785942492013	114.12201809883118
32	Kaiming uniform	0.01	0.5	0.8816892971246006	121.22853493690491
8	Kaiming uniform	0.01	0.5	0.8847843450479234	122.16109561920166
64	Xavier uniform	0.01	0.9	0.8867811501597445	124.66351342201233
32	Xavier uniform	0.01	0.9	0.8957667731629393	127.01051115989685

Fig 2.2.b:
Experiment 2 results sorted by increasing training time required to reach 90% train accuracy.

Top 3 results are as shown below:

	#1	*#2*	*#3*
Batch size	32	8	8
Initialization	Xavier Uni.	Kaiming Uni.	Xavier Uni.
Learning rate	0.01	0.01	0.01
Momentum	0.9	0.9	0.9
Test Accuracy	89.57 %	89.48 %	89.37 %
Training Time	127s	81s	111s

Table 2.2.a:
Top 3 results based on test accuracy.

	#1	*#2*	*#3*
Batch size	16	8	64
Initialization	Kaiming Uni.	Kaiming Uni.	Kaiming Uni.
Learning rate	0.01	0.01	0.01
Momentum	0.9	0.9	0.9
Test Accuracy	88.38 %	89.48 %	89.01 %
Training Time	70s	81s	96s

Table 2.2.b:
Top 3 results based on training time.

Learning rate of 0.01 performed well in most cases. It converges faster and results in better performance on the test dataset. Also models with momentum of 0.9 outperformed models with momentum of 0.5 because it is better in escaping local minima traps. Kaiming initialization is found to converge faster. A smaller batch size give rise to gradients that are more randomized comparitively. This might help in escaping the local minima traps.

Here are some scatter plots that can help us choose even better models. However, not every one of these plots are conclusive. Plots like the one for learning rate, momentum, and mumber of filters can help us generalise how different models behave according to different hyperparameters. The MLflow logs are converted to CSV files and uploaded to Google Facets.

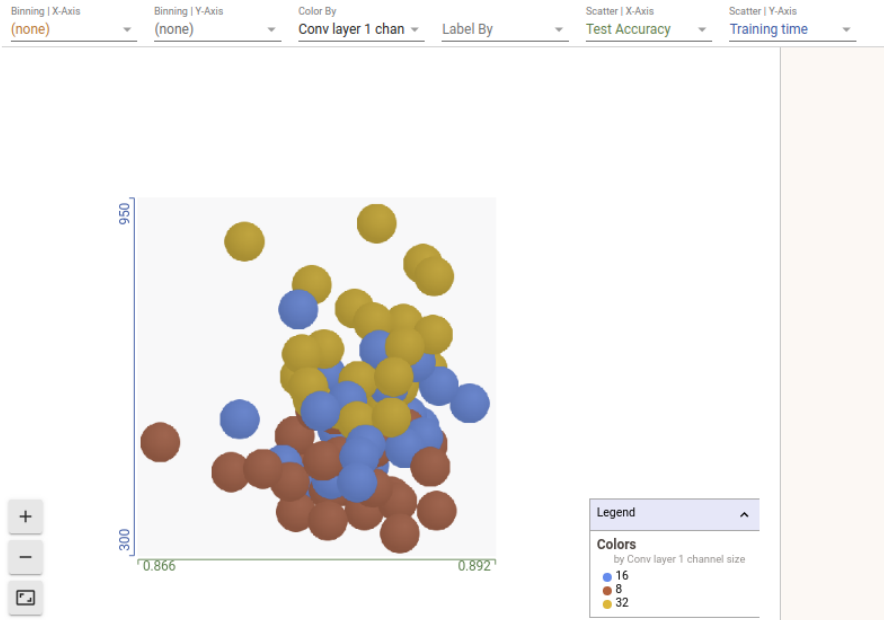


Fig 2.3.a:
Conv 1 no of filters
x-axis : Test accuracy
y-axis: Training time

Fig 2.3.b:
Conv 1 kernel size
x-axis : Test accuracy
y-axis: Training time

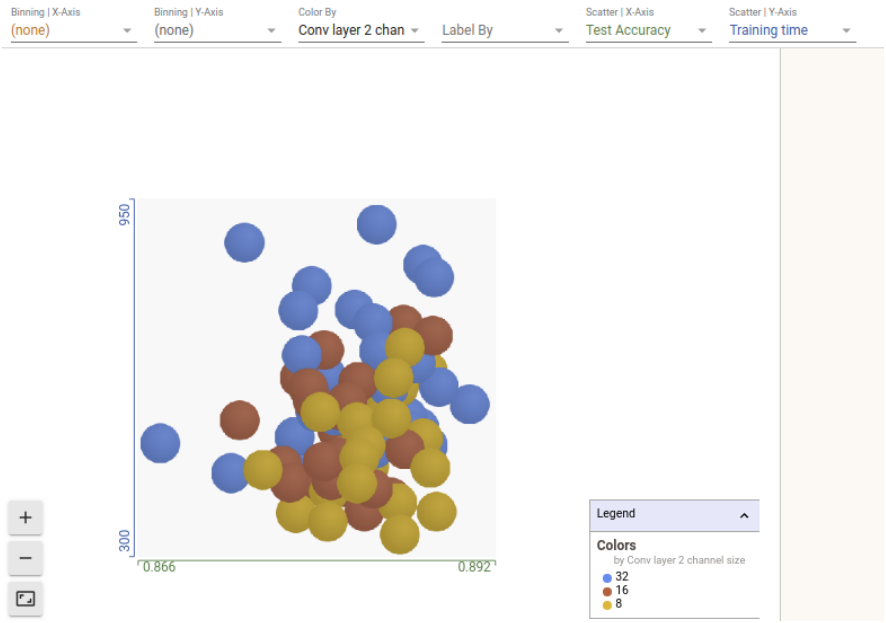


Fig 2.3.c:
Conv 2 no of filters
x-axis : Test accuracy
y-axis: Training time

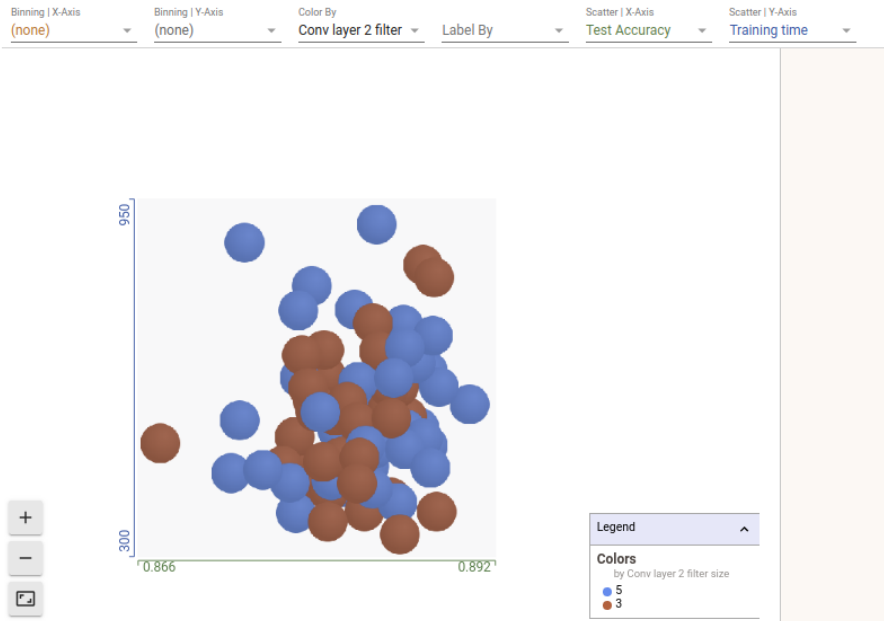


Fig 2.3.d:
Conv 2 kernel size
x-axis : Test accuracy
y-axis: Training time

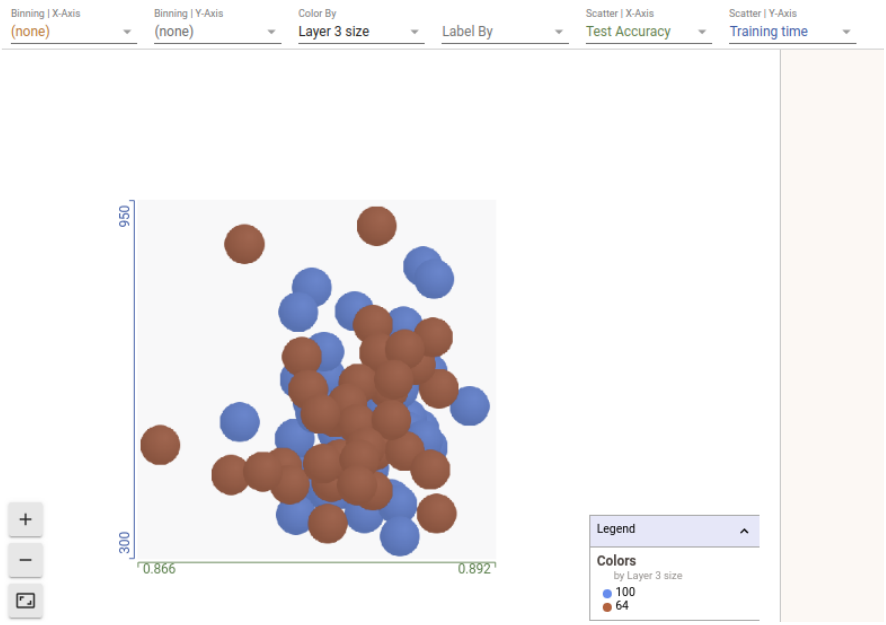


Fig 2.3.e:
Number of neurons in layer 3
x-axis : Test accuracy
y-axis: Training time

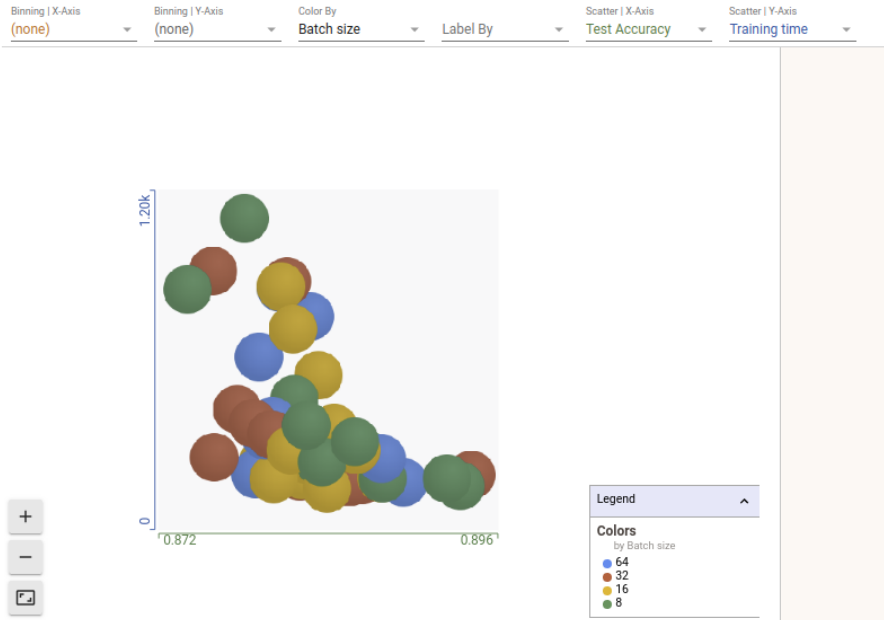


Fig 2.3.f:
Batch size
x-axis : Test accuracy
y-axis: Training time

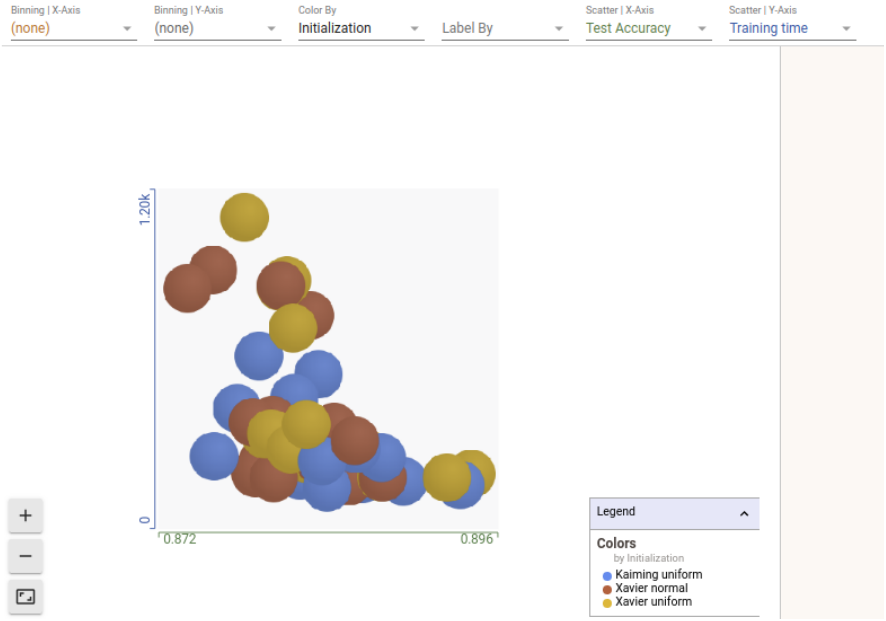


Fig 2.3.g:
Initialization
x-axis : Test accuracy
y-axis: Training time

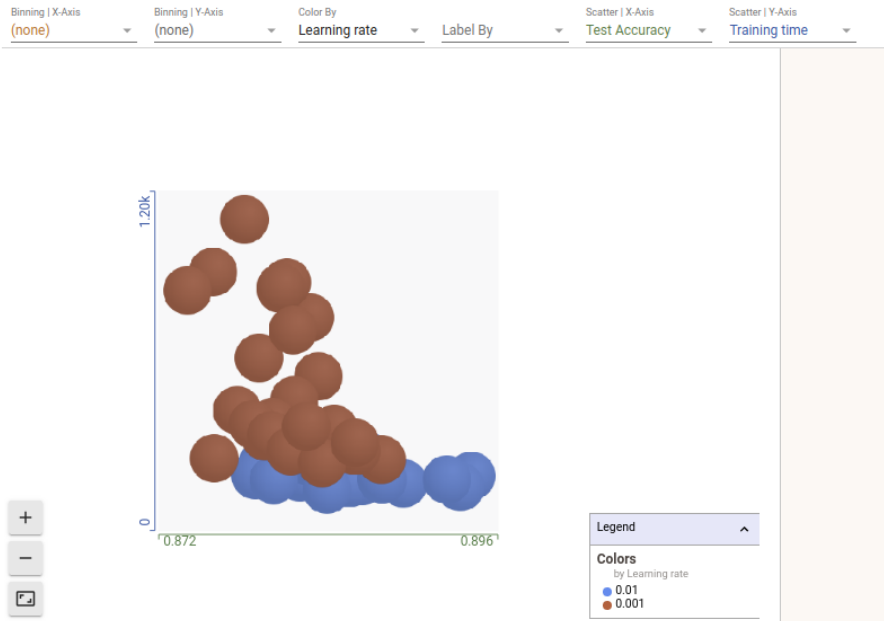


Fig 2.3.h:
Learning rate
x-axis : Test accuracy
y-axis: Training time

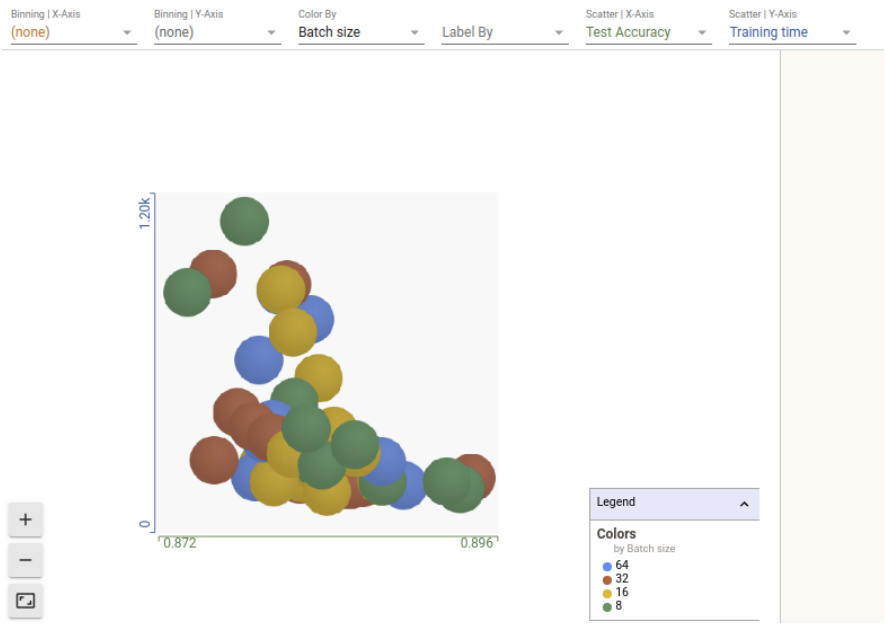


Fig 2.3.i:
Momentum
x-axis : Test accuracy
y-axis: Training time

The pareto plots of all models with respect to testing accuracy and training time are as given below.

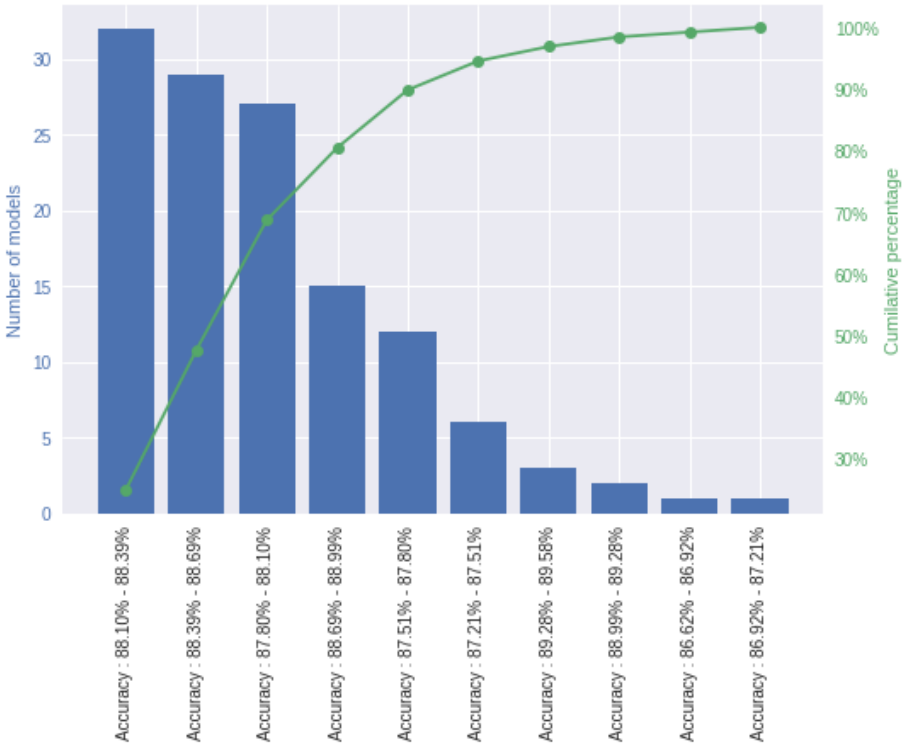


Fig 2.4.a:
Pareto plot of all models with respect to testing accuracy.

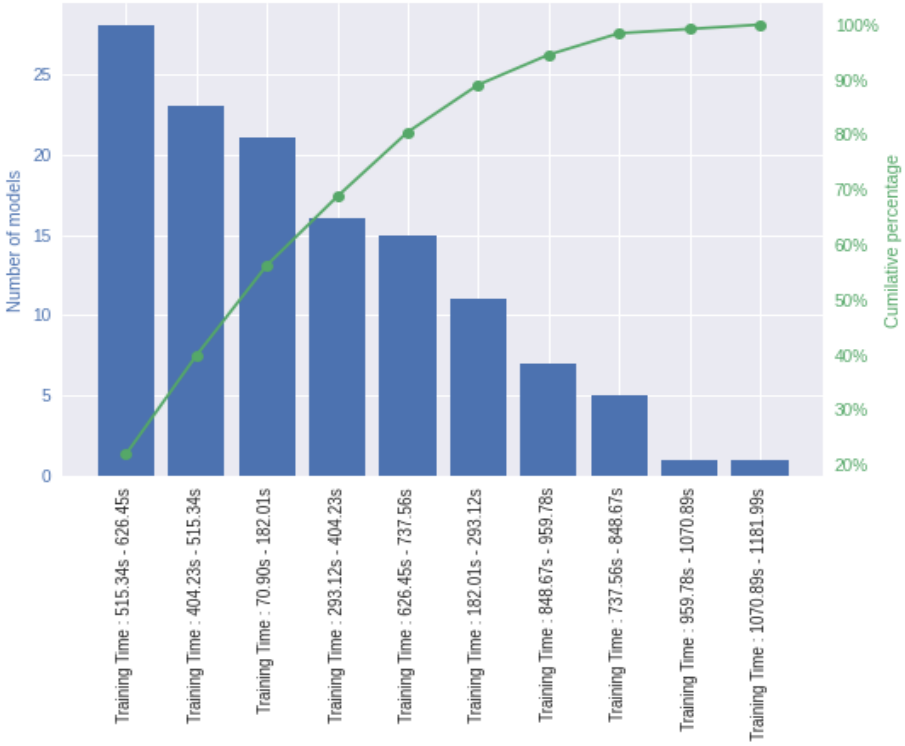


Fig 2.4.b:
Pareto plot of all models with respect to training time.

Loss vs epoch/batches plots for some special cases asked in the question are given below.

Learning rate too high: The largest learning rate used for the experiment was 0.01. This is not a high learning rate. Therfore to produce the plot, I trained a model separately with learning rate. We can see that the loss plot has got many irregular jumps.

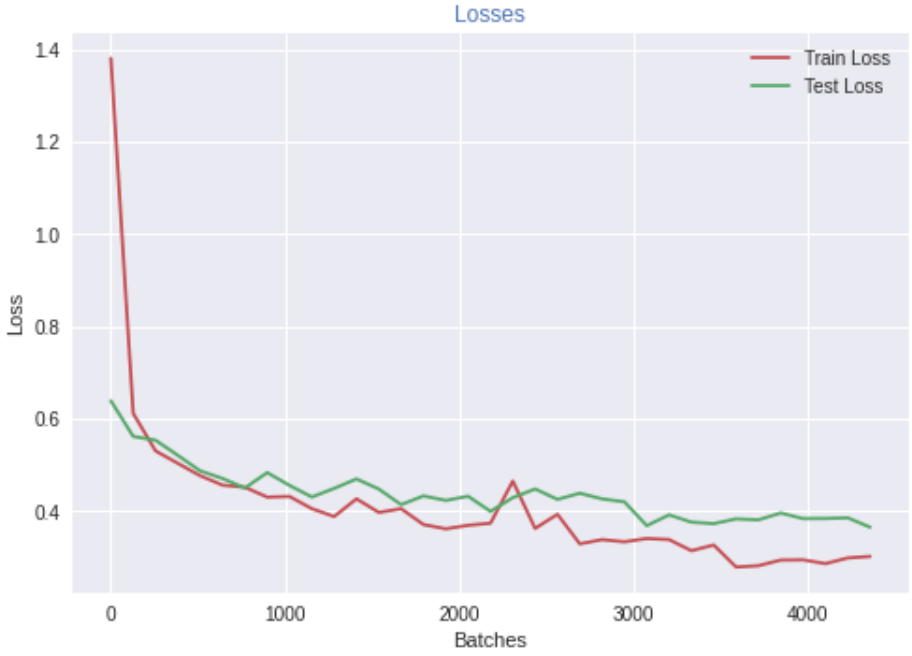


Fig 2.5.a: High learning rate (0.05). Loss plot has irregular jumps.

Learning rate too low: The MLflow experiment did not contain any examples for low learning rates. So I trained a separate model to demonstrate. The network is taking longer to converge.

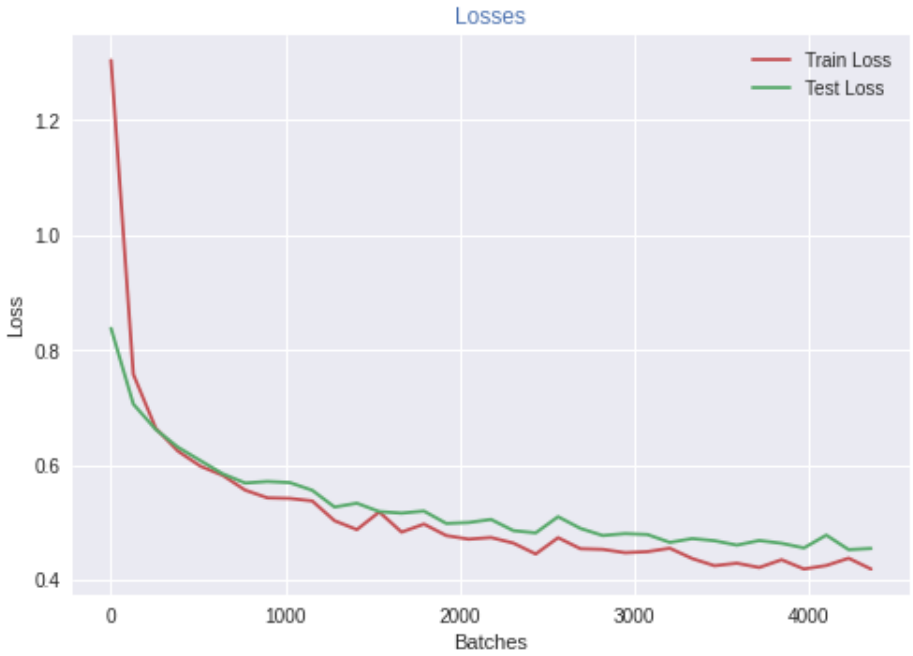


Fig 2.5.b: Low learning rate (0.0001). Loss plot takes very longer to converge.

Momentum too high: This plot is also generated by running an experement separately. We can see that the plot has got an oscillatory nature. The model oscillates around local minimas. Sometimes the network is able to escape local minimas, but sometimes it keeps on oscillating.

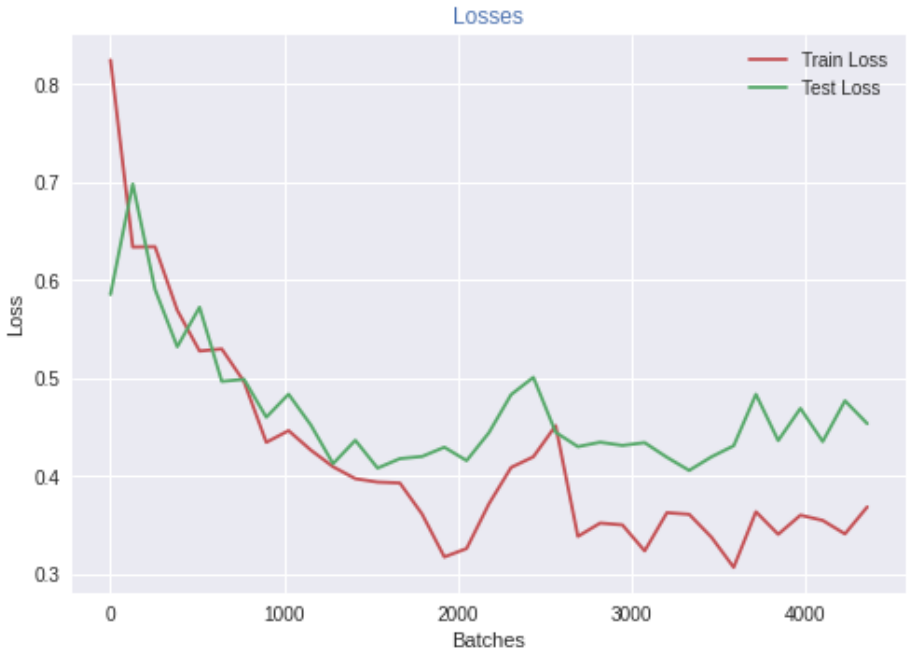


Fig 2.5.c:
High momentum (0.99, lr: 0.001). The loss oscillates too much.

Batch size too low: When a network is trained using stochastic gradient descend on a very small batch size. The updates become more randomized. The plot below shows a network trained with batch size of 4. All other settings were similar to that of the above given networks.

Fig 2.5.d:
Low batch size. All the updates become more approximate and randomized, thus leading to a rugged loss plot.

Overfitting due to large model: The experiments conducted did not have any good exaples of overfitting. So a different larger model was trained to demonstrate the effect. This example was trained longer than others to make the effect more profound. We can see the test loss actually diverging.

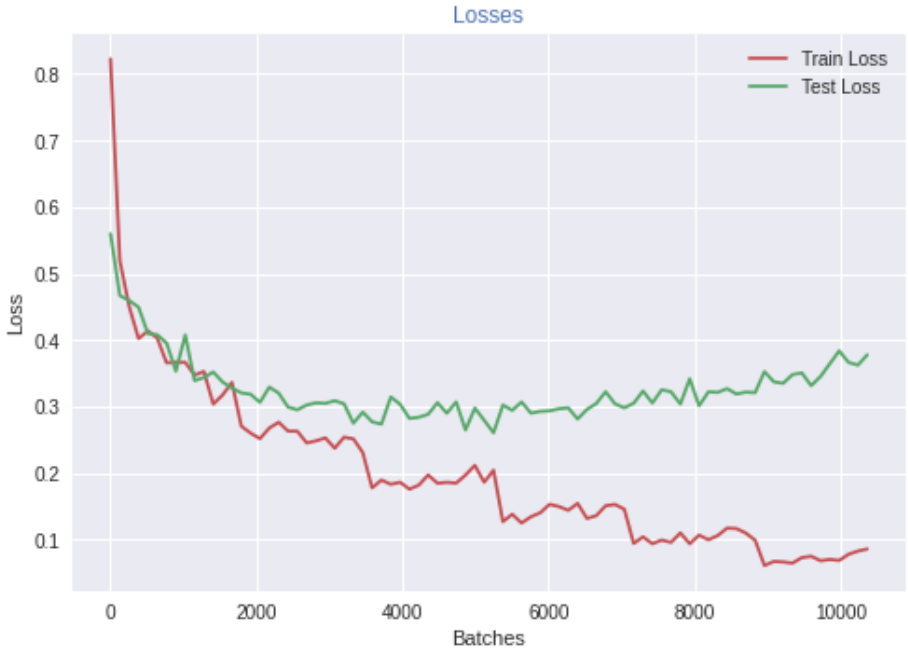


Fig 2.5.e: Overfitting on a large model.(Conv 5x5, 64; Conv 5x5, 64; 100 neurons)