

---

# **sasoptpy Documentation**

***Release 1.0.0***

**SAS Institute Inc.**

**Apr 28, 2020**



# CONTENTS

<b>1</b>	<b>Overview</b>	<b>3</b>
1.1	About sasoptpy . . . . .	3
1.2	What's New . . . . .	5
1.3	License . . . . .	5
<b>2</b>	<b>Installation</b>	<b>9</b>
2.1	Python Version Support and Dependencies . . . . .	9
2.2	Getting sasoptpy . . . . .	9
<b>3</b>	<b>User Guide</b>	<b>11</b>
3.1	Introduction to Optimization . . . . .	11
3.2	Quick Reference . . . . .	13
3.3	Sessions . . . . .	20
3.4	Models . . . . .	21
3.5	Model Components . . . . .	31
3.6	Workspaces . . . . .	37
3.7	Handling Data . . . . .	43
3.8	Workflows . . . . .	48
<b>4</b>	<b>Examples</b>	<b>57</b>
4.1	SAS Viya Examples (Concrete) . . . . .	57
4.2	SAS Viya Examples (Abstract) . . . . .	143
4.3	SAS 9.4 Examples . . . . .	159
<b>5</b>	<b>API Reference</b>	<b>167</b>
5.1	Core . . . . .	167
5.2	Abstract . . . . .	225
5.3	Interface . . . . .	232
5.4	Functions . . . . .	239
5.5	Tests . . . . .	266
<b>6</b>	<b>Version History</b>	<b>273</b>
6.1	v0.2.1 (February 26, 2019) . . . . .	273
6.2	v0.2.0 (July 30, 2018) . . . . .	274
6.3	v0.1.2 (April 24, 2018) . . . . .	275
6.4	v0.1.1 (February 26, 2018) . . . . .	276
6.5	v0.1.0 (December 22, 2017) . . . . .	277
	<b>Python Module Index</b>	<b>279</b>
	<b>Index</b>	<b>281</b>



## PDF Version

**Date:** Apr 28, 2020 | **Version:** 1.0 | **Release:** 1.0.0 | **Reference:** 1.0.0-9-g347d8932

**Links:** [Repository](#) | [Issues](#) | [Releases](#) | [Community](#)

sasoptpy is a Python package that provides a modeling interface for SAS Optimization and SAS/OR optimization solvers. It provides a quick way for users to deploy optimization models and solve them using SAS Viya and SAS 9.4.

sasoptpy can handle linear, mixed integer linear, nonlinear, and black-box optimization problems. You can use native Python structures such as dictionaries, tuples, and lists to define an optimization problem. sasoptpy offers extensive support of [pandas](#) objects.

Under the hood, sasoptpy uses the [SAS Scripting Wrapper for Analytic Transfer \(SWAT\)](#) package to communicate with SAS Viya, and uses the [SASPy](#) package to communicate with SAS 9.4 installations.

sasoptpy is an interface to SAS Optimization solvers. See [SAS Optimization: Mathematical Optimization Procedures](#) for more information about SAS optimization tools.

See the SAS Global Forum paper: [Optimization Modeling with Python and SAS Viya](#)



## **OVERVIEW**

### **1.1 About sasoptpy**

sasoptpy is a Python package that provides easy and integrated ways of working with optimization solvers in SAS Optimization and SAS/OR. It enables developers to model optimization problems with ease by providing high-level building blocks.

#### **1.1.1 Capabilities**

sasoptpy is very flexible in terms of the optimization problem types and workflow alternatives.

##### **Solvers**

sasoptpy currently supports the following problem types:

- Linear problems
- Integer linear problems / Mixed integer linear problems
- Quadratic problems
- Nonlinear problems
- Black-box problems

##### **Data**

sasoptpy supports working with both client-side data and server-side data. When data are available on the client, it populates the model with integrated data and brings the solution back to the client. When data are available on the server, it generates the code to populate the model on the server. You can retrieve the final solution afterward.

## Platforms

sasoptpy can be used with SAS Viya 3.3 or later and SAS 9.4, in all the supported operating systems.

### 1.1.2 Road Map

The goal of sasoptpy is to support all the functionality of the SAS Optimization and SAS/OR solvers and provide a high-level set of tools for easily working with models.

### 1.1.3 Versioning

sasoptpy follows [Semantic Versioning](#) as of version 1.0.0.

- Any backward incompatible changes increase the major version number (X.y.z).
- Minor changes and improvements increase the the minor version number (x.Y.z).
- Patches increase the patch version number (x.y.Z).
- Pre-releases are marked by using *alpha* and *beta*, and release candidates are marked by using *rc* identifiers.

### 1.1.4 License

sasoptpy is an open-source package and uses the standard [Apache 2.0 license](#).

### 1.1.5 Support

Have any questions?

- If you have a package-related issue, feel free to report it on [GitHub](#).
- If you have an optimization-related question, consider asking it on [SAS Communities](#).
- For further technical support, contact [SAS Technical Support](#).

### 1.1.6 Contribution

Contributions are always welcome. Clone the project to your working environment and submit pull requests as you see fit. For more information, see the guidelines at the GitHub repository.

### 1.1.7 Highlighted Works

A list of highlighted projects and blog posts:

- [Fastest, cheapest, greenest: How will football fans choose which matches to attend?](#)
- [1 tournament, 12 countries: A logistical maze?](#)
- [Using SAS Optimization with Python and containers](#)
- [Bringing Analytics to the Soccer Transfer Season](#)
- [Visiting all 30 Major League Baseball Stadiums - with Python and SAS Viya](#)



## 1.2 What's New

### 1.2.1 New Features

- Added workspaces; for more information, see *Workspaces in User Guide* and *Efficiency Analysis example*
- Added *package configurations*
- Added *abstract actions* that allow server-side operations. Highlights include:
  - `actions.read_data()` and `actions.create_data()`
  - `actions.for_loop()` and `actions.cofor_loop()`
  - `actions.print_item()`
  - `actions.solve()`
- Added structure decorators for better control of submissions

### 1.2.2 Changes

- Refactored the entire package; sasoptpy now has *core*, *abstract*, *interface*, *session*, and *util* directories
- Experimental RESTful API was dropped
- `get_obj_by_name` function was removed
- *Iso* solver was renamed *blackbox*
- Because of the use of literal strings ([PEP 498](#)), only Python 3.6 or later versions are supported

### 1.2.3 Bug Fixes

- Fixed: Arithmetic operations with powers are generating incorrect results
- Fixed: Variable groups with space in their index are not getting values
- Fixed: Constraints without directions do not produce an error
- Fixed: Documentation does not mention conda-forge library requirement
- Fixed: Single-dimensional parameters are hard to access

## 1.3 License

Apache License  
Version 2.0, January 2004  
<http://www.apache.org/licenses/>

TERMS AND CONDITIONS FOR USE, REPRODUCTION, AND DISTRIBUTION

1. Definitions.

"License" shall mean the terms and conditions for use, reproduction, and distribution as defined by Sections 1 through 9 of this document.

(continues on next page)

(continued from previous page)

"Licensor" shall mean the copyright owner or entity authorized by the copyright owner that is granting the License.

"Legal Entity" shall mean the union of the acting entity and all other entities that control, are controlled by, or are under common control with that entity. For the purposes of this definition, "control" means (i) the power, direct or indirect, to cause the direction or management of such entity, whether by contract or otherwise, or (ii) ownership of fifty percent (50%) or more of the outstanding shares, or (iii) beneficial ownership of such entity.

"You" (or "Your") shall mean an individual or Legal Entity exercising permissions granted by this License.

"Source" form shall mean the preferred form for making modifications, including but not limited to software source code, documentation source, and configuration files.

"Object" form shall mean any form resulting from mechanical transformation or translation of a Source form, including but not limited to compiled object code, generated documentation, and conversions to other media types.

"Work" shall mean the work of authorship, whether in Source or Object form, made available under the License, as indicated by a copyright notice that is included in or attached to the work (an example is provided in the Appendix below).

"Derivative Works" shall mean any work, whether in Source or Object form, that is based on (or derived from) the Work and for which the editorial revisions, annotations, elaborations, or other modifications represent, as a whole, an original work of authorship. For the purposes of this License, Derivative Works shall not include works that remain separable from, or merely link (or bind by name) to the interfaces of, the Work and Derivative Works thereof.

"Contribution" shall mean any work of authorship, including the original version of the Work and any modifications or additions to that Work or Derivative Works thereof, that is intentionally submitted to Licensor for inclusion in the Work by the copyright owner or by an individual or Legal Entity authorized to submit on behalf of the copyright owner. For the purposes of this definition, "submitted" means any form of electronic, verbal, or written communication sent to the Licensor or its representatives, including but not limited to communication on electronic mailing lists, source code control systems, and issue tracking systems that are managed by, or on behalf of, the Licensor for the purpose of discussing and improving the Work, but excluding communication that is conspicuously marked or otherwise designated in writing by the copyright owner as "Not a Contribution."

"Contributor" shall mean Licensor and any individual or Legal Entity on behalf of whom a Contribution has been received by Licensor and subsequently incorporated within the Work.

2. Grant of Copyright License. Subject to the terms and conditions of this License, each Contributor hereby grants to You a perpetual, worldwide, non-exclusive, no-charge, royalty-free, irrevocable

(continues on next page)

(continued from previous page)

copyright license to reproduce, prepare Derivative Works of, publicly display, publicly perform, sublicense, and distribute the Work and such Derivative Works in Source or Object form.

3. Grant of Patent License. Subject to the terms and conditions of this License, each Contributor hereby grants to You a perpetual, worldwide, non-exclusive, no-charge, royalty-free, irrevocable (except as stated in this section) patent license to make, have made, use, offer to sell, sell, import, and otherwise transfer the Work, where such license applies only to those patent claims licensable by such Contributor that are necessarily infringed by their Contribution(s) alone or by combination of their Contribution(s) with the Work to which such Contribution(s) was submitted. If You institute patent litigation against any entity (including a cross-claim or counterclaim in a lawsuit) alleging that the Work or a Contribution incorporated within the Work constitutes direct or contributory patent infringement, then any patent licenses granted to You under this License for that Work shall terminate as of the date such litigation is filed.
4. Redistribution. You may reproduce and distribute copies of the Work or Derivative Works thereof in any medium, with or without modifications, and in Source or Object form, provided that You meet the following conditions:
  - (a) You must give any other recipients of the Work or Derivative Works a copy of this License; and
  - (b) You must cause any modified files to carry prominent notices stating that You changed the files; and
  - (c) You must retain, in the Source form of any Derivative Works that You distribute, all copyright, patent, trademark, and attribution notices from the Source form of the Work, excluding those notices that do not pertain to any part of the Derivative Works; and
  - (d) If the Work includes a "NOTICE" text file as part of its distribution, then any Derivative Works that You distribute must include a readable copy of the attribution notices contained within such NOTICE file, excluding those notices that do not pertain to any part of the Derivative Works, in at least one of the following places: within a NOTICE text file distributed as part of the Derivative Works; within the Source form or documentation, if provided along with the Derivative Works; or, within a display generated by the Derivative Works, if and wherever such third-party notices normally appear. The contents of the NOTICE file are for informational purposes only and do not modify the License. You may add Your own attribution notices within Derivative Works that You distribute, alongside or as an addendum to the NOTICE text from the Work, provided that such additional attribution notices cannot be construed as modifying the License.

You may add Your own copyright statement to Your modifications and may provide additional or different license terms and conditions for use, reproduction, or distribution of Your modifications, or

(continues on next page)

(continued from previous page)

for any such Derivative Works as a whole, provided Your use, reproduction, and distribution of the Work otherwise complies with the conditions stated in this License.

5. Submission of Contributions. Unless You explicitly state otherwise, any Contribution intentionally submitted for inclusion in the Work by You to the Licensor shall be under the terms and conditions of this License, without any additional terms or conditions. Notwithstanding the above, nothing herein shall supersede or modify the terms of any separate license agreement you may have executed with Licensor regarding such Contributions.
6. Trademarks. This License does not grant permission to use the trade names, trademarks, service marks, or product names of the Licensor, except as required for reasonable and customary use in describing the origin of the Work and reproducing the content of the NOTICE file.
7. Disclaimer of Warranty. Unless required by applicable law or agreed to in writing, Licensor provides the Work (and each Contributor provides its Contributions) on an "AS IS" BASIS, WITHOUT WARRANTIES OR CONDITIONS OF ANY KIND, either express or implied, including, without limitation, any warranties or conditions of TITLE, NON-INFRINGEMENT, MERCHANTABILITY, or FITNESS FOR A PARTICULAR PURPOSE. You are solely responsible for determining the appropriateness of using or redistributing the Work and assume any risks associated with Your exercise of permissions under this License.
8. Limitation of Liability. In no event and under no legal theory, whether in tort (including negligence), contract, or otherwise, unless required by applicable law (such as deliberate and grossly negligent acts) or agreed to in writing, shall any Contributor be liable to You for damages, including any direct, indirect, special, incidental, or consequential damages of any character arising as a result of this License or out of the use or inability to use the Work (including but not limited to damages for loss of goodwill, work stoppage, computer failure or malfunction, or any and all other commercial damages or losses), even if such Contributor has been advised of the possibility of such damages.
9. Accepting Warranty or Additional Liability. While redistributing the Work or Derivative Works thereof, You may choose to offer, and charge a fee for, acceptance of support, warranty, indemnity, or other liability obligations and/or rights consistent with this License. However, in accepting such obligations, You may act only on Your own behalf and on Your sole responsibility, not on behalf of any other Contributor, and only if You agree to indemnify, defend, and hold each Contributor harmless for any liability incurred by, or claims asserted against, such Contributor by reason of your accepting any such warranty or additional liability.

END OF TERMS AND CONDITIONS

## INSTALLATION

### 2.1 Python Version Support and Dependencies

Current version is developed and tested for Python 3.6 and later.

It requires the following packages:

- NumPy
- SASPy
- SWAT
- pandas

### 2.2 Getting sasoptpy

You can install sasoptpy by using *pip* or *conda*:

```
pip install sasoptpy  
conda install -c sas-institute sasoptpy
```

Any dependencies are installed automatically.

Depending on your installation, you might need to add the *conda-forge* channel to *conda*:

```
conda config --append channels conda-forge
```

#### 2.2.1 GitHub repository

You can also get stable and development versions of sasoptpy from the GitHub repository. To get the latest version, call:

```
git clone https://github.com/sassoftware/sasoptpy.git
```

Then inside the sasoptpy folder, call:

```
pip install .
```

Alternatively, you can use:

```
python setup.py install
```

## 3.1 Introduction to Optimization

Optimization is an umbrella term for maximizing or minimizing a specified target; given as a mathematical function. Optimization is often used in real-life problems from finance to aviation, from chemistry to sports analytics.

Optimization problems can describe a business problem or a physical concept. Any phenomenon that can be represented as a function can be optimized by several algorithms. Optimization lies at the heart of several tools you use every day, from routing to machine learning.

### 3.1.1 Steps of Optimization

Optimization problems often consist of the following steps:<sup>1,2</sup>

1. Observe the system and define the problem.
2. Gather relevant data.
3. Develop a formulation.
4. Solve the model.
5. Interpret the solution.

A modeler observes the process in order to identify the problems and potential improvements. Several examples of optimization problems are finding the shortest path between two locations, maximizing a profit, and maximizing the accuracy of a handwriting recognition algorithm.

Collecting data is often the most daunting process. In the age of big data, it is often difficult to distinguish noise from relevant data. After data are gathered, you can write a formulation. A proper formulation is critical because features such as linearity and convexity greatly impact the performance of solution algorithms, especially for large problems.

Solving a problem requires an optimization algorithm. SAS Optimization provides several optimization algorithms to solve a variety of different problem types. For more information, see *Types of Optimization*.

Finally, the modeler decides whether the result of an optimization process is valid. If not, the process is repeated by adding the missing pieces until a satisfactory result is obtained.

---

<sup>1</sup> Hillier, Frederick S., and Gerald J. Lieberman. Introduction to operations research. McGraw-Hill Science, Engineering & Mathematics, 1995.

<sup>2</sup> SAS Institute. SAS/OR 15.1 User's Guide: Mathematical Programming Examples. SAS institute, 2018.

### 3.1.2 Basic Elements

An optimization formulation has the following elements:

- *Variables* are parameters that the optimization algorithm tunes. An optimization algorithm determines optimal values for variables in the problem. As an example, in an optimization problem of finding a route from your home to the airport, which roads to use are decision variables.
- An *objective* is a performance measure that is to be maximized or minimized. An objective is a function of variables in an optimization problem, meaning an objective value is obtained for specified values of variables. In the home to airport route example, the objective function is the time to reach the airport. The optimization algorithm decides which roads to use in order to minimize the travel time.
- *Constraints* are restrictions on variables that are added in order to prevent illogical or undesired solutions. In the example, the amount of fuel in the car restricts how far you can drive. You can the force optimization algorithm to find a solution under a certain mileage, even if there are other solutions that might be shorter in terms of travel time.

In short, *optimization* consists of choosing *variable* values to maximize or minimize an *objective* function subject to certain *constraints*.

### 3.1.3 Simple Problem

Consider a simple example. The following problem (brewer's dilemma) is a simplified resource allocation problem, presented by Robert G. Bland.<sup>3</sup>

In the problem, a brewer has limited corn, hops, and barley malt inventory. The brewer wants to produce ale and beer that will maximize the total profit. Each product requires a certain amount of these three ingredients, as follows:

(per barrel)	Amount Required			
Product	Corn (Pounds)	Hops (Ounces)	Barley Malt (Pounds)	Profit (\$)
Ale	5	4	35	13
Beer	15	4	20	23
(Total Available)	480	160	1,190	

The variables (*ale* and *beer*) in this problem are the number of barrels of ale and beer to produce. It might be intuitive to prefer beer to ale because of its higher profit rate. However, doing so might deplete all the resources faster and might leave you with an excess amount of hops and barley malt.

The objective in this problem is to maximize the total profit function, which is  $13 \times \text{ale} + 23 \times \text{beer}$ .

Each limitation on ingredients is a constraint. For corn, hops, and barley malt, the following constraints apply:

$$5 \times \text{ale} + 15 \times \text{beer} \leq 480$$

$$4 \times \text{ale} + 4 \times \text{beer} \leq 160$$

$$35 \times \text{ale} + 20 \times \text{beer} \leq 1,190$$

Combining all items, the optimization formulation is written as follows:

$$\begin{array}{ll}
 \text{maximize:} & 13 \times \text{ale} + 23 \times \text{beer} \\
 \text{subject to:} & \\
 & 5 \times \text{ale} + 15 \times \text{beer} \leq 480 \\
 & 4 \times \text{ale} + 4 \times \text{beer} \leq 160 \\
 & 35 \times \text{ale} + 20 \times \text{beer} \leq 1,190 \\
 & \text{ale} \geq 0 \\
 & \text{beer} \geq 0
 \end{array}$$

<sup>3</sup> Bland, Robert G. "The Allocation of Resources by Linear Programming." Scientific American 244 (1981): 126-144.



This problem is small enough to be solved by hand, but consider some alternatives.

#	Barrels Produced		Profit (\$)
	Ale	Beer	
1	34	0	442
2	0	32	736
3	15	25	770
4	12	28	800

The preceding table indicates that producing only ale or beer creates less profit than producing a combination of the two. Alternative solution 4 gives the optimal values that maximize the profit in this example.

Following are additional examples of problems that can be formulated as optimization problems:

- scheduling project steps to minimize total completion time, where some tasks might depend on completion of earlier tasks
- choosing distribution centers for retailers to minimize total cost while satisfying customer demands on delivery time
- assigning soccer players to a squad to maximize the total rating of the team under foreign player rules
- finding the cheapest travel option and shortest route between two cities
- blending chemical products to minimize the total cost while achieving a certain efficiency of detergents
- choosing a price that will maximize the total profit in a competitive market

For more information about optimization problems and examples, see the related section of [SAS Optimization Mathematical Optimization Procedures](#).

### 3.1.4 Types of Optimization

The structure of a formulation affects which algorithms can be deployed to solve a problem. The most common optimization types are as follows:

- **Linear optimization:** If the objective function and all constraints of a problem can be described by linear mathematical relations and if all decision variables are continuous, the formulation is called a linear problem (LP). LPs are among the easiest problems in terms of solution time and are well-studied in literature.
- **Mixed integer linear optimization:** If a linear formulation involves binary (yes or no type decisions), or integer variables, the problem is an integer linear problem (ILP) or mixed integer linear problem (MILP), depending on the variables. MILPs are very popular as many real-life problems can be represented as MILPs.
- **Nonlinear optimization:** If a problem involves nonlinear objectives or constraints (such as exponential, polynomial, or absolute values), the problem is called a nonlinear problem (NLP).

## 3.2 Quick Reference

This is a short introduction to sasoptpy functionality, mainly for new users. You can find more details in the linked chapters.

Using sasoptpy usually consists of the following steps:

1. Create a *CAS session* or a *SAS session*
2. Initialize the *model*

3. Process the *input data*
4. Add the *model components*
5. *Solve the model*

Solving an optimization problem via sasoptpy starts with having a running CAS (SAS Viya) Server or having a SAS 9.4 installation. It is possible to model a problem without a connection but solving a problem requires access to SAS Optimization or SAS/OR solvers at runtime.

### 3.2.1 Creating a session

#### Creating a SAS Viya session

To create a SAS Viya session (also called a CAS session), see [SWAT documentation](#). A simple connection can be made using:

```
In [1]: from swat import CAS
In [2]: s = CAS(hostname, port, userid, password)
```

The last two parameters are optional for some use cases.

#### Creating a SAS 9.4 session

To create a SAS 9.4 session (also called a SAS session), see [SASPy documentation](#). After customizing the configurations for your setup, you can create a session as follows:

```
import saspy
s = saspy.SASsession(cfgname='winlocal')
```

### 3.2.2 Initializing a model

After creating a CAS or SAS session, you can create an empty model as follows:

```
In [3]: import sasoptpy as so
In [4]: m = so.Model(name='my_first_model', session=s)
NOTE: Initialized model my_first_model.
```

This command initializes the optimization model as a *Model* object, called *m*.

### 3.2.3 Processing input data

The easiest way to work with sasoptpy is to define problem inputs as pandas DataFrames. You can define objective and cost coefficients, and lower and upper bounds by using the DataFrame and Series objects, respectively. See [pandas documentation](#) to learn more.

```
In [5]: import pandas as pd
In [6]: prob_data = pd.DataFrame([
...:     ['Period1', 30, 5],
...:     ['Period2', 15, 5],
```

(continues on next page)

(continued from previous page)

```

....:      ['Period3', 25, 0]
....:      ], columns=['period', 'demand', 'min_prod']).set_index(['period'])
....:

In [7]: price_per_product = 10

In [8]: capacity_cost = 10

```

You can refer the set PERIODS and the other fields demand and min\_production as follows:

```

In [9]: PERIODS = prob_data.index.tolist()

In [10]: demand = prob_data['demand']

In [11]: min_production = prob_data['min_prod']

```

### 3.2.4 Adding variables

You can add a single variable or a set of variables to *Model* objects.

- *Model.add\_variable()* method is used to add a single variable.

```

In [12]: production_cap = m.add_variable(vartype=so.INT, name='production_cap',
    ↪ lb=0)

```

When working with multiple models, you can create a variable independent of the model, such as

```
>>> production_cap = so.Variable(name='production_cap', vartype=so.INT, lb=0)
```

Then you can add it to an existing model by using *Model.include()*:

```
>>> m.include(production_cap)
```

- *Model.add\_variables()* method is used to add a set of variables.

```

In [13]: production = m.add_variables(PERIODS, vartype=so.INT, name='production',
    ....:                               lb=min_production)
    ....:
    ....:

```

When the input is a set of variables, you can retrieve individual variables by using individual keys, such as `production['Period1']`. To create multidimensional variables, simply list all the keys as follows:

```
>>> multivar = m.add_variables(KEYS1, KEYS2, KEYS3, name='multivar')
```

### 3.2.5 Creating expressions

*Expression* objects hold mathematical expressions. Although these objects are mostly used under the hood when defining a model, it is possible to define a custom *Expression* to use later.

When *Variable* objects are used in a mathematical expression, sasoptpy creates an *Expression* object automatically:

```
In [14]: totalRevenue = production.sum('*')*price_per_product
In [15]: totalCost = production_cap * capacity_cost
```

Note the use of the `VariableGroup.sum()` method over a variable group. This method returns the sum of variables inside the group as an `Expression` object. Its multiplication with a scalar `price_per_product` gives the final expression.

Similarly, `totalCost` is simply multiplication of a `Variable` object with a scalar.

### 3.2.6 Setting an objective function

You can define objective functions in terms of expressions. In this problem, the objective is to maximize the profit, so the `Model.set_objective()` method is used as follows:

```
In [16]: m.set_objective(totalRevenue-totalCost, sense=so.MAX, name='totalProfit')
Out [16]: sasoptpy.Expression(exp = 10 * production[Period1] + 10 *
↳ production[Period2] + 10 * production[Period3] - 10 * production_cap, name=
↳ 'totalProfit')
```

Notice that you can define the same objective by using:

```
>>> m.set_objective(production.sum('*')*price_per_product - production_cap*capacity_
↳ cost, sense=so.MAX, name='totalProfit')
```

The mandatory argument `sense` should be assigned the value of either `so.MIN` for a minimization problem or `so.MAX` for a maximization problems.

### 3.2.7 Adding constraints

In `sasoptpy`, constraints are simply expressions that have a direction. It is possible to define an expression and add it to a model by defining which direction the linear relation should have.

There are two methods to add constraints. The first is `Model.add_constraint()`, which adds a single constraint to a model.

The second is `Model.add_constraints()`, which adds multiple constraints to a model.

```
In [17]: m.add_constraints((production[i] <= production_cap for i in PERIODS),
.....:                    name='capacity')
.....:
Out [17]: sasoptpy.ConstraintGroup([production[Period1] - production_cap <= 0,
↳ production[Period2] - production_cap <= 0, production[Period3] - production_cap <=
↳ 0], name='capacity')
```

```
In [18]: m.add_constraints((production[i] <= demand[i] for i in PERIODS),
.....:                    name='demand')
.....:
Out [18]: sasoptpy.ConstraintGroup([production[Period1] <= 30, production[Period2] <=
↳ 15, production[Period3] <= 25], name='demand')
```

The first term, provides a Python generator, which is then translated into constraints in the problem. The symbols `<=`, `>=`, and `==` are used for less than or equal to, greater than or equal to, and equal to, respectively. You can define range constraints by using the `==` symbol followed by a list of two values that represent lower and upper bounds.

```
In [19]: m.add_constraint(production['Period1'] == [10, 100], name='production_bounds
↳')
Out[19]: sasoptpy.Constraint(production[Period1] == [10, 100], name='production_
↳bounds')
```

### 3.2.8 Solving a problem

After a problem is defined, you can send it to the CAS server or SAS session by calling the `Model.solve()` method, which returns the primal solution when it is available, and `None` otherwise.

```
In [20]: m.solve()
NOTE: Added action set 'optimization'.
NOTE: Converting model my_first_model to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 4 variables (0 free, 0 fixed).
NOTE: The problem has 0 binary and 4 integer variables.
NOTE: The problem has 7 linear constraints (6 LE, 0 EQ, 0 GE, 1 range).
NOTE: The problem has 10 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed all variables and constraints.
NOTE: Optimal.
NOTE: Objective = 400.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 4 rows and 6_
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 7 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4_
↳columns.
Out[20]:
Selected Rows from Table SOLUTION
```

	i	var	value	lb	ub	rc
0	1.0	production_cap	25.0	-0.0	1.797693e+308	NaN
1	2.0	production[Period1]	25.0	5.0	1.797693e+308	NaN
2	3.0	production[Period2]	15.0	5.0	1.797693e+308	NaN
3	4.0	production[Period3]	25.0	-0.0	1.797693e+308	NaN

At the end of the solve operation, the solver returns a “Problem Summary” table and a “Solution Summary” table. These tables can later be accessed by using `m.get_problem_summary()` and `m.get_solution_summary()`.

```
In [21]: print(m.get_solution_summary())
Selected Rows from Table SOLUTIONSUMMARY
```

	Value
Label	
Solver	MILP
Algorithm	Branch and Cut
Objective Function	totalProfit
Solution Status	Optimal

(continues on next page)

(continued from previous page)

Objective Value	400
Relative Gap	0
Absolute Gap	0
Primal Infeasibility	0
Bound Infeasibility	0
Integer Infeasibility	0
Best Bound	400
Nodes	0
Solutions Found	3
Iterations	0
Presolve Time	0.00
Solution Time	0.02

### 3.2.9 Printing solutions

You can retrieve the solutions by using the `get_solution_table()` method. It is strongly suggested that you group variables and expressions that share the same keys in a call.

```
In [22]: print(so.get_solution_table(demand, production))
          demand  production
period
Period1      30         25.0
Period2      15         15.0
Period3      25         25.0
```

### 3.2.10 Initializing a workspace

If you want to use the extensive abstract modeling capabilities of sasoptpy, you can create a workspace. Workspaces support features such as server-side for loops, cofor loops (parallel), reading and creating CAS tables. You can initialize a *Workspace* by using Python's `with` keyword. For example, you can create a workspace that has a set and a variable group as follows:

```
In [23]: def create_workspace():
...:     with so.Workspace(name='my_workspace', session=s) as w:
...:         I = so.Set(name='I', value=range(1, 11))
...:         x = so.VariableGroup(I, name='x', lb=0)
...:         return w
...:
```

```
In [24]: workspace = create_workspace()
```

```
In [25]: print(so.to_optmodel(workspace))
proc optmodel;
  set I = 1..10;
  var x {{I}} >= 0;
quit;
```

You can submit a workspace to a CAS server and retrieve the response by using:

```
In [26]: workspace.submit()
NOTE: Added action set 'optimization'.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 10 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 0 rows and 4 columns.
Out [26]:
Selected Rows from Table SOLUTION
```

	i	var	value	lb	ub	rc
0	1.0	x[1]	0.0	0.0	1.797693e+308	NaN
1	2.0	x[2]	0.0	0.0	1.797693e+308	NaN
2	3.0	x[3]	0.0	0.0	1.797693e+308	NaN
3	4.0	x[4]	0.0	0.0	1.797693e+308	NaN
4	5.0	x[5]	0.0	0.0	1.797693e+308	NaN
5	6.0	x[6]	0.0	0.0	1.797693e+308	NaN
6	7.0	x[7]	0.0	0.0	1.797693e+308	NaN
7	8.0	x[8]	0.0	0.0	1.797693e+308	NaN
8	9.0	x[9]	0.0	0.0	1.797693e+308	NaN
9	10.0	x[10]	0.0	0.0	1.797693e+308	NaN

### 3.2.11 Package configurations

sasoptpy comes with certain package configurations. The configuration parameters and their default values are as follows:

- verbosity (default 3)
- max\_digits (default 12)
- print\_digits (default 6)
- default\_sense (default so.minimization)
- default\_bounds
- valid\_outcomes

It is possible to override these configuration parameters. As an example, consider the following constraint representation:

```
In [27]: x = so.Variable(name='x')

In [28]: c = so.Constraint(10 / 3 * x + 1e-20 * x ** 2 <= 30 + 1e-11, name='c')

In [29]: print(so.to_definition(c))
con c : 3.333333333333 * x + 0.0 * ((x) ^ (2)) <= 30.000000000001;
```

You can change the number of digits to be printed as follows:

```
In [30]: so.config['max_digits'] = 2

In [31]: print(so.to_definition(c))
con c : 3.33 * x + 0.0 * ((x) ^ (2)) <= 30.0;
```

You can remove the maximum number of digits to print as follows:

```
In [32]: so.config['max_digits'] = None
```

```
In [33]: print(so.to_definition(c))
con c : 3.3333333333333335 * x + 1e-20 * ((x) ^ (2)) <= 30.000000000001;
```

You can reset the parameter to its default value by deleting the parameter:

```
In [34]: del so.config['max_digits']
```

You can also create a new configuration to be used globally:

```
In [35]: so.config['myvalue'] = 2
```

## 3.3 Sessions

### 3.3.1 CAS Sessions

A `swat.cas.connection.CAS` session is needed in order to use `sasoptpy` and SAS Optimization solvers to solve optimization problems. You can find more details about CAS sessions in [SWAT Documentation](#).

You can create a sample CAS Session as follows:

```
>>> import sasoptpy as so
>>> from swat import CAS
>>> s = CAS(hostname=cas_host, username=cas_username, password=cas_password, port=cas_
↪port)
>>> m = so.Model(name='demo', session=s)
>>> print(repr(m))
sasoptpy.Model(name='demo', session=CAS(hostname, port, username, protocol='cas',
↪name='py-session-1', session=session-no))
```

You can end the session and close the connection as follows:

```
>>> s.terminate()
```

### 3.3.2 SAS Sessions

A `saspy.SASsession` session is needed in order to use `sasoptpy` and SAS/OR solvers to solve optimization problems on SAS 9.4 clients.

You can create a sample SAS session as follows:

```
>>> import sasoptpy as so
>>> import saspy
>>> sas_session = saspy.SASsession(cfgname='winlocal')
>>> m = so.Model(name='demo', session=sas_session)
>>> print(repr(m))
sasoptpy.Model(name='demo', session=saspy.SASsession(cfgname='winlocal'))
```

You can connect to a SAS session by using a configuration file

```
In [1]: sas = saspy.SASsession(cfgfile=config_file)
Using SAS Config named: sshsas
SAS Connection established. Subprocess id is 161
```



```
In [2]: m = so.Model(name='demo', session=sas)
NOTE: Initialized model demo.
```

```
In [3]: print(m.get_session().sasver)
9.04.01M6P11072018
```

You can terminate the SAS session as follows:

```
In [4]: sas.endsas()
SAS Connection terminated. Subprocess id was 161
```

## 3.4 Models

### 3.4.1 Creating a model

You can create an empty model by using the *Model* constructor:

```
In [1]: import sasoptpy as so

In [2]: m = so.Model(name='model1')
NOTE: Initialized model model1.
```

### 3.4.2 Adding new components to a model

Add a variable:

```
In [3]: x = m.add_variable(name='x', vartype=so.BIN)

In [4]: print(m)
Model: [
  Name: model1
  Objective: MIN [0]
  Variables (1): [
    x
  ]
  Constraints (0): [
  ]
]

In [5]: y = m.add_variable(name='y', lb=1, ub=10)

In [6]: print(m)
Model: [
  Name: model1
  Objective: MIN [0]
  Variables (2): [
    x
    y
  ]
  Constraints (0): [
  ]
]
```

Add a constraint:

```
In [7]: c1 = m.add_constraint(x + 2 * y <= 10, name='c1')

In [8]: print(m)
Model: [
  Name: model1
  Objective: MIN [0]
  Variables (2): [
    x
    y
  ]
  Constraints (1): [
    x + 2 * y <= 10
  ]
]
```

### 3.4.3 Adding existing components to a model

A new model can use existing variables. The typical way to include a variable is to use the `Model.include()` method:

```
In [9]: new_model = so.Model(name='new_model')
NOTE: Initialized model new_model.

In [10]: new_model.include(x, y)

In [11]: print(new_model)
Model: [
  Name: new_model
  Objective: MIN [0]
  Variables (2): [
    x
    y
  ]
  Constraints (0): [
  ]
]

In [12]: new_model.include(c1)

In [13]: print(new_model)
Model: [
  Name: new_model
  Objective: MIN [0]
  Variables (2): [
    x
    y
  ]
  Constraints (1): [
    x + 2 * y <= 10
  ]
]

In [14]: z = so.Variable(name='z', vartype=so.INT, lb=3)
```

(continues on next page)

(continued from previous page)

```
In [15]: new_model.include(z)

In [16]: print(new_model)
Model: [
  Name: new_model
  Objective: MIN [0]
  Variables (3): [
    x
    y
    z
  ]
  Constraints (1): [
    x + 2 * y <= 10
  ]
]
```

Note that variables are added to *Model* objects by reference. Therefore, after *Model.solve()* is called, the values of variables are replaced with optimal values.

### 3.4.4 Accessing components

You can access a list of model variables by using the *Model.get\_variables()* method:

```
In [17]: print(m.get_variables())
[sasoptpy.Variable(name='x', lb=0, ub=1, vartype='BIN'), sasoptpy.Variable(name='y',
↳ lb=1, ub=10, vartype='CONT')]
```

Similarly, you can access a list of constraints by using the *Model.get\_constraints()* method:

```
In [18]: c2 = m.add_constraint(2 * x - y >= 1, name='c2')

In [19]: print(m.get_constraints())
[sasoptpy.Constraint(x + 2 * y <= 10, name='c1'), sasoptpy.Constraint(2 * x - y >=
↳ 1, name='c2')]
```

To access a certain constraint by using its name, you can use the *Model.get\_constraint()* method:

```
In [20]: print(m.get_constraint('c2'))
2 * x - y >= 1
```

### 3.4.5 Dropping components

You can drop a variable inside a model by using *Model.drop\_variable()* method. Similarly, you can drop a set of variables by using the *Model.drop\_variables()* method.

```
In [21]: m.drop_variable(y)

In [22]: print(m)
Model: [
  Name: model1
  Objective: MIN [0]
  Variables (1): [
    x
  ]
]
```

(continues on next page)

(continued from previous page)

```
]
Constraints (2): [
    x + 2 * y <= 10
    2 * x - y >= 1
]
]
```

You can drop a constraint by using the `Model.drop_constraint()` method. Similarly, you can drop a set of constraints by using the `Model.drop_constraints()` method.

```
In [23]: m.drop_constraint(c1)
```

```
In [24]: m.drop_constraint(c2)
```

```
In [25]: print(m)
```

```
Model: [
  Name: model1
  Objective: MIN [0]
  Variables (2): [
    x
    y
  ]
  Constraints (0): [
  ]
]
```

```
In [26]: m.include(c1)
```

```
In [27]: print(m)
```

```
Model: [
  Name: model1
  Objective: MIN [0]
  Variables (2): [
    x
    y
  ]
  Constraints (1): [
    x + 2 * y <= 10
  ]
]
```

### 3.4.6 Copying a model

You can copy an existing model by including the `Model` object itself.

```
In [28]: copy_model = so.Model(name='copy_model')
```

NOTE: Initialized model `copy_model`.

```
In [29]: copy_model.include(m)
```

```
In [30]: print(copy_model)
```

```
Model: [
  Name: copy_model
  Objective: MIN [0]
]
```

(continues on next page)

(continued from previous page)

```

Variables (2): [
    x
    y
]
Constraints (1): [
    x + 2 * y <= 10
]
]

```

Note that all variables and constraints are included by reference.

### 3.4.7 Solving a model

A model is solved by using the `Model.solve()` method. This method converts Python definitions into OPTMODEL language and submits using SWAT or SASPy packages.

```

>>> m.solve()
NOTE: Initialized model model_1
NOTE: Added action set 'optimization'.
NOTE: Converting model model_1 to OPTMODEL.
...
NOTE: Optimal.
NOTE: Objective = 124.343.
NOTE: The Dual Simplex solve time is 0.01 seconds.

```

### 3.4.8 Solve options

#### Solver Options

You can pass either solve options from the OPTMODEL procedure or solve parameter from the `solveLp` and `solveMilp` actions by using the `options` parameter of the `Model.solve()` method.

```

>>> m.solve(options={'with': 'milp', 'maxtime': 600})
>>> m.solve(options={'with': 'lp', 'algorithm': 'ipm'})

```

The parameter `with` is used to specify the optimization solver in OPTMODEL procedure. If the `with` parameter is not passed, PROC OPTMODEL chooses a solver that depends on the problem type. Possible `with` values are listed in the [SAS/OR documentation](#).

You can find specific solver options in the SAS Optimization documentation:

- [LP solver options](#)
- [MILP solver options](#)
- [NLP solver options](#)
- [QP solver options](#)
- [Black-box solver options](#) (formerly called LSO solver)

The `options` parameter can also pass `solveLp` and `solveMilp` action parameter when `frame=True` is used when the `Model.solve()` method is called.

- [solveLp options](#)
- [solveMilp options](#)

## Call parameters

Besides the `options` parameter, you can pass following parameters into the `Model.solve()` method:

- `name`: Name of the uploaded problem information
- `drop`: Drops the data from server after the solve
- `replace`: Replaces an existing data with the same name
- **primalin**: Uses the current values of the variables as an initial solution. When the value of this parameter is `True`, the solve method grabs `Variable` objects' `_init` fields. You can modify this field by using the `Variable.set_init()` method.
- `submit`: Calls the CAS action or SAS procedure
- `frame`: Uses the frame (MPS) method. If the value of this parameter is `False`, then the method uses OPT-MODEL codes.
- `verbose`: Prints the generated PROC OPTMODEL code or MPS DataFrame object before the solve

### 3.4.9 Getting solutions

After the solve is completed, all variable and constraint values are parsed automatically. You can access a summary of the problem by using the `Model.get_problem_summary()` method, and a summary of the solution by using the `Model.get_solution_summary()` method.

To print the values of any object, you can use the `get_solution_table()` method:

```
>>> print(so.get_solution_table(x, y))
```

All variables and constraints that are passed into this method are returned on the basis of their indices. See [Examples](#) for more details.

### 3.4.10 Tuning MILP model parameters

SAS Optimization solvers provide a variety of settings. However, it might be difficult to find the best settings for a particular model. In order to compare parameters and make a good choice, you can use the `optimization.tune` action for mixed integer linear optimization problems.

The `Model.tune_parameters()` method is a wrapper for the `tune` action. Consider the following knapsack problem example:

```
In [31]: def get_model():
...:     m = so.Model(name='knapsack_with_tuner', session=cas_conn)
...:     data = [
...:         ['clock', 8, 4, 3],
...:         ['mug', 10, 6, 5],
...:         ['headphone', 15, 7, 2],
...:         ['book', 20, 12, 10],
...:         ['pen', 1, 1, 15]
...:     ]
...:     df = pd.DataFrame(data, columns=['item', 'value', 'weight', 'limit']).set_
↪index(['item'])
...:     ITEMS = df.index
...:     value = df['value']
...:     weight = df['weight']
...:     limit = df['limit']
```

(continues on next page)

(continued from previous page)

```

.....: total_weight = 55
.....: get = m.add_variables(ITEMS, name='get', vartype=so.INT)
.....: m.add_constraints((get[i] <= limit[i] for i in ITEMS), name='limit_con')
.....: m.add_constraint(so.expr_sum(weight[i] * get[i] for i in ITEMS) <= total_
↪weight, name='weight_con')
.....: total_value = so.expr_sum(value[i] * get[i] for i in ITEMS)
.....: m.set_objective(total_value, name='total_value', sense=so.MAX)
.....: return m
.....:

```

In [32]: m = get\_model()

NOTE: Initialized model knapsack\_with\_tuner.

For this problem, you can compare configurations as follows:

In [33]: results = m.tune\_parameters(tunerParameters={'maxConfigs': 10})

NOTE: Added action set 'optimization'.

NOTE: Uploading the problem DataFrame to the server.

NOTE: Cloud Analytic Services made the uploaded file available as table KNAPSACK\_WITH\_↪TUNER in caslib CASUSER(casuser).

NOTE: The table KNAPSACK\_WITH\_TUNER has been created in caslib CASUSER(casuser) from\_↪binary data uploaded to Cloud Analytic Services.

NOTE: Start to tune the MILP

SolveCalls	Configurations	BestTime	Time
1	1	0.22	0.28
2	2	0.20	0.50
3	3	0.20	0.73
4	4	0.20	0.96
5	5	0.20	1.19
6	6	0.20	1.41
7	7	0.18	1.62
8	8	0.18	1.85
9	9	0.18	2.06
10	10	0.18	2.27

NOTE: Configuration limit reached.

NOTE: The tuning time is 2.27 seconds.

In [34]: print(results)

	Configuration	conflictSearch	cutGomory	cutMiLifted	cutStrategy	\
0	0.0	automatic	automatic	automatic	automatic	
1	1.0	none	none	moderate	aggressive	
2	2.0	automatic	moderate	none	aggressive	
3	3.0	automatic	moderate	none	aggressive	
4	4.0	none	moderate	moderate	none	
5	5.0	automatic	none	none	moderate	
6	6.0	aggressive	none	aggressive	none	
7	7.0	aggressive	none	none	aggressive	
8	8.0	moderate	none	automatic	moderate	
9	9.0	moderate	none	automatic	automatic	

	cutZeroHalf	heuristics	modelSel	presolver	probe	restarts	\
0	automatic	automatic	automatic	automatic	automatic	automatic	
1	none	automatic	bestEstimateddepth	moderate	none	basic	
2	aggressive	automatic	automatic	moderate	automatic	basic	
3	aggressive	automatic	automatic	basic	automatic	basic	
4	aggressive	none	depth	automatic	automatic	automatic	

(continues on next page)

(continued from previous page)

5	moderate	automatic	automatic	none	automatic	none
6	moderate	automatic	bestBound	moderate	automatic	none
7	moderate	none	depth	automatic	automatic	none
8	aggressive	none	bestBound	moderate	automatic	none
9	none	automatic	automatic	none	none	basic
	symmetry	varSel	Mean of Run Times	Sum of Run Times	\	
0	automatic	automatic	0.22	0.22		
1	none	automatic	0.18	0.18		
2	basic	ryanFoster	0.18	0.18		
3	basic	ryanFoster	0.18	0.18		
4	none	minInfeas	0.19	0.19		
5	basic	minInfeas	0.20	0.20		
6	moderate	ryanFoster	0.20	0.20		
7	aggressive	minInfeas	0.20	0.20		
8	automatic	ryanFoster	0.20	0.20		
9	automatic	pseudo	0.20	0.20		
	Percentage Successful					
0	100.0					
1	100.0					
2	100.0					
3	100.0					
4	100.0					
5	100.0					
6	100.0					
7	100.0					
8	100.0					
9	100.0					

`Model.tune_parameters()` accepts three main arguments

- `milpParameters`
- `tunerParameters`
- `tuningParameters`

For a full set of tuning parameters and acceptable values of these arguments, see the [SAS Optimization documentation](#).

For the example problem, you can tune the *presolver*, *cutStrategy*, and *strongIter* settings, by using initial values and candidate values, and limit the maximum number of configurations and maximum running time as follows:

```
In [35]: results = m.tune_parameters(
.....:     milpParameters={'maxtime': 10},
.....:     tunerParameters={'maxConfigs': 20, 'logfreq': 5},
.....:     tuningParameters=[
.....:         {'option': 'presolver', 'initial': 'none', 'values': ['basic',
↪ 'aggressive', 'none']},
.....:         {'option': 'cutStrategy'},
.....:         {'option': 'strongIter', 'initial': -1, 'values': [-1, 100, 1000]}
.....:     ])
.....:
```

NOTE: Added action set 'optimization'.

NOTE: Uploading the problem DataFrame to the server.

NOTE: Cloud Analytic Services made the uploaded file available as table KNAPSACK\_WITH\_TUNER in caslib CASUSER(casuser).

NOTE: The table KNAPSACK\_WITH\_TUNER has been created in caslib CASUSER(casuser) from ↪ binary data uploaded to Cloud Analytic Services.

(continues on next page)



(continued from previous page)

NOTE: Start to tune the MILP

SolveCalls	Configurations	BestTime	Time
5	5	0.19	1.09
10	10	0.18	2.14
15	15	0.18	3.22
20	20	0.18	4.28

NOTE: Configuration limit reached.

NOTE: The tuning time is 4.28 seconds.

In [36]: print(results)

	Configuration	conflictSearch	cutGomory	cutMiLifted	cutStrategy	\
0	0.0	automatic	automatic	automatic	automatic	
1	1.0	none	none	moderate	aggressive	
2	2.0	none	none	moderate	aggressive	
3	3.0	moderate	automatic	none	aggressive	
4	4.0	moderate	none	none	aggressive	
5	5.0	automatic	none	none	moderate	
6	6.0	none	none	moderate	aggressive	
7	7.0	moderate	none	aggressive	aggressive	
8	8.0	moderate	none	none	aggressive	
9	9.0	moderate	none	automatic	automatic	
10	10.0	moderate	none	automatic	moderate	
11	11.0	none	none	moderate	aggressive	
12	12.0	aggressive	none	aggressive	none	
13	13.0	moderate	none	none	aggressive	
14	14.0	moderate	none	none	aggressive	
15	15.0	none	moderate	moderate	none	
16	16.0	moderate	none	none	aggressive	
17	17.0	moderate	none	none	aggressive	
18	18.0	aggressive	none	none	aggressive	
19	19.0	moderate	none	none	aggressive	

	cutZeroHalf	heuristics	modelSel	presolver	probe	\
0	automatic	automatic	automatic	automatic	automatic	
1	none	automatic	bestEstimateddepth	moderate	none	
2	none	automatic	bestEstimateddepth	moderate	none	
3	none	aggressive	bestBound	aggressive	basic	
4	none	aggressive	bestBound	aggressive	basic	
5	moderate	automatic	automatic	none	automatic	
6	none	automatic	automatic	moderate	none	
7	none	aggressive	bestBound	aggressive	basic	
8	none	aggressive	automatic	aggressive	basic	
9	none	automatic	automatic	none	none	
10	aggressive	none	bestBound	moderate	automatic	
11	none	aggressive	bestEstimateddepth	moderate	none	
12	moderate	automatic	bestBound	moderate	automatic	
13	aggressive	aggressive	bestBound	aggressive	basic	
14	none	aggressive	depth	aggressive	basic	
15	aggressive	none	depth	automatic	automatic	
16	none	aggressive	bestBound	basic	basic	
17	none	aggressive	bestBound	aggressive	none	
18	moderate	none	depth	automatic	automatic	
19	none	aggressive	bestBound	aggressive	basic	

	restarts	symmetry	varSel	Mean of Run Times	Sum of Run Times	\
0	automatic	automatic	automatic	0.19	0.19	

(continues on next page)

(continued from previous page)

1	basic	none	automatic	0.18	0.18
2	basic	automatic	automatic	0.18	0.18
3	moderate	none	ryanFoster	0.18	0.18
4	moderate	none	ryanFoster	0.18	0.18
5	none	basic	minInfeas	0.18	0.18
6	basic	none	automatic	0.18	0.18
7	moderate	none	ryanFoster	0.18	0.18
8	moderate	none	ryanFoster	0.18	0.18
9	basic	automatic	pseudo	0.18	0.18
10	none	automatic	ryanFoster	0.19	0.19
11	basic	none	automatic	0.19	0.19
12	none	moderate	ryanFoster	0.19	0.19
13	moderate	none	ryanFoster	0.19	0.19
14	moderate	none	ryanFoster	0.19	0.19
15	automatic	none	minInfeas	0.19	0.19
16	moderate	none	ryanFoster	0.19	0.19
17	moderate	none	ryanFoster	0.19	0.19
18	none	aggressive	minInfeas	0.19	0.19
19	moderate	none	maxInfeas	0.20	0.20

	Percentage Successful
0	100.0
1	100.0
2	100.0
3	100.0
4	100.0
5	100.0
6	100.0
7	100.0
8	100.0
9	100.0
10	100.0
11	100.0
12	100.0
13	100.0
14	100.0
15	100.0
16	100.0
17	100.0
18	100.0
19	100.0

You can retrieve full details by using the `Model.get_tuner_results()` method.

## 3.5 Model Components

In this section, several model components are discussed with examples. See [Examples](#) to learn more about how you can use these components to define optimization models.

### 3.5.1 Expressions

*Expression* objects represent linear and nonlinear mathematical expressions in sasoptpy.

#### Creating expressions

You can create an *Expression* object as follows:

```
In [1]: profit = so.Expression(5 * sales - 3 * material, name='profit')

In [2]: print(repr(profit))
sasoptpy.Expression(exp = 5 * sales - 3 * material, name='profit')
```

#### Nonlinear expressions

*Expression* objects are linear by default. It is possible to create nonlinear expressions, but there are some limitations.

```
In [3]: nonexp = sales ** 2 + (1 / material) ** 3

In [4]: print(nonexp)
(sales) ** (2) + ((1) / (material)) ** (3)
```

Currently, it is not possible to get or print values of nonlinear expressions. Moreover, if your model includes a nonlinear expression, you need to use SAS Viya 3.4 or later or any SAS/OR release for solving your problem.

To use mathematical operations, you need to import *sasoptpy.math* functions.

#### Mathematical expressions

sasoptpy provides mathematical functions for generating mathematical expressions to be used in optimization models.

You need to import *sasoptpy.math* into your code to use these functions. Available mathematical functions are listed in [Math Functions](#).

```
In [5]: import sasoptpy.math as sm

In [6]: newexp = sm.max(sales, 10) ** 2

In [7]: print(newexp._expr())
(max(sales , 10)) ^ (2)

In [8]: import sasoptpy.math as sm

In [9]: angle = so.Variable(name='angle')

In [10]: newexp = sm.sin(angle) ** 2 + sm.cos(angle) ** 2
```

(continues on next page)

(continued from previous page)

```
In [11]: print(newexp._expr())  
(sin(angle)) ^ (2) + (cos(angle)) ^ (2)
```

## Operations

### Getting the current value

After the solve is completed, you can obtain the current value of an expression by using the `Expression.get_value()` method:

```
>>> print(profit.get_value())  
42.0
```

### Getting the dual value

You can retrieve the dual values of `Expression` objects by using `Variable.get_dual()` and `Constraint.get_dual()` methods.

```
>>> m.solve()  
>>> ...  
>>> print(x.get_dual())  
1.0
```

## Addition

You can add, subtract, multiply and divide components using regular Python functionality:

```
In [12]: tax = 0.5
```

```
In [13]: profit_after_tax = profit - tax
```

```
In [14]: print(repr(profit_after_tax))  
sasoptpy.Expression(exp = 5 * sales - 3 * material - 0.5, name=None)
```

```
In [15]: share = 0.2 * profit
```

```
In [16]: print(share)  
sales - 0.6 * material
```

## Summation

For faster summations compared to Python's native `sum` function, sasoptpy provides `expr_sum()` (formerly `quick_sum()`)

```
In [17]: import time
```

```
In [18]: x = m.add_variables(1000, name='x')
```

```
In [19]: t0 = time.time()
```

```
In [20]: e = so.expr_sum(2 * x[i] for i in range(1000))
```

```
In [21]: print(time.time()-t0)  
0.06784749031066895
```

```
In [22]: t0 = time.time()

In [23]: f = sum(2 * x[i] for i in range(1000))

In [24]: print(time.time()-t0)
1.353301763534546
```

## Renaming an expression

You can rename expressions by using the `Expression.set_name()` method:

```
In [25]: e = so.Expression(x[5] + 2 * x[6], name='e1')

In [26]: print(repr(e))
sasoptpy.Expression(exp = x[5] + 2 * x[6], name='e1')

In [27]: e.set_name('e2');

In [28]: print(repr(e))
sasoptpy.Expression(exp = x[5] + 2 * x[6], name='e2')
```

## Copying an expression

You can copy an `Expression` by using the `Expression.copy()` method:

```
In [29]: copy_profit = profit.copy(name='copy_profit')

In [30]: print(repr(copy_profit))
sasoptpy.Expression(exp = 5 * sales - 3 * material, name='copy_profit')
```

## 3.5.2 Objective Functions

### Setting and getting an objective function

You can use any valid `Expression` as the objective function of a model. You can also use an existing expression as an objective function by using the `Model.set_objective()` method. The objective function of a model can be obtained by using the `Model.get_objective()` method.

```
>>> profit = so.Expression(5 * sales - 2 * material, name='profit')
>>> m.set_objective(profit, so.MAX)
>>> print(m.get_objective())
- 2.0 * material + 5.0 * sales
```

## Getting the value

After a solve, you can retrieve the objective value by using the `Model.get_objective_value()` method.

```
>>> m.solve()
>>> print(m.get_objective_value())
42.0
```

## 3.5.3 Variables

### Creating variables

You can create variables either stand-alone or inside a model.

#### Creating a variable outside a model

The first way to create a variable uses the default constructor:

```
>>> x = so.Variable(vartype=so.INT, ub=5, name='x')
```

When a variable is created separately, it needs to be included (or added) inside the model:

```
>>> y = so.Variable(name='y', lb=5)
>>> m.add_variable(y)
```

Equivalently, you could do this in one step:

```
>>> y = m.add_variable(name='y', lb=5)
```

#### Creating a variable inside a model

The second way is to use `Model.add_variable()`. This method creates a `Variable` object and returns a pointer.

```
>>> x = m.add_variable(vartype=so.INT, ub=5, name='x')
```

## Arguments

There are three types of variables: continuous variables, integer variables, and binary variables. Continuous variables are the default type, which you can specify by using the `vartype=so.CONT` argument. You can create integer variables and binary variables by using the `vartype=so.INT` and `vartype=so.BIN` arguments, respectively.

The default lower bound for variables is 0, and the upper bound is infinity. Name is a required argument.

## Changing bounds

The `Variable.set_bounds()` method changes the bounds of a variable.

```
>>> x = so.Variable(name='x', lb=0, ub=20)
>>> print(repr(x))
sasoptpy.Variable(name='x', lb=0, ub=20, vartype='CONT')
>>> x.set_bounds(lb=5, ub=15)
>>> print(repr(x))
sasoptpy.Variable(name='x', lb=5, ub=15, vartype='CONT')
```

## Setting initial values

You can pass the initial values of variables to the solvers for certain problems. The `Variable.set_init()` method changes the initial value for variables. You can set also this value at the creation of the variable.

```
>>> x.set_init(5)
>>> print(repr(x))
sasoptpy.Variable(name='x', ub=20, init=5, vartype='CONT')
```

## Working with a set of variables

You can create a set of variables by using a single index or by using multiple indices. Valid index sets include list, dict, and `pandas.Index` objects. See [Handling Data](#) for more information about allowed index types.

### Creating a set of variables outside a model

```
>>> production = VariableGroup(PERIODS, vartype=so.INT, name='production',
                               lb=min_production)
>>> print(repr(production))
sasoptpy.VariableGroup(['Period1', 'Period2', 'Period3'], name='production')
>>> m.include(production)
```

### Creating a set of variables inside a model

```
>>> production = m.add_variables(PERIODS, vartype=so.INT,
                                name='production', lb=min_production)
>>> print(production)
>>> print(repr(production))
Variable Group (production) [
  [Period1: production['Period1',]]
  [Period2: production['Period2',]]
  [Period3: production['Period3',]]
]
sasoptpy.VariableGroup(['Period1', 'Period2', 'Period3'],
name='production')
```

## 3.5.4 Constraints

### Creating constraints

Similar to `Variable` objects, you can create `Constraint` objects inside or outside optimization models.

#### Creating a constraint outside a model

```
>>> c1 = so.Constraint(3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint(- 5.0 * y + 3.0 * x <= 10, name='c1')
```

#### Creating a constraint inside a model

```
>>> c1 = m.add_constraint(3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint(- 5.0 * y + 3.0 * x <= 10, name='c1')
```

## Modifying variable coefficients

You can update the coefficient of a variable inside a constraint by using the `Constraint.update_var_coef()` method:

```
>>> c1 = so.Constraint(exp=3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint( - 5.0 * y + 3.0 * x <= 10, name='c1')
>>> c1.update_var_coef(x, -1)
>>> print(repr(c1))
sasoptpy.Constraint( - 5.0 * y - x <= 10, name='c1')
```

## Working with a set of constraints

You can add a set of constraints by using a single index or by using multiple indices. Valid index sets include list, dict, and `pandas.Index` objects. See [Handling Data](#) for more information about allowed index types.

### Creating a set of constraints outside a model

```
>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z', lb=0, ub=10)
>>> cg = so.ConstraintGroup((2 * z[i, j] + 3 * z[i-1, j] >= 2 for i in
                             [1] for j in ['a', 'b', 'c']), name='cg')
>>> print(cg)
Constraint Group (cg) [
  [(1, 'a'): 3.0 * z[0, 'a'] + 2.0 * z[1, 'a'] >= 2]
  [(1, 'b'): 3.0 * z[0, 'b'] + 2.0 * z[1, 'b'] >= 2]
  [(1, 'c'): 2.0 * z[1, 'c'] + 3.0 * z[0, 'c'] >= 2]
]
```

### Creating a set of constraints inside a model

```
>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z', lb=0, ub=10)
>>> cg2 = m.add_constraints((2 * z[i, j] + 3 * z[i-1, j] >= 2 for i in
                             [1] for j in ['a', 'b', 'c']), name='cg2')
>>> print(cg2)
Constraint Group (cg2) [
  [(1, 'a'): 2.0 * z[1, 'a'] + 3.0 * z[0, 'a'] >= 2]
  [(1, 'b'): 3.0 * z[0, 'b'] + 2.0 * z[1, 'b'] >= 2]
  [(1, 'c'): 2.0 * z[1, 'c'] + 3.0 * z[0, 'c'] >= 2]
]
```

## Range constraints

You can give a range for an expression by using a list of two values (lower and upper bound) after an `==` sign:

```
>>> x = m.add_variable(name='x')
>>> y = m.add_variable(name='y')
>>> c1 = m.add_constraint(x + 2*y == [2, 9], name='c1')
>>> print(repr(c1))
sasoptpy.Constraint( x + 2.0 * y == [2, 9], name='c1')
```



## 3.6 Workspaces

One of the most powerful features of SAS Optimization and PROC OPTMODEL is the ability to combine several optimization models in a single call. You can read a common data set once, or parallelize solve steps for similar subproblems by using this ability.

The newly introduced *Workspace* provides this ability in a familiar syntax. Compared to *Model* objects, a *Workspace* can consist of several models and can use server-side data and OPTMODEL statements in a more detailed way.

You can create several models in the same workspace, and you can solve problems sequentially and concurrently. All the statements are sent to the server after *Workspace.submit()* is called.

### 3.6.1 Creating a workspace

A *Workspace* should be called by using the `with` Python keyword as follows:

```
>>> with so.Workspace('my_workspace') as w:
>>> ...
```

### 3.6.2 Adding components

Unlike *Model* objects, whose components are added explicitly, objects that are defined inside a *Workspace* are added automatically.

For example, adding a new variable is performed as follows:

```
In [1]: with so.Workspace(name='my_workspace') as w:
...:     x = so.Variable(name='x', vartype=so.integer)
...:
```

You can display contents of a workspace by using the *Workspace.to\_optmodel()* method:

```
In [2]: print(w.to_optmodel())
proc optmodel;
  var x integer;
quit;
```

In the following example, data are loaded into the server and a problem is solved by using a workspace:

1. Create CAS session:

```
In [3]: import os

In [4]: hostname = os.getenv('CASHOST')

In [5]: port = os.getenv('CASPORT')

In [6]: from swat import CAS

In [7]: cas_conn = CAS(hostname, port)

In [8]: import sasoptpy as so

In [9]: import pandas as pd
```

## 2. Upload data:

```
In [10]: def send_data():
.....:     data = [
.....:         ['clock', 8, 4, 3],
.....:         ['mug', 10, 6, 5],
.....:         ['headphone', 15, 7, 2],
.....:         ['book', 20, 12, 10],
.....:         ['pen', 1, 1, 15]
.....:     ]
.....:     df = pd.DataFrame(data, columns=['item', 'value', 'weight', 'limit'])
.....:     cas_conn.upload_frame(df, casout={'name': 'mydata', 'replace': True})
.....:     send_data()
.....:
```

NOTE: Cloud Analytic Services made the uploaded file available as table MYDATA in `caslib CASUSER(casuser)`.

NOTE: The table MYDATA has been created in caslib CASUSER(casuser) from binary data uploaded to Cloud Analytic Services.

## 3. Create workspace and model:

```
In [11]: from sasoptpy.actions import read_data, solve

In [12]: def create_workspace():
.....:     with so.Workspace('my_knapsack', session=cas_conn) as w:
.....:         items = so.Set(name='ITEMS', settype=so.string)
.....:         value = so.ParameterGroup(items, name='value')
.....:         weight = so.ParameterGroup(items, name='weight')
.....:         limit = so.ParameterGroup(items, name='limit')
.....:         total_weight = so.Parameter(name='total_weight', value=55)
.....:         read_data(
.....:             table='mydata', index={'target': items, 'key': ['item']},
.....:             columns=[value, weight, limit]
.....:         )
.....:         get = so.VariableGroup(items, name='get', vartype=so.integer, lb=0)
.....:         limit_con = so.ConstraintGroup((get[i] <= limit[i] for i in items),
.....:                                     name='limit_con')
.....:         weight_con = so.Constraint(
.....:             so.expr_sum(weight[i] * get[i] for i in items) <= total_weight,
.....:             name='weight_con')
.....:         total_value = so.Objective(
.....:             so.expr_sum(value[i] * get[i] for i in items), name='total_value'
.....:         ),
.....:         sense=so.maximize)
.....:         solve()
.....:     return w

In [13]: my_workspace = create_workspace()
```

## 4. Print content:

```
In [14]: print(so.to_optmodel(my_workspace))
proc optmodel;
  set <str> ITEMS;
  num value {ITEMS};
  num weight {ITEMS};
  num limit {ITEMS};
```

(continues on next page)

(continued from previous page)

```

num total_weight = 55;
read data mydata into ITEMS=[item] value weight limit;
var get {{ITEMS}} integer >= 0;
con limit_con {o72 in ITEMS} : get[o72] - limit[o72] <= 0;
con weight_con : total_weight - (sum {i in ITEMS} (weight[i] * get[i])) >= 0;
max total_value = sum {i in ITEMS} (value[i] * get[i]);
solve;
quit;

```

## 5. Submit:

```

In [15]: my_workspace.submit()
NOTE: Added action set 'optimization'.
NOTE: There were 5 rows read from table 'MYDATA' in caslib 'CASUSER(casuser)'.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 5 variables (0 free, 0 fixed).
NOTE: The problem has 0 binary and 5 integer variables.
NOTE: The problem has 6 linear constraints (5 LE, 0 EQ, 1 GE, 0 range).
NOTE: The problem has 10 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 5 constraints.
NOTE: The MILP presolver removed 5 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The presolved problem has 5 variables, 1 constraints, and 5 constraint_
↪coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.

```

	Node	Active	Sols	BestInteger	BestBound	Gap	Time
	0	1	4	99.0000000	199.0000000	50.25%	0
	0	1	4	99.0000000	102.3333333	3.26%	0
	0	0	4	99.0000000	99.0000000	0.00%	0

```

NOTE: Optimal.
NOTE: Objective = 99.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 5 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 6 rows and 4_
↪columns.

```

### Out [15]:

Selected Rows from Table SOLUTION

	i	var	value	lb	ub	rc
0	1.0	get[book]	2.0	-0.0	1.797693e+308	NaN
1	2.0	get[clock]	3.0	-0.0	1.797693e+308	NaN
2	3.0	get[headphone]	2.0	-0.0	1.797693e+308	NaN
3	4.0	get[mug]	-0.0	-0.0	1.797693e+308	NaN
4	5.0	get[pen]	5.0	-0.0	1.797693e+308	NaN

### 3.6.3 Abstract actions

As shown in the previous example, a *Workspace* can contain statements such as `actions.read_data()` and `actions.solve()`.

These statements are called “Abstract Statements” and are fully supported inside *Workspace* objects. These actions are performed on the server at runtime.

A list of abstract actions is available in the [API section](#).

#### Adding abstract actions

You can import abstract actions through `sasoptpy.actions` as follows:

```
>>> from sasoptpy.actions import read_data, create_data
```

These abstract actions are performed on the server side by generating equivalent OPTMODEL code at execution.

#### Retrieving results

In order to solve a problem, you need to use the `actions.solve()` function explicitly. Because *Workspace* objects allow several models and solve statements to be included, each of these solve statements is retrieved separately. You can return the solution after each solve by using the `actions.print()` function or by using the `actions.create_data()` function to create table.

In the following example, a parameter is changed and the same problem is solved twice:

1. Create workspace and components:

```
In [16]: from sasoptpy.actions import read_data, solve, print_item

In [17]: def create_multi_solve_workspace():
.....:     with so.Workspace('my_knapsack', session=cas_conn) as w:
.....:         items = so.Set(name='ITEMS', settype=so.string)
.....:         value = so.ParameterGroup(items, name='value')
.....:         weight = so.ParameterGroup(items, name='weight')
.....:         limit = so.ParameterGroup(items, name='limit')
.....:         total_weight = so.Parameter(name='total_weight', init=55)
.....:         read_data(table='mydata', index={'target': items, 'key': ['item
↪']}, columns=[value, weight, limit])
.....:         get = so.VariableGroup(items, name='get', vartype=so.integer,
↪lb=0)
.....:         limit_con = so.ConstraintGroup((get[i] <= limit[i] for i in
↪items), name='limit_con')
.....:         weight_con = so.Constraint(
.....:             so.expr_sum(weight[i] * get[i] for i in items) <= total_
↪weight, name='weight_con')
.....:         total_value = so.Objective(so.expr_sum(value[i] * get[i] for i
↪in items), name='total_value', sense=so.MAX)
.....:         s1 = solve()
.....:         p1 = print_item(get)
.....:         total_weight.set_value(40)
.....:         s2 = solve()
.....:         p2 = print_item(get)
.....:         return w, s1, p1, s2, p2
.....:
```

(continues on next page)

(continued from previous page)

```
In [18]: (my_workspace, solve1, print1, solve2, print2) = create_multi_solve_
↳workspace()
```

## 2. Submit to the server:

```
In [19]: my_workspace.submit()
NOTE: Added action set 'optimization'.
NOTE: There were 5 rows read from table 'MYDATA' in caslib 'CASUSER(casuser)'.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 5 variables (0 free, 0 fixed).
NOTE: The problem has 0 binary and 5 integer variables.
NOTE: The problem has 6 linear constraints (5 LE, 0 EQ, 1 GE, 0 range).
NOTE: The problem has 10 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 5 constraints.
NOTE: The MILP presolver removed 5 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The resolved problem has 5 variables, 1 constraints, and 5 constraint_
↳coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.
      Node   Active   Sols   BestInteger   BestBound   Gap   Time
      0       1       4     99.0000000    199.0000000  50.25%  0
      0       1       4     99.0000000    102.3333333  3.26%   0
      0       0       4     99.0000000     99.0000000  0.00%   0
NOTE: Optimal.
NOTE: Objective = 99.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 5 variables (0 free, 0 fixed).
NOTE: The problem has 0 binary and 5 integer variables.
NOTE: The problem has 6 linear constraints (5 LE, 0 EQ, 1 GE, 0 range).
NOTE: The problem has 10 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 5 constraints.
NOTE: The MILP presolver removed 5 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The resolved problem has 5 variables, 1 constraints, and 5 constraint_
↳coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.
      Node   Active   Sols   BestInteger   BestBound   Gap   Time
      0       1       4     76.0000000    179.0000000  57.54%  0
      0       1       4     76.0000000     77.3333333  1.72%   0
      0       0       4     76.0000000     76.0000000  0.00%   0
NOTE: Optimal.
NOTE: Objective = 76.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 5 rows and 6_
↳columns.
```

(continues on next page)

(continued from previous page)

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 6 rows and 4 columns.

**Out [19]:**

Selected Rows from Table SOLUTION

	i	var	value	lb	ub	rc
0	1.0	get[book]	1.0	-0.0	1.797693e+308	NaN
1	2.0	get[clock]	3.0	-0.0	1.797693e+308	NaN
2	3.0	get[headphone]	2.0	-0.0	1.797693e+308	NaN
3	4.0	get[mug]	-0.0	-0.0	1.797693e+308	NaN
4	5.0	get[pen]	2.0	-0.0	1.797693e+308	NaN

### 3. Print results:

**In [20]:** `print(solve1.get_solution_summary())`

Solution Summary

	Value
Label	
Solver	MILP
Algorithm	Branch and Cut
Objective Function	total_value
Solution Status	Optimal
Objective Value	99
Relative Gap	0
Absolute Gap	0
Primal Infeasibility	0
Bound Infeasibility	0
Integer Infeasibility	0
Best Bound	99
Nodes	1
Solutions Found	4
Iterations	7
Presolve Time	0.00
Solution Time	0.20

**In [21]:** `print(print1.get_response())`

	COL1	get
0	book	2.0
1	clock	3.0
2	headphone	2.0
3	mug	-0.0
4	pen	5.0

**In [22]:** `print(solve2.get_solution_summary())`

Solution Summary

	Value
Label	
Solver	MILP
Algorithm	Branch and Cut
Objective Function	total_value
Solution Status	Optimal
Objective Value	76

(continues on next page)

(continued from previous page)

```

Relative Gap                0
Absolute Gap                0
Primal Infeasibility        0
Bound Infeasibility         0
Integer Infeasibility        0

Best Bound                  76
Nodes                      1
Solutions Found             4
Iterations                   3
Presolve Time               0.00
Solution Time               0.20

```

```

In [23]: print(print2.get_response())
          COL1  get
0        book  1.0
1        clock  3.0
2  headphone  2.0
3         mug -0.0
4         pen  2.0

```

## 3.7 Handling Data

sasoptpy can work with native Python types and pandas objects for all data operations. Among pandas object types, sasoptpy works with `pandas.DataFrame` and `pandas.Series` objects to construct and manipulate model components.

### 3.7.1 Indices

Methods like `Model.add_variables()` can use native Python object types such as list and range as variable and constraint indices. You can also use `pandas.Index` objects as indices as well.

#### List

```

In [1]: m = so.Model(name='demo')
NOTE: Initialized model demo.

In [2]: SEASONS = ['Fall', 'Winter', 'Spring', 'Summer']

In [3]: prod_lb = {'Fall': 100, 'Winter': 200, 'Spring': 100, 'Summer': 400}

In [4]: production = m.add_variables(SEASONS, lb=prod_lb, name='production')

In [5]: print(production)
Variable Group (production) [
  [Fall: production[Fall]]
  [Winter: production[Winter]]
  [Spring: production[Spring]]
  [Summer: production[Summer]]
]

```

```
In [6]: print(repr(production['Summer']))
sasoptpy.Variable(name='production[Summer]', lb=400, vartype='CONT')
```

If a list is used as the index set, associated fields such as *lb*, and *ub* should be accessible by using the index keys. Accepted types are dict and `pandas.Series`.

## Range

```
In [7]: link = m.add_variables(range(3), range(2), vartype=so.BIN, name='link')
```

```
In [8]: print(link)
Variable Group (link) [
  [(0, 0): link[0, 0]]
  [(0, 1): link[0, 1]]
  [(1, 0): link[1, 0]]
  [(1, 1): link[1, 1]]
  [(2, 0): link[2, 0]]
  [(2, 1): link[2, 1]]
]
```

```
In [9]: print(repr(link[2, 1]))
sasoptpy.Variable(name='link[2,1]', lb=0, ub=1, vartype='BIN')
```

## pandas.Index

```
In [10]: import pandas as pd
```

```
In [11]: p_data = [[3, 5, 9],
.....:             [0, -1, 14],
.....:             [5, 6, 20]]
.....:
```

```
In [12]: df = pd.DataFrame(p_data, columns=['c1', 'col_lb', 'col_ub'])
```

```
In [13]: x = m.add_variables(df.index, lb=df['c1'], vartype=so.INT, name='x')
```

```
In [14]: print(x)
Variable Group (x) [
  [0: x[0]]
  [1: x[1]]
  [2: x[2]]
]
```

```
In [15]: df2 = df.set_index(['r1', 'r2', 'r3'])
```

```
In [16]: y = m.add_variables(df2.index, lb=df2['col_lb'], ub=df2['col_ub'], name='y')
```

```
In [17]: print(y)
Variable Group (y) [
  [r1: y[r1]]
  [r2: y[r2]]
  [r3: y[r3]]
]
```



```
In [18]: print(repr(y['r1']))
sasoptpy.Variable(name='y[r1]', lb=5, ub=9, vartype='CONT')
```

## Set

sasoptpy can work with data on the server and generate abstract expressions. For this purpose, you can use `Set` objects to represent PROC OPTMODEL sets.

```
In [19]: m2 = so.Model(name='m2')
NOTE: Initialized model m2.

In [20]: I = m2.add_set(name='I')

In [21]: u = m2.add_variables(I, name='u')

In [22]: print(I, u)
I Variable Group (u) [
]
```

See [Workflows](#) for more information about working with server-side models.

## 3.7.2 Data

sasoptpy can work with both client-side and server-side data. Here are some options to load data into the optimization models.

### pandas DataFrame

`pandas.DataFrame` is the preferred object type for passing data into sasoptpy models.

```
In [23]: data = [
.....:     ['clock', 8, 4, 3],
.....:     ['mug', 10, 6, 5],
.....:     ['headphone', 15, 7, 2],
.....:     ['book', 20, 12, 10],
.....:     ['pen', 1, 1, 15]
.....: ]

In [24]: df = pd.DataFrame(data, columns=['item', 'value', 'weight', 'limit']).set_
↳ index(['item'])

In [25]: get = so.VariableGroup(df.index, ub=df['limit'], name='get')

In [26]: print(get)
Variable Group (get) [
  [clock: get[clock]]
  [mug: get[mug]]
  [headphone: get[headphone]]
  [book: get[book]]
  [pen: get[pen]]
]
```

## Dictionaries

You can use lists and dictionaries in expressions and when you create variables.

```
In [27]: items = ['clock', 'mug', 'headphone', 'book', 'pen']

In [28]: limits = {'clock': 3, 'mug': 5, 'headphone': 2, 'book': 10, 'pen': 15}

In [29]: get2 = so.VariableGroup(items, ub=limits, name='get2')

In [30]: print(get2)
Variable Group (get2) [
  [clock: get2[clock]]
  [mug: get2[mug]]
  [headphone: get2[headphone]]
  [book: get2[book]]
  [pen: get2[pen]]
]
```

## CASTable

When data are available on the server-side, you can pass a reference to the object. Using `swat.cas.table.CASTable` and abstract data requires SAS Viya 3.4 or later.

```
In [31]: m2 = so.Model(name='m2', session=session)
NOTE: Initialized model m2.
```

```
In [32]: table = session.upload_frame(df)
NOTE: Cloud Analytic Services made the uploaded file available as table TMPL8QPO6IN_
↳in caslib CASUSER(casuser).
NOTE: The table TMPL8QPO6IN has been created in caslib CASUSER(casuser) from binary_
↳data uploaded to Cloud Analytic Services.
```

```
In [33]: print(type(table), table)
<class 'swat.cas.table.CASTable'> CASTable('TMPL8QPO6IN', caslib='CASUSER(casuser)')
```

```
In [34]: df = pd.DataFrame(data, columns=['item', 'value', 'weight', 'limit'])

In [35]: ITEMS = m.add_set(name='ITEMS')

In [36]: value = m.add_parameter(ITEMS, name='value')

In [37]: weight = m.add_parameter(ITEMS, name='weight')

In [38]: limit = m.add_parameter(ITEMS, name='limit')

In [39]: from sasoptpy.actions import read_data

In [40]: m.include(read_data(table=table, index={'target': ITEMS, 'key': None},
.....:                               columns=[value, weight, limit]))
.....:

In [41]: get3 = m2.add_variables(ITEMS, name='get3')

In [42]: print(get3)
```

(continues on next page)

(continued from previous page)

```
Variable Group (get3) [
]
```

## Abstract Data

If you would like to model your problem first and load data later, you can pass a string for the data that will be available later.

```
In [43]: from sasoptpy.actions import read_data

In [44]: m3 = so.Model(name='m3', session=session)
NOTE: Initialized model m3.

In [45]: ITEMS = m.add_set(name='ITEMS')

In [46]: limit = m.add_parameter(ITEMS, name='limit')

In [47]: m3.include(read_data(table='DF', index=['item'], columns=[limit]))

In [48]: print(type(ITEMS), ITEMS)
<class 'sasoptpy.abstract.set.Set'> ITEMS
```

Note that the key set is created as a reference. You can solve the problem later after having the data available with the same name (for example, by using the `swat.cas.connection.CAS.upload_frame()` function)

```
In [49]: session.upload_frame(df, casout='DF')
NOTE: Cloud Analytic Services made the uploaded file available as table DF in caslib_
↳CASUSER(casuser).
NOTE: The table DF has been created in caslib CASUSER(casuser) from binary data_
↳uploaded to Cloud Analytic Services.
Out[49]: CASTable('DF', caslib='CASUSER(casuser)')
```

## 3.7.3 Operations

You can use lists, `pandas.Series`, and `pandas.DataFrame` objects for mathematical operations such as `VariableGroup.mult()`.

```
In [50]: sd = [3, 5, 6]

In [51]: z = m.add_variables(3, name='z')
```

```
In [52]: print(z)
Variable Group (z) [
  [0: z[0]]
  [1: z[1]]
  [2: z[2]]
]
```

```
In [53]: print(repr(z))
sasoptpy.VariableGroup([0, 1, 2], name='z')
```

```
In [54]: e1 = z.mult(sd)

In [55]: print(e1)
3 * z[0] + 5 * z[1] + 6 * z[2]
```

```
In [56]: ps = pd.Series(sd)

In [57]: e2 = z.mult(ps)

In [58]: print(e2)
3 * z[0] + 5 * z[1] + 6 * z[2]
```

## 3.8 Workflows

sasoptpy can work with both client-side data and server-side data. Some limitations to the functionalities might apply in terms of which workflow is used. In this section, the overall flow of the package is explained.

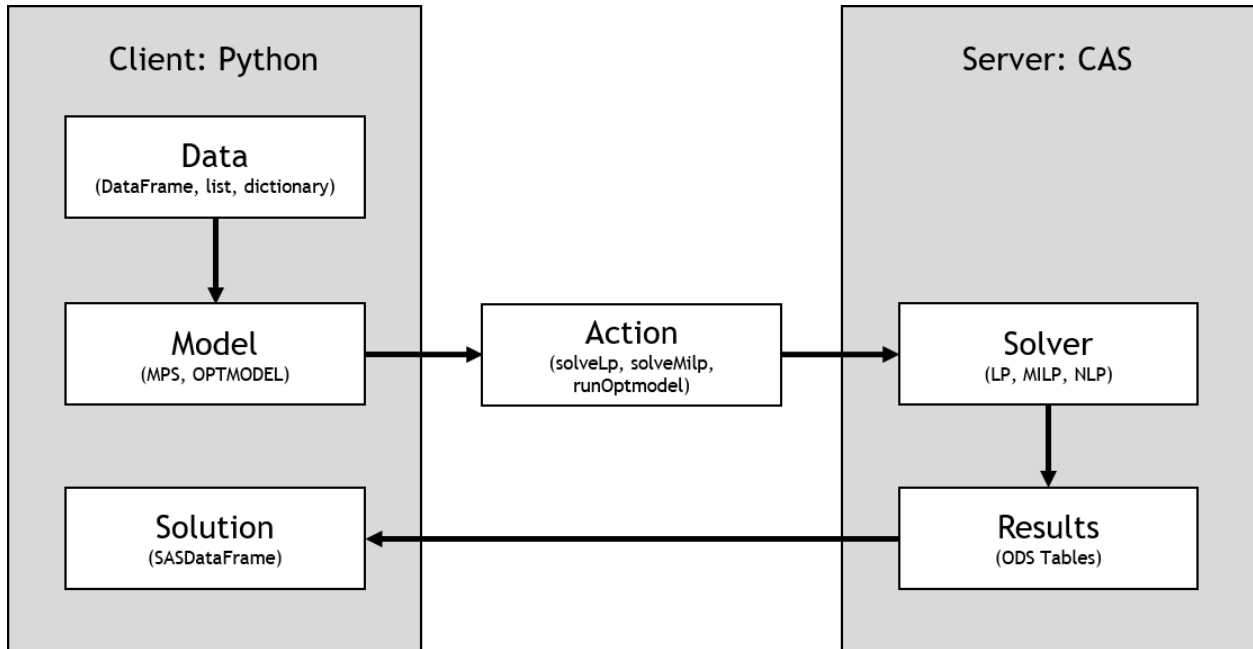
### 3.8.1 Client-side models

If the data are client-side (Python), then a concrete model is generated on the client and is uploaded by using one of the available CAS actions.

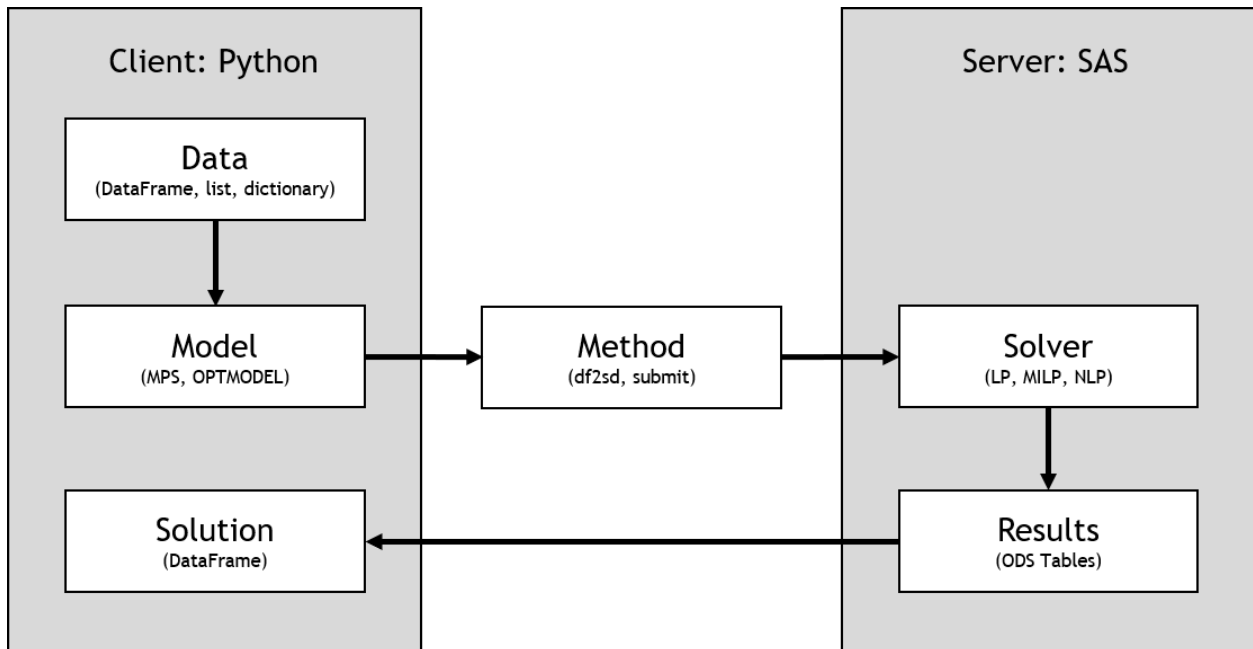
Using a client-side model brings several advantages, such as directly accessing variables, expressions, and constraints. You can more easily perform computationally intensive operations such as filtering data, sorting values, changing variable values, and printing expressions.

There are two main disadvantages of working with client-side models. First, if your model is relatively large, the generated MPS DataFrame or OPTMODEL code might allocate a large amount of memory on your machine. Second, the information that needs to be passed from client to server might be larger than it would be if you use a server-side model.

See the following representation of the client-side model workflow for CAS (Viya) servers:



See the following representation of the client-side model workflow for SAS clients:



Steps of modeling a simple knapsack problem are shown in the following subsections.

#### 1. Reading data:

```

In [1]: import sasoptpy as so

In [2]: import pandas as pd

In [3]: from swat import CAS

In [4]: session = CAS(hostname, port)
  
```

(continues on next page)

(continued from previous page)

```

In [5]: m = so.Model(name='client_CAS', session=session)
NOTE: Initialized model client_CAS.

In [6]: data = [
...:     ['clock', 8, 4, 3],
...:     ['mug', 10, 6, 5],
...:     ['headphone', 15, 7, 2],
...:     ['book', 20, 12, 10],
...:     ['pen', 1, 1, 15]
...: ]

In [7]: df = pd.DataFrame(data, columns=['item', 'value', 'weight', 'limit'])

In [8]: ITEMS = df.index

In [9]: value = df['value']

In [10]: weight = df['weight']

In [11]: limit = df['limit']

In [12]: total_weight = 55

In [13]: print(type(ITEMS), ITEMS)
<class 'pandas.core.indexes.range.RangeIndex'> RangeIndex(start=0, stop=5, step=1)

In [14]: print(type(total_weight), total_weight)
<class 'int'> 55

```

Here, you can obtain the column values one by one:

```

>>> df = df.set_index('item')
>>> ITEMS = df.index.tolist()
>>> value = df['value']
>>> weight = df['weight']
>>> limit = df['limit']

```

## 2. Creating the optimization model:

```

# Variables
In [15]: get = m.add_variables(ITEMS, name='get', vartype=so.INT, lb=0)

# Constraints
In [16]: m.add_constraints((get[i] <= limit[i] for i in ITEMS), name='limit_con');

In [17]: m.add_constraint(
...:     so.expr_sum(weight[i] * get[i] for i in ITEMS) <= total_weight,
...:     name='weight_con');
...:

# Objective
In [18]: total_value = so.expr_sum(value[i] * get[i] for i in ITEMS)

In [19]: m.set_objective(total_value, name='total_value', sense=so.MAX);

```

(continues on next page)

(continued from previous page)

```
# Solve
In [20]: m.solve(verbose=True)
NOTE: Added action set 'optimization'.
NOTE: Converting model client_CAS to OPTMODEL.
    var get {{0,1,2,3,4}} integer >= 0;
    con limit_con_0 : get[0] <= 3;
    con limit_con_1 : get[1] <= 5;
    con limit_con_2 : get[2] <= 2;
    con limit_con_3 : get[3] <= 10;
    con limit_con_4 : get[4] <= 15;
    con weight_con : 4 * get[0] + 6 * get[1] + 7 * get[2] + 12 * get[3] + get[4]
    <= 55;
    max total_value = 8 * get[0] + 10 * get[1] + 15 * get[2] + 20 * get[3] +
    get[4];
    solve;
    create data solution from [i]= {1.._NVAR_} var=_VAR_.name value=_VAR_ lb=_VAR_.
    lb ub=_VAR_.ub rc=_VAR_.rc;
    create data dual from [j] = {1.._NCON_} con=_CON_.name value=_CON_.body dual=_
    CON_.dual;

NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 5 variables (0 free, 0 fixed).
NOTE: The problem has 0 binary and 5 integer variables.
NOTE: The problem has 6 linear constraints (6 LE, 0 EQ, 0 GE, 0 range).
NOTE: The problem has 10 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 5 constraints.
NOTE: The MILP presolver removed 5 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The presolved problem has 5 variables, 1 constraints, and 5 constraint
    coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.
```

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	4	99.0000000	199.0000000	50.25%	0
0	1	4	99.0000000	102.3333333	3.26%	0
0	1	4	99.0000000	102.3333333	3.26%	0

```
NOTE: The MILP presolver is applied again.
    0      1      4      99.0000000      102.3333333      3.26%      0
NOTE: Optimal.
NOTE: Objective = 99.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 5 rows and 6
    columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 6 rows and 4
    columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows
    and 4 columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and
    4 columns.
Out [20]:
Selected Rows from Table SOLUTION
```

(continues on next page)

(continued from previous page)

	i	var	value	lb	ub	rc
0	1.0	get[0]	2.0	-0.0	1.797693e+308	NaN
1	2.0	get[1]	5.0	-0.0	1.797693e+308	NaN
2	3.0	get[2]	2.0	-0.0	1.797693e+308	NaN
3	4.0	get[3]	-0.0	-0.0	1.797693e+308	NaN
4	5.0	get[4]	3.0	-0.0	1.797693e+308	NaN

You can display the generated OPTMODEL code at run time by using the `verbose=True` option. Here, you can see the coefficient values of the parameters inside the model.

### 3. Parsing the results:

After the solve, the primal and dual solution tables are obtained. You can print the solution tables by using the `Model.get_solution()` method.

It is also possible to print the optimal solution by using the `get_solution_table()` function.

```
In [21]: print(m.get_solution())
Selected Rows from Table SOLUTION
```

	i	var	value	lb	ub	rc
0	1.0	get[0]	2.0	-0.0	1.797693e+308	NaN
1	2.0	get[1]	5.0	-0.0	1.797693e+308	NaN
2	3.0	get[2]	2.0	-0.0	1.797693e+308	NaN
3	4.0	get[3]	-0.0	-0.0	1.797693e+308	NaN
4	5.0	get[4]	3.0	-0.0	1.797693e+308	NaN

```
In [22]: print(so.get_solution_table(get, key=ITEMS))
get
0 2.0
1 5.0
2 2.0
3 -0.0
4 3.0
```

```
In [23]: print('Total value:', total_value.get_value())
Total value: 99.0
```

## 3.8.2 Server-side models

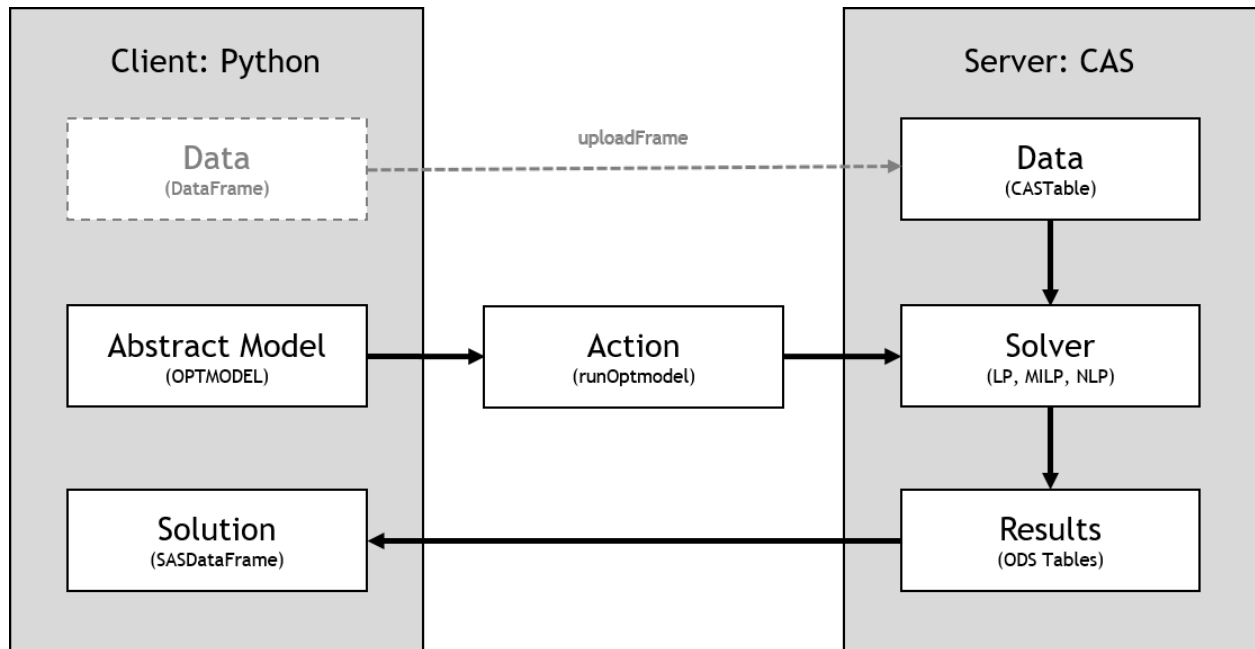
If the data are server-side (CAS or SAS), then an abstract model is generated on the client. This abstract model is later converted to PROC OPTMODEL code, which reads the data on the server.

The main advantage of the server-side models is faster upload times compared to client-side models. This is especially noticeable when using large numbers of variable and constraint groups.

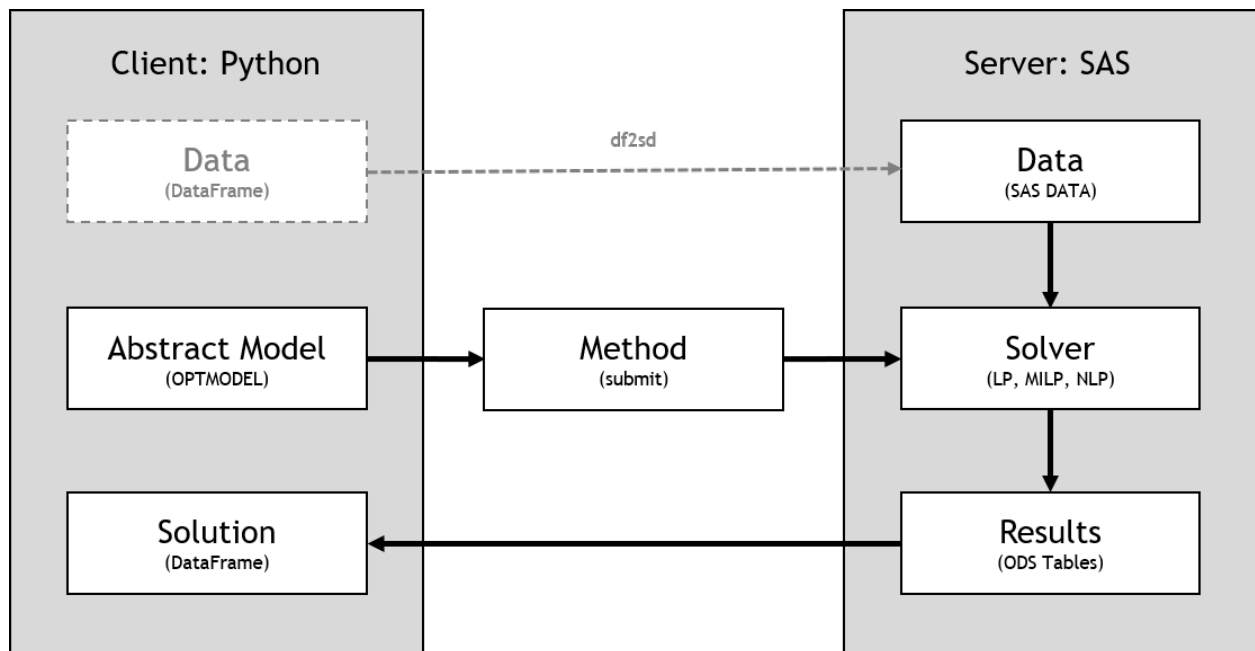
The only disadvantage of using server-side models is that variables often need to be accessed directly from the resulting SAS DataFrame objects. Because components of the models are abstract, accessing objects directly is often not possible.

See the following representation of the server-side model workflow for CAS (Viya) servers:





See the following representation of the server-side model workflow for SAS clients:



In the following steps, the same example is solved by using server-side data.

1. Creating the optimization model:

```
In [24]: from sasoptpy.actions import read_data
```

```
In [25]: m = so.Model(name='client_CAS', session=session)
NOTE: Initialized model client_CAS.
```

```
In [26]: cas_table = session.upload_frame(df, casout='data')
```

NOTE: Cloud Analytic Services made the uploaded file available as table DATA in\_ (continues on next page)  
 ↳ caslib CASUSER(casuser).

(continued from previous page)

NOTE: The table DATA has been created in caslib CASUSER(casuser) from binary data, uploaded to Cloud Analytic Services.

```
In [27]: ITEMS = m.add_set(name='ITEMS', settype=so.STR)

In [28]: value = m.add_parameter(ITEMS, name='value')

In [29]: weight = m.add_parameter(ITEMS, name='weight')

In [30]: limit = m.add_parameter(ITEMS, name='limit')

In [31]: m.include(read_data(
.....:     table=cas_table, index={'target':ITEMS, 'key': 'item'},
.....:     columns=[value, weight, limit]))
.....:

# Variables
In [32]: get = m.add_variables(ITEMS, name='get', vartype=so.INT, lb=0)

# Constraints
In [33]: m.add_constraints((get[i] <= limit[i] for i in ITEMS), name='limit_con');

In [34]: m.add_constraint(
.....:     so.expr_sum(weight[i] * get[i] for i in ITEMS) <= total_weight,
.....:     name='weight_con');
.....:

# Objective
In [35]: total_value = so.expr_sum(value[i] * get[i] for i in ITEMS)

In [36]: m.set_objective(total_value, name='total_value', sense=so.MAX);

# Solve
In [37]: m.solve(verbose=True)
NOTE: Added action set 'optimization'.
NOTE: Converting model client_CAS to OPTMODEL.
    set <str> ITEMS;
    num value {{ITEMS}};
    num weight {{ITEMS}};
    num limit {{ITEMS}};
    read data DATA into ITEMS=[item] value weight limit;
    var get {{ITEMS}} integer >= 0;
    con limit_con {o37 in ITEMS} : get[o37] - limit[o37] <= 0;
    con weight_con : sum {i in ITEMS} (weight[i] * get[i]) <= 55;
    max total_value = sum {i in ITEMS} (value[i] * get[i]);
    solve;
    create data solution from [i]= {1.._NVAR_} var=_VAR_.name value=_VAR_ lb=_VAR_.
    ↳lb ub=_VAR_.ub rc=_VAR_.rc;
    create data dual from [j] = {1.._NCON_} con=_CON_.name value=_CON_.body dual=_
    ↳CON_.dual;

NOTE: Submitting OPTMODEL code to CAS server.
NOTE: There were 5 rows read from table 'DATA' in caslib 'CASUSER(casuser)'.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 5 variables (0 free, 0 fixed).
NOTE: The problem has 0 binary and 5 integer variables.
```

(continues on next page)

(continued from previous page)

```

NOTE: The problem has 6 linear constraints (6 LE, 0 EQ, 0 GE, 0 range).
NOTE: The problem has 10 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 5 constraints.
NOTE: The MILP presolver removed 5 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The presolved problem has 5 variables, 1 constraints, and 5 constraint_
↪coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.

```

	Node	Active	Sols	BestInteger	BestBound	Gap	Time
	0	1	4	99.0000000	199.0000000	50.25%	0
	0	1	4	99.0000000	102.3333333	3.26%	0
	0	0	4	99.0000000	99.0000000	0.00%	0

```

NOTE: Optimal.
NOTE: Objective = 99.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 5 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 6 rows and 4_
↪columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows_
↪and 4 columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and_
↪4 columns.
Out [37]:
Selected Rows from Table SOLUTION

```

	i	var	value	lb	ub	rc
0	1.0	get[book]	2.0	-0.0	1.797693e+308	NaN
1	2.0	get[clock]	3.0	-0.0	1.797693e+308	NaN
2	3.0	get[headphone]	2.0	-0.0	1.797693e+308	NaN
3	4.0	get[mug]	-0.0	-0.0	1.797693e+308	NaN
4	5.0	get[pen]	5.0	-0.0	1.797693e+308	NaN

## 2. Parsing the results:

```

# Print results
In [38]: print(m.get_solution())
Selected Rows from Table SOLUTION

```

	i	var	value	lb	ub	rc
0	1.0	get[book]	2.0	-0.0	1.797693e+308	NaN
1	2.0	get[clock]	3.0	-0.0	1.797693e+308	NaN
2	3.0	get[headphone]	2.0	-0.0	1.797693e+308	NaN
3	4.0	get[mug]	-0.0	-0.0	1.797693e+308	NaN
4	5.0	get[pen]	5.0	-0.0	1.797693e+308	NaN

```

In [39]: print('Total value:', m.get_objective_value())
Total value: 99.0

```

Because there is no direct access to expressions and variables, the optimal solution is printed by using the server response.

### **3.8.3 Limitations**

- In SAS Viya, nonlinear models can be solved only by using the `runOptmodel` action, which requires SAS Viya 3.4 or later.
- User-defined decomposition blocks are available only in MPS mode, and therefore work only with client-side data.
- Mixed usage (client-side and server-side data) might not work in some cases. A quick fix would be transferring the data in either direction.

## EXAMPLES

Examples are provided from [SAS/OR documentation](#).

This chapter is split into 3 parts.

- The *first part* of examples demonstrate using SAS Viya (SAS Optimization) solvers with concrete problem formulation.
- The *second part* of examples demonstrate using SAS Viya (SAS Optimization) solvers with abstract problem formulation.
- The *third part* of examples demonstrate using SAS 9.4 (SAS/OR) solvers.

### 4.1 SAS Viya Examples (Concrete)

#### 4.1.1 Food Manufacture 1

##### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex1\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex1_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex01.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex01.html)

##### Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn):

    # Problem data
    OILS = ['veg1', 'veg2', 'oil1', 'oil2', 'oil3']
    PERIODS = range(1, 7)
    cost_data = [
        [110, 120, 130, 110, 115],
        [130, 130, 110, 90, 115],
        [110, 140, 130, 100, 95],
        [120, 110, 120, 120, 125],
        [100, 120, 150, 110, 105],
        [90, 100, 140, 80, 135]]
```

(continues on next page)

(continued from previous page)

```

cost = pd.DataFrame(cost_data, columns=OILS, index=PERIODS).transpose()
hardness_data = [8.8, 6.1, 2.0, 4.2, 5.0]
hardness = {OILS[i]: hardness_data[i] for i in range(len(OILS))}

revenue_per_ton = 150
veg_ub = 200
nonveg_ub = 250
store_ub = 1000
storage_cost_per_ton = 5
hardness_lb = 3
hardness_ub = 6
init_storage = 500

# Problem initialization
m = so.Model(name='food_manufacture_1', session=cas_conn)

# Problem definition
buy = m.add_variables(OILS, PERIODS, lb=0, name='buy')
use = m.add_variables(OILS, PERIODS, lb=0, name='use')
manufacture = m.add_implicit_variable((use.sum('*', p) for p in PERIODS),
                                       name='manufacture')

last_period = len(PERIODS)
store = m.add_variables(OILS, [0] + list(PERIODS), lb=0, ub=store_ub,
                        name='store')

for oil in OILS:
    store[oil, 0].set_bounds(lb=init_storage, ub=init_storage)
    store[oil, last_period].set_bounds(lb=init_storage, ub=init_storage)
VEG = [i for i in OILS if 'veg' in i]
NONVEG = [i for i in OILS if i not in VEG]
revenue = so.expr_sum(revenue_per_ton * manufacture[p] for p in PERIODS)
rawcost = so.expr_sum(cost.at[o, p] * buy[o, p]
                      for o in OILS for p in PERIODS)
storagecost = so.expr_sum(storage_cost_per_ton * store[o, p]
                          for o in OILS for p in PERIODS)
m.set_objective(revenue - rawcost - storagecost, sense=so.MAX,
               name='profit')

# Constraints
m.add_constraints((use.sum(VEG, p) <= veg_ub for p in PERIODS),
                 name='veg_ub')
m.add_constraints((use.sum(NONVEG, p) <= nonveg_ub for p in PERIODS),
                 name='nonveg_ub')
m.add_constraints((store[o, p-1] + buy[o, p] == use[o, p] + store[o, p]
                  for o in OILS for p in PERIODS),
                 name='flow_balance')
m.add_constraints((so.expr_sum(hardness[o]*use[o, p] for o in OILS) >=
                  hardness_lb * manufacture[p] for p in PERIODS),
                 name='hardness_ub')
m.add_constraints((so.expr_sum(hardness[o]*use[o, p] for o in OILS) <=
                  hardness_ub * manufacture[p] for p in PERIODS),
                 name='hardness_lb')

# Solver call
res = m.solve()

# With other solve options
m.solve(options={'with': 'lp', 'algorithm': 'PS'})

```

(continues on next page)

(continued from previous page)

```

m.solve(options={'with': 'lp', 'algorithm': 'IP'})
m.solve(options={'with': 'lp', 'algorithm': 'NS'})

if res is not None:
    print(so.get_solution_table(buy, use, store))

return m.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.client_side.food_manufacture_1 import test

In [8]: test(cas_conn)
NOTE: Initialized model food_manufacture_1.
NOTE: Added action set 'optimization'.
NOTE: Converting model food_manufacture_1 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 95 variables (0 free, 10 fixed).
NOTE: The problem has 54 linear constraints (18 LE, 30 EQ, 6 GE, 0 range).
NOTE: The problem has 210 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 44 variables and 4 constraints.
NOTE: The LP presolver removed 48 constraint coefficients.
NOTE: The presolved problem has 51 variables, 50 constraints, and 162 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

	Phase	Iteration	Objective Value	Time	
	D	2	4.755480E+05	0	
	P	2	49	1.078426E+05	0

```

NOTE: Optimal.
NOTE: Objective = 107842.59259.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 95 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 54 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↪columns.

```

(continues on next page)

(continued from previous page)

```

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.
NOTE: Added action set 'optimization'.
NOTE: Converting model food_manufacture_1 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 95 variables (0 free, 10 fixed).
NOTE: The problem has 54 linear constraints (18 LE, 30 EQ, 6 GE, 0 range).
NOTE: The problem has 210 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 44 variables and 4 constraints.
NOTE: The LP presolver removed 48 constraint coefficients.
NOTE: The presolved problem has 51 variables, 50 constraints, and 162 constraint_
↳coefficients.
NOTE: The LP solver is called.
NOTE: The Primal Simplex algorithm is used.

```

		Objective		
Phase Iteration		Value	Time	
P	1	1.749040E+03	0	
P	2	3.638889E+04	0	
D	2	1.078426E+05	0	

```

NOTE: Optimal.
NOTE: Objective = 107842.59259.
NOTE: The Primal Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 95 rows and 6_
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 54 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.
NOTE: Added action set 'optimization'.
NOTE: Converting model food_manufacture_1 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 95 variables (0 free, 10 fixed).
NOTE: The problem has 54 linear constraints (18 LE, 30 EQ, 6 GE, 0 range).
NOTE: The problem has 210 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 44 variables and 4 constraints.
NOTE: The LP presolver removed 48 constraint coefficients.
NOTE: The LP presolver modified 0 constraint coefficients.
NOTE: The presolved problem has 51 variables, 50 constraints, and 162 constraint_
↳coefficients.
NOTE: The LP solver is called.
NOTE: The Interior Point algorithm is used.
NOTE: The deterministic parallel mode is enabled.
NOTE: The Interior Point algorithm is using up to 8 threads.

```

		Primal		Bound		Dual	Time
Iter	Complement	Duality Gap	Infeas	Infeas	Infeas	Infeas	
0	1.1003E+04	1.3994E+01	2.0602E-02	1.1145E-02	1.2444E+00	0	
1	1.0498E+04	4.1015E+01	1.7385E-02	9.4051E-03	1.0928E+00	0	
2	7.2084E+03	7.4551E+00	5.6703E-03	3.0675E-03	6.8365E-01	0	

(continues on next page)



(continued from previous page)

3	1.7518E+03	1.1221E+00	1.5798E-03	8.5465E-04	1.1852E-01	0
4	4.1038E+02	2.5544E-01	5.6092E-04	3.0344E-04	1.1852E-03	0
5	3.9774E+01	2.2775E-02	7.2994E-05	3.9488E-05	1.9281E-05	0
6	9.9400E-01	5.6526E-04	7.9112E-07	4.2798E-07	7.7185E-07	0
7	9.9572E-03	5.6615E-06	7.9420E-09	4.2964E-09	7.7239E-09	0
8	0.0000E+00	1.8686E-08	1.6613E-07	1.1864E-10	6.2833E-07	0

NOTE: The Interior Point solve time is 0.01 seconds.

NOTE: The Crossover option is enabled.

NOTE: The crossover basis contains 11 primal and 3 dual superbasic variables.

		Objective		
Phase	Iteration	Value	Time	
P	C	1	1.014226E+03	0
D	C	13	9.697429E+00	0
D	2	16	1.078426E+05	0
P	2	17	1.078426E+05	0
D	2	18	1.078426E+05	0

NOTE: The Crossover time is 0.01 seconds.

NOTE: Optimal.

NOTE: Objective = 107842.59259.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 95 rows and 6 columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 54 rows and 4 columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 16 rows and 4 columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4 columns.

NOTE: Added action set 'optimization'.

NOTE: Converting model food\_manufacture\_1 to OPTMODEL.

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 95 variables (0 free, 10 fixed).

NOTE: The problem has 54 linear constraints (18 LE, 30 EQ, 6 GE, 0 range).

NOTE: The problem has 210 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The LP presolver value AUTOMATIC is applied.

NOTE: The LP presolver time is 0.00 seconds.

NOTE: The LP presolver removed 44 variables and 4 constraints.

NOTE: The LP presolver removed 48 constraint coefficients.

NOTE: The presolved problem has 51 variables, 50 constraints, and 162 constraint coefficients.

NOTE: The LP solver is called.

NOTE: The Network Simplex algorithm is used.

NOTE: The network has 20 rows (40.00%), 29 columns (56.86%), and 1 component.

NOTE: The network extraction and setup time is 0.01 seconds.

		Primal	Primal	Dual	
Iteration	Objective	Infeasibility	Infeasibility	Time	
1	3.750000E+03	5.000000E+02	1.551000E+03	0.01	
24	7.125000E+04	0.000000E+00	0.000000E+00	0.01	

NOTE: The Network Simplex solve time is 0.00 seconds.

NOTE: The total Network Simplex solve time is 0.01 seconds.

NOTE: The Dual Simplex algorithm is used.

		Objective		
Phase	Iteration	Value	Time	
D	2	1	2.240180E+05	0
P	2	43	1.078426E+05	0

NOTE: Optimal.

NOTE: Objective = 107842.59259.

(continues on next page)

(continued from previous page)

NOTE: The Simplex solve time is 0.02 seconds.  
 NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 95 rows and 6\_  
 ↪columns.  
 NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 54 rows and 4 columns.  
 NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 14 rows and 4\_  
 ↪columns.  
 NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4\_  
 ↪columns.

		buy	use	store
veg1	1	0.000000e+00	8.518519e+01	4.148148e+02
veg1	2	0.000000e+00	1.592593e+02	2.555556e+02
veg1	3	2.842171e-14	0.000000e+00	2.555556e+02
veg1	4	-1.421085e-14	1.592593e+02	9.629630e+01
veg1	5	7.105427e-14	9.629630e+01	0.000000e+00
veg1	6	6.592593e+02	1.592593e+02	5.000000e+02
veg2	1	-5.684342e-14	1.148148e+02	3.851852e+02
veg2	2	0.000000e+00	4.074074e+01	3.444444e+02
veg2	3	2.842171e-14	2.000000e+02	1.444444e+02
veg2	4	-2.842171e-14	4.074074e+01	1.037037e+02
veg2	5	0.000000e+00	1.037037e+02	0.000000e+00
veg2	6	5.407407e+02	4.074074e+01	5.000000e+02
oil1	1	0.000000e+00	0.000000e+00	5.000000e+02
oil1	2	0.000000e+00	0.000000e+00	5.000000e+02
oil1	3	0.000000e+00	0.000000e+00	5.000000e+02
oil1	4	0.000000e+00	-1.744059e-14	5.000000e+02
oil1	5	0.000000e+00	0.000000e+00	5.000000e+02
oil1	6	0.000000e+00	0.000000e+00	5.000000e+02
oil2	1	0.000000e+00	0.000000e+00	5.000000e+02
oil2	2	2.500000e+02	2.500000e+02	5.000000e+02
oil2	3	0.000000e+00	2.273737e-13	5.000000e+02
oil2	4	2.842171e-14	2.500000e+02	2.500000e+02
oil2	5	0.000000e+00	2.500000e+02	0.000000e+00
oil2	6	7.500000e+02	2.500000e+02	5.000000e+02
oil3	1	0.000000e+00	2.500000e+02	2.500000e+02
oil3	2	0.000000e+00	0.000000e+00	2.500000e+02
oil3	3	-5.048710e-29	2.500000e+02	-2.842171e-13
oil3	4	2.842171e-13	0.000000e+00	0.000000e+00
oil3	5	5.000000e+02	0.000000e+00	5.000000e+02
oil3	6	0.000000e+00	0.000000e+00	5.000000e+02
veg1	0	NaN	NaN	5.000000e+02
veg2	0	NaN	NaN	5.000000e+02
oil1	0	NaN	NaN	5.000000e+02
oil2	0	NaN	NaN	5.000000e+02
oil3	0	NaN	NaN	5.000000e+02

**Out [8]:** 107842.59259259264

## 4.1.2 Food Manufacture 2

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex2\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex2_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex02.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex02.html)

### Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn):

    # Problem data
    OILS = ['veg1', 'veg2', 'oil1', 'oil2', 'oil3']
    PERIODS = range(1, 7)
    cost_data = [
        [110, 120, 130, 110, 115],
        [130, 130, 110, 90, 115],
        [110, 140, 130, 100, 95],
        [120, 110, 120, 120, 125],
        [100, 120, 150, 110, 105],
        [90, 100, 140, 80, 135]]
    cost = pd.DataFrame(cost_data, columns=OILS, index=PERIODS).transpose()
    hardness_data = [8.8, 6.1, 2.0, 4.2, 5.0]
    hardness = {OILS[i]: hardness_data[i] for i in range(len(OILS))}

    revenue_per_ton = 150
    veg_ub = 200
    nonveg_ub = 250
    store_ub = 1000
    storage_cost_per_ton = 5
    hardness_lb = 3
    hardness_ub = 6
    init_storage = 500
    max_num_oils_used = 3
    min_oil_used_threshold = 20

    # Problem initialization
    m = so.Model(name='food_manufacture_2', session=cas_conn)

    # Problem definition
    buy = m.add_variables(OILS, PERIODS, lb=0, name='buy')
    use = m.add_variables(OILS, PERIODS, lb=0, name='use')
    manufacture = m.add_implicit_variable((use.sum('*', p) for p in PERIODS),
                                           name='manufacture')

    last_period = len(PERIODS)
    store = m.add_variables(OILS, [0] + list(PERIODS), lb=0, ub=store_ub,
                           name='store')

    for oil in OILS:
        store[oil, 0].set_bounds(lb=init_storage, ub=init_storage)
        store[oil, last_period].set_bounds(lb=init_storage, ub=init_storage)
```

(continues on next page)

(continued from previous page)

```

VEG = [i for i in OILS if 'veg' in i]
NONVEG = [i for i in OILS if i not in VEG]
revenue = so.expr_sum(revenue_per_ton * manufacture[p] for p in PERIODS)
rawcost = so.expr_sum(cost.at[o, p] * buy[o, p]
                      for o in OILS for p in PERIODS)
storagecost = so.expr_sum(storage_cost_per_ton * store[o, p]
                          for o in OILS for p in PERIODS)
m.set_objective(revenue - rawcost - storagecost, sense=so.MAX,
               name='profit')

# Constraints
m.add_constraints((use.sum(VEG, p) <= veg_ub for p in PERIODS),
                 name='veg_ub')
m.add_constraints((use.sum(NONVEG, p) <= nonveg_ub for p in PERIODS),
                 name='nonveg_ub')
m.add_constraints((store[o, p-1] + buy[o, p] == use[o, p] + store[o, p]
                  for o in OILS for p in PERIODS),
                 name='flow_balance')
m.add_constraints((so.expr_sum(hardness[o]*use[o, p] for o in OILS) >=
                  hardness_lb * manufacture[p] for p in PERIODS),
                 name='hardness_ub')
m.add_constraints((so.expr_sum(hardness[o]*use[o, p] for o in OILS) <=
                  hardness_ub * manufacture[p] for p in PERIODS),
                 name='hardness_lb')

# Additions to the first problem
isUsed = m.add_variables(OILS, PERIODS, vartype=so.BIN, name='is_used')
for p in PERIODS:
    for o in VEG:
        use[o, p].set_bounds(ub=veg_ub)
    for o in NONVEG:
        use[o, p].set_bounds(ub=nonveg_ub)
m.add_constraints((use[o, p] <= use[o, p].ub * isUsed[o, p]
                  for o in OILS for p in PERIODS), name='link')
m.add_constraints((isUsed.sum('*', p) <= max_num_oils_used
                  for p in PERIODS), name='logical1')
m.add_constraints((use[o, p] >= min_oil_used_threshold * isUsed[o, p]
                  for o in OILS for p in PERIODS), name='logical2')
m.add_constraints((isUsed[o, p] <= isUsed['oil3', p]
                  for o in ['veg1', 'veg2'] for p in PERIODS),
                 name='logical3')

res = m.solve()
if res is not None:
    print(so.get_solution_table(buy, use, store, isUsed))

return m.get_objective_value()

```

## Output

```
In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.client_side.food_manufacture_2 import test

In [8]: test(cas_conn)
NOTE: Initialized model food_manufacture_2.
NOTE: Added action set 'optimization'.
NOTE: Converting model food_manufacture_2 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 125 variables (0 free, 10 fixed).
NOTE: The problem has 30 binary and 0 integer variables.
NOTE: The problem has 132 linear constraints (66 LE, 30 EQ, 36 GE, 0 range).
NOTE: The problem has 384 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 50 variables and 10 constraints.
NOTE: The MILP presolver removed 66 constraint coefficients.
NOTE: The MILP presolver modified 6 constraint coefficients.
NOTE: The presolved problem has 75 variables, 122 constraints, and 318 constraint_
↪coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.
```

	Node	Active	Sols	BestInteger	BestBound	Gap	Time
	0	1	5	36900.0000000	343250	89.25%	0
	0	1	5	36900.0000000	107333	65.62%	0
	0	1	5	36900.0000000	105799	65.12%	0
	0	1	5	36900.0000000	105650	65.07%	0
	0	1	5	36900.0000000	105650	65.07%	0
	0	1	5	36900.0000000	105650	65.07%	0
	0	1	5	36900.0000000	105650	65.07%	0
	0	1	5	36900.0000000	105650	65.07%	0
	0	1	6	99491.6666667	105650	5.83%	0
NOTE: The MILP solver added 15 cuts with 77 cut coefficients at the root.							
	10	6	7	99683.3343492	105090	5.15%	0
	28	19	8	99908.3333333	104782	4.65%	0
	68	45	9	99908.3333333	104564	4.45%	0
	139	80	10	100054	104225	4.00%	0
	145	75	11	100192	103683	3.37%	0
	177	86	12	100192	103516	3.21%	0
	183	87	13	100214	103516	3.19%	0
	189	85	14	100279	103268	2.89%	0

(continues on next page)

(continued from previous page)

283	40	15	100279	102053	1.74%	0
284	40	16	100279	102053	1.74%	0
333	0	16	100279	100279	0.00%	0

NOTE: Optimal.

NOTE: Objective = 100278.70577.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 125 rows and 6 columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 132 rows and 4 columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4 columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4 columns.

	buy	use	store	is_used
veg1 1	0.000000e+00	8.518519e+01	4.148148e+02	1.000000e+00
veg1 2	0.000000e+00	8.518519e+01	3.296296e+02	1.000000e+00
veg1 3	0.000000e+00	0.000000e+00	3.296296e+02	0.000000e+00
veg1 4	0.000000e+00	1.550000e+02	1.746296e+02	9.999948e-01
veg1 5	0.000000e+00	1.550000e+02	1.962960e+01	1.000000e+00
veg1 6	4.803704e+02	0.000000e+00	5.000000e+02	0.000000e+00
veg2 1	0.000000e+00	1.148148e+02	3.851852e+02	1.000000e+00
veg2 2	0.000000e+00	1.148148e+02	2.703704e+02	1.000000e+00
veg2 3	0.000000e+00	2.000000e+02	7.037037e+01	1.000000e+00
veg2 4	-1.421085e-14	0.000000e+00	7.037037e+01	-1.949310e-15
veg2 5	0.000000e+00	0.000000e+00	7.037037e+01	-0.000000e+00
veg2 6	6.296296e+02	2.000000e+02	5.000000e+02	1.000000e+00
oil1 1	0.000000e+00	0.000000e+00	5.000000e+02	0.000000e+00
oil1 2	-5.684342e-14	0.000000e+00	5.000000e+02	0.000000e+00
oil1 3	0.000000e+00	0.000000e+00	5.000000e+02	-0.000000e+00
oil1 4	5.684342e-14	0.000000e+00	5.000000e+02	0.000000e+00
oil1 5	0.000000e+00	0.000000e+00	5.000000e+02	0.000000e+00
oil1 6	0.000000e+00	0.000000e+00	5.000000e+02	0.000000e+00
oil2 1	0.000000e+00	0.000000e+00	5.000000e+02	-0.000000e+00
oil2 2	1.900001e+02	2.273737e-13	6.900001e+02	9.094947e-16
oil2 3	0.000000e+00	2.300000e+02	4.600001e+02	1.000000e+00
oil2 4	-2.842171e-14	2.300001e+02	2.300000e+02	1.000000e+00
oil2 5	2.842171e-14	2.300000e+02	0.000000e+00	1.000000e+00
oil2 6	7.300000e+02	2.300000e+02	5.000000e+02	1.000000e+00
oil3 1	0.000000e+00	2.500000e+02	2.500000e+02	1.000000e+00
oil3 2	0.000000e+00	2.500000e+02	2.557954e-13	1.000000e+00
oil3 3	5.799999e+02	2.000000e+01	5.599999e+02	1.000000e+00
oil3 4	0.000000e+00	1.999990e+01	5.400000e+02	9.999948e-01
oil3 5	0.000000e+00	2.000000e+01	5.200000e+02	1.000000e+00
oil3 6	0.000000e+00	2.000000e+01	5.000000e+02	1.000000e+00
veg1 0	NaN	NaN	5.000000e+02	NaN
veg2 0	NaN	NaN	5.000000e+02	NaN
oil1 0	NaN	NaN	5.000000e+02	NaN
oil2 0	NaN	NaN	5.000000e+02	NaN
oil3 0	NaN	NaN	5.000000e+02	NaN

Out [8]: 100278.70576513262

### 4.1.3 Factory Planning 1

#### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex3\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex3_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [https://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex03.html](https://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex03.html)

#### Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='factory_planning_1', session=cas_conn)

    # Input data
    product_list = ['prod{}'.format(i) for i in range(1, 8)]
    product_data = pd.DataFrame([10, 6, 8, 4, 11, 9, 3],
                                columns=['profit'], index=product_list)

    demand_data = [
        [500, 1000, 300, 300, 800, 200, 100],
        [600, 500, 200, 0, 400, 300, 150],
        [300, 600, 0, 0, 500, 400, 100],
        [200, 300, 400, 500, 200, 0, 100],
        [0, 100, 500, 100, 1000, 300, 0],
        [500, 500, 100, 300, 1100, 500, 60]]
    demand_data = pd.DataFrame(
        demand_data, columns=product_list, index=range(1, 7))
    machine_types_data = [
        ['grinder', 4],
        ['vdrill', 2],
        ['hdrill', 3],
        ['borer', 1],
        ['planer', 1]]
    machine_types_data = pd.DataFrame(machine_types_data, columns=[
        'machine_type', 'num_machines']).set_index(['machine_type'])
    machine_type_period_data = [
        ['grinder', 1, 1],
        ['hdrill', 2, 2],
        ['borer', 3, 1],
        ['vdrill', 4, 1],
        ['grinder', 5, 1],
        ['vdrill', 5, 1],
        ['planer', 6, 1],
        ['hdrill', 6, 1]]
    machine_type_period_data = pd.DataFrame(machine_type_period_data, columns=[
        'machine_type', 'period', 'num_down'])
    machine_type_product_data = [
        ['grinder', 0.5, 0.7, 0, 0, 0.3, 0.2, 0.5],
        ['vdrill', 0.1, 0.2, 0, 0.3, 0, 0.6, 0],
        ['hdrill', 0.2, 0, 0.8, 0, 0, 0, 0.6],
        ['borer', 0.05, 0.03, 0, 0.07, 0.1, 0, 0.08],
```

(continues on next page)

(continued from previous page)

```

    ['planer', 0, 0, 0.01, 0, 0.05, 0, 0.05]]
machine_type_product_data = \
    pd.DataFrame(machine_type_product_data, columns=['machine_type'] +
                  product_list).set_index(['machine_type'])
store_ub = 100
storage_cost_per_unit = 0.5
final_storage = 50
num_hours_per_period = 24 * 2 * 8

# Problem definition
PRODUCTS = product_list
PERIODS = range(1, 7)
MACHINE_TYPES = machine_types_data.index.values

num_machine_per_period = pd.DataFrame()
for i in range(1, 7):
    num_machine_per_period[i] = machine_types_data['num_machines']
for _, row in machine_type_period_data.iterrows():
    num_machine_per_period.at[row['machine_type'],
                              row['period']] -= row['num_down']

make = m.add_variables(PRODUCTS, PERIODS, lb=0, name='make')
sell = m.add_variables(PRODUCTS, PERIODS, lb=0, ub=demand_data.transpose(),
                       name='sell')

store = m.add_variables(PRODUCTS, PERIODS, lb=0, ub=store_ub, name='store')
for p in PRODUCTS:
    store[p, 6].set_bounds(lb=final_storage, ub=final_storage+1)

storageCost = storage_cost_per_unit * store.sum('*', '*')
revenue = so.expr_sum(product_data.at[p, 'profit'] * sell[p, t]
                      for p in PRODUCTS for t in PERIODS)
m.set_objective(revenue-storageCost, sense=so.MAX, name='total_profit')

production_time = machine_type_product_data
m.add_constraints((
    so.expr_sum(production_time.at[mc, p] * make[p, t] for p in PRODUCTS)
    <= num_hours_per_period * num_machine_per_period.at[mc, t]
    for mc in MACHINE_TYPES for t in PERIODS), name='machine_hours')
m.add_constraints(((store[p, t-1] if t-1 in PERIODS else 0) + make[p, t] ==
                   sell[p, t] + store[p, t] for p in PRODUCTS
                   for t in PERIODS),
                  name='flow_balance')

res = m.solve()
if res is not None:
    print(so.get_solution_table(make, sell, store))

return m.get_objective_value()

```



## Output

```
In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.client_side.factory_planning_1 import test

In [8]: test(cas_conn)
NOTE: Initialized model factory_planning_1.
NOTE: Added action set 'optimization'.
NOTE: Converting model factory_planning_1 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 126 variables (0 free, 6 fixed).
NOTE: The problem has 72 linear constraints (30 LE, 42 EQ, 0 GE, 0 range).
NOTE: The problem has 281 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 60 variables and 46 constraints.
NOTE: The LP presolver removed 178 constraint coefficients.
NOTE: The presolved problem has 66 variables, 26 constraints, and 103 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

      Objective
      Value
Phase Iteration      Time
D 2          1  9.478510E+04  0
P 2          21  9.371518E+04  0

NOTE: Optimal.
NOTE: Objective = 93715.178571.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 126 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 72 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↪columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↪columns.

      make      sell      store
(prod1, 1)  500.000000  500.000000  0.0
(prod1, 2)  700.000000  600.000000  100.0
(prod1, 3)   0.000000  100.000000  0.0
(prod1, 4)  200.000000  200.000000  0.0
(prod1, 5)   0.000000   0.000000  0.0
(prod1, 6)  550.000000  500.000000  50.0
(prod2, 1)  888.571429  888.571429  0.0
```

(continues on next page)

(continued from previous page)

```
(prod2, 2) 600.000000 500.000000 100.0
(prod2, 3)  0.000000 100.000000  0.0
(prod2, 4) 300.000000 300.000000  0.0
(prod2, 5) 100.000000 100.000000  0.0
(prod2, 6) 550.000000 500.000000  50.0
(prod3, 1) 382.500000 300.000000  82.5
(prod3, 2) 117.500000 200.000000  0.0
(prod3, 3)  0.000000  0.000000  0.0
(prod3, 4) 400.000000 400.000000  0.0
(prod3, 5) 600.000000 500.000000 100.0
(prod3, 6)  0.000000  50.000000  50.0
(prod4, 1) 300.000000 300.000000  0.0
(prod4, 2)  0.000000  0.000000  0.0
(prod4, 3)  0.000000  0.000000  0.0
(prod4, 4) 500.000000 500.000000  0.0
(prod4, 5) 100.000000 100.000000  0.0
(prod4, 6) 350.000000 300.000000  50.0
(prod5, 1) 800.000000 800.000000  0.0
(prod5, 2) 500.000000 400.000000 100.0
(prod5, 3)  0.000000 100.000000  0.0
(prod5, 4) 200.000000 200.000000  0.0
(prod5, 5) 1100.000000 1000.000000 100.0
(prod5, 6)  0.000000  50.000000  50.0
(prod6, 1) 200.000000 200.000000  0.0
(prod6, 2) 300.000000 300.000000  0.0
(prod6, 3) 400.000000 400.000000  0.0
(prod6, 4)  0.000000  0.000000  0.0
(prod6, 5) 300.000000 300.000000  0.0
(prod6, 6) 550.000000 500.000000  50.0
(prod7, 1)  0.000000  0.000000  0.0
(prod7, 2) 250.000000 150.000000 100.0
(prod7, 3)  0.000000 100.000000  0.0
(prod7, 4) 100.000000 100.000000  0.0
(prod7, 5) 100.000000  0.000000 100.0
(prod7, 6)  0.000000  50.000000  50.0
```

**Out [8] :** 93715.17857142858

## 4.1.4 Factory Planning 2

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex4\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex4_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex04.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex04.html)

## Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='factory_planning_2', session=cas_conn)

    # Input data
    product_list = ['prod{}'.format(i) for i in range(1, 8)]
    product_data = pd.DataFrame([10, 6, 8, 4, 11, 9, 3],
                                columns=['profit'], index=product_list)

    demand_data = [
        [500, 1000, 300, 300, 800, 200, 100],
        [600, 500, 200, 0, 400, 300, 150],
        [300, 600, 0, 0, 500, 400, 100],
        [200, 300, 400, 500, 200, 0, 100],
        [0, 100, 500, 100, 1000, 300, 0],
        [500, 500, 100, 300, 1100, 500, 60]]
    demand_data = pd.DataFrame(
        demand_data, columns=product_list, index=range(1, 7))
    machine_type_product_data = [
        ['grinder', 0.5, 0.7, 0, 0, 0.3, 0.2, 0.5],
        ['vdrill', 0.1, 0.2, 0, 0.3, 0, 0.6, 0],
        ['hdrill', 0.2, 0, 0.8, 0, 0, 0, 0.6],
        ['borer', 0.05, 0.03, 0, 0.07, 0.1, 0, 0.08],
        ['planer', 0, 0, 0.01, 0, 0.05, 0, 0.05]]
    machine_type_product_data = \
        pd.DataFrame(machine_type_product_data, columns=['machine_type'] +
                    product_list).set_index(['machine_type'])
    machine_types_data = [
        ['grinder', 4, 2],
        ['vdrill', 2, 2],
        ['hdrill', 3, 3],
        ['borer', 1, 1],
        ['planer', 1, 1]]
    machine_types_data = pd.DataFrame(machine_types_data, columns=[
        'machine_type', 'num_machines', 'num_machines_needing_maintenance'])\
        .set_index(['machine_type'])

    store_ub = 100
    storage_cost_per_unit = 0.5
    final_storage = 50
    num_hours_per_period = 24 * 2 * 8

    # Problem definition
    PRODUCTS = product_list
    profit = product_data['profit']
    PERIODS = range(1, 7)
    MACHINE_TYPES = machine_types_data.index.tolist()

    num_machines = machine_types_data['num_machines']

    make = m.add_variables(PRODUCTS, PERIODS, lb=0, name='make')
    sell = m.add_variables(PRODUCTS, PERIODS, lb=0, ub=demand_data.transpose(),
```

(continues on next page)

(continued from previous page)

```

        name='sell')

store = m.add_variables(PRODUCTS, PERIODS, lb=0, ub=store_ub, name='store')
for p in PRODUCTS:
    store[p, 6].set_bounds(lb=final_storage, ub=final_storage)

storageCost = so.expr_sum(
    storage_cost_per_unit * store[p, t] for p in PRODUCTS for t in PERIODS)
revenue = so.expr_sum(profit[p] * sell[p, t]
    for p in PRODUCTS for t in PERIODS)
m.set_objective(revenue-storageCost, sense=so.MAX, name='total_profit')

num_machines_needing_maintenance = \
    machine_types_data['num_machines_needing_maintenance']
numMachinesDown = m.add_variables(MACHINE_TYPES, PERIODS, vartype=so.INT,
    lb=0, name='numMachinesDown')

production_time = machine_type_product_data
m.add_constraints((
    so.expr_sum(production_time.at[mc, p] * make[p, t] for p in PRODUCTS)
    <= num_hours_per_period *
    (num_machines[mc] - numMachinesDown[mc, t])
    for mc in MACHINE_TYPES for t in PERIODS), name='machine_hours_con')

m.add_constraints((so.expr_sum(numMachinesDown[mc, t] for t in PERIODS) ==
    num_machines_needing_maintenance[mc]
    for mc in MACHINE_TYPES), name='maintenance_con')

m.add_constraints(((store[p, t-1] if t-1 in PERIODS else 0) + make[p, t] ==
    sell[p, t] + store[p, t]
    for p in PRODUCTS for t in PERIODS),
    name='flow_balance_con')

res = m.solve()
if res is not None:
    print(so.get_solution_table(make, sell, store))
    print(so.get_solution_table(numMachinesDown).unstack(level=-1))

print(m.get_solution_summary())
print(m.get_problem_summary())

return m.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

```

(continues on next page)

(continued from previous page)

```
In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.factory_planning_2 import test
```

```
In [8]: test(cas_conn)
```

```
NOTE: Initialized model factory_planning_2.
NOTE: Added action set 'optimization'.
NOTE: Converting model factory_planning_2 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 156 variables (0 free, 13 fixed).
NOTE: The problem has 0 binary and 30 integer variables.
NOTE: The problem has 77 linear constraints (30 LE, 47 EQ, 0 GE, 0 range).
NOTE: The problem has 341 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 27 variables and 15 constraints.
NOTE: The MILP presolver removed 63 constraint coefficients.
NOTE: The MILP presolver modified 16 constraint coefficients.
NOTE: The presolved problem has 129 variables, 62 constraints, and 278 constraint_
↪coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.
```

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	2	92755.0000000	116455	20.35%	0
0	1	2	92755.0000000	116455	20.35%	0
0	1	2	92755.0000000	116141	20.14%	0
0	1	2	92755.0000000	115660	19.80%	0
0	1	2	92755.0000000	114136	18.73%	0
0	1	2	92755.0000000	113334	18.16%	0
0	1	2	92755.0000000	112487	17.54%	0
0	1	2	92755.0000000	111392	16.73%	0
0	1	2	92755.0000000	111136	16.54%	0
0	1	2	92755.0000000	110056	15.72%	0
0	1	2	92755.0000000	109718	15.46%	0
0	1	2	92755.0000000	109122	15.00%	0
0	1	2	92755.0000000	108904	14.83%	0
0	1	2	92755.0000000	108868	14.80%	0
0	1	2	92755.0000000	108855	14.79%	0
0	1	3	108855	108855	0.00%	0

```
NOTE: The MILP solver added 38 cuts with 136 cut coefficients at the root.
NOTE: Optimal within relative gap.
NOTE: Objective = 108855.00961.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 156 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 77 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↪columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4_
↪columns.
```

	make	sell	store
(prod1, 1)	500.000000	500.000000	0.000000

(continues on next page)

(continued from previous page)

```

(prod1, 2) 600.000200 600.000000 0.000200
(prod1, 3) 399.999201 300.000000 99.999401
(prod1, 4) 0.001198 100.000599 0.000000
(prod1, 5) 0.000000 0.000000 0.000000
(prod1, 6) 550.000000 500.000000 50.000000
(prod2, 1) 1000.000000 1000.000000 0.000000
(prod2, 2) 500.000188 500.000000 0.000188
(prod2, 3) 699.998215 599.999002 99.999401
(prod2, 4) 0.001797 100.001198 0.000000
(prod2, 5) 100.002196 100.000000 0.002196
(prod2, 6) 549.997804 500.000000 50.000000
(prod3, 1) 300.000000 300.000000 0.000000
(prod3, 2) 200.000000 200.000000 0.000000
(prod3, 3) 100.000000 0.000000 100.000000
(prod3, 4) 0.001283 100.001283 0.000000
(prod3, 5) 500.000072 500.000000 0.000072
(prod3, 6) 149.999928 100.000000 50.000000
(prod4, 1) 300.000000 300.000000 0.000000
(prod4, 2) 0.000000 0.000000 0.000000
(prod4, 3) 99.999401 0.000000 99.999401
(prod4, 4) 0.002994 100.002396 0.000000
(prod4, 5) 100.000000 100.000000 0.000000
(prod4, 6) 350.000000 300.000000 50.000000
(prod5, 1) 800.000522 800.000000 0.000522
(prod5, 2) 399.999338 399.999460 0.000399
(prod5, 3) 599.998374 499.999201 99.999572
(prod5, 4) 0.001027 100.000599 0.000000
(prod5, 5) 1000.006512 1000.000000 0.006512
(prod5, 6) 1149.992981 1099.999493 50.000000
(prod6, 1) 200.000000 200.000000 0.000000
(prod6, 2) 300.000000 300.000000 0.000000
(prod6, 3) 400.000000 400.000000 0.000000
(prod6, 4) 0.000000 0.000000 0.000000
(prod6, 5) 300.000000 300.000000 0.000000
(prod6, 6) 550.000000 500.000000 50.000000
(prod7, 1) 100.000000 100.000000 0.000000
(prod7, 2) 150.000000 150.000000 0.000000
(prod7, 3) 199.999572 100.000000 99.999572
(prod7, 4) 0.000428 100.000000 0.000000
(prod7, 5) 0.000000 0.000000 0.000000
(prod7, 6) 110.000000 60.000000 50.000000
numMachinesDown (grinder, 1) -0.000000e+00
numMachinesDown (grinder, 2) -0.000000e+00
numMachinesDown (grinder, 3) -0.000000e+00
numMachinesDown (grinder, 4) 2.000000e+00
numMachinesDown (grinder, 5) -0.000000e+00
numMachinesDown (grinder, 6) -0.000000e+00
numMachinesDown (vdrill, 1) 0.000000e+00
numMachinesDown (vdrill, 2) -0.000000e+00
numMachinesDown (vdrill, 3) -0.000000e+00
numMachinesDown (vdrill, 4) 1.999994e+00
numMachinesDown (vdrill, 5) 3.955573e-06
numMachinesDown (vdrill, 6) 2.033239e-06
numMachinesDown (hdrill, 1) 1.000000e+00
numMachinesDown (hdrill, 2) 2.000000e+00
numMachinesDown (hdrill, 3) -0.000000e+00
numMachinesDown (hdrill, 4) -0.000000e+00

```

(continues on next page)

(continued from previous page)

```

numMachinesDown (hdrill, 5) -0.000000e+00
numMachinesDown (hdrill, 6) -0.000000e+00
numMachinesDown (borer, 1)  0.000000e+00
numMachinesDown (borer, 2) -0.000000e+00
numMachinesDown (borer, 3)  1.996271e-06
numMachinesDown (borer, 4)  9.999940e-01
numMachinesDown (borer, 5) -0.000000e+00
numMachinesDown (borer, 6)  3.992541e-06
numMachinesDown (planer, 1) 0.000000e+00
numMachinesDown (planer, 2) 1.798545e-06
numMachinesDown (planer, 3) 1.996271e-06
numMachinesDown (planer, 4) 9.999957e-01
numMachinesDown (planer, 5) 8.120488e-16
numMachinesDown (planer, 6) 4.829074e-07
dtype: float64

```

Selected Rows from Table SOLUTIONSUMMARY

	Value
Label	
Solver	MILP
Algorithm	Branch and Cut
Objective Function	total_profit
Solution Status	Optimal within Relative Gap
Objective Value	108855.00961
Relative Gap	3.0634424E-6
Absolute Gap	0.3334720743
Primal Infeasibility	5.684342E-14
Bound Infeasibility	0
Integer Infeasibility	5.9888119E-6
Best Bound	108855.34308
Nodes	1
Solutions Found	3
Iterations	377
Presolve Time	0.00
Solution Time	0.33

Selected Rows from Table PROBLEMSUMMARY

	Value
Label	
Objective Sense	Maximization
Objective Function	total_profit
Objective Type	Linear
Number of Variables	156
Bounded Above	0
Bounded Below	72
Bounded Below and Above	71
Free	0
Fixed	13
Binary	0
Integer	30
Number of Constraints	77
Linear LE (<=)	30
Linear EQ (=)	47

(continues on next page)

(continued from previous page)

```

Linear GE (>=)          0
Linear Range            0

Constraint Coefficients 341
Out[8]: 108855.00960810453

```

## 4.1.5 Manpower Planning

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex5\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex5_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex05.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex05.html)

### Model

```

import sasoptpy as so
import pandas as pd
import math

def test(cas_conn):
    # Input data
    demand_data = pd.DataFrame([
        [0, 2000, 1500, 1000],
        [1, 1000, 1400, 1000],
        [2, 500, 2000, 1500],
        [3, 0, 2500, 2000]
    ], columns=['period', 'unskilled', 'semiskilled', 'skilled'])\
        .set_index(['period'])
    worker_data = pd.DataFrame([
        ['unskilled', 0.25, 0.10, 500, 200, 1500, 50, 500],
        ['semiskilled', 0.20, 0.05, 800, 500, 2000, 50, 400],
        ['skilled', 0.10, 0.05, 500, 500, 3000, 50, 400]
    ], columns=['worker', 'waste_new', 'waste_old', 'recruit_ub',
               'redundancy_cost', 'overmanning_cost', 'shorttime_ub',
               'shorttime_cost']).set_index(['worker'])
    retrain_data = pd.DataFrame([
        ['unskilled', 'semiskilled', 200, 400],
        ['semiskilled', 'skilled', math.inf, 500],
    ], columns=['worker1', 'worker2', 'retrain_ub', 'retrain_cost'])\
        .set_index(['worker1', 'worker2'])
    downgrade_data = pd.DataFrame([
        ['semiskilled', 'unskilled'],
        ['skilled', 'semiskilled'],
        ['skilled', 'unskilled']
    ], columns=['worker1', 'worker2'])

    semiskill_retrain_frac_ub = 0.25
    downgrade_leave_frac = 0.5
    overmanning_ub = 150
    shorttime_frac = 0.5

```

(continues on next page)



(continued from previous page)

```

# Sets
WORKERS = worker_data.index.tolist()
PERIODS0 = demand_data.index.tolist()
PERIODS = PERIODS0[1:]
RETRAIN_PAIRS = [i for i, _ in retrain_data.iterrows()]
DOWNGRADE_PAIRS = [(row['worker1'], row['worker2'])
                    for _, row in downgrade_data.iterrows()]

waste_old = worker_data['waste_old']
waste_new = worker_data['waste_new']
redundancy_cost = worker_data['redundancy_cost']
overmanning_cost = worker_data['overmanning_cost']
shorttime_cost = worker_data['shorttime_cost']
retrain_cost = retrain_data['retrain_cost'].unstack(level=-1)

# Initialization
m = so.Model(name='manpower_planning', session=cas_conn)

# Variables
numWorkers = m.add_variables(WORKERS, PERIODS0, name='numWorkers', lb=0)
demand0 = demand_data.loc[0]
for w in WORKERS:
    numWorkers[w, 0].set_bounds(lb=demand0[w], ub=demand0[w])
numRecruits = m.add_variables(WORKERS, PERIODS, name='numRecruits', lb=0)
worker_ub = worker_data['recruit_ub']
for w in WORKERS:
    for p in PERIODS:
        numRecruits[w, p].set_bounds(ub=worker_ub[w])
numRedundant = m.add_variables(WORKERS, PERIODS, name='numRedundant', lb=0)
numShortTime = m.add_variables(WORKERS, PERIODS, name='numShortTime', lb=0)
shorttime_ub = worker_data['shorttime_ub']
for w in WORKERS:
    for p in PERIODS:
        numShortTime.set_bounds(ub=shorttime_ub[w])
numExcess = m.add_variables(WORKERS, PERIODS, name='numExcess', lb=0)

retrain_ub = pd.DataFrame()
for i in PERIODS:
    retrain_ub[i] = retrain_data['retrain_ub']
numRetrain = m.add_variables(RETRAIN_PAIRS, PERIODS, name='numRetrain',
                             lb=0, ub=retrain_ub)

numDowngrade = m.add_variables(DOWNGRADE_PAIRS, PERIODS,
                               name='numDowngrade', lb=0)

# Constraints
m.add_constraints((numWorkers[w, p]
                  - (1-shorttime_frac) * numShortTime[w, p]
                  - numExcess[w, p] == demand_data.loc[p, w]
                  for w in WORKERS for p in PERIODS), name='demand')
m.add_constraints((numWorkers[w, p] ==
                  (1 - waste_old[w]) * numWorkers[w, p-1]
                  + (1 - waste_new[w]) * numRecruits[w, p]
                  + (1 - waste_old[w]) * numRetrain.sum('*', w, p)
                  + (1 - downgrade_leave_frac) *
                  numDowngrade.sum('*', w, p)
                  - numRetrain.sum(w, '*', p)

```

(continues on next page)

(continued from previous page)

```

        - numDowngrade.sum(w, '*', p)
        - numRedundant[w, p]
        for w in WORKERS for p in PERIODS),
        name='flow_balance')
m.add_constraints((numRetrain['semiskilled', 'skilled', p] <=
    semiskill_retrain_frac_ub * numWorkers['skilled', p]
    for p in PERIODS), name='semiskill_retrain')
m.add_constraints((numExcess.sum('*', p) <= overmanning_ub
    for p in PERIODS), name='overmanning')

# Objectives
redundancy = so.Expression(numRedundant.sum('*', '*'), name='redundancy')
cost = so.Expression(so.expr_sum(redundancy_cost[w] * numRedundant[w, p] +
    shorttime_cost[w] * numShortTime[w, p] +
    overmanning_cost[w] * numExcess[w, p]
    for w in WORKERS for p in PERIODS)
    + so.expr_sum(
        retrain_cost.loc[i, j] * numRetrain[i, j, p]
        for i, j in RETRAIN_PAIRS for p in PERIODS),
    name='cost')

m.set_objective(redundancy, sense=so.MIN, name='redundancy_obj')
res = m.solve()
if res is not None:
    print('Redundancy:', redundancy.get_value())
    print('Cost:', cost.get_value())
    print(so.get_solution_table(
        numWorkers, numRecruits, numRedundant, numShortTime, numExcess))
    print(so.get_solution_table(numRetrain))
    print(so.get_solution_table(numDowngrade))

m.set_objective(cost, sense=so.MIN, name='cost_obj')
res = m.solve()
if res is not None:
    print('Redundancy:', redundancy.get_value())
    print('Cost:', cost.get_value())
    print(so.get_solution_table(numWorkers, numRecruits, numRedundant,
        numShortTime, numExcess))
    print(so.get_solution_table(numRetrain))
    print(so.get_solution_table(numDowngrade))

return m.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

```

```
In [7]: from examples.client_side.manpower_planning import test
```

```
In [8]: test(cas_conn)
```

```
NOTE: Initialized model manpower_planning.
NOTE: Added action set 'optimization'.
NOTE: Converting model manpower_planning to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 63 variables (0 free, 3 fixed).
NOTE: The problem has 24 linear constraints (6 LE, 18 EQ, 0 GE, 0 range).
NOTE: The problem has 108 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 36 variables and 12 constraints.
NOTE: The LP presolver removed 52 constraint coefficients.
NOTE: The presolved problem has 27 variables, 12 constraints, and 56 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
```

		Objective	
	Phase Iteration	Value	Time
	D 2 1	-1.032250E+03	0
	P 2 17	8.417969E+02	0

```
NOTE: Optimal.
NOTE: Objective = 841.796875.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 63 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 24 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↪columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↪columns.
```

```
Redundancy: 841.796875
```

```
Cost: 1668750.0
```

		numWorkers	numRecruits	numRedundant	numShortTime	numExcess
unskilled	0	2000.00000	NaN	NaN	NaN	NaN
unskilled	1	1157.03125	0.0	442.968750	50.0	132.03125
unskilled	2	675.00000	0.0	166.328125	50.0	150.00000
unskilled	3	175.00000	0.0	232.500000	50.0	150.00000
semiskilled	0	1500.00000	NaN	NaN	NaN	NaN
semiskilled	1	1442.96875	0.0	0.000000	50.0	17.96875
semiskilled	2	2025.00000	800.0	0.000000	50.0	0.00000
semiskilled	3	2500.00000	800.0	0.000000	0.0	0.00000
skilled	0	1000.00000	NaN	NaN	NaN	NaN
skilled	1	1025.00000	0.0	0.000000	50.0	0.00000
skilled	2	1500.00000	500.0	0.000000	0.0	0.00000
skilled	3	2000.00000	500.0	0.000000	0.0	0.00000
		numRetrain				
(unskilled, semiskilled, 1)		200.000000				
(unskilled, semiskilled, 2)		200.000000				
(unskilled, semiskilled, 3)		200.000000				
(semiskilled, skilled, 1)		256.250000				
(semiskilled, skilled, 2)		262.276786				
(semiskilled, skilled, 3)		364.285714				

(continues on next page)

(continued from previous page)

```

                                numDowngrade
(semiskilled, unskilled, 1)  0.000000e+00
(semiskilled, unskilled, 2) -1.421085e-14
(semiskilled, unskilled, 3)  0.000000e+00
(skilled, semiskilled, 1)    1.684375e+02
(skilled, semiskilled, 2)    1.729129e+02
(skilled, semiskilled, 3)    2.210714e+02
(skilled, unskilled, 1)      0.000000e+00
(skilled, unskilled, 2)      0.000000e+00
(skilled, unskilled, 3)      0.000000e+00
NOTE: Added action set 'optimization'.
NOTE: Converting model manpower_planning to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 63 variables (0 free, 3 fixed).
NOTE: The problem has 24 linear constraints (6 LE, 18 EQ, 0 GE, 0 range).
NOTE: The problem has 108 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 38 variables and 13 constraints.
NOTE: The LP presolver removed 56 constraint coefficients.
NOTE: The presolved problem has 25 variables, 11 constraints, and 52 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
                                Objective
Phase Iteration      Value      Time
D 2          1    -4.018114E+04      0
D 2          6     4.986773E+05      0
NOTE: Optimal.
NOTE: Objective = 498677.28532.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 63 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 24 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↪columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↪columns.
Redundancy: 1423.7188365650968
Cost: 498677.2853185596
                                numWorkers  numRecruits  numRedundant  numShortTime  numExcess
unskilled  0          2000.0          NaN          NaN          NaN          NaN
unskilled  1          1000.0          0.000000      812.500000      0.0          0.0
unskilled  2           500.0          0.000000      257.617729      0.0          0.0
unskilled  3           0.0          0.000000      353.601108      0.0          0.0
semiskilled 0         1500.0          NaN          NaN          NaN          NaN
semiskilled 1         1400.0          0.000000      0.000000      0.0          0.0
semiskilled 2         2000.0          800.000000      0.000000      0.0          0.0
semiskilled 3         2500.0          800.000000      0.000000      0.0          0.0
skilled    0          1000.0          NaN          NaN          NaN          NaN
skilled    1          1000.0          55.555556      0.000000      0.0          0.0
skilled    2          1500.0          500.000000      0.000000      0.0          0.0
skilled    3          2000.0          500.000000      0.000000      0.0          0.0
                                numRetrain

```

(continues on next page)

(continued from previous page)

```

(unskilled, semiskilled, 1)    0.000000
(unskilled, semiskilled, 2)    142.382271
(unskilled, semiskilled, 3)    96.398892
(semiskilled, skilled, 1)      0.000000
(semiskilled, skilled, 2)      105.263158
(semiskilled, skilled, 3)      131.578947
                                numDowngrade
(semiskilled, unskilled, 1)    2.500000e+01
(semiskilled, unskilled, 2)    2.842171e-14
(semiskilled, unskilled, 3)    -2.842171e-14
(skilled, semiskilled, 1)      0.000000e+00
(skilled, semiskilled, 2)      0.000000e+00
(skilled, semiskilled, 3)      0.000000e+00
(skilled, unskilled, 1)        0.000000e+00
(skilled, unskilled, 2)        1.136868e-13
(skilled, unskilled, 3)        1.421085e-14
Out[8]: 498677.2853185596

```

## 4.1.6 Refinery Optimization

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex6\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex6_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex06.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex06.html)

### Model

```

import sasoptpy as so
import pandas as pd
import numpy as np

def test(cas_conn, **kwargs):

    m = so.Model(name='refinery_optimization', session=cas_conn)

    crude_data = pd.DataFrame([
        ['crude1', 20000],
        ['crude2', 30000]
    ], columns=['crude', 'crude_ub']).set_index(['crude'])

    arc_data = pd.DataFrame([
        ['source', 'crude1', 6],
        ['source', 'crude2', 6],
        ['crude1', 'light_naphtha', 0.1],
        ['crude1', 'medium_naphtha', 0.2],
        ['crude1', 'heavy_naphtha', 0.2],
        ['crude1', 'light_oil', 0.12],
        ['crude1', 'heavy_oil', 0.2],
        ['crude1', 'residuum', 0.13],
        ['crude2', 'light_naphtha', 0.15],

```

(continues on next page)

(continued from previous page)

```

['crude2', 'medium_naphtha', 0.25],
['crude2', 'heavy_naphtha', 0.18],
['crude2', 'light_oil', 0.08],
['crude2', 'heavy_oil', 0.19],
['crude2', 'residuum', 0.12],
['light_naphtha', 'regular_petrol', np.nan],
['light_naphtha', 'premium_petrol', np.nan],
['medium_naphtha', 'regular_petrol', np.nan],
['medium_naphtha', 'premium_petrol', np.nan],
['heavy_naphtha', 'regular_petrol', np.nan],
['heavy_naphtha', 'premium_petrol', np.nan],
['light_naphtha', 'reformed_gasoline', 0.6],
['medium_naphtha', 'reformed_gasoline', 0.52],
['heavy_naphtha', 'reformed_gasoline', 0.45],
['light_oil', 'jet_fuel', np.nan],
['light_oil', 'fuel_oil', np.nan],
['heavy_oil', 'jet_fuel', np.nan],
['heavy_oil', 'fuel_oil', np.nan],
['light_oil', 'light_oil_cracked', 2],
['light_oil_cracked', 'cracked_oil', 0.68],
['light_oil_cracked', 'cracked_gasoline', 0.28],
['heavy_oil', 'heavy_oil_cracked', 2],
['heavy_oil_cracked', 'cracked_oil', 0.75],
['heavy_oil_cracked', 'cracked_gasoline', 0.2],
['cracked_oil', 'jet_fuel', np.nan],
['cracked_oil', 'fuel_oil', np.nan],
['reformed_gasoline', 'regular_petrol', np.nan],
['reformed_gasoline', 'premium_petrol', np.nan],
['cracked_gasoline', 'regular_petrol', np.nan],
['cracked_gasoline', 'premium_petrol', np.nan],
['residuum', 'lube_oil', 0.5],
['residuum', 'jet_fuel', np.nan],
['residuum', 'fuel_oil', np.nan],
], columns=['i', 'j', 'multiplier']).set_index(['i', 'j'])

octane_data = pd.DataFrame([
    ['light_naphtha', 90],
    ['medium_naphtha', 80],
    ['heavy_naphtha', 70],
    ['reformed_gasoline', 115],
    ['cracked_gasoline', 105],
], columns=['i', 'octane']).set_index(['i'])

petrol_data = pd.DataFrame([
    ['regular_petrol', 84],
    ['premium_petrol', 94],
], columns=['petrol', 'octane_lb']).set_index(['petrol'])

vapour_pressure_data = pd.DataFrame([
    ['light_oil', 1.0],
    ['heavy_oil', 0.6],
    ['cracked_oil', 1.5],
    ['residuum', 0.05],
], columns=['oil', 'vapour_pressure']).set_index(['oil'])

fuel_oil_ratio_data = pd.DataFrame([
    ['light_oil', 10],

```

(continues on next page)

(continued from previous page)

```

    ['cracked_oil', 4],
    ['heavy_oil', 3],
    ['residuum', 1],
    ], columns=['oil', 'coefficient']).set_index(['oil'])

final_product_data = pd.DataFrame([
    ['premium_petrol', 700],
    ['regular_petrol', 600],
    ['jet_fuel', 400],
    ['fuel_oil', 350],
    ['lube_oil', 150],
    ], columns=['product', 'profit']).set_index(['product'])

vapour_pressure_ub = 1
crude_total_ub = 45000
naphtha_ub = 10000
cracked_oil_ub = 8000
lube_oil_lb = 500
lube_oil_ub = 1000
premium_ratio = 0.40

ARCS = arc_data.index.tolist()
arc_mult = arc_data['multiplier'].fillna(1)

FINAL_PRODUCTS = final_product_data.index.tolist()
final_product_data['profit'] = final_product_data['profit'] / 100
profit = final_product_data['profit']

ARCS = ARCS + [(i, 'sink') for i in FINAL_PRODUCTS]
flow = m.add_variables(ARCS, name='flow', lb=0)
NODES = np.unique([i for j in ARCS for i in j])

m.set_objective(so.expr_sum(profit[i] * flow[i, 'sink']
                           for i in FINAL_PRODUCTS
                           if (i, 'sink') in ARCS),
               name='totalProfit', sense=so.MAX)

m.add_constraints((so.expr_sum(flow[a] for a in ARCS if a[0] == n) ==
                  so.expr_sum(arc_mult[a] * flow[a]
                              for a in ARCS if a[1] == n)
                  for n in NODES if n not in ['source', 'sink']),
                 name='flow_balance')

CRUDES = crude_data.index.tolist()
crudeDistilled = m.add_variables(CRUDES, name='crudesDistilled', lb=0)
crudeDistilled.set_bounds(ub=crude_data['crude_ub'])
m.add_constraints((flow[i, j] == crudeDistilled[i]
                  for (i, j) in ARCS if i in CRUDES), name='distillation')

OILS = ['light_oil', 'heavy_oil']
CRACKED_OILS = [i+'_cracked' for i in OILS]
oilCracked = m.add_variables(CRACKED_OILS, name='oilCracked', lb=0)
m.add_constraints((flow[i, j] == oilCracked[i] for (i, j) in ARCS
                  if i in CRACKED_OILS), name='cracking')

octane = octane_data['octane']
PETROLS = petrol_data.index.tolist()

```

(continues on next page)

(continued from previous page)

```

octane_lb = petrol_data['octane_lb']
vapour_pressure = vapour_pressure_data['vapour_pressure']

m.add_constraints((so.expr_sum(octane[a[0]] * arc_mult[a] * flow[a]
                             for a in ARCS if a[1] == p)
                 >= octane_lb[p] *
                 so.expr_sum(arc_mult[a] * flow[a]
                             for a in ARCS if a[1] == p)
                 for p in PETROLS), name='blending_petrol')

m.add_constraint(so.expr_sum(vapour_pressure[a[0]] * arc_mult[a] * flow[a]
                             for a in ARCS if a[1] == 'jet_fuel') <=
                 vapour_pressure_ub *
                 so.expr_sum(arc_mult[a] * flow[a]
                             for a in ARCS if a[1] == 'jet_fuel'),
                 name='blending_jet_fuel')

fuel_oil_coefficient = fuel_oil_ratio_data['coefficient']
sum_fuel_oil_coefficient = sum(fuel_oil_coefficient)
m.add_constraints((sum_fuel_oil_coefficient * flow[a] ==
                 fuel_oil_coefficient[a[0]] * flow.sum('*', ['fuel_oil'])
                 for a in ARCS if a[1] == 'fuel_oil'),
                 name='blending_fuel_oil')

m.add_constraint(crudeDistilled.sum('*') <= crude_total_ub,
                 name='crude_total_ub')

m.add_constraint(so.expr_sum(flow[a] for a in ARCS
                             if a[0].find('naphtha') > -1 and
                             a[1] == 'reformed_gasoline')
                 <= naphtha_ub, name='naphtha_ub')

m.add_constraint(so.expr_sum(flow[a] for a in ARCS if a[1] ==
                             'cracked_oil') <=
                 cracked_oil_ub, name='cracked_oil_ub')

m.add_constraint(flow['lube_oil', 'sink'] == [lube_oil_lb, lube_oil_ub],
                 name='lube_oil_range')

m.add_constraint(flow.sum('premium_petrol', '*') >= premium_ratio *
                 flow.sum('regular_petrol', '*'), name='premium_ratio')

res = m.solve(**kwargs)
if res is not None:
    print(so.get_solution_table(crudeDistilled))
    print(so.get_solution_table(oilCracked))
    print(so.get_solution_table(flow))

octane_sol = []
for p in PETROLS:
    octane_sol.append(so.expr_sum(octane[a[0]] * arc_mult[a] *
                                flow[a].get_value() for a in ARCS
                                if a[1] == p) /
                      sum(arc_mult[a] * flow[a].get_value()
                          for a in ARCS if a[1] == p))
octane_sol = pd.Series(octane_sol, name='octane_sol', index=PETROLS)
print(so.get_solution_table(octane_sol, octane_lb))

```

(continues on next page)



(continued from previous page)

```

print(so.get_solution_table(vapour_pressure))
vapour_pressure_sol = sum(vapour_pressure[a[0]] *
                          arc_mult[a] *
                          flow[a].get_value() for a in ARCS
                          if a[1] == 'jet_fuel') /\
sum(arc_mult[a] * flow[a].get_value() for a in ARCS
    if a[1] == 'jet_fuel')
print('Vapour_pressure_sol: {:.4f}'.format(vapour_pressure_sol))

num_fuel_oil_ratio_sol = [arc_mult[a] * flow[a].get_value() /
                          sum(arc_mult[b] *
                              flow[b].get_value()
                              for b in ARCS if b[1] == 'fuel_oil')
                          for a in ARCS if a[1] == 'fuel_oil']
num_fuel_oil_ratio_sol = pd.Series(num_fuel_oil_ratio_sol,
                                   name='num_fuel_oil_ratio_sol',
                                   index=[a[0] for a in ARCS
                                         if a[1] == 'fuel_oil'])
print(so.get_solution_table(fuel_oil_coefficient,
                            num_fuel_oil_ratio_sol))

return m.get_objective_value()

```

## Output

```
In [1]: import os
```

```
In [2]: hostname = os.getenv('CASHOST')
```

```
In [3]: port = os.getenv('CASPORT')
```

```
In [4]: from swat import CAS
```

```
In [5]: cas_conn = CAS(hostname, port)
```

```
In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.refinery_optimization import test
```

```
In [8]: test(cas_conn)
```

```
NOTE: Initialized model refinery_optimization.
```

```
NOTE: Added action set 'optimization'.
```

```
NOTE: Converting model refinery_optimization to OPTMODEL.
```

```
NOTE: Submitting OPTMODEL code to CAS server.
```

```
NOTE: Problem generation will use 8 threads.
```

```
NOTE: The problem has 51 variables (0 free, 0 fixed).
```

```
NOTE: The problem has 46 linear constraints (4 LE, 38 EQ, 3 GE, 1 range).
```

```
NOTE: The problem has 158 linear constraint coefficients.
```

```
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
```

```
NOTE: The OPTMODEL presolver is disabled for linear problems.
```

```
NOTE: The LP presolver value AUTOMATIC is applied.
```

```
NOTE: The LP presolver time is 0.00 seconds.
```

```
NOTE: The LP presolver removed 29 variables and 30 constraints.
```

```
NOTE: The LP presolver removed 86 constraint coefficients.
```

(continues on next page)

(continued from previous page)

NOTE: The presolved problem has 22 variables, 16 constraints, and 72 constraint\_  
 ↪coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

	Phase	Iteration	Objective Value	Time
	D	2	9.878656E+05	0
	P	2	2.113651E+05	0

NOTE: Optimal.

NOTE: Objective = 211365.13477.

NOTE: The Dual Simplex solve time is 0.02 seconds.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 51 rows and 6\_  
 ↪columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 46 rows and 4 columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4\_  
 ↪columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4\_  
 ↪columns.

crudesDistilled	
crude1	15000.0
crude2	30000.0

oilCracked	
light_oil_cracked	4200.0
heavy_oil_cracked	3800.0

flow	
(source, crude1)	15000.000000
(source, crude2)	30000.000000
(crude1, light_naphtha)	15000.000000
(crude1, medium_naphtha)	15000.000000
(crude1, heavy_naphtha)	15000.000000
(crude1, light_oil)	15000.000000
(crude1, heavy_oil)	15000.000000
(crude1, residuum)	15000.000000
(crude2, light_naphtha)	30000.000000
(crude2, medium_naphtha)	30000.000000
(crude2, heavy_naphtha)	30000.000000
(crude2, light_oil)	30000.000000
(crude2, heavy_oil)	30000.000000
(crude2, residuum)	30000.000000
(light_naphtha, regular_petrol)	3293.112993
(light_naphtha, premium_petrol)	2706.887007
(medium_naphtha, regular_petrol)	10500.000000
(medium_naphtha, premium_petrol)	0.000000
(heavy_naphtha, regular_petrol)	1315.334140
(heavy_naphtha, premium_petrol)	1677.804016
(light_naphtha, reformed_gasoline)	0.000000
(medium_naphtha, reformed_gasoline)	0.000000
(heavy_naphtha, reformed_gasoline)	5406.861844
(light_oil, jet_fuel)	0.000000
(light_oil, fuel_oil)	0.000000
(heavy_oil, jet_fuel)	4900.000000
(heavy_oil, fuel_oil)	0.000000
(light_oil, light_oil_cracked)	4200.000000
(light_oil_cracked, cracked_oil)	4200.000000
(light_oil_cracked, cracked_gasoline)	4200.000000
(heavy_oil, heavy_oil_cracked)	3800.000000
(heavy_oil_cracked, cracked_oil)	3800.000000

(continues on next page)

(continued from previous page)

```

(heavy_oil_cracked, cracked_gasoline) 3800.000000
(cracked_oil, jet_fuel) 5706.000000
(cracked_oil, fuel_oil) 0.000000
(reformed_gasoline, regular_petrol) 0.000000
(reformed_gasoline, premium_petrol) 2433.087830
(cracked_gasoline, regular_petrol) 1936.000000
(cracked_gasoline, premium_petrol) 0.000000
(residuum, lube_oil) 1000.000000
(residuum, jet_fuel) 4550.000000
(residuum, fuel_oil) 0.000000
(premium_petrol, sink) 6817.778853
(regular_petrol, sink) 17044.447133
(jet_fuel, sink) 15156.000000
(fuel_oil, sink) 0.000000
(lube_oil, sink) 500.000000
      octane_sol octane_lb
petrol
regular_petrol      84.0      84
premium_petrol      94.0      94
      vapour_pressure
oil
light_oil      1.0
heavy_oil      0.6
cracked_oil      1.5
residuum      0.05
Vapour_pressure_sol: 0.7737
      coefficient num_fuel_oil_ratio_sol
light_oil      10      nan
cracked_oil      4      nan
heavy_oil      3      nan
residuum      1      nan
Out [8]: 211365.13476893297

```

## 4.1.7 Mining Optimization

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex7\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex7_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex07.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex07.html)

### Model

```

import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='mining_optimization', session=cas_conn)

    mine_data = pd.DataFrame([

```

(continues on next page)

(continued from previous page)

```

    ['mine1', 5, 2, 1.0],
    ['mine2', 4, 2.5, 0.7],
    ['mine3', 4, 1.3, 1.5],
    ['mine4', 5, 3, 0.5],
], columns=['mine', 'cost', 'extract_ub', 'quality']).\
set_index(['mine'])

year_data = pd.DataFrame([
    [1, 0.9],
    [2, 0.8],
    [3, 1.2],
    [4, 0.6],
    [5, 1.0],
], columns=['year', 'quality_required']).set_index(['year'])

max_num_worked_per_year = 3
revenue_per_ton = 10
discount_rate = 0.10

MINES = mine_data.index.tolist()
cost = mine_data['cost']
extract_ub = mine_data['extract_ub']
quality = mine_data['quality']
YEARS = year_data.index.tolist()
quality_required = year_data['quality_required']

isOpen = m.add_variables(MINES, YEARS, vartype=so.BIN, name='isOpen')
isWorked = m.add_variables(MINES, YEARS, vartype=so.BIN, name='isWorked')
extract = m.add_variables(MINES, YEARS, lb=0, name='extract')
[extract[i, j].set_bounds(ub=extract_ub[i]) for i in MINES for j in YEARS]

extractedPerYear = {j: extract.sum('*', j) for j in YEARS}
discount = {j: 1 / (1+discount_rate) ** (j-1) for j in YEARS}

totalRevenue = revenue_per_ton *\
    so.expr_sum(discount[j] * extractedPerYear[j] for j in YEARS)
totalCost = so.expr_sum(discount[j] * cost[i] * isOpen[i, j]
                        for i in MINES for j in YEARS)
m.set_objective(totalRevenue-totalCost, sense=so.MAX, name='totalProfit')

m.add_constraints((extract[i, j] <= extract[i, j]._ub * isWorked[i, j]
                  for i in MINES for j in YEARS), name='link')

m.add_constraints((isWorked.sum('*', j) <= max_num_worked_per_year
                  for j in YEARS), name='cardinality')

m.add_constraints((isWorked[i, j] <= isOpen[i, j] for i in MINES
                  for j in YEARS), name='worked_implies_open')

m.add_constraints((isOpen[i, j] <= isOpen[i, j-1] for i in MINES
                  for j in YEARS if j != 1), name='continuity')

m.add_constraints((so.expr_sum(quality[i] * extract[i, j] for i in MINES)
                  == quality_required[j] * extractedPerYear[j]
                  for j in YEARS), name='quality_con')

res = m.solve()

```

(continues on next page)

(continued from previous page)

```

if res is not None:
    print(so.get_solution_table(isOpen, isWorked, extract))
    quality_sol = {j: so.expr_sum(quality[i] * extract[i, j].get_value()
                                for i in MINES)
                  / extractedPerYear[j].get_value() for j in YEARS}
    qs = so.dict_to_frame(quality_sol, ['quality_sol'])
    epy = so.dict_to_frame(extractedPerYear, ['extracted_per_year'])
    print(so.get_solution_table(epy, qs, quality_required))

return m.get_objective_value()

```

## Output

```
In [1]: import os
```

```
In [2]: hostname = os.getenv('CASHOST')
```

```
In [3]: port = os.getenv('CASPORT')
```

```
In [4]: from swat import CAS
```

```
In [5]: cas_conn = CAS(hostname, port)
```

```
In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.mining_optimization import test
```

```
In [8]: test(cas_conn)
```

NOTE: Initialized model mining\_optimization.

NOTE: Added action set 'optimization'.

NOTE: Converting model mining\_optimization to OPTMODEL.

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 60 variables (0 free, 0 fixed).

NOTE: The problem has 40 binary and 0 integer variables.

NOTE: The problem has 66 linear constraints (61 LE, 5 EQ, 0 GE, 0 range).

NOTE: The problem has 151 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver is disabled for linear problems.

NOTE: The initial MILP heuristics are applied.

NOTE: The MILP presolver value AUTOMATIC is applied.

NOTE: The MILP presolver removed 8 variables and 8 constraints.

NOTE: The MILP presolver removed 16 constraint coefficients.

NOTE: The MILP presolver modified 8 constraint coefficients.

NOTE: The presolved problem has 52 variables, 58 constraints, and 135 constraint\_

→coefficients.

NOTE: The MILP solver is called.

NOTE: The parallel Branch and Cut algorithm is used.

NOTE: The Branch and Cut algorithm is using up to 8 threads.

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	14	96.5802313	157.7309278	38.77%	0
0	1	14	96.5802313	150.9548680	36.02%	0
0	1	14	96.5802313	147.3693449	34.46%	0
0	1	15	146.8619974	146.8619974	0.00%	0

(continues on next page)

(continued from previous page)

```

0          0          15      146.8619974      146.8619974      0.00%          0
NOTE: The MILP solver added 7 cuts with 34 cut coefficients at the root.
NOTE: Optimal.
NOTE: Objective = 146.86199735.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 60 rows and 6_
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 66 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4_
↳columns.
      isOpen  isWorked      extract
(mine1, 1)  1.000000  1.000000  2.000000e+00
(mine1, 2)  0.999994  0.000006  1.252000e-05
(mine1, 3)  0.999994  0.999994  1.950000e+00
(mine1, 4)  0.999994  0.999994  1.250007e-01
(mine1, 5)  0.999994  0.999994  1.999987e+00
(mine2, 1)  1.000000  0.000000  0.000000e+00
(mine2, 2)  1.000000  0.999995  2.499988e+00
(mine2, 3)  0.999998 -0.000000  0.000000e+00
(mine2, 4)  0.999998  0.999998  2.499994e+00
(mine2, 5)  0.999998  0.999998  2.166667e+00
(mine3, 1)  1.000000  1.000000  1.300000e+00
(mine3, 2)  1.000000  0.999998  1.299997e+00
(mine3, 3)  1.000000  1.000000  1.300000e+00
(mine3, 4)  1.000000  0.000001  3.477765e-07
(mine3, 5)  1.000000  1.000000  1.300000e+00
(mine4, 1)  1.000000  1.000000  2.450000e+00
(mine4, 2)  1.000000  1.000000  2.200005e+00
(mine4, 3)  1.000000 -0.000000  0.000000e+00
(mine4, 4)  1.000000  1.000000  3.000000e+00
(mine4, 5) -0.000000 -0.000000  0.000000e+00
      extracted_per_year  quality_sol  quality_required
1          5.750000          0.9          0.9
2          6.000003          0.8          0.8
3          3.250000          1.2          1.2
4          5.624995          0.6          0.6
5          5.466654          1.0          1.0
Out [8]: 146.861997350257

```

## 4.1.8 Farm Planning

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex8\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex8_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex08.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex08.html)

## Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='farm_planning', session=cas_conn)

    # Input Data

    cow_data_raw = []
    for age in range(12):
        if age < 2:
            row = {'age': age,
                  'init_num_cows': 10,
                  'acres_needed': 2/3.0,
                  'annual_loss': 0.05,
                  'bullock_yield': 0,
                  'heifer_yield': 0,
                  'milk_revenue': 0,
                  'grain_req': 0,
                  'sugar_beet_req': 0,
                  'labour_req': 10,
                  'other_costs': 50}
        else:
            row = {'age': age,
                  'init_num_cows': 10,
                  'acres_needed': 1,
                  'annual_loss': 0.02,
                  'bullock_yield': 1.1/2,
                  'heifer_yield': 1.1/2,
                  'milk_revenue': 370,
                  'grain_req': 0.6,
                  'sugar_beet_req': 0.7,
                  'labour_req': 42,
                  'other_costs': 100}
        cow_data_raw.append(row)
    cow_data = pd.DataFrame(cow_data_raw).set_index(['age'])
    grain_data = pd.DataFrame([
        ['group1', 20, 1.1],
        ['group2', 30, 0.9],
        ['group3', 20, 0.8],
        ['group4', 10, 0.65]
    ], columns=['group', 'acres', 'yield']).set_index(['group'])
    num_years = 5
    num_acres = 200
    bullock_revenue = 30
    heifer_revenue = 40
    dairy_cow_selling_age = 12
    dairy_cow_selling_revenue = 120
    max_num_cows = 130
    sugar_beet_yield = 1.5
    grain_cost = 90
    grain_revenue = 75
    grain_labour_req = 4
```

(continues on next page)

(continued from previous page)

```

grain_other_costs = 15
sugar_beet_cost = 70
sugar_beet_revenue = 58
sugar_beet_labour_req = 14
sugar_beet_other_costs = 10
nominal_labour_cost = 4000
nominal_labour_hours = 5500
excess_labour_cost = 1.2
capital_outlay_unit = 200
num_loan_years = 10
annual_interest_rate = 0.15
max_decrease_ratio = 0.50
max_increase_ratio = 0.75

# Sets

AGES = cow_data.index.tolist()
init_num_cows = cow_data['init_num_cows']
acres_needed = cow_data['acres_needed']
annual_loss = cow_data['annual_loss']
bullock_yield = cow_data['bullock_yield']
heifer_yield = cow_data['heifer_yield']
milk_revenue = cow_data['milk_revenue']
grain_req = cow_data['grain_req']
sugar_beet_req = cow_data['sugar_beet_req']
cow_labour_req = cow_data['labour_req']
cow_other_costs = cow_data['other_costs']

YEARS = list(range(1, num_years+1))
YEARS0 = [0] + YEARS

# Variables

numCows = m.add_variables(AGES + [dairy_cow_selling_age], YEARS0, lb=0,
                          name='numCows')

for age in AGES:
    numCows[age, 0].set_bounds(lb=init_num_cows[age],
                               ub=init_num_cows[age])
numCows[dairy_cow_selling_age, 0].set_bounds(lb=0, ub=0)

numBullocksSold = m.add_variables(YEARS, lb=0, name='numBullocksSold')
numHeifersSold = m.add_variables(YEARS, lb=0, name='numHeifersSold')

GROUPS = grain_data.index.tolist()
acres = grain_data['acres']
grain_yield = grain_data['yield']
grainAcres = m.add_variables(GROUPS, YEARS, lb=0, name='grainAcres')
for group in GROUPS:
    for year in YEARS:
        grainAcres[group, year].set_bounds(ub=acres[group])
grainBought = m.add_variables(YEARS, lb=0, name='grainBought')
grainSold = m.add_variables(YEARS, lb=0, name='grainSold')

sugarBeetAcres = m.add_variables(YEARS, lb=0, name='sugarBeetAcres')
sugarBeetBought = m.add_variables(YEARS, lb=0, name='sugarBeetBought')
sugarBeetSold = m.add_variables(YEARS, lb=0, name='sugarBeetSold')

```

(continues on next page)



(continued from previous page)

```

numExcessLabourHours = m.add_variables(YEARS, lb=0,
                                       name='numExcessLabourHours')
capitalOutlay = m.add_variables(YEARS, lb=0, name='capitalOutlay')

yearly_loan_payment = (annual_interest_rate * capital_outlay_unit) /\
                      (1 - (1+annual_interest_rate)**(-num_loan_years))

# Objective function

revenue = {year:
            bullock_revenue * numBullocksSold[year] +
            heifer_revenue * numHeifersSold[year] +
            dairy_cow_selling_revenue * numCows[dairy_cow_selling_age,
                                                year] +
            so.expr_sum(milk_revenue[age] * numCows[age, year]
                        for age in AGES) +
            grain_revenue * grainSold[year] +
            sugar_beet_revenue * sugarBeetSold[year]
            for year in YEARS}

cost = {year:
        grain_cost * grainBought[year] +
        sugar_beet_cost * sugarBeetBought[year] +
        nominal_labour_cost +
        excess_labour_cost * numExcessLabourHours[year] +
        so.expr_sum(cow_other_costs[age] * numCows[age, year]
                    for age in AGES) +
        so.expr_sum(grain_other_costs * grainAcres[group, year]
                    for group in GROUPS) +
        sugar_beet_other_costs * sugarBeetAcres[year] +
        so.expr_sum(yearly_loan_payment * capitalOutlay[y]
                    for y in YEARS if y <= year)
        for year in YEARS}

profit = {year: revenue[year] - cost[year] for year in YEARS}

totalProfit = so.expr_sum(profit[year] -
                          yearly_loan_payment * (num_years - 1 + year) *
                          capitalOutlay[year] for year in YEARS)

m.set_objective(totalProfit, sense=so.MAX, name='totalProfit')

# Constraints

m.add_constraints((
    so.expr_sum(acres_needed[age] * numCows[age, year] for age in AGES) +
    so.expr_sum(grainAcres[group, year] for group in GROUPS) +
    sugarBeetAcres[year] <= num_acres
    for year in YEARS), name='num_acres')

m.add_constraints((
    numCows[age+1, year+1] == (1-annual_loss[age]) * numCows[age, year]
    for age in AGES if age != dairy_cow_selling_age
    for year in YEARS0 if year != num_years), name='aging')

m.add_constraints((
    numBullocksSold[year] == so.expr_sum(
        bullock_yield[age] * numCows[age, year] for age in AGES)

```

(continues on next page)

(continued from previous page)

```

    for year in YEARS), name='numBullocksSold_def')

m.add_constraints((
    numCows[0, year] == so.expr_sum(
        heifer_yield[age] * numCows[age, year]
        for age in AGES) - numHeifersSold[year]
    for year in YEARS), name='numHeifersSold_def')

m.add_constraints((
    so.expr_sum(numCows[age, year] for age in AGES) <= max_num_cows +
    so.expr_sum(capitalOutlay[y] for y in YEARS if y <= year)
    for year in YEARS), name='max_num_cows_def')

grainGrown = {(group, year): grain_yield[group] * grainAcres[group, year]
               for group in GROUPS for year in YEARS}
m.add_constraints((
    so.expr_sum(grain_req[age] * numCows[age, year] for age in AGES) <=
    so.expr_sum(grainGrown[group, year] for group in GROUPS)
    + grainBought[year] - grainSold[year]
    for year in YEARS), name='grain_req_def')

sugarBeetGrown = {(year): sugar_beet_yield * sugarBeetAcres[year]
                  for year in YEARS}
m.add_constraints((
    so.expr_sum(sugar_beet_req[age] * numCows[age, year] for age in AGES)
    <=
    sugarBeetGrown[year] + sugarBeetBought[year] - sugarBeetSold[year]
    for year in YEARS), name='sugar_beet_req_def')

m.add_constraints((
    so.expr_sum(cow_labour_req[age] * numCows[age, year]
                for age in AGES) +
    so.expr_sum(grain_labour_req * grainAcres[group, year]
                for group in GROUPS) +
    sugar_beet_labour_req * sugarBeetAcres[year] <=
    nominal_labour_hours + numExcessLabourHours[year]
    for year in YEARS), name='labour_req_def')
m.add_constraints((profit[year] >= 0 for year in YEARS), name='cash_flow')

m.add_constraint(so.expr_sum(numCows[age, num_years] for age in AGES
                             if age >= 2) /
                 sum(init_num_cows[age] for age in AGES if age >= 2) ==
                 [1-max_decrease_ratio, 1+max_increase_ratio],
                 name='final_dairy_cows_range')

res = m.solve()

if res is not None:
    so.pd.display_all()
    print(so.get_solution_table(numCows))
    revenue_df = so.dict_to_frame(revenue, cols=['revenue'])
    cost_df = so.dict_to_frame(cost, cols=['cost'])
    profit_df = so.dict_to_frame(profit, cols=['profit'])
    print(so.get_solution_table(numBullocksSold, numHeifersSold,
                                capitalOutlay, numExcessLabourHours,
                                revenue_df, cost_df, profit_df))
    gg_df = so.dict_to_frame(grainGrown, cols=['grainGrown'])

```

(continues on next page)

(continued from previous page)

```

print(so.get_solution_table(grainAcres, gg_df))
sbg_df = so.dict_to_frame(sugarBeetGrown, cols=['sugerBeetGrown'])
print(so.get_solution_table(
    grainBought, grainSold, sugarBeetAcres,
    sbg_df, sugarBeetBought, sugarBeetSold))
num_acres = m.get_constraint('num_acres')
na_df = num_acres.get_expressions()
max_num_cows_con = m.get_constraint('max_num_cows_def')
mnc_df = max_num_cows_con.get_expressions()
print(so.get_solution_table(na_df, mnc_df))

return m.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

```

```

In [7]: from examples.client_side.farm_planning import test

In [8]: test(cas_conn)
NOTE: Initialized model farm_planning.
NOTE: Added action set 'optimization'.
NOTE: Converting model farm_planning to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 143 variables (0 free, 13 fixed).
NOTE: The problem has 101 linear constraints (25 LE, 70 EQ, 5 GE, 1 range).
NOTE: The problem has 780 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 86 variables and 71 constraints.
NOTE: The LP presolver removed 551 constraint coefficients.
NOTE: The presolved problem has 57 variables, 30 constraints, and 229 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

	Phase	Iteration	Objective Value	Time
	D 1	1	4.195000E+02	0
	D 2	37	1.971960E+05	0
	D 2	55	1.217192E+05	0

```

NOTE: Optimal.

```

(continues on next page)

(continued from previous page)

```
NOTE: Objective = 121719.17286.
NOTE: The Dual Simplex solve time is 0.02 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 143 rows and 6
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 101 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4
↳columns.
```

```
      numCows
(0, 0)  10.000000
(0, 1)  22.800000
(0, 2)  11.584427
(0, 3)   0.000000
(0, 4)   0.000000
(0, 5)   0.000000
(1, 0)  10.000000
(1, 1)   9.500000
(1, 2)  21.660000
(1, 3)  11.005205
(1, 4)   0.000000
(1, 5)   0.000000
(2, 0)  10.000000
(2, 1)   9.500000
(2, 2)   9.025000
(2, 3)  20.577000
(2, 4)  10.454945
(2, 5)   0.000000
(3, 0)  10.000000
(3, 1)   9.800000
(3, 2)   9.310000
(3, 3)   8.844500
(3, 4)  20.165460
(3, 5)  10.245846
(4, 0)  10.000000
(4, 1)   9.800000
(4, 2)   9.604000
(4, 3)   9.123800
(4, 4)   8.667610
(4, 5)  19.762151
(5, 0)  10.000000
(5, 1)   9.800000
(5, 2)   9.604000
(5, 3)   9.411920
(5, 4)   8.941324
(5, 5)   8.494258
(6, 0)  10.000000
(6, 1)   9.800000
(6, 2)   9.604000
(6, 3)   9.411920
(6, 4)   9.223682
(6, 5)   8.762498
(7, 0)  10.000000
(7, 1)   9.800000
(7, 2)   9.604000
(7, 3)   9.411920
(7, 4)   9.223682
```

(continues on next page)

(continued from previous page)

```

(7, 5)      9.039208
(8, 0)     10.000000
(8, 1)      9.800000
(8, 2)      9.604000
(8, 3)      9.411920
(8, 4)      9.223682
(8, 5)      9.039208
(9, 0)     10.000000
(9, 1)      9.800000
(9, 2)      9.604000
(9, 3)      9.411920
(9, 4)      9.223682
(9, 5)      9.039208
(10, 0)    10.000000
(10, 1)     9.800000
(10, 2)     9.604000
(10, 3)     9.411920
(10, 4)     9.223682
(10, 5)     9.039208
(11, 0)    10.000000
(11, 1)     9.800000
(11, 2)     9.604000
(11, 3)     9.411920
(11, 4)     9.223682
(11, 5)     9.039208
(12, 0)     0.000000
(12, 1)     9.800000
(12, 2)     9.604000
(12, 3)     9.411920
(12, 4)     9.223682
(12, 5)     9.039208
  numBullocksSold  numHeifersSold  capitalOutlay  numExcessLabourHours  \
1          53.735000         30.935000           0.0           0.0
2          52.341850         40.757423           0.0           0.0
3          57.435807         57.435807           0.0           0.0
4          56.964286         56.964286           0.0           0.0
5          50.853436         50.853436           0.0           0.0

      revenue      cost      profit
1  41494.530000  19588.466667  21906.063333
2  41153.336497  19264.639818  21888.696679
3  45212.490308  19396.435208  25816.055100
4  45860.056078  19034.285714  26825.770363
5  42716.941438  17434.354053  25282.587385
      grainAcres  grainGrown
(group1, 1)      20.000000    22.000000
(group1, 2)      20.000000    22.000000
(group1, 3)      20.000000    22.000000
(group1, 4)      20.000000    22.000000
(group1, 5)      20.000000    22.000000
(group2, 1)       0.000000     0.000000
(group2, 2)       0.000000     0.000000
(group2, 3)       3.134152     2.820737
(group2, 4)       0.000000     0.000000
(group2, 5)       0.000000     0.000000
(group3, 1)       0.000000     0.000000
(group3, 2)       0.000000     0.000000

```

(continues on next page)

(continued from previous page)

```

(group3, 3)    0.000000    0.000000
(group3, 4)    0.000000    0.000000
(group3, 5)    0.000000    0.000000
(group4, 1)    0.000000    0.000000
(group4, 2)    0.000000    0.000000
(group4, 3)    0.000000    0.000000
(group4, 4)    0.000000    0.000000
(group4, 5)    0.000000    0.000000
   grainBought  grainSold  sugarBeetAcres  sugerBeetGrown  sugarBeetBought  \
1    36.620000         0.0         60.766667         91.150000             0.0
2    35.100200         0.0         62.670049         94.005073             0.0
3    37.836507         0.0         65.100304         97.650456             0.0
4    40.142857         0.0         76.428571        114.642857             0.0
5    33.476475         0.0         87.539208        131.308812             0.0

   sugarBeetSold
1    22.760000
2    27.388173
3    24.550338
4    42.142857
5    66.586258
   num_acres  max_num_cows_def
1    200.0         130.000000
2    200.0        128.411427
3    200.0        115.433945
4    200.0        103.571429
5    200.0         92.460792
Out [8]: 121719.17286133638

```

## 4.1.9 Economic Planning

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex9\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex9_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex09.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex09.html)

### Model

```

import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='economic_planning', session=cas_conn)

    industry_data = pd.DataFrame([
        ['coal', 150, 300, 60],
        ['steel', 80, 350, 60],
        ['transport', 100, 280, 30]
    ], columns=['industry', 'init_stocks', 'init_productive_capacity',

```

(continues on next page)

(continued from previous page)

```

        'demand']).set_index(['industry'])

production_data = pd.DataFrame([
    ['coal', 0.1, 0.5, 0.4],
    ['steel', 0.1, 0.1, 0.2],
    ['transport', 0.2, 0.1, 0.2],
    ['manpower', 0.6, 0.3, 0.2],
], columns=['input', 'coal',
            'steel', 'transport']).set_index(['input'])

productive_capacity_data = pd.DataFrame([
    ['coal', 0.0, 0.7, 0.9],
    ['steel', 0.1, 0.1, 0.2],
    ['transport', 0.2, 0.1, 0.2],
    ['manpower', 0.4, 0.2, 0.1],
], columns=['input', 'coal',
            'steel', 'transport']).set_index(['input'])

manpower_capacity = 470
num_years = 5

YEARS = list(range(1, num_years+1))
YEARS0 = [0] + list(YEARS)
INDUSTRIES = industry_data.index.tolist()

init_stocks = industry_data['init_stocks']
init_productive_capacity = industry_data['init_productive_capacity']
demand = industry_data['demand']

production_coeff = so.flatten_frame(production_data)
productive_capacity_coeff = so.flatten_frame(productive_capacity_data)

static_production = m.add_variables(INDUSTRIES, lb=0,
                                   name='static_production')
m.set_objective(0, sense=so.MIN, name='Zero')
m.add_constraints((static_production[i] == demand[i] +
                    so.expr_sum(
                        production_coeff[i, j] * static_production[j]
                        for j in INDUSTRIES) for i in INDUSTRIES),
                  name='static_con')

m.solve()
print(so.get_value_table(static_production))

final_demand = so.get_value_table(
    static_production)['static_production']

production = m.add_variables(INDUSTRIES, range(0, num_years+2), lb=0,
                             name='production')
stock = m.add_variables(INDUSTRIES, range(0, num_years+2), lb=0,
                        name='stock')
extra_capacity = m.add_variables(INDUSTRIES, range(2, num_years+3), lb=0,
                                name='extra_capacity')

productive_capacity = so.ImplicitVar(
    (init_productive_capacity[i] +
     so.expr_sum(extra_capacity[i, y] for y in range(2, year+1))

```

(continues on next page)

(continued from previous page)

```

        for i in INDUSTRIES for year in range(1, num_years+2)),
        name='productive_capacity'
    )

    for i in INDUSTRIES:
        production[i, 0].set_bounds(ub=0)
        stock[i, 0].set_bounds(lb=init_stocks[i], ub=init_stocks[i])

    total_productive_capacity = sum(productive_capacity[i, num_years]
                                   for i in INDUSTRIES)
    total_production = so.expr_sum(production[i, year] for i in INDUSTRIES
                                   for year in [4, 5])
    total_manpower = so.expr_sum(production_coeff['manpower', i] *
                                production[i, year+1] +
                                productive_capacity_coeff['manpower', i] *
                                extra_capacity[i, year+2]
                                for i in INDUSTRIES for year in YEARS)

    continuity_con = m.add_constraints((
        stock[i, year] + production[i, year] ==
        (demand[i] if year in YEARS else 0) +
        so.expr_sum(production_coeff[i, j] * production[j, year+1] +
                    productive_capacity_coeff[i, j] *
                    extra_capacity[j, year+2] for j in INDUSTRIES) +
        stock[i, year+1]
        for i in INDUSTRIES for year in YEARS0), name='continuity_con')

    manpower_con = m.add_constraints((
        so.expr_sum(production_coeff['manpower', j] * production[j, year] +
                    productive_capacity_coeff['manpower', j] *
                    extra_capacity[j, year+1]
                    for j in INDUSTRIES)
        <= manpower_capacity for year in range(1, num_years+2)),
        name='manpower_con')

    capacity_con = m.add_constraints((production[i, year] <=
                                    productive_capacity[i, year]
                                    for i in INDUSTRIES
                                    for year in range(1, num_years+2)),
                                    name='capacity_con')

    for i in INDUSTRIES:
        production[i, num_years+1].set_bounds(lb=final_demand[i])

    for i in INDUSTRIES:
        for year in [num_years+1, num_years+2]:
            extra_capacity[i, year].set_bounds(ub=0)

    problem1 = so.Model(name='Problem1', session=cas_conn)
    problem1.include(
        production, stock, extra_capacity, continuity_con, manpower_con,
        capacity_con, productive_capacity)
    problem1.set_objective(total_productive_capacity, sense=so.MAX,
                           name='total_productive_capacity')

    problem1.solve()
    so.pd.display_dense()
    print(so.get_value_table(production, stock, extra_capacity,

```

(continues on next page)



(continued from previous page)

```

        productive_capacity).sort_index())
print(so.get_value_table(manpower_con.get_expressions()))

# Problem 2

problem2 = so.Model(name='Problem2', session=cas_conn)
problem2.include(problem1)
problem2.set_objective(total_production, name='total_production',
                       sense=so.MAX)
for i in INDUSTRIES:
    for year in YEARS:
        continuity_con[i, year].set_rhs(0)
problem2.solve()
print(so.get_value_table(production, stock, extra_capacity,
                        productive_capacity).sort_index())
print(so.get_value_table(manpower_con.get_expressions()))

# Problem 3

problem3 = so.Model(name='Problem3', session=cas_conn)
problem3.include(production, stock, extra_capacity, continuity_con,
                capacity_con)
problem3.set_objective(total_manpower, sense=so.MAX, name='total_manpower')
for i in INDUSTRIES:
    for year in YEARS:
        continuity_con[i, year].set_rhs(demand[i])
problem3.solve()
print(so.get_value_table(production, stock, extra_capacity,
                        productive_capacity).sort_index())
print(so.get_value_table(manpower_con.get_expressions()))

return problem3.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.client_side.economic_planning import test

In [8]: test(cas_conn)
NOTE: Initialized model economic_planning.
NOTE: Added action set 'optimization'.
NOTE: Converting model economic_planning to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.

```

(continues on next page)

(continued from previous page)

```

NOTE: Problem generation will use 8 threads.
NOTE: The problem has 3 variables (0 free, 0 fixed).
NOTE: The problem has 3 linear constraints (0 LE, 3 EQ, 0 GE, 0 range).
NOTE: The problem has 9 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.01 seconds.
NOTE: The LP presolver removed all variables and constraints.
NOTE: Optimal.
NOTE: Objective = 0.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 3 rows and 6
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 3 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4
↳columns.
      static_production
coal          166.396761
steel         105.668016
transport      92.307692
NOTE: Initialized model Problem1.
NOTE: Added action set 'optimization'.
NOTE: Converting model Problem1 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 60 variables (0 free, 12 fixed).
NOTE: The problem has 42 linear constraints (24 LE, 18 EQ, 0 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 15 variables and 3 constraints.
NOTE: The LP presolver removed 37 constraint coefficients.
NOTE: The presolved problem has 45 variables, 39 constraints, and 218 constraint
↳coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      2.683246E+04      0
      P 2          42      2.141875E+03      0
NOTE: Optimal.
NOTE: Objective = 2141.8751967.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 60 rows and 6
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 42 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4
↳columns.
      production      stock      extra_capacity      productive_capacity
coal      0      0.000000      1.500000e+02      NaN      NaN
coal      1      260.402615      0.000000e+00      NaN      300.000000

```

(continues on next page)

(continued from previous page)

coal	2	293.406208	0.000000e+00	0.000000	300.000000
coal	3	300.000000	0.000000e+00	0.000000	300.000000
coal	4	17.948718	1.484480e+02	189.203132	489.203132
coal	5	166.396761	0.000000e+00	1022.672065	1511.875197
coal	6	166.396761	1.421085e-14	0.000000	1511.875197
coal	7	NaN	NaN	0.000000	NaN
steel	0	0.000000	8.000000e+01	NaN	NaN
steel	1	135.341540	1.228110e+01	NaN	350.000000
steel	2	181.659854	0.000000e+00	0.000000	350.000000
steel	3	193.090418	0.000000e+00	0.000000	350.000000
steel	4	105.668016	0.000000e+00	0.000000	350.000000
steel	5	105.668016	0.000000e+00	0.000000	350.000000
steel	6	105.668016	-1.456613e-13	0.000000	350.000000
steel	7	NaN	NaN	0.000000	NaN
transport	0	0.000000	1.000000e+02	NaN	NaN
transport	1	140.722422	6.240839e+00	NaN	280.000000
transport	2	200.580168	0.000000e+00	0.000000	280.000000
transport	3	267.152497	0.000000e+00	0.000000	280.000000
transport	4	92.307692	0.000000e+00	0.000000	280.000000
transport	5	92.307692	0.000000e+00	0.000000	280.000000
transport	6	92.307692	-3.907985e-14	0.000000	280.000000
transport	7	NaN	NaN	0.000000	NaN

manpower\_con

1	224.988515
2	270.657715
3	367.038878
4	470.000000
5	150.000000
6	150.000000

NOTE: Initialized model Problem2.

NOTE: Added action set 'optimization'.

NOTE: Converting model Problem2 to OPTMODEL.

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 60 variables (0 free, 12 fixed).

NOTE: The problem has 42 linear constraints (24 LE, 18 EQ, 0 GE, 0 range).

NOTE: The problem has 255 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver is disabled for linear problems.

NOTE: The LP presolver value AUTOMATIC is applied.

NOTE: The LP presolver time is 0.00 seconds.

NOTE: The LP presolver removed 15 variables and 3 constraints.

NOTE: The LP presolver removed 37 constraint coefficients.

NOTE: The presolved problem has 45 variables, 39 constraints, and 218 constraint\_  
↪coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

		Objective	
Phase	Iteration	Value	Time
D	2	1.504360E+04	0
P	2	46	2.618579E+03
			0

NOTE: Optimal.

NOTE: Objective = 2618.5791147.

NOTE: The Dual Simplex solve time is 0.01 seconds.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 60 rows and 6\_  
↪columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 42 rows and 4 columns.

(continues on next page)

(continued from previous page)

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4 columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4 columns.

		production	stock	extra_capacity	productive_capacity
coal	0	0.000000	150.000000	NaN	NaN
coal	1	184.818327	31.628509	NaN	300.000000
coal	2	430.504654	16.372454	1.305047e+02	430.504654
coal	3	430.504654	0.000000	0.000000e+00	430.504654
coal	4	430.504654	0.000000	-1.207321e-12	430.504654
coal	5	430.504654	0.000000	0.000000e+00	430.504654
coal	6	166.396761	324.107893	0.000000e+00	430.504654
coal	7	NaN	NaN	0.000000e+00	NaN
steel	0	0.000000	80.000000	NaN	NaN
steel	1	86.729504	11.532298	NaN	350.000000
steel	2	155.337478	0.000000	0.000000e+00	350.000000
steel	3	182.867219	0.000000	0.000000e+00	350.000000
steel	4	359.402270	0.000000	9.402270e+00	359.402270
steel	5	359.402270	176.535051	0.000000e+00	359.402270
steel	6	105.668016	490.269305	0.000000e+00	359.402270
steel	7	NaN	NaN	0.000000e+00	NaN
transport	0	0.000000	100.000000	NaN	NaN
transport	1	141.312267	0.000000	NaN	280.000000
transport	2	198.387943	0.000000	0.000000e+00	280.000000
transport	3	225.917684	0.000000	0.000000e+00	280.000000
transport	4	519.382633	0.000000	2.393826e+02	519.382633
transport	5	519.382633	293.464949	0.000000e+00	519.382633
transport	6	92.307692	750.539890	0.000000e+00	519.382633
transport	7	NaN	NaN	0.000000e+00	NaN
manpower_con					
1		217.374162			
2		344.581624			
3		384.165212			
4		470.000000			
5		470.000000			
6		150.000000			

NOTE: Initialized model Problem3.

NOTE: Added action set 'optimization'.

NOTE: Converting model Problem3 to OPTMODEL.

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 60 variables (0 free, 12 fixed).

NOTE: The problem has 36 linear constraints (18 LE, 18 EQ, 0 GE, 0 range).

NOTE: The problem has 219 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver is disabled for linear problems.

NOTE: The LP presolver value AUTOMATIC is applied.

NOTE: The LP presolver time is 0.00 seconds.

NOTE: The LP presolver removed 15 variables and 3 constraints.

NOTE: The LP presolver removed 31 constraint coefficients.

NOTE: The presolved problem has 45 variables, 33 constraints, and 188 constraint coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

		Objective	
Phase	Iteration	Value	Time
D 2	1	1.464016E+05	0

(continues on next page)

(continued from previous page)

```

      D 2          54      2.450706E+03      0
      P 2          56      2.450027E+03      0
NOTE: Optimal.
NOTE: Objective = 2450.0266228.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 60 rows and 6_
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 36 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.

      production      stock      extra_capacity      productive_capacity
coal      0      0.000000      150.000000      NaN      NaN
coal      1      251.792754      0.000000      NaN      300.000000
coal      2      316.015222      0.000000      16.015222      316.015222
coal      3      319.832020      0.000000      3.816798      319.832020
coal      4      366.349753      0.000000      46.517734      366.349753
coal      5      859.359606      0.000000      493.009853      859.359606
coal      6      859.359606      460.207993      0.000000      859.359606
coal      7      NaN      NaN      0.000000      NaN
steel     0      0.000000      80.000000      NaN      NaN
steel     1      134.794583      11.028028      NaN      350.000000
steel     2      175.041379      0.000000      0.000000      350.000000
steel     3      224.064039      0.000000      0.000000      350.000000
steel     4      223.136289      0.000000      0.000000      350.000000
steel     5      220.043787      0.000000      0.000000      350.000000
steel     6      350.000000      0.000000      0.000000      350.000000
steel     7      NaN      NaN      0.000000      NaN
transport 0      0.000000      100.000000      NaN      NaN
transport 1      143.558583      4.247230      NaN      280.000000
transport 2      181.676355      0.000000      0.000000      280.000000
transport 3      280.000000      0.000000      0.000000      280.000000
transport 4      279.072249      0.000000      0.000000      280.000000
transport 5      275.979748      0.000000      0.000000      280.000000
transport 6      195.539132      0.000000      0.000000      280.000000
transport 7      NaN      NaN      0.000000      NaN
manpower_con
1      226.631832
2      279.983537
3      333.725517
4      539.769130
5      636.824849
6      659.723590
Out [8]: 2450.026622821294

```

## 4.1.10 Decentralization

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex10\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex10_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex10.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex10.html)

### Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='decentralization', session=cas_conn)

    DEPTS = ['A', 'B', 'C', 'D', 'E']
    CITIES = ['Bristol', 'Brighton', 'London']

    benefit_data = pd.DataFrame([
        ['Bristol', 10, 15, 10, 20, 5],
        ['Brighton', 10, 20, 15, 15, 15]],
        columns=['city'] + DEPTS).set_index('city')

    comm_data = pd.DataFrame([
        ['A', 'B', 0.0],
        ['A', 'C', 1.0],
        ['A', 'D', 1.5],
        ['A', 'E', 0.0],
        ['B', 'C', 1.4],
        ['B', 'D', 1.2],
        ['B', 'E', 0.0],
        ['C', 'D', 0.0],
        ['C', 'E', 2.0],
        ['D', 'E', 0.7]], columns=['i', 'j', 'comm']).set_index(['i', 'j'])

    cost_data = pd.DataFrame([
        ['Bristol', 'Bristol', 5],
        ['Bristol', 'Brighton', 14],
        ['Bristol', 'London', 13],
        ['Brighton', 'Brighton', 5],
        ['Brighton', 'London', 9],
        ['London', 'London', 10]], columns=['i', 'j', 'cost']).set_index(
        ['i', 'j'])

    max_num_depts = 3

    benefit = {}
    for city in CITIES:
        for dept in DEPTS:
            try:
                benefit[dept, city] = benefit_data.loc[city, dept]
            except:
```

(continues on next page)

(continued from previous page)

```

        benefit[dept, city] = 0

comm = {}
for row in comm_data.iterrows():
    (i, j) = row[0]
    comm[i, j] = row[1]['comm']
    comm[j, i] = comm[i, j]

cost = {}
for row in cost_data.iterrows():
    (i, j) = row[0]
    cost[i, j] = row[1]['cost']
    cost[j, i] = cost[i, j]

assign = m.add_variables(DEPTS, CITIES, vartype=so.BIN, name='assign')
IJKL = [(i, j, k, l)
        for i in DEPTS for j in CITIES for k in DEPTS for l in CITIES
        if i < k]
product = m.add_variables(IJKL, vartype=so.BIN, name='product')

totalBenefit = so.expr_sum(benefit[i, j] * assign[i, j]
                          for i in DEPTS for j in CITIES)

totalCost = so.expr_sum(comm[i, k] * cost[j, l] * product[i, j, k, l]
                       for (i, j, k, l) in IJKL)

m.set_objective(totalBenefit-totalCost, name='netBenefit', sense=so.MAX)

m.add_constraints((so.expr_sum(assign[dept, city] for city in CITIES)
                  == 1 for dept in DEPTS), name='assign_dept')

m.add_constraints((so.expr_sum(assign[dept, city] for dept in DEPTS)
                  <= max_num_depts for city in CITIES), name='cardinality')

product_def1 = m.add_constraints((assign[i, j] + assign[k, l] - 1
                                <= product[i, j, k, l]
                                for (i, j, k, l) in IJKL),
                                name='pd1')

product_def2 = m.add_constraints((product[i, j, k, l] <= assign[i, j]
                                for (i, j, k, l) in IJKL),
                                name='pd2')

product_def3 = m.add_constraints((product[i, j, k, l] <= assign[k, l]
                                for (i, j, k, l) in IJKL),
                                name='pd3')

m.solve()
print(m.get_problem_summary())

m.drop_constraints(product_def1)
m.drop_constraints(product_def2)
m.drop_constraints(product_def3)

m.add_constraints((
    so.expr_sum(product[i, j, k, l]
                for j in CITIES if (i, j, k, l) in IJKL) == assign[k, l]

```

(continues on next page)

(continued from previous page)

```

    for i in DEPTS for k in DEPTS for l in CITIES if i < k),
    name='pd4')

m.add_constraints((
    so.expr_sum(product[i, j, k, l]
                 for l in CITIES if (i, j, k, l) in IJKL) == assign[i, j]
    for k in DEPTS for i in DEPTS for j in CITIES if i < k),
    name='pd5')

m.solve()
print(m.get_problem_summary())
totalBenefit.set_name('totalBenefit')
totalCost.set_name('totalCost')
print(so.get_solution_table(totalBenefit, totalCost))
print(so.get_solution_table(assign).unstack(level=-1))

return m.get_objective_value()

```

## Output

```
In [1]: import os
```

```
In [2]: hostname = os.getenv('CASHOST')
```

```
In [3]: port = os.getenv('CASPORT')
```

```
In [4]: from swat import CAS
```

```
In [5]: cas_conn = CAS(hostname, port)
```

```
In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.decentralization import test
```

```
In [8]: test(cas_conn)
```

```
NOTE: Initialized model decentralization.
```

```
NOTE: Added action set 'optimization'.
```

```
NOTE: Converting model decentralization to OPTMODEL.
```

```
NOTE: Submitting OPTMODEL code to CAS server.
```

```
NOTE: Problem generation will use 8 threads.
```

```
NOTE: The problem has 105 variables (0 free, 0 fixed).
```

```
NOTE: The problem has 105 binary and 0 integer variables.
```

```
NOTE: The problem has 278 linear constraints (183 LE, 5 EQ, 90 GE, 0 range).
```

```
NOTE: The problem has 660 linear constraint coefficients.
```

```
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
```

```
NOTE: The OPTMODEL presolver is disabled for linear problems.
```

```
NOTE: The initial MILP heuristics are applied.
```

```
NOTE: The MILP presolver value AUTOMATIC is applied.
```

```
NOTE: The MILP presolver removed 0 variables and 120 constraints.
```

```
NOTE: The MILP presolver removed 120 constraint coefficients.
```

```
NOTE: The MILP presolver added 120 constraint coefficients.
```

```
NOTE: The MILP presolver modified 0 constraint coefficients.
```

```
NOTE: The presolved problem has 105 variables, 158 constraints, and 540 constraint_
->coefficients.
```

(continues on next page)



(continued from previous page)

NOTE: The MILP solver is called.

NOTE: The parallel Branch and Cut algorithm is used.

NOTE: The Branch and Cut algorithm is using up to 8 threads.

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	2	-14.9000000	135.0000000	111.04%	0
0	1	2	-14.9000000	67.5000000	122.07%	0
0	1	2	-14.9000000	55.0000000	127.09%	0
0	1	3	8.1000000	55.0000000	85.27%	0
0	1	3	8.1000000	48.0000000	83.12%	0
0	1	3	8.1000000	44.8375000	81.93%	0
0	1	3	8.1000000	42.0000000	80.71%	0
0	1	3	8.1000000	39.0666667	79.27%	0
0	1	3	8.1000000	34.7500000	76.69%	0
0	1	3	8.1000000	33.3692308	75.73%	0
0	1	3	8.1000000	32.6500000	75.19%	0
0	1	3	8.1000000	31.9066667	74.61%	0
0	1	3	8.1000000	30.7000000	73.62%	0
0	1	3	8.1000000	30.1600000	73.14%	0
0	1	3	8.1000000	29.8800000	72.89%	0
0	1	3	8.1000000	29.8000000	72.82%	0
0	1	3	8.1000000	29.4722222	72.52%	0
0	1	3	8.1000000	28.9117647	71.98%	0
0	1	3	8.1000000	28.6716667	71.75%	0
0	1	3	8.1000000	28.5000000	71.58%	0
0	1	4	14.9000000	14.9000000	0.00%	0

NOTE: The MILP solver added 34 cuts with 185 cut coefficients at the root.

NOTE: Optimal.

NOTE: Objective = 14.9.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 105 rows and 6 columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 278 rows and 4 columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4 columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4 columns.

Selected Rows from Table PROBLEMSUMMARY

	Value
Label	
Objective Sense	Maximization
Objective Function	netBenefit
Objective Type	Linear
Number of Variables	105
Bounded Above	0
Bounded Below	0
Bounded Below and Above	105
Free	0
Fixed	0
Binary	105
Integer	0
Number of Constraints	278
Linear LE (<=)	183
Linear EQ (=)	5
Linear GE (>=)	90
Linear Range	0

(continues on next page)

(continued from previous page)

```

Constraint Coefficients          660
NOTE: Added action set 'optimization'.
NOTE: Converting model decentralization to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 105 variables (0 free, 0 fixed).
NOTE: The problem has 105 binary and 0 integer variables.
NOTE: The problem has 68 linear constraints (3 LE, 65 EQ, 0 GE, 0 range).
NOTE: The problem has 270 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 0 constraints.
NOTE: The MILP presolver removed 0 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The presolved problem has 105 variables, 68 constraints, and 270 constraint_
↳coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 8 threads.

```

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	2	-28.1000000	135.0000000	120.81%	0
0	1	2	-28.1000000	30.0000000	193.67%	0
0	1	3	-16.3000000	30.0000000	154.33%	0
0	1	3	-16.3000000	30.0000000	154.33%	0
2	0	4	14.9000000	14.9000000	0.00%	0

```

NOTE: The MILP solver added 4 cuts with 24 cut coefficients at the root.
NOTE: Optimal.
NOTE: Objective = 14.9.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 105 rows and 6_
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 68 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4_
↳columns.
Selected Rows from Table PROBLEMSUMMARY

```

Label	Value
Objective Sense	Maximization
Objective Function	netBenefit
Objective Type	Linear
Number of Variables	105
Bounded Above	0
Bounded Below	0
Bounded Below and Above	105
Free	0
Fixed	0
Binary	105
Integer	0
Number of Constraints	68
Linear LE (<=)	3

(continues on next page)

(continued from previous page)

```

Linear EQ (=)                65
Linear GE (>=)               0
Linear Range                 0

Constraint Coefficients      270
  totalBenefit  totalCost
-      80.0      65.1
assign  (A, Bristol)        1.0
        (A, Brighton)       0.0
        (A, London)         0.0
        (B, Bristol)         0.0
        (B, Brighton)        1.0
        (B, London)          0.0
        (C, Bristol)         0.0
        (C, Brighton)        1.0
        (C, London)         -0.0
        (D, Bristol)         1.0
        (D, Brighton)        0.0
        (D, London)          0.0
        (E, Bristol)         0.0
        (E, Brighton)        1.0
        (E, London)          0.0
dtype: float64
Out[8]: 14.9

```

### 4.1.11 Optimal Wedding Seating

#### Reference

SAS blog: <https://blogs.sas.com/content/operations/2014/11/10/do-you-have-an-uncle-louie-optimal-wedding-seat-assignments/>

#### Model

```

import sasoptpy as so
import math

def test(cas_conn, num_guests=20, max_table_size=3, max_tables=None):

    m = so.Model("wedding", session=cas_conn)

    # Check max. tables
    if max_tables is None:
        max_tables = math.ceil(num_guests/max_table_size)

    # Sets
    guests = range(1, num_guests+1)
    tables = range(1, max_tables+1)
    guest_pairs = [[i, j] for i in guests for j in range(i+1, num_guests+1)]

    # Variables
    x = m.add_variables(guests, tables, vartype=so.BIN, name="x")
    unhappy = m.add_variables(tables, name="unhappy", lb=0)

```

(continues on next page)

(continued from previous page)

```

# Objective
m.set_objective(unhappy.sum('*'), sense=so.MIN, name="obj")

# Constraints
m.add_constraints((x.sum(g, '*') == 1 for g in guests), name="assigncon")
m.add_constraints((x.sum('*', t) <= max_table_size for t in tables),
                  name="tablesizecon")
m.add_constraints((unhappy[t] >= abs(g-h)*(x[g, t] + x[h, t] - 1)
                  for t in tables for [g, h] in guest_pairs),
                  name="measurecon")

# Solve
res = m.solve(options={
    'with': 'milp', 'decomp': {'method': 'set'}, 'presolver': 'none'})

if res is not None:

    print(so.get_solution_table(x))

    # Print assignments
    for t in tables:
        print('Table {} : [ '.format(t), end='')
        for g in guests:
            if x[g, t].get_value() == 1:
                print('{} '.format(g), end='')
        print(']')

    return m.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.client_side.sas_optimal_wedding import test

In [8]: test(cas_conn)
NOTE: Initialized model wedding.
NOTE: Added action set 'optimization'.
NOTE: Converting model wedding to DataFrame.
NOTE: Uploading the problem DataFrame to the server.
NOTE: Cloud Analytic Services made the uploaded file available as table TMP9UWNOKOC_
↳in caslib CASUSER(casuser).
NOTE: The table TMP9UWNOKOC has been created in caslib CASUSER(casuser) from binary_
↳data uploaded to Cloud Analytic Services.

```

(continues on next page)

(continued from previous page)

NOTE: The problem wedding has 147 variables (140 binary, 0 integer, 0 free, 0 fixed).  
 NOTE: The problem has 1357 constraints (7 LE, 20 EQ, 1330 GE, 0 range).  
 NOTE: The problem has 4270 constraint coefficients.  
 NOTE: The initial MILP heuristics are applied.  
 NOTE: The MILP presolver value NONE is applied.  
 NOTE: The MILP solver is called.  
 NOTE: The Decomposition algorithm is used.  
 NOTE: The Decomposition algorithm is executing in the distributed computing\_↵  
 ↵environment in single-machine mode.  
 NOTE: The DECOMP method value SET is applied.  
 NOTE: All blocks are identical and the master model is set partitioning.  
 NOTE: The Decomposition algorithm is using an aggregate formulation and Ryan-Foster\_↵  
 ↵branching.  
 NOTE: The number of block threads has been reduced to 1 threads.  
 NOTE: The problem has a decomposable structure with 7 blocks. The largest block\_↵  
 ↵covers 14.08% of the constraints in the problem.  
 NOTE: The decomposition subproblems cover 147 (100%) variables and 1337 (98.53%)\_↵  
 ↵constraints.  
 NOTE: The deterministic parallel mode is enabled.  
 NOTE: The Decomposition algorithm is using up to 8 threads.

Iter	Best	Master	Best	LP	IP	CPU	Real
	Bound	Objective	Integer	Gap	Gap	Time	Time
.	0.0000	13.0000	13.0000	1.30e+01	1.30e+01	0	0
1	0.0000	13.0000	13.0000	1.30e+01	1.30e+01	0	0
.	0.0000	13.0000	13.0000	1.30e+01	1.30e+01	1	2
10	0.0000	13.0000	13.0000	1.30e+01	1.30e+01	1	2
18	4.2500	13.0000	13.0000	205.88%	205.88%	6	7
19	6.0000	13.0000	13.0000	116.67%	116.67%	6	7
.	6.0000	13.0000	13.0000	116.67%	116.67%	6	7
20	6.0000	13.0000	13.0000	116.67%	116.67%	7	8
21	9.5000	13.0000	13.0000	36.84%	36.84%	7	8
23	13.0000	13.0000	13.0000	0.00%	0.00%	7	9

Node	Active	Sols	Best	Best	Gap	CPU	Real
			Integer	Bound		Time	Time
0	1	3	13.0000	13.0000	0.00%	7	9

NOTE: The Decomposition algorithm used 8 threads.

NOTE: The Decomposition algorithm time is 9.22 seconds.

NOTE: Optimal.

NOTE: Objective = 13.

x

(1, 1)	1.0
(1, 2)	0.0
(1, 3)	0.0
(1, 4)	0.0
(1, 5)	0.0
(1, 6)	0.0
(1, 7)	0.0
(2, 1)	1.0
(2, 2)	0.0
(2, 3)	0.0
(2, 4)	0.0
(2, 5)	0.0
(2, 6)	0.0
(2, 7)	0.0
(3, 1)	1.0
(3, 2)	0.0
(3, 3)	0.0

(continues on next page)

(continued from previous page)

```
(3, 4) 0.0
(3, 5) 0.0
(3, 6) 0.0
(3, 7) 0.0
(4, 1) 0.0
(4, 2) 1.0
(4, 3) 0.0
(4, 4) 0.0
(4, 5) 0.0
(4, 6) 0.0
(4, 7) 0.0
(5, 1) 0.0
(5, 2) 1.0
(5, 3) 0.0
(5, 4) 0.0
(5, 5) 0.0
(5, 6) 0.0
(5, 7) 0.0
(6, 1) 0.0
(6, 2) 1.0
(6, 3) 0.0
(6, 4) 0.0
(6, 5) 0.0
(6, 6) 0.0
(6, 7) 0.0
(7, 1) 0.0
(7, 2) 0.0
(7, 3) 1.0
(7, 4) 0.0
(7, 5) 0.0
(7, 6) 0.0
(7, 7) 0.0
(8, 1) 0.0
(8, 2) 0.0
(8, 3) 1.0
(8, 4) 0.0
(8, 5) 0.0
(8, 6) 0.0
(8, 7) 0.0
(9, 1) 0.0
(9, 2) 0.0
(9, 3) 1.0
(9, 4) 0.0
(9, 5) 0.0
(9, 6) 0.0
(9, 7) 0.0
(10, 1) 0.0
(10, 2) 0.0
(10, 3) 0.0
(10, 4) 1.0
(10, 5) 0.0
(10, 6) 0.0
(10, 7) 0.0
(11, 1) 0.0
(11, 2) 0.0
(11, 3) 0.0
(11, 4) 1.0
```

(continues on next page)

(continued from previous page)

```
(11, 5) 0.0
(11, 6) 0.0
(11, 7) 0.0
(12, 1) 0.0
(12, 2) 0.0
(12, 3) 0.0
(12, 4) 1.0
(12, 5) 0.0
(12, 6) 0.0
(12, 7) 0.0
(13, 1) 0.0
(13, 2) 0.0
(13, 3) 0.0
(13, 4) 0.0
(13, 5) 1.0
(13, 6) 0.0
(13, 7) 0.0
(14, 1) 0.0
(14, 2) 0.0
(14, 3) 0.0
(14, 4) 0.0
(14, 5) 1.0
(14, 6) 0.0
(14, 7) 0.0
(15, 1) 0.0
(15, 2) 0.0
(15, 3) 0.0
(15, 4) 0.0
(15, 5) 1.0
(15, 6) 0.0
(15, 7) 0.0
(16, 1) 0.0
(16, 2) 0.0
(16, 3) 0.0
(16, 4) 0.0
(16, 5) 0.0
(16, 6) 1.0
(16, 7) 0.0
(17, 1) 0.0
(17, 2) 0.0
(17, 3) 0.0
(17, 4) 0.0
(17, 5) 0.0
(17, 6) 1.0
(17, 7) 0.0
(18, 1) 0.0
(18, 2) 0.0
(18, 3) 0.0
(18, 4) 0.0
(18, 5) 0.0
(18, 6) 1.0
(18, 7) 0.0
(19, 1) 0.0
(19, 2) 0.0
(19, 3) 0.0
(19, 4) 0.0
(19, 5) 0.0
```

(continues on next page)

(continued from previous page)

```
(19, 6) 0.0
(19, 7) 1.0
(20, 1) 0.0
(20, 2) 0.0
(20, 3) 0.0
(20, 4) 0.0
(20, 5) 0.0
(20, 6) 0.0
(20, 7) 1.0
Table 1 : [ 1 2 3 ]
Table 2 : [ 4 5 6 ]
Table 3 : [ 7 8 9 ]
Table 4 : [ 10 11 12 ]
Table 5 : [ 13 14 15 ]
Table 6 : [ 16 17 18 ]
Table 7 : [ 19 20 ]
Out[8]: 13.0
```

## 4.1.12 Kidney Exchange

### Reference

SAS blog: <https://blogs.sas.com/content/operations/2015/02/06/the-kidney-exchange-problem/>

### Model

```
import sasoptpy as so
import random

def test(cas_conn, **kwargs):
    # Data generation
    n = 80
    p = 0.02

    random.seed(1)

    ARCS = {}
    for i in range(0, n):
        for j in range(0, n):
            if random.random() < p:
                ARCS[i, j] = random.random()

    max_length = 10

    # Model
    model = so.Model("kidney_exchange", session=cas_conn)

    # Sets
    NODES = set().union(*ARCS.keys())
    MATCHINGS = range(1, int(len(NODES)/2)+1)

    # Variables
```

(continues on next page)



(continued from previous page)

```

UseNode = model.add_variables(NODES, MATCHINGS, vartype=so.BIN,
                              name="usenode")
UseArc = model.add_variables(ARCS, MATCHINGS, vartype=so.BIN,
                             name="usearc")
Slack = model.add_variables(NODES, vartype=so.BIN, name="slack")

print('Setting objective...')

# Objective
model.set_objective(so.expr_sum((ARCS[i, j] * UseArc[i, j, m]
                                for [i, j] in ARCS for m in MATCHINGS)),
                    name="total_weight", sense=so.MAX)

print('Adding constraints...')
# Constraints
Node_Packing = model.add_constraints((UseNode.sum(i, '*') + Slack[i] == 1
                                     for i in NODES), name="node_packing")
Donate = model.add_constraints((UseArc.sum(i, '*', m) == UseNode[i, m]
                               for i in NODES
                               for m in MATCHINGS), name="donate")
Receive = model.add_constraints((UseArc.sum('*', j, m) == UseNode[j, m]
                                for j in NODES
                                for m in MATCHINGS), name="receive")
Cardinality = model.add_constraints((UseArc.sum('*', '*', m) <= max_length
                                    for m in MATCHINGS),
                                   name="cardinality")

# Solve
model.solve(options={'with': 'milp', 'maxtime': 300}, **kwargs)

# Define decomposition blocks
for i in NODES:
    for m in MATCHINGS:
        Donate[i, m].set_block(m-1)
        Receive[i, m].set_block(m-1)
for m in MATCHINGS:
    Cardinality[m].set_block(m-1)

model.solve(options={
    'with': 'milp', 'maxtime': 300, 'presolver': 'basic',
    'decomp': {'method': 'user'}}, **kwargs)

return model.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

```

(continues on next page)

(continued from previous page)

```
In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.sas_kidney_exchange import test
```

```
In [8]: test(cas_conn)
```

NOTE: Initialized model kidney\_exchange.

Setting objective...

Adding constraints...

NOTE: Added action set 'optimization'.

NOTE: Converting model kidney\_exchange to OPTMODEL.

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 8133 variables (0 free, 0 fixed).

NOTE: The problem has 8133 binary and 0 integer variables.

NOTE: The problem has 5967 linear constraints (38 LE, 5929 EQ, 0 GE, 0 range).

NOTE: The problem has 24245 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The remaining solution time after problem generation and solver initialization  
→ is 299.82 seconds.

NOTE: The initial MILP heuristics are applied.

NOTE: The MILP presolver value AUTOMATIC is applied.

NOTE: The MILP presolver removed 6193 variables and 5357 constraints.

NOTE: The MILP presolver removed 17478 constraint coefficients.

NOTE: The MILP presolver modified 0 constraint coefficients.

NOTE: The presolved problem has 1940 variables, 610 constraints, and 6767 constraint  
→ coefficients.

NOTE: The MILP solver is called.

NOTE: The parallel Branch and Cut algorithm is used.

NOTE: The Branch and Cut algorithm is using up to 8 threads.

	Node	Active	Sols	BestInteger	BestBound	Gap	Time
	0	1	4	12.0775275	2279.8770216	99.47%	1
	0	1	4	12.0775275	18.3085704	34.03%	1

NOTE: The MILP solver's symmetry detection found 140 orbits. The largest orbit  
→ contains 37 variables.

	0	1	4	12.0775275	18.3085704	34.03%	1
	0	1	4	12.0775275	18.3085704	34.03%	1
	0	1	4	12.0775275	18.3085704	34.03%	1
	0	1	4	12.0775275	18.3085704	34.03%	1

NOTE: The MILP solver added 4 cuts with 196 cut coefficients at the root.

	11	8	5	17.1113590	18.1252274	5.59%	2
	28	6	6	17.1113590	18.0210902	5.05%	2
	30	5	7	17.1113590	18.0210902	5.05%	2
	40	6	8	17.1113590	18.0210902	5.05%	2
	66	0	8	17.1113590	17.1113590	0.00%	2

NOTE: Optimal.

NOTE: Objective = 17.111358985.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 8133 rows and 6  
→ columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 5967 rows and 4  
→ columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4  
→ columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4  
→ columns.

NOTE: Added action set 'optimization'.

(continues on next page)

(continued from previous page)

NOTE: Converting model kidney\_exchange to DataFrame.  
 NOTE: Cloud Analytic Services made the uploaded file available as table BLOCKSTABLE\_ in caslib CASUSER(casuser).  
 NOTE: The table BLOCKSTABLE has been created in caslib CASUSER(casuser) from binary\_ data uploaded to Cloud Analytic Services.  
 NOTE: Uploading the problem DataFrame to the server.  
 NOTE: Cloud Analytic Services made the uploaded file available as table TMPBU19006P\_ in caslib CASUSER(casuser).  
 NOTE: The table TMPBU19006P has been created in caslib CASUSER(casuser) from binary\_ data uploaded to Cloud Analytic Services.  
 NOTE: The problem kidney\_exchange has 8133 variables (8133 binary, 0 integer, 0 free, 0 fixed).  
 NOTE: The problem has 5967 constraints (38 LE, 5929 EQ, 0 GE, 0 range).  
 NOTE: The problem has 24245 constraint coefficients.  
 NOTE: The initial MILP heuristics are applied.  
 NOTE: The MILP presolver value BASIC is applied.  
 NOTE: The MILP presolver removed 2685 variables and 1925 constraints.  
 NOTE: The MILP presolver removed 8005 constraint coefficients.  
 NOTE: The MILP presolver modified 0 constraint coefficients.  
 NOTE: The presolved problem has 5448 variables, 4042 constraints, and 16240\_ constraint coefficients.  
 NOTE: The MILP solver is called.  
 NOTE: The Decomposition algorithm is used.  
 NOTE: The Decomposition algorithm is executing in the distributed computing\_ environment in single-machine mode.  
 NOTE: The DECOMP method value USER is applied.  
 NOTE: All blocks are identical and the master model is set partitioning.  
 NOTE: The Decomposition algorithm is using an aggregate formulation and Ryan-Foster\_ branching.  
 NOTE: The number of block threads has been reduced to 1 threads.  
 NOTE: The problem has a decomposable structure with 38 blocks. The largest block\_ covers 2.598% of the constraints in the problem.  
 NOTE: The decomposition subproblems cover 5396 (99.05%) variables and 3990 (98.71%)\_ constraints.  
 NOTE: The deterministic parallel mode is enabled.  
 NOTE: The Decomposition algorithm is using up to 8 threads.

Iter	Best Bound	Master Objective	Best Integer	LP Gap	IP Gap	CPU Time	Real Time
.	283.4155	10.5814	10.5814	96.27%	96.27%	1	1
1	259.0121	10.5814	10.5814	95.91%	95.91%	1	1
2	230.6758	10.5814	10.5814	95.41%	95.41%	1	2
3	204.2627	10.5814	10.5814	94.82%	94.82%	2	2
4	192.9770	14.7394	14.7394	92.36%	92.36%	2	3
6	162.6582	15.6274	15.6274	90.39%	90.39%	6	7
7	140.2584	15.6274	15.6274	88.86%	88.86%	6	7
8	109.9454	15.6274	15.6274	85.79%	85.79%	7	8
9	65.4530	16.1007	15.6274	75.40%	76.12%	7	8
10	65.4530	16.1007	17.1114	75.40%	73.86%	7	8
11	51.8662	17.1114	17.1114	67.01%	67.01%	7	9
14	25.6849	17.1114	17.1114	33.38%	33.38%	8	10
15	17.1114	17.1114	17.1114	0.00%	0.00%	9	10

Node	Active	Sols	Best Integer	Best Bound	Gap	CPU Time	Real Time
0	1	9	17.1114	17.1114	0.00%	9	10

NOTE: The Decomposition algorithm used 8 threads.  
 NOTE: The Decomposition algorithm time is 10.78 seconds.  
 NOTE: Optimal.

(continues on next page)

(continued from previous page)

NOTE: Objective = 17.111358985.

Out [8]: 17.11135898487

### 4.1.13 Multiobjective

#### Reference

SAS/OR example: [https://go.documentation.sas.com/?cdcId=pgmsascdc&cdcVersion=9.4\\_3.4&docsetId=ormpug&docsetTarget=ormpug\\_lsosolver\\_examples07.htm&locale=en](https://go.documentation.sas.com/?cdcId=pgmsascdc&cdcVersion=9.4_3.4&docsetId=ormpug&docsetTarget=ormpug_lsosolver_examples07.htm&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/lsoe10.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/lsoe10.html)

#### Model

```
import sasoptpy as so

def test(cas_conn, sols=False):

    m = so.Model(name='multiobjective', session=cas_conn)

    x = m.add_variables([1, 2], lb=0, ub=5, name='x')

    f1 = m.set_objective((x[1]-1)**2 + (x[1] - x[2])**2, name='f1', sense=so.MIN)
    f2 = m.append_objective((x[1]-x[2])**2 + (x[2] - 3)**2, name='f2', sense=so.MIN)

    m.solve(verbose=True, options={'with': 'blackbox', 'obj': (f1, f2), 'logfreq': 50}
    ↪)

    print('f1', f1.get_value())
    print('f2', f2.get_value())

    if sols:
        return dict(solutions=cas_conn.CASTable('allsols').to_frame(),
                    x=x, f1=f1, f2=f2)
    else:
        return f1.get_value()
```

#### Output

```
In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.multiobjective import test
```

```
In [8]: response = test(cas_conn, sols=True)
```

NOTE: Initialized model multiobjective.

NOTE: Added action set 'optimization'.

NOTE: Converting model multiobjective to OPTMODEL.

```
var x {{1,2}} >= 0 <= 5;
min f1 = (x[1] - 1) ^ (2) + (x[1] - x[2]) ^ (2);
min f2 = (x[1] - x[2]) ^ (2) + (x[2] - 3) ^ (2);
solve with blackbox obj (f1 f2) / logfreq=50;
create data solution from [i]= {1.._NVAR_} var=_VAR_.name value=_VAR_ lb=_VAR_.lb_
↳ub=_VAR_.ub rc=_VAR_.rc;
create data dual from [j] = {1.._NCON_} con=_CON_.name value=_CON_.body dual=_CON_.
↳dual;
create data allsols from [s]=(1.._NVAR_) name=_VAR_[s].name {j in 1.._NSOL_} <col(
↳'sol_'||j)=_VAR_[s].sol[j]>;
```

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 2 variables (0 free, 0 fixed).

NOTE: The problem has 0 linear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver removed 0 variables, 0 linear constraints, and 0\_

↳nonlinear constraints.

NOTE: The black-box solver is using up to 8 threads.

NOTE: The black-box solver is using the EAGLS optimizer algorithm.

NOTE: The problem has 2 variables (0 integer, 2 continuous).

NOTE: The problem has 0 constraints (0 linear, 0 nonlinear).

NOTE: The problem has 2 user-defined functions.

NOTE: The deterministic parallel mode is enabled.

Iteration	Nondom	Progress	Infeasibility	Evals	Time
1	4	.	0	84	0
51	877	0.0000811	0	2876	0
101	1654	0.0000123	0	5576	1
151	2290	0.000003230545	0	8181	2
201	2874	0.0000182	0	10796	3
251	3422	0.000003148003	0	13447	4
301	3847	0.000001559509	0	16046	5
351	4282	0.000001159917	0	18733	7
401	4712	0.000002423148	0	21315	9
428	4932	0.000000704951	0	22734	10

NOTE: Function convergence criteria reached.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 2 rows and 6\_

↳columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 0 rows and 4 columns.

NOTE: The output table 'ALLSOLS' in caslib 'CASUSER(casuser)' has 2 rows and 4934\_

↳columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 14 rows and 4\_

↳columns.

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4\_

↳columns.

f1 0.01497094056129493

f2 4.721632618656377

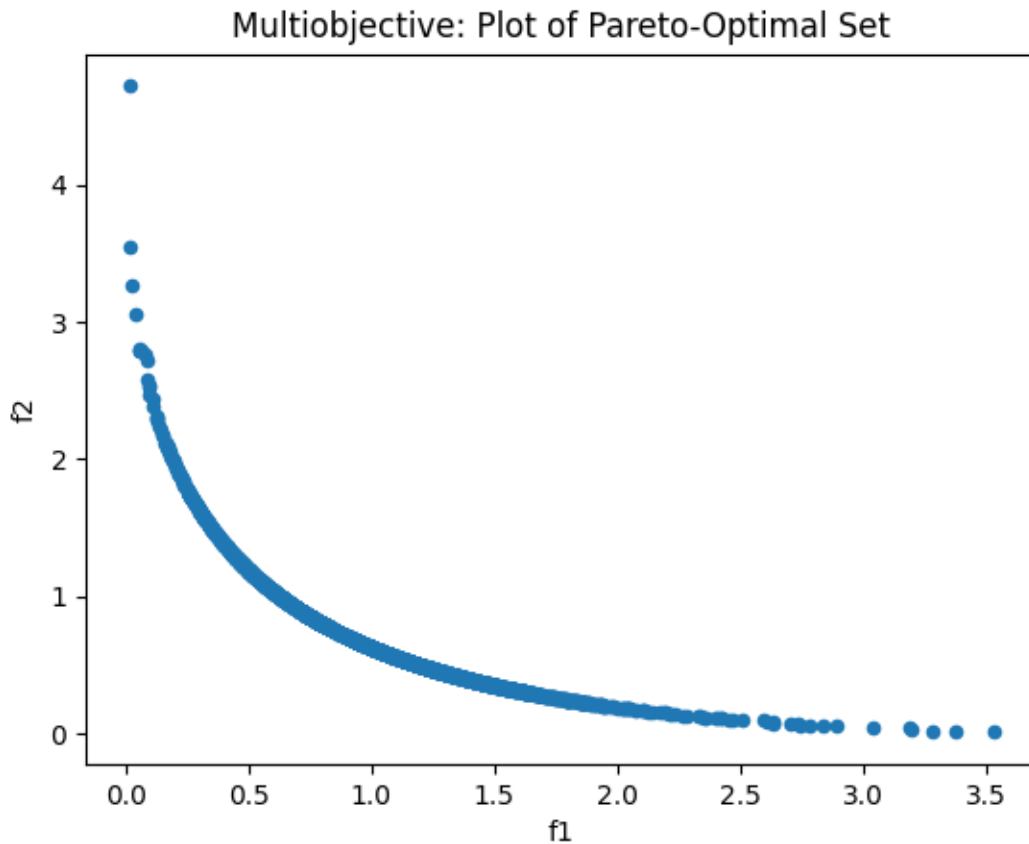
```
In [9]: import matplotlib.pyplot as plt
```

```
In [10]: sols = response['solutions']
```

(continues on next page)

(continued from previous page)

```
In [11]: x = response['x']
In [12]: f1 = response['f1']
In [13]: f2 = response['f2']
In [14]: tr = sols.transpose()
In [15]: scvalues = tr.iloc[2:]
In [16]: scvalues = scvalues.astype({0: float, 1: float})
In [17]: x[1].set_value(scvalues[0])
In [18]: x[2].set_value(scvalues[1])
In [19]: scvalues['f1'] = f1.get_value()
In [20]: scvalues['f2'] = f2.get_value()
In [21]: f = scvalues.plot.scatter(x='f1', y='f2')
In [22]: f.set_title('Multiobjective: Plot of Pareto-Optimal Set');
In [23]: f
Out[23]: <matplotlib.axes._subplots.AxesSubplot at 0x7faab2d6cf98>
```



#### 4.1.14 Least Squares

##### Reference

SAS/OR example: [https://go.documentation.sas.com/?docsetId=ormpug&docsetTarget=ormpug\\_nlpsolver\\_gettingstarted05.htm&docsetVersion=15.1&locale=en](https://go.documentation.sas.com/?docsetId=ormpug&docsetTarget=ormpug_nlpsolver_gettingstarted05.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [https://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/nlpsg01.html](https://support.sas.com/documentation/onlinedoc/or/ex_code/151/nlpsg01.html)

##### Model

```
import sasoptpy as so
import pandas as pd

def test(cas_conn, data=None):

    # Use default data if not passed
    if data is None:
        data = pd.DataFrame([
            [4, 8, 43.71],
            [62, 5, 351.29],
```

(continues on next page)

(continued from previous page)

```

        [81, 62, 2878.91],
        [85, 75, 3591.59],
        [65, 54, 2058.71],
        [96, 84, 4487.87],
        [98, 29, 1773.52],
        [36, 33, 767.57],
        [30, 91, 1637.66],
        [3, 59, 215.28],
        [62, 57, 2067.42],
        [11, 48, 394.11],
        [66, 21, 932.84],
        [68, 24, 1069.21],
        [95, 30, 1770.78],
        [34, 14, 368.51],
        [86, 81, 3902.27],
        [37, 49, 1115.67],
        [46, 80, 2136.92],
        [87, 72, 3537.84],
    ], columns=['x1', 'x2', 'y'])

m = so.Model(name='least_squares', session=cas_conn)

# Regression model:  $L(a,b,c) = a * x1 + b * x2 + c * x1 * x2$ 
a = m.add_variable(name='a')
b = m.add_variable(name='b')
c = m.add_variable(name='c')

x1 = data['x1']
x2 = data['x2']
y = data['y']

err = m.add_implicit_variable((
    y[i] - (a * x1[i] + b * x2[i] + c * x1[i] * x2[i]) for i in data.index
), name='error')
m.set_objective(so.expr_sum(err[i]**2 for i in data.index),
                sense=so.MIN,
                name='total_error')
m.solve(verbose=True, options={'with': 'nlp'})
return m.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

```



```
In [7]: from examples.client_side.least_squares import test
```

```
In [8]: test(cas_conn)
```

NOTE: Initialized model least\_squares.

NOTE: Added action set 'optimization'.

NOTE: Converting model least\_squares to OPTMODEL.

```
var a;
var b;
var c;
impvar error_0 = - 4 * a - 8 * b - 32 * c + 43.71;
impvar error_1 = - 62 * a - 5 * b - 310 * c + 351.29;
impvar error_2 = - 81 * a - 62 * b - 5022 * c + 2878.91;
impvar error_3 = - 85 * a - 75 * b - 6375 * c + 3591.59;
impvar error_4 = - 65 * a - 54 * b - 3510 * c + 2058.71;
impvar error_5 = - 96 * a - 84 * b - 8064 * c + 4487.87;
impvar error_6 = - 98 * a - 29 * b - 2842 * c + 1773.52;
impvar error_7 = - 36 * a - 33 * b - 1188 * c + 767.57;
impvar error_8 = - 30 * a - 91 * b - 2730 * c + 1637.66;
impvar error_9 = - 3 * a - 59 * b - 177 * c + 215.28;
impvar error_10 = - 62 * a - 57 * b - 3534 * c + 2067.42;
impvar error_11 = - 11 * a - 48 * b - 528 * c + 394.11;
impvar error_12 = - 66 * a - 21 * b - 1386 * c + 932.84;
impvar error_13 = - 68 * a - 24 * b - 1632 * c + 1069.21;
impvar error_14 = - 95 * a - 30 * b - 2850 * c + 1770.78;
impvar error_15 = - 34 * a - 14 * b - 476 * c + 368.51;
impvar error_16 = - 86 * a - 81 * b - 6966 * c + 3902.27;
impvar error_17 = - 37 * a - 49 * b - 1813 * c + 1115.67;
impvar error_18 = - 46 * a - 80 * b - 3680 * c + 2136.92;
impvar error_19 = - 87 * a - 72 * b - 6264 * c + 3537.84;
min total_error = (- 4 * a - 8 * b - 32 * c + 43.71) ^ (2) + (- 62 * a - 5 * b -
↳ 310 * c + 351.29) ^ (2) + (- 81 * a - 62 * b - 5022 * c + 2878.91) ^ (2) + (- 85 *
↳ a - 75 * b - 6375 * c + 3591.59) ^ (2) + (- 65 * a - 54 * b - 3510 * c + 2058.71) ^
↳ (2) + (- 96 * a - 84 * b - 8064 * c + 4487.87) ^ (2) + (- 98 * a - 29 * b - 2842 *
↳ c + 1773.52) ^ (2) + (- 36 * a - 33 * b - 1188 * c + 767.57) ^ (2) + (- 30 * a - 91
↳ * b - 2730 * c + 1637.66) ^ (2) + (- 3 * a - 59 * b - 177 * c + 215.28) ^ (2) + (-
↳ 62 * a - 57 * b - 3534 * c + 2067.42) ^ (2) + (- 11 * a - 48 * b - 528 * c + 394.
↳ 11) ^ (2) + (- 66 * a - 21 * b - 1386 * c + 932.84) ^ (2) + (- 68 * a - 24 * b -
↳ 1632 * c + 1069.21) ^ (2) + (- 95 * a - 30 * b - 2850 * c + 1770.78) ^ (2) + (- 34
↳ * a - 14 * b - 476 * c + 368.51) ^ (2) + (- 86 * a - 81 * b - 6966 * c + 3902.27) ^
↳ (2) + (- 37 * a - 49 * b - 1813 * c + 1115.67) ^ (2) + (- 46 * a - 80 * b - 3680 *
↳ c + 2136.92) ^ (2) + (- 87 * a - 72 * b - 6264 * c + 3537.84) ^ (2);
solve with nlp / ;
create data solution from [i]= {1..NVAR} var=_VAR_.name value=_VAR_.lb _VAR_.ub
↳ _VAR_.ub rc=_VAR_.rc;
create data dual from [j] = {1..NCON} con=_CON_.name value=_CON_.body dual=_CON_.
↳ dual;
```

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 3 variables (3 free, 0 fixed).

NOTE: The problem has 0 linear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver removed 0 variables, 0 linear constraints, and 0
↳ nonlinear constraints.

NOTE: Using analytic derivatives for objective.

NOTE: The NLP solver is called.

NOTE: The Interior Point Direct algorithm is used.

(continues on next page)

(continued from previous page)

Iter	Objective Value	Infeasibility	Optimality Error
0	95424613	0	3.48646173
1	7.18629678	0	0.000000055789

NOTE: Optimal.  
 NOTE: Objective = 7.1862967833.  
 NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 3 rows and 6 columns.  
 NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 0 rows and 4 columns.  
 NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4 columns.  
 NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4 columns.  
**Out [8]:** 7.186296783293

## Workspace Examples

### 4.1.15 Efficiency Analysis

#### Reference

SAS/OR example: [https://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex22\\_toc.htm&docsetVersion=15.1&locale=en](https://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex22_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex22.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex22.html)

#### Model

```
import sasoptpy as so
import pandas as pd
from sasoptpy.util import iterate, concat
from sasoptpy.actions import (
    read_data, create_data, cofor_loop, for_loop, solve, if_condition, diff,
    print_item, inline_condition)

def test(cas_conn, get_tables=False):

    input_list = pd.DataFrame(
        ['staff', 'showroom', 'pop1', 'pop2', 'alpha_enq', 'beta_enq'],
        columns=['input'])
    input_data = cas_conn.upload_frame(
        data=input_list, casout={'name': 'input_data', 'replace': True})

    output_list = pd.DataFrame(
        ['alpha_sales', 'beta_sales', 'profit'], columns=['output'])
    output_data = cas_conn.upload_frame(
        data=output_list, casout={'name': 'output_data', 'replace': True})

    problem_data = pd.DataFrame([
        ['Winchester', 7, 8, 10, 12, 8.5, 4, 2, 0.6, 1.5],
        ['Andover', 6, 6, 20, 30, 9, 4.5, 2.3, 0.7, 1.6],
        ['Basingstoke', 2, 3, 40, 40, 2, 1.5, 0.8, 0.25, 0.5],
        ['Poole', 14, 9, 20, 25, 10, 6, 2.6, 0.86, 1.9],
```

(continues on next page)

(continued from previous page)

```

['Woking', 10, 9, 10, 10, 11, 5, 2.4, 1, 2],
['Newbury', 24, 15, 15, 13, 25, 19, 8, 2.6, 4.5],
['Portsmouth', 6, 7, 50, 40, 8.5, 3, 2.5, 0.9, 1.6],
['Alresford', 8, 7.5, 5, 8, 9, 4, 2.1, 0.85, 2],
['Salisbury', 5, 5, 10, 10, 5, 2.5, 2, 0.65, 0.9],
['Guildford', 8, 10, 30, 35, 9.5, 4.5, 2.05, 0.75, 1.7],
['Alton', 7, 8, 7, 8, 3, 2, 1.9, 0.7, 0.5],
['Weybridge', 5, 6.5, 9, 12, 8, 4.5, 1.8, 0.63, 1.4],
['Dorchester', 6, 7.5, 10, 10, 7.5, 4, 1.5, 0.45, 1.45],
['Bridport', 11, 8, 8, 10, 10, 6, 2.2, 0.65, 2.2],
['Weymouth', 4, 5, 10, 10, 7.5, 3.5, 1.8, 0.62, 1.6],
['Portland', 3, 3.5, 3, 2, 2, 1.5, 0.9, 0.35, 0.5],
['Chichester', 5, 5.5, 8, 10, 7, 3.5, 1.2, 0.45, 1.3],
['Petersfield', 21, 12, 6, 8, 15, 8, 6, 0.25, 2.9],
['Petworth', 6, 5.5, 2, 2, 8, 5, 1.5, 0.55, 1.55],
['Midhurst', 3, 3.6, 3, 3, 2.5, 1.5, 0.8, 0.2, 0.45],
['Reading', 30, 29, 120, 80, 35, 20, 7, 2.5, 8],
['Southampton', 25, 16, 110, 80, 27, 12, 6.5, 3.5, 5.4],
['Bournemouth', 19, 10, 90, 12, 25, 13, 5.5, 3.1, 4.5],
['Henley', 7, 6, 5, 7, 8.5, 4.5, 1.2, 0.48, 2],
['Maidenhead', 12, 8, 7, 10, 12, 7, 4.5, 2, 2.3],
['Fareham', 4, 6, 1, 1, 7.5, 3.5, 1.1, 0.48, 1.7],
['Romsey', 2, 2.5, 1, 1, 2.5, 1, 0.4, 0.1, 0.55],
['Ringwood', 2, 3.5, 2, 2, 1.9, 1.2, 0.3, 0.09, 0.4],
], columns=['garage_name', 'staff', 'showroom', 'pop1', 'pop2', 'alpha_enq',
            'beta_enq', 'alpha_sales', 'beta_sales', 'profit'])
garage_data = cas_conn.upload_frame(
    data=problem_data, casout={'name': 'garage_data', 'replace': True})

with so.Workspace(name='efficiency_analysis', session=cas_conn) as w:
    inputs = so.Set(name='INPUTS', settype=so.string)
    read_data(table=input_data, index={'target': inputs, 'key': 'input'})

    outputs = so.Set(name='OUTPUTS', settype=so.string)
    read_data(table=output_data, index={'target': outputs, 'key': 'output'})

    garages = so.Set(name='GARAGES', settype=so.number)
    garage_name = so.ParameterGroup(garages, name='garage_name', ptype=so.string)
    input = so.ParameterGroup(inputs, garages, name='input')
    output = so.ParameterGroup(outputs, garages, name='output')
    r = read_data(table=garage_data, index={'target': garages, 'key': so.N},
                  columns=[garage_name])
    with iterate(inputs, 'i') as i:
        r.append({'index': i, 'target': input[i, so.N], 'column': i})
    with iterate(outputs, 'i') as i:
        r.append({'index': i, 'target': output[i, so.N], 'column': i})

    k = so.Parameter(name='k', ptype=so.number)
    efficiency_number = so.ParameterGroup(garages, name='efficiency_number')
    weight_sol = so.ParameterGroup(garages, garages, name='weight_sol')

    weight = so.VariableGroup(garages, name='Weight', lb=0)
    inefficiency = so.Variable(name='Inefficiency', lb=0)

    obj = so.Objective(inefficiency, name='Objective', sense=so.maximize)

    input_con = so.ConstraintGroup(

```

(continues on next page)

(continued from previous page)

```

        (so.expr_sum(input[i, j] * weight[j] for j in garages) <= input[i, k]
         for i in inputs), name='input_con')
    output_con = so.ConstraintGroup(
        (so.expr_sum(output[i, j] * weight[j] for j in garages) >= output[i, k] *
         ↪ inefficiency
         for i in outputs), name='output_con')

    for kk in cofor_loop(garages):
        k.set_value(kk)
        solve()
        efficiency_number[k] = 1 / inefficiency.sol
        for j in for_loop(garages):
            def if_block():
                weight_sol[k, j] = weight[j].sol
            def else_block():
                weight_sol[k, j] = None
            if_condition(weight[j].sol > 1e-6, if_block, else_block)

    efficient_garages = so.Set(
        name='EFFICIENT_GARAGES',
        value=[j.sym for j in garages if j.sym.under_condition(efficiency_
         ↪ number[j] >= 1)])
    inefficient_garages = so.Set(value=diff(garages, efficient_garages), name=
         ↪ 'INEFFICIENT_GARAGES')

    p1 = print_item(garage_name, efficiency_number)
    ed = create_data(table='efficiency_data', index={'key': ['garage']}, columns=[
        garage_name, efficiency_number
    ])
    with iterate(inefficient_garages, 'inefficient_garage') as i:
        wd = create_data(table='weight_data_dense',
                        index={'key': [i], 'set': [i.get_set()]},
                        columns=[garage_name, efficiency_number])
        with iterate(efficient_garages, 'efficient_garage') as j:
            wd.append({
                'name': concat('w', j),
                'expression': weight_sol[i, j],
                'index': j
            })

    filtered_set = so.InlineSet(
        lambda: ((g1, g2)
                 for g1 in inefficient_garages
                 for g2 in efficient_garages
                 if inline_condition(weight_sol[g1, g2] != None)))
    wds = create_data(table='weight_data_sparse',
                    index={'key': ['i', 'j'], 'set': [filtered_set]},
                    columns=[weight_sol])

    print(w.to_optmodel())
    w.submit()

    print('Print Table:')
    print(p1.get_response())

    print('Efficiency Data:')
    print(ed.get_response())

```

(continues on next page)

(continued from previous page)

```

print('Weight Data (Dense):')
print(wd.get_response())

print('Weight Data (Sparse):')
print(wds.get_response())

if get_tables:
    return obj.get_value(), ed.get_response()
else:
    return obj.get_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.server_side. efficiency_analysis import test

```

```

In [8]: test(cas_conn)
NOTE: Cloud Analytic Services made the uploaded file available as table INPUT_DATA in
↳caslib CASUSER(casuser).
NOTE: The table INPUT_DATA has been created in caslib CASUSER(casuser) from binary
↳data uploaded to Cloud Analytic Services.
NOTE: Cloud Analytic Services made the uploaded file available as table OUTPUT_DATA
↳in caslib CASUSER(casuser).
NOTE: The table OUTPUT_DATA has been created in caslib CASUSER(casuser) from binary
↳data uploaded to Cloud Analytic Services.
NOTE: Cloud Analytic Services made the uploaded file available as table GARAGE_DATA
↳in caslib CASUSER(casuser).
NOTE: The table GARAGE_DATA has been created in caslib CASUSER(casuser) from binary
↳data uploaded to Cloud Analytic Services.
proc optmodel;
    set <str> INPUTS;
    read data INPUT_DATA into INPUTS=[input] ;
    set <str> OUTPUTS;
    read data OUTPUT_DATA into OUTPUTS=[output] ;
    set GARAGES;
    str garage_name {GARAGES};
    num input {INPUTS, GARAGES};
    num output {OUTPUTS, GARAGES};
    read data GARAGE_DATA into GARAGES=[_N_] garage_name {i in INPUTS} < input[i, _N_]
↳]=col(i) > {i in OUTPUTS} < output[i, _N_]=col(i) >;
    num k;
    num efficiency_number {GARAGES};

```

(continues on next page)

(continued from previous page)

```

num weight_sol {GARAGES, GARAGES};
var Weight {{GARAGES}} >= 0;
var Inefficiency >= 0;
max Objective = Inefficiency;
con input_con {o21 in INPUTS} : input[o21, k] - (sum {j in GARAGES} (input[o21, j]_
↳ * Weight[j])) >= 0;
con output_con {o33 in OUTPUTS} : sum {j in GARAGES} (output[o33, j] * Weight[j]) -
↳ output[o33, k] * Inefficiency >= 0;
cofor {o46 in GARAGES} do;
    k = o46;
    solve;
    efficiency_number[k] = (1) / (Inefficiency.sol);
    for {o58 in GARAGES} do;
        if Weight[o58].sol > 1e-06 then do;
            weight_sol[k, o58] = Weight[o58].sol;
        end;
        else do;
            weight_sol[k, o58] = .;
        end;
    end;
end;
end;
set EFFICIENT_GARAGES = {{o69 in GARAGES: efficiency_number[o69] >= 1}};
set INEFFICIENT_GARAGES = GARAGES diff EFFICIENT_GARAGES;
print garage_name efficiency_number;
create data efficiency_data from [garage] garage_name efficiency_number;
create data weight_data_dense from [inefficient_garage] = {{INEFFICIENT_GARAGES}}_
↳ garage_name efficiency_number {efficient_garage in EFFICIENT_GARAGES} < col('w' ||_
↳ efficient_garage)=(weight_sol[inefficient_garage, efficient_garage]) >;
create data weight_data_sparse from [i j] = {{o83 in INEFFICIENT_GARAGES, o85 in_
↳ EFFICIENT_GARAGES: weight_sol[o83, o85] ne .}} weight_sol;
quit;
NOTE: Added action set 'optimization'.
NOTE: There were 6 rows read from table 'INPUT_DATA' in caslib 'CASUSER(casuser)'.
NOTE: There were 3 rows read from table 'OUTPUT_DATA' in caslib 'CASUSER(casuser)'.
NOTE: There were 28 rows read from table 'GARAGE_DATA' in caslib 'CASUSER(casuser)'.
NOTE: The COFOR statement is executing in single-machine mode.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↳ coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
	Phase Iteration	Value	Time
	D 2	1	2.788571E+01
	P 2	6	1.000000E+00

```

NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.

```

(continues on next page)

(continued from previous page)

```

NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
	Phase Iteration	Value	Time
	D 2	1	6.185408E+01
	P 2	6	1.000000E+00

```

NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 6 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
	Phase Iteration	Value	Time
	D 2	1	6.669507E+01
	P 2	15	1.152977E+00

```

NOTE: Optimal.
NOTE: Objective = 1.1529771581.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
--	--	-----------	--

(continues on next page)

(continued from previous page)

Phase	Iteration	Value	Time	
D	2	1	6.771196E+01	0
P	2	5	1.000000E+00	0

NOTE: Optimal.  
NOTE: Objective = 1.  
NOTE: The Dual Simplex solve time is 0.01 seconds.  
NOTE: Problem generation will use 7 threads.  
NOTE: The problem has 29 variables (0 free, 0 fixed).  
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
NOTE: The problem has 255 linear constraint coefficients.  
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
NOTE: The OPTMODEL presolver is disabled for linear problems.  
NOTE: The LP presolver value AUTOMATIC is applied.  
NOTE: The LP presolver time is 0.00 seconds.  
NOTE: The LP presolver removed 0 variables and 0 constraints.  
NOTE: The LP presolver removed 0 constraint coefficients.  
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
↪coefficients.  
NOTE: The LP solver is called.  
NOTE: The Dual Simplex algorithm is used.

Phase	Iteration	Objective Value	Time	
D	2	1	9.367804E+01	0
P	2	18	1.191606E+00	0

NOTE: Optimal.  
NOTE: Objective = 1.1916056975.  
NOTE: The Dual Simplex solve time is 0.01 seconds.  
NOTE: Problem generation will use 7 threads.  
NOTE: The problem has 29 variables (0 free, 0 fixed).  
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
NOTE: The problem has 255 linear constraint coefficients.  
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
NOTE: The OPTMODEL presolver is disabled for linear problems.  
NOTE: The LP presolver value AUTOMATIC is applied.  
NOTE: The LP presolver time is 0.00 seconds.  
NOTE: The LP presolver removed 0 variables and 0 constraints.  
NOTE: The LP presolver removed 0 constraint coefficients.  
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
↪coefficients.  
NOTE: The LP solver is called.  
NOTE: The Dual Simplex algorithm is used.

Phase	Iteration	Objective Value	Time	
D	2	1	6.282477E+01	0
P	2	7	1.000000E+00	0

NOTE: Optimal.  
NOTE: Objective = 1.  
NOTE: The Dual Simplex solve time is 0.01 seconds.  
NOTE: Problem generation will use 7 threads.  
NOTE: The problem has 29 variables (0 free, 0 fixed).  
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
NOTE: The problem has 255 linear constraint coefficients.  
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
NOTE: The OPTMODEL presolver is disabled for linear problems.  
NOTE: The LP presolver value AUTOMATIC is applied.  
NOTE: The LP presolver time is 0.00 seconds.  
NOTE: The LP presolver removed 0 variables and 0 constraints.

(continues on next page)



(continued from previous page)

NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_↵  
 ↵coefficients.  
 NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

	Phase	Iteration	Objective Value	Time	
	D	2	1	2.113425E+02	0
	P	2	7	1.141723E+00	0

NOTE: Optimal.  
 NOTE: Objective = 1.141723356.  
 NOTE: The Dual Simplex solve time is 0.01 seconds.  
 NOTE: Problem generation will use 6 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_↵  
 ↵coefficients.  
 NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

	Phase	Iteration	Objective Value	Time	
	D	2	1	8.984164E+01	0
	P	2	20	1.190229E+00	0

NOTE: Optimal.  
 NOTE: Objective = 1.1902294108.  
 NOTE: The Dual Simplex solve time is 0.01 seconds.  
 NOTE: Problem generation will use 8 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_↵  
 ↵coefficients.  
 NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

	Phase	Iteration	Objective Value	Time	
	D	2	1	7.496160E+01	0
	P	2	7	1.000000E+00	0

NOTE: Optimal.  
 NOTE: Objective = 1.  
 NOTE: The Dual Simplex solve time is 0.01 seconds.  
 NOTE: Problem generation will use 7 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).

(continues on next page)

(continued from previous page)

NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
 ↪coefficients.

NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

		Objective	
	Phase Iteration	Value	Time
	D 2	1	6.137365E+01
	P 2	9	1.011903E+00

NOTE: Optimal.  
 NOTE: Objective = 1.0119030842.  
 NOTE: The Dual Simplex solve time is 0.01 seconds.  
 NOTE: Problem generation will use 7 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
 ↪coefficients.

NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

		Objective	
	Phase Iteration	Value	Time
	D 2	1	5.430205E+01
	P 2	18	1.018276E+00

NOTE: Optimal.  
 NOTE: Objective = 1.0182756046.  
 NOTE: The Dual Simplex solve time is 0.01 seconds.  
 NOTE: Problem generation will use 7 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
 ↪coefficients.

NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

		Objective	
	Phase Iteration	Value	Time
	D 2	1	9.121193E+01
	P 2	17	1.170487E+00

(continues on next page)

(continued from previous page)

```

NOTE: Optimal.
NOTE: Objective = 1.170487106.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
Phase	Iteration	Value	Time
D 2	1	7.130206E+01	0
P 2	12	1.000000E+00	0

```

NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
Phase	Iteration	Value	Time
D 2	1	7.942787E+01	0
P 2	15	1.090062E+00	0

```

NOTE: Optimal.
NOTE: Objective = 1.0900621118.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.

```

(continues on next page)

(continued from previous page)

```

NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      3.333800E+01      0
      P 2          8      1.000000E+00      0
NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
      ↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      3.269636E+01      0
      P 2          5      1.000000E+00      0
NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
      ↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      1.483009E+02      0
      P 2         12      1.000000E+00      0
NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.

```

(continues on next page)

(continued from previous page)

```

NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      7.522880E+01      0
      P 2          9      1.000000E+00      0
NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      8.552410E+01      0
      P 2         14      1.160239E+00      0
NOTE: Optimal.
NOTE: Objective = 1.1602389558.
NOTE: The Dual Simplex solve time is 0.00 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
      Phase Iteration      Value      Time
      D 2          1      6.743350E+01      0
      P 2         20      1.029858E+00      0
NOTE: Optimal.
NOTE: Objective = 1.0298577511.
NOTE: The Dual Simplex solve time is 0.01 seconds.

```

(continues on next page)

(continued from previous page)

```

NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
	Phase Iteration	Value	Time
	D 2	1	1.119904E+02
	P 2	6	1.000000E+00

```

NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
	Phase Iteration	Value	Time
	D 2	1	3.162476E+01
	P 2	5	1.000000E+00

```

NOTE: Optimal.
NOTE: Objective = 1.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: Problem generation will use 7 threads.
NOTE: The problem has 29 variables (0 free, 0 fixed).
NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).
NOTE: The problem has 255 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint_
↪coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.

```

		Objective	
--	--	-----------	--

(continues on next page)

(continued from previous page)

Phase	Iteration	Value	Time	
D	2	1	1.462372E+02	0
P	2	9	1.205868E+00	0

NOTE: Optimal.  
 NOTE: Objective = 1.2058683067.  
 NOTE: The Dual Simplex solve time is 0.00 seconds.  
 NOTE: Problem generation will use 7 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
 ↪coefficients.  
 NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

Phase	Iteration	Objective Value	Time	
D	2	1	9.913941E+01	0
P	2	16	1.228251E+00	0

NOTE: Optimal.  
 NOTE: Objective = 1.2282514234.  
 NOTE: The Dual Simplex solve time is 0.00 seconds.  
 NOTE: Problem generation will use 7 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.  
 NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_  
 ↪coefficients.  
 NOTE: The LP solver is called.  
 NOTE: The Dual Simplex algorithm is used.

Phase	Iteration	Objective Value	Time	
D	2	1	1.428026E+02	0
P	2	5	1.000000E+00	0

NOTE: Optimal.  
 NOTE: Objective = 1.  
 NOTE: The Dual Simplex solve time is 0.01 seconds.  
 NOTE: Problem generation will use 7 threads.  
 NOTE: The problem has 29 variables (0 free, 0 fixed).  
 NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).  
 NOTE: The problem has 255 linear constraint coefficients.  
 NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
 NOTE: The OPTMODEL presolver is disabled for linear problems.  
 NOTE: The LP presolver value AUTOMATIC is applied.  
 NOTE: The LP presolver time is 0.00 seconds.  
 NOTE: The LP presolver removed 0 variables and 0 constraints.

(continues on next page)

(continued from previous page)

NOTE: The LP presolver removed 0 constraint coefficients.  
 NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_↵  
 ↵coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

		Objective		
Phase	Iteration	Value		Time
D 2	1	9.575369E+01		0
P 2	16	1.213087E+00		0

NOTE: Optimal.

NOTE: Objective = 1.2130872456.

NOTE: The Dual Simplex solve time is 0.00 seconds.

NOTE: Problem generation will use 7 threads.

NOTE: The problem has 29 variables (0 free, 0 fixed).

NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).

NOTE: The problem has 255 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver is disabled for linear problems.

NOTE: The LP presolver value AUTOMATIC is applied.

NOTE: The LP presolver time is 0.00 seconds.

NOTE: The LP presolver removed 0 variables and 0 constraints.

NOTE: The LP presolver removed 0 constraint coefficients.

NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_↵  
 ↵coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

		Objective		
Phase	Iteration	Value		Time
D 2	1	3.928295E+01		0
P 2	7	1.000000E+00		0

NOTE: Optimal.

NOTE: Objective = 1.

NOTE: The Dual Simplex solve time is 0.01 seconds.

NOTE: Problem generation will use 7 threads.

NOTE: The problem has 29 variables (0 free, 0 fixed).

NOTE: The problem has 9 linear constraints (0 LE, 0 EQ, 9 GE, 0 range).

NOTE: The problem has 255 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver is disabled for linear problems.

NOTE: The LP presolver value AUTOMATIC is applied.

NOTE: The LP presolver time is 0.00 seconds.

NOTE: The LP presolver removed 0 variables and 0 constraints.

NOTE: The LP presolver removed 0 constraint coefficients.

NOTE: The presolved problem has 29 variables, 9 constraints, and 255 constraint\_↵  
 ↵coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

		Objective		
Phase	Iteration	Value		Time
D 2	1	4.906079E+01		0
P 2	5	1.000000E+00		0

NOTE: Optimal.

NOTE: Objective = 1.

NOTE: The Dual Simplex solve time is 0.00 seconds.

NOTE: The output table 'EFFICIENCY\_DATA' in caslib 'CASUSER(casuser)' has 28 rows and\_↵  
 ↵3 columns.

NOTE: The output table 'WEIGHT\_DATA\_DENSE' in caslib 'CASUSER(casuser)' has 17 rows\_↵  
 ↵and 14 columns.

(continues on next page)



(continued from previous page)

NOTE: The output table 'WEIGHT\_DATA\_SPARSE' in caslib 'CASUSER(casuser)' has 43 rows and 3 columns.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 29 rows and 6 columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 9 rows and 4 columns.  
Print Table:

	COL1	garage_name	efficiency_number
0	1.0	Bournemouth	1.000000
1	2.0	Henley	1.000000
2	3.0	Woking	0.867320
3	4.0	Alton	1.000000
4	5.0	Dorchester	0.839204
5	6.0	Alresford	1.000000
6	7.0	Ringwood	0.875869
7	8.0	Winchester	0.840174
8	9.0	Weymouth	1.000000
9	10.0	Petworth	0.988237
10	11.0	Reading	0.982052
11	12.0	Weybridge	0.854345
12	13.0	Portsmouth	1.000000
13	14.0	Andover	0.917379
14	15.0	Newbury	1.000000
15	16.0	Maidenhead	1.000000
16	17.0	Basingstoke	1.000000
17	18.0	Salisbury	1.000000
18	19.0	Poole	0.861891
19	20.0	Bridport	0.971008
20	21.0	Portland	1.000000
21	22.0	Petersfield	1.000000
22	23.0	Midhurst	0.829278
23	24.0	Guildford	0.814166
24	25.0	Romsey	1.000000
25	26.0	Chichester	0.824343
26	27.0	Southampton	1.000000
27	28.0	Fareham	1.000000

Efficiency Data:

Selected Rows from Table EFFICIENCY\_DATA

	garage	garage_name	efficiency_number
0	1.0	Bournemouth	1.000000
1	2.0	Henley	1.000000
2	3.0	Woking	0.867320
3	4.0	Alton	1.000000
4	5.0	Dorchester	0.839204
5	6.0	Alresford	1.000000
6	7.0	Ringwood	0.875869
7	8.0	Winchester	0.840174
8	9.0	Weymouth	1.000000
9	10.0	Petworth	0.988237
10	11.0	Reading	0.982052
11	12.0	Weybridge	0.854345
12	13.0	Portsmouth	1.000000
13	14.0	Andover	0.917379
14	15.0	Newbury	1.000000
15	16.0	Maidenhead	1.000000
16	17.0	Basingstoke	1.000000
17	18.0	Salisbury	1.000000

(continues on next page)

(continued from previous page)

```

18 19.0 Poole 0.861891
19 20.0 Bridport 0.971008
20 21.0 Portland 1.000000
21 22.0 Petersfield 1.000000
22 23.0 Midhurst 0.829278
23 24.0 Guildford 0.814166
24 25.0 Romsey 1.000000
25 26.0 Chichester 0.824343
26 27.0 Southampton 1.000000
27 28.0 Fareham 1.000000

```

Weight Data (Dense):

Selected Rows from Table WEIGHT\_DATA\_DENSE

	inefficient_garage	garage_name	efficiency_number	...	w22	w25	w27
0	1.0	Bournemouth	1.000000	...	NaN	NaN	NaN
1	3.0	Woking	0.867320	...	NaN	NaN	0.009093
2	5.0	Dorchester	0.839204	...	NaN	NaN	NaN
3	7.0	Ringwood	0.875869	...	NaN	NaN	NaN
4	8.0	Winchester	0.840174	...	NaN	NaN	NaN
5	10.0	Petworth	0.988237	...	0.015212	NaN	NaN
6	11.0	Reading	0.982052	...	NaN	NaN	NaN
7	12.0	Weybridge	0.854345	...	NaN	NaN	NaN
8	13.0	Portsmouth	1.000000	...	NaN	NaN	NaN
9	14.0	Andover	0.917379	...	NaN	NaN	NaN
10	17.0	Basingstoke	1.000000	...	NaN	NaN	NaN
11	19.0	Poole	0.861891	...	NaN	NaN	NaN
12	20.0	Bridport	0.971008	...	NaN	NaN	NaN
13	23.0	Midhurst	0.829278	...	0.043482	NaN	NaN
14	24.0	Guildford	0.814166	...	NaN	NaN	NaN
15	26.0	Chichester	0.824343	...	NaN	NaN	NaN
16	28.0	Fareham	1.000000	...	NaN	NaN	NaN

[17 rows x 14 columns]

Weight Data (Sparse):

Selected Rows from Table WEIGHT\_DATA\_SPARSE

	i	j	weight_sol
0	5.0	2.0	0.035318
1	7.0	2.0	0.146485
2	11.0	2.0	2.862469
3	19.0	2.0	0.434419
4	20.0	2.0	0.783097
5	26.0	2.0	0.236367
6	3.0	4.0	0.021078
7	3.0	6.0	0.952525
8	5.0	6.0	0.104478
9	8.0	6.0	0.416268
10	24.0	6.0	0.622715
11	26.0	6.0	0.096820
12	5.0	9.0	0.119287
13	8.0	9.0	0.333333
14	11.0	9.0	0.544410
15	12.0	9.0	0.796562
16	14.0	9.0	0.857143
17	23.0	9.0	0.066511
18	24.0	9.0	0.191804
19	26.0	9.0	0.335428

(continues on next page)

(continued from previous page)

```

20 10.0 15.0 0.066345
21 3.0 16.0 0.148376
22 10.0 16.0 0.034089
23 11.0 16.0 0.137534
24 12.0 16.0 0.145236
25 14.0 16.0 0.214286
26 19.0 16.0 0.344634
27 20.0 16.0 0.194894
28 23.0 16.0 0.008940
29 8.0 18.0 0.403284
30 23.0 18.0 0.059574
31 5.0 21.0 0.751632
32 7.0 21.0 0.319728
33 8.0 21.0 0.096138
34 11.0 21.0 1.199139
35 19.0 21.0 0.757330
36 20.0 21.0 0.469693
37 23.0 21.0 0.471893
38 24.0 21.0 0.168067
39 26.0 21.0 0.165227
40 10.0 22.0 0.015212
41 23.0 22.0 0.043482
42 3.0 27.0 0.009093
Out [8]: 1.0000000000000002

```

## 4.2 SAS Viya Examples (Abstract)

### 4.2.1 Curve Fitting

#### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex11\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex11_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex11.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex11.html)

#### Model

```

import sasoptpy as so
import pandas as pd

def test(cas_conn, sols=False):

    # Upload data to server first
    xy_raw = pd.DataFrame([
        [0.0, 1.0],
        [0.5, 0.9],
        [1.0, 0.7],
        [1.5, 1.5],
        [1.9, 2.0],
        [2.5, 2.4],

```

(continues on next page)

(continued from previous page)

```

[3.0, 3.2],
[3.5, 2.0],
[4.0, 2.7],
[4.5, 3.5],
[5.0, 1.0],
[5.5, 4.0],
[6.0, 3.6],
[6.6, 2.7],
[7.0, 5.7],
[7.6, 4.6],
[8.5, 6.0],
[9.0, 6.8],
[10.0, 7.3]
], columns=['x', 'y'])
xy_data = cas_conn.upload_frame(xy_raw, casout={'name': 'xy_data',
                                              'replace': True})

# Read observations
from sasoptpy.actions import read_data
POINTS = so.Set(name='POINTS')
x = so.ParameterGroup(POINTS, name='x')
y = so.ParameterGroup(POINTS, name='y')
read_st = read_data(
    table=xy_data,
    index={'target': POINTS, 'key': so.N},
    columns=[
        {'target': x, 'column': 'x'},
        {'target': y, 'column': 'y'}
    ]
)

# Parameters and variables
order = so.Parameter(name='order')
beta = so.VariableGroup(so.exp_range(0, order), name='beta')
estimate = so.ImplicitVar(
    (beta[0] + so.expr_sum(beta[k] * x[i] ** k
                           for k in so.exp_range(1, order))
     for i in POINTS), name='estimate')

surplus = so.VariableGroup(POINTS, name='surplus', lb=0)
slack = so.VariableGroup(POINTS, name='slack', lb=0)

objective1 = so.Expression(
    so.expr_sum(surplus[i] + slack[i] for i in POINTS), name='objective1')
abs_dev_con = so.ConstraintGroup(
    (estimate[i] - surplus[i] + slack[i] == y[i] for i in POINTS),
    name='abs_dev_con')

minmax = so.Variable(name='minmax')
objective2 = so.Expression(minmax + 0.0, name='objective2')
minmax_con = so.ConstraintGroup(
    (minmax >= surplus[i] + slack[i] for i in POINTS), name='minmax_con')

order.set_init(1)
L1 = so.Model(name='L1', session=cas_conn)
L1.set_objective(objective1, sense=so.MIN, name='L1obj')
L1.include(POINTS, x, y, read_st)

```

(continues on next page)

(continued from previous page)

```

L1.include(order, beta, estimate, surplus, slack, abs_dev_con)
L1.add_postsolve_statement('print x y estimate surplus slack;')

L1.solve(verbose=True)
if sols:
    sol_data1 = L1.response['Print1.PrintTable'].sort_values('x')
    print(so.get_solution_table(beta))
    print(sol_data1.to_string())

Linf = so.Model(name='Linf', session=cas_conn)
Linf.include(L1, minmax, minmax_con)
Linf.set_objective(objective2, sense=so.MIN, name='Linfobj')

Linf.solve()
if sols:
    sol_data2 = Linf.response['Print1.PrintTable'].sort_values('x')
    print(so.get_solution_table(beta))
    print(sol_data2.to_string())

order.set_init(2)

L1.solve()
if sols:
    sol_data3 = L1.response['Print1.PrintTable'].sort_values('x')
    print(so.get_solution_table(beta))
    print(sol_data3.to_string())

Linf.solve()
if sols:
    sol_data4 = Linf.response['Print1.PrintTable'].sort_values('x')
    print(so.get_solution_table(beta))
    print(sol_data4.to_string())

if sols:
    return (sol_data1, sol_data2, sol_data3, sol_data4)
else:
    return Linf.get_objective_value()

```

## Output

```

In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.server_side.curve_fitting import test

```

(continues on next page)

(continued from previous page)

```
In [8]: (s1, s2, s3, s4) = test(cas_conn, sols=True)
NOTE: Cloud Analytic Services made the uploaded file available as table XY_DATA in
↳caslib CASUSER(casuser).
NOTE: The table XY_DATA has been created in caslib CASUSER(casuser) from binary data
↳uploaded to Cloud Analytic Services.
NOTE: Initialized model L1.
NOTE: Added action set 'optimization'.
NOTE: Converting model L1 to OPTMODEL.
    set POINTS;
    num x {POINTS};
    num y {POINTS};
    read data XY_DATA into POINTS=[_N_] x y;
    num order init 1;
    var beta {{0..order}};
    impvar estimate {o8 in POINTS} = beta[0] + sum {k in 1..order} (beta[k] * (x[o8]) ^
↳(k));
    var surplus {{POINTS}} >= 0;
    var slack {{POINTS}} >= 0;
    con abs_dev_con {o32 in POINTS} : y[o32] - estimate[o32] + surplus[o32] -
↳slack[o32] = 0;
    min L1obj = sum {i in POINTS} (surplus[i] + slack[i]);
    solve;
    create data solution from [i]= {1.._NVAR_} var=_VAR_.name value=_VAR_.lb=_VAR_.lb
↳ub=_VAR_.ub rc=_VAR_.rc;
    create data dual from [j] = {1.._NCON_} con=_CON_.name value=_CON_.body dual=_CON_.
↳dual;
    print x y estimate surplus slack;

NOTE: Submitting OPTMODEL code to CAS server.
NOTE: There were 19 rows read from table 'XY_DATA' in caslib 'CASUSER(casuser)'.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 40 variables (2 free, 0 fixed).
NOTE: The problem uses 19 implicit variables.
NOTE: The problem has 19 linear constraints (0 LE, 19 EQ, 0 GE, 0 range).
NOTE: The problem has 75 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 38 variables and 0 constraints.
NOTE: The LP presolver removed 38 constraint coefficients.
NOTE: The LP presolver formulated the dual of the problem.
NOTE: The presolved problem has 19 variables, 2 constraints, and 37 constraint
↳coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
```

		Objective	
Phase	Iteration	Value	Time
D 2	1	6.160000E+01	0
D 2	5	1.146625E+01	0

```
NOTE: Optimal.
NOTE: Objective = 11.46625.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 40 rows and 6
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 19 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4
↳columns.
```

(continues on next page)

(continued from previous page)

```

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4
↳columns.
      beta
0  0.58125
1  0.63750
      COL1      x      y estimate      surplus      slack
10  11.0      0.0      1.0  0.58125  0.000000e+00  0.41875
18  19.0      0.5      0.9  0.90000  5.551115e-17  0.00000
12  13.0      1.0      0.7  1.21875  5.187500e-01  0.00000
4   5.0      1.5      1.5  1.53750  3.750000e-02  0.00000
0   1.0      1.9      2.0  1.79250  0.000000e+00  0.20750
15  16.0      2.5      2.4  2.17500  0.000000e+00  0.22500
1   2.0      3.0      3.2  2.49375  0.000000e+00  0.70625
11  12.0      3.5      2.0  2.81250  8.125000e-01  0.00000
5   6.0      4.0      2.7  3.13125  4.312500e-01  0.00000
3   4.0      4.5      3.5  3.45000  0.000000e+00  0.05000
8   9.0      5.0      1.0  3.76875  2.768750e+00  0.00000
14  15.0      5.5      4.0  4.08750  8.750000e-02  0.00000
13  14.0      6.0      3.6  4.40625  8.062500e-01  0.00000
7   8.0      6.6      2.7  4.78875  2.088750e+00  0.00000
9   10.0      7.0      5.7  5.04375  0.000000e+00  0.65625
17  18.0      7.6      4.6  5.42625  8.262500e-01  0.00000
2   3.0      8.5      6.0  6.00000  0.000000e+00  0.00000
6   7.0      9.0      6.8  6.31875  0.000000e+00  0.48125
16  17.0     10.0      7.3  6.95625  0.000000e+00  0.34375
NOTE: Initialized model Linf.
NOTE: Added action set 'optimization'.
NOTE: Converting model Linf to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: There were 19 rows read from table 'XY_DATA' in caslib 'CASUSER(casuser)'.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 41 variables (3 free, 0 fixed).
NOTE: The problem uses 19 implicit variables.
NOTE: The problem has 38 linear constraints (0 LE, 19 EQ, 19 GE, 0 range).
NOTE: The problem has 132 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 0 variables and 0 constraints.
NOTE: The LP presolver removed 0 constraint coefficients.
NOTE: The presolved problem has 41 variables, 38 constraints, and 132 constraint
↳coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
Phase Iteration      Value      Time
D 2          1  -1.900000E+00      0
P 2         26   1.725000E+00      0
NOTE: Optimal.
NOTE: Objective = 1.725.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 41 rows and 6
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 38 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4
↳columns.

```

(continues on next page)

(continued from previous page)

```

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4_
↳columns.
    beta
0 -0.400
1 0.625
    COL1      x      y estimate  surplus  slack
10 11.0     0.0     1.0  -0.4000    0.000  1.4000
18 19.0     0.5     0.9  -0.0875    0.000  0.9875
12 13.0     1.0     0.7   0.2250    0.000  0.4750
4   5.0     1.5     1.5   0.5375    0.000  0.9625
0   1.0     1.9     2.0   0.7875    0.000  1.2125
15 16.0     2.5     2.4   1.1625    0.000  1.2375
1   2.0     3.0     3.2   1.4750    0.000  1.7250
11 12.0     3.5     2.0   1.7875    0.000  0.2125
5   6.0     4.0     2.7   2.1000    0.000  0.6000
3   4.0     4.5     3.5   2.4125    0.000  1.0875
8   9.0     5.0     1.0   2.7250    1.725  0.0000
14 15.0     5.5     4.0   3.0375    0.000  0.9625
13 14.0     6.0     3.6   3.3500    0.000  0.2500
7   8.0     6.6     2.7   3.7250    1.025  0.0000
9  10.0     7.0     5.7   3.9750    0.000  1.7250
17 18.0     7.6     4.6   4.3500    0.000  0.2500
2   3.0     8.5     6.0   4.9125    0.000  1.0875
6   7.0     9.0     6.8   5.2250    0.000  1.5750
16 17.0    10.0     7.3   5.8500    0.000  1.4500
NOTE: Added action set 'optimization'.
NOTE: Converting model L1 to OPTMODEL.
NOTE: Submitting OPTMODEL code to CAS server.
NOTE: There were 19 rows read from table 'XY_DATA' in caslib 'CASUSER(casuser)'.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 41 variables (3 free, 0 fixed).
NOTE: The problem uses 19 implicit variables.
NOTE: The problem has 19 linear constraints (0 LE, 19 EQ, 0 GE, 0 range).
NOTE: The problem has 93 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The LP presolver value AUTOMATIC is applied.
NOTE: The LP presolver time is 0.00 seconds.
NOTE: The LP presolver removed 38 variables and 0 constraints.
NOTE: The LP presolver removed 38 constraint coefficients.
NOTE: The LP presolver formulated the dual of the problem.
NOTE: The presolved problem has 19 variables, 3 constraints, and 55 constraint_
↳coefficients.
NOTE: The LP solver is called.
NOTE: The Dual Simplex algorithm is used.
      Objective
Phase Iteration      Value      Time
    D 2          1  6.160000E+01      0
    D 2          5  1.045896E+01      0
NOTE: Optimal.
NOTE: Objective = 10.458964706.
NOTE: The Dual Simplex solve time is 0.01 seconds.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 41 rows and 6_
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 19 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4_
↳columns.

```

(continues on next page)



(continued from previous page)

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4 columns.

```

      beta
0  0.982353
1  0.294510
2  0.033725

      COL1      x      y estimate      surplus      slack
10  11.0      0.0      1.0  0.982353  0.000000e+00  0.017647
18  19.0      0.5      0.9  1.138039  2.380392e-01  0.000000
12  13.0      1.0      0.7  1.310588  6.105882e-01  0.000000
4   5.0      1.5      1.5  1.500000 -6.938894e-17  0.000000
0   1.0      1.9      2.0  1.663671  0.000000e+00  0.336329
15  16.0      2.5      2.4  1.929412  0.000000e+00  0.470588
1   2.0      3.0      3.2  2.169412  0.000000e+00  1.030588
11  12.0      3.5      2.0  2.426275  4.262745e-01  0.000000
5   6.0      4.0      2.7  2.700000 -1.110223e-16  0.000000
3   4.0      4.5      3.5  2.990588  0.000000e+00  0.509412
8   9.0      5.0      1.0  3.298039  2.298039e+00  0.000000
14  15.0      5.5      4.0  3.622353  0.000000e+00  0.377647
13  14.0      6.0      3.6  3.963529  3.635294e-01  0.000000
7   8.0      6.6      2.7  4.395200  1.695200e+00  0.000000
9   10.0      7.0      5.7  4.696471  0.000000e+00  1.003529
17  18.0      7.6      4.6  5.168612  5.686118e-01  0.000000
2   3.0      8.5      6.0  5.922353  0.000000e+00  0.077647
6   7.0      9.0      6.8  6.364706  0.000000e+00  0.435294
16  17.0     10.0      7.3  7.300000  4.440892e-16  0.000000

```

NOTE: Added action set 'optimization'.

NOTE: Converting model Linf to OPTMODEL.

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: There were 19 rows read from table 'XY\_DATA' in caslib 'CASUSER(casuser)'.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 42 variables (4 free, 0 fixed).

NOTE: The problem uses 19 implicit variables.

NOTE: The problem has 38 linear constraints (0 LE, 19 EQ, 19 GE, 0 range).

NOTE: The problem has 150 linear constraint coefficients.

NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The OPTMODEL presolver is disabled for linear problems.

NOTE: The LP presolver value AUTOMATIC is applied.

NOTE: The LP presolver time is 0.00 seconds.

NOTE: The LP presolver removed 0 variables and 0 constraints.

NOTE: The LP presolver removed 0 constraint coefficients.

NOTE: The presolved problem has 42 variables, 38 constraints, and 150 constraint coefficients.

NOTE: The LP solver is called.

NOTE: The Dual Simplex algorithm is used.

		Objective	
Phase	Iteration	Value	Time
D 2	1	-1.900000E+00	0
P 2	29	1.475000E+00	0

NOTE: Optimal.

NOTE: Objective = 1.475.

NOTE: The Dual Simplex solve time is 0.01 seconds.

NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 42 rows and 6 columns.

NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 38 rows and 4 columns.

NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 13 rows and 4 columns.

(continues on next page)

(continued from previous page)

NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 18 rows and 4\_  
 ↪columns.

```

    beta
0  2.475
1 -0.625
2  0.125
    COL1      x      y estimate    surplus    slack
10  11.0    0.0    1.0   2.47500   1.475000   0.000000
18  19.0    0.5    0.9   2.19375   1.293750   0.000000
12  13.0    1.0    0.7   1.97500   1.275000   0.000000
 4   5.0    1.5    1.5   1.81875   0.318750   0.000000
0   1.0    1.9    2.0   1.73875   0.606875   0.868125
15  16.0    2.5    2.4   1.69375   0.000000   0.706250
 1   2.0    3.0    3.2   1.72500   0.000000   1.475000
11  12.0    3.5    2.0   1.81875   0.000000   0.181250
 5   6.0    4.0    2.7   1.97500   0.000000   0.725000
 3   4.0    4.5    3.5   2.19375   0.000000   1.306250
 8   9.0    5.0    1.0   2.47500   1.475000   0.000000
14  15.0    5.5    4.0   2.81875   0.000000   1.181250
13  14.0    6.0    3.6   3.22500   0.000000   0.375000
 7   8.0    6.6    2.7   3.79500   1.095000   0.000000
 9  10.0    7.0    5.7   4.22500   0.000000   1.475000
17  18.0    7.6    4.6   4.94500   0.345000   0.000000
 2   3.0    8.5    6.0   6.19375   0.193750   0.000000
 6   7.0    9.0    6.8   6.97500   0.175000   0.000000
16  17.0   10.0    7.3   8.72500   1.425000   0.000000

```

```

# Plots
In [1]: import matplotlib.pyplot as plt

In [2]: p1 = s1.plot.scatter(x='x', y='y', c='g')

In [3]: s1.plot.line(ax=p1, x='x', y='estimate', label='Line1');

In [4]: s2.plot.line(ax=p1, x='x', y='estimate', label='Line2');

In [5]: p1
Out[5]: <matplotlib.axes._subplots.AxesSubplot at 0x7faabb2ed438>

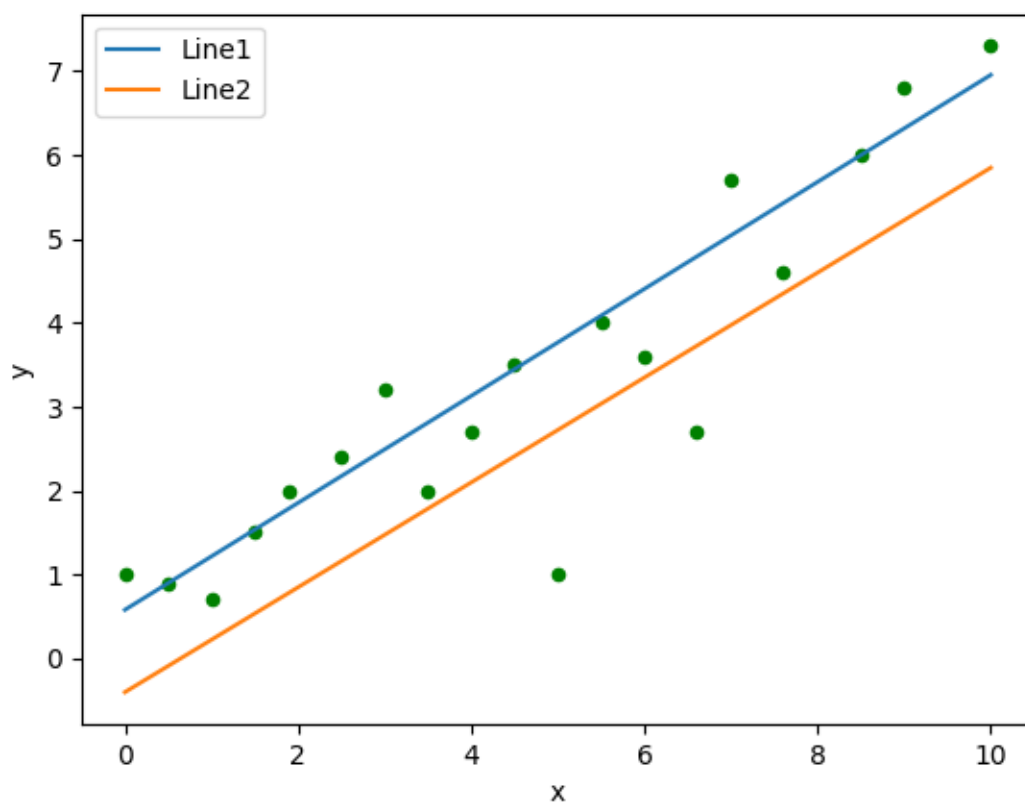
In [6]: p2 = s3.plot.scatter(x='x', y='y', c='g')

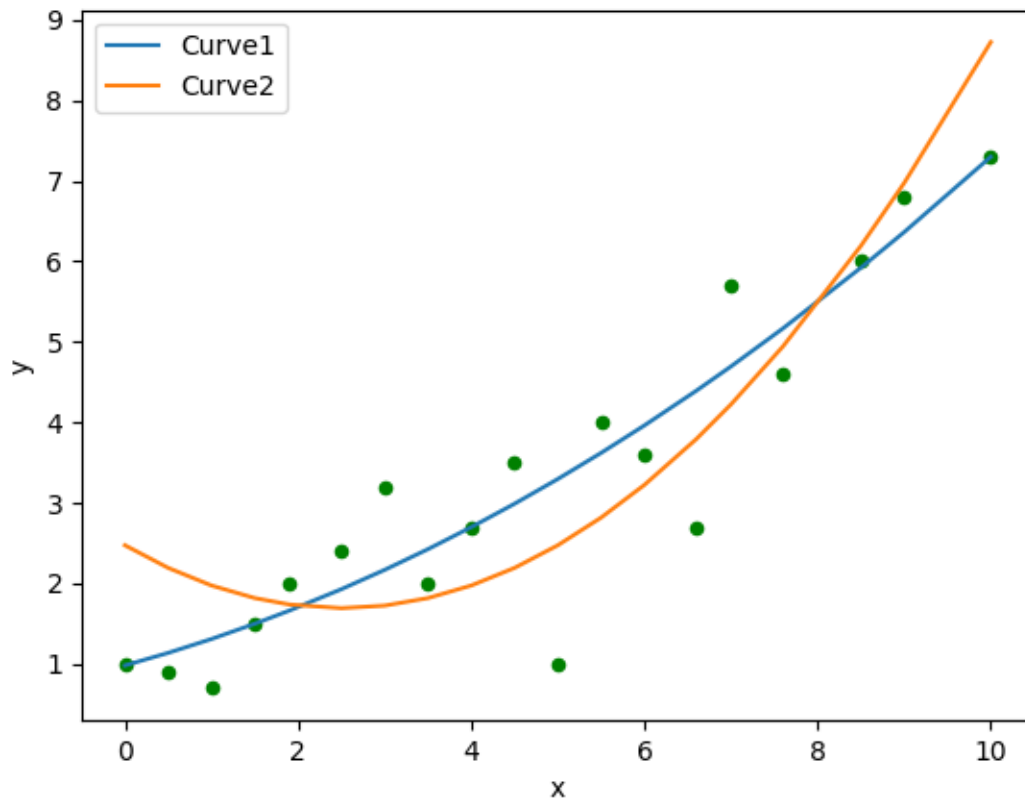
In [7]: s3.plot.line(ax=p2, x='x', y='estimate', label='Curve1');

In [8]: s4.plot.line(ax=p2, x='x', y='estimate', label='Curve2');

In [9]: p2
Out[9]: <matplotlib.axes._subplots.AxesSubplot at 0x7faabaf7a9e8>

```





## 4.2.2 Nonlinear 1

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpug&docsetTarget=ormpug\\_nlpsolver\\_examples01.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpug&docsetTarget=ormpug_nlpsolver_examples01.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/nlpse01.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/nlpse01.html)

### Model

```
import sasoptpy as so

def test(cas_conn):

    m = so.Model(name='nlpse01', session=cas_conn)
    x = m.add_variables(range(1, 9), lb=0.1, ub=10, name='x')

    f = so.Expression(0.4 * (x[1]/x[7]) ** 0.67 + 0.4 * (x[2]/x[8]) ** 0.67 + 10 -
    ↪ x[1] - x[2], name='f')
    m.set_objective(f, sense=so.MIN, name='f1')
```

(continues on next page)

(continued from previous page)

```

m.add_constraint(1 - 0.0588*x[5]*x[7] - 0.1*x[1] >= 0, name='c1')
m.add_constraint(1 - 0.0588*x[6]*x[8] - 0.1*x[1] - 0.1*x[2] >= 0, name='c2')
m.add_constraint(1 - 4*x[3]/x[5] - 2/(x[3]**0.71 * x[5]) - 0.0588*(x[7]/x[3]**1.
↳3) >= 0, name='c3')
m.add_constraint(1 - 4*x[4]/x[6] - 2/(x[4]**0.71 * x[6]) - 0.0588*(x[8]/x[4]**1.
↳3) >= 0, name='c4')
m.add_constraint(f == [0.1, 4.2], name='frange')

x[1].set_init(6)
x[2].set_init(3)
x[3].set_init(0.4)
x[4].set_init(0.2)
x[5].set_init(6)
x[6].set_init(6)
x[7].set_init(1)
x[8].set_init(0.5)

m.solve(verbose=True, options={'with': 'nlp', 'algorithm': 'activeset'})

print(m.get_problem_summary())
print(m.get_solution_summary())
if m.get_session_type() == 'CAS':
    print(m.get_solution()[['var', 'value']])

return m.get_objective_value()

```

## Output

```
In [1]: import os
```

```
In [2]: hostname = os.getenv('CASHOST')
```

```
In [3]: port = os.getenv('CASPORT')
```

```
In [4]: from swat import CAS
```

```
In [5]: cas_conn = CAS(hostname, port)
```

```
In [6]: import sasoptpy
```

```
In [7]: from examples.client_side.nonlinear_1 import test
```

```
In [8]: test(cas_conn)
```

```
NOTE: Initialized model nlpse01.
```

```
NOTE: Added action set 'optimization'.
```

```
NOTE: Converting model nlpse01 to OPTMODEL.
```

```
var x {{1,2,3,4,5,6,7,8}} >= 0.1 <= 10;
```

```
x[1] = 6;
```

```
x[2] = 3;
```

```
x[3] = 0.4;
```

```
x[4] = 0.2;
```

```
x[5] = 6;
```

(continues on next page)

(continued from previous page)

```

x[6] = 6;
x[7] = 1;
x[8] = 0.5;
min f1 = 0.4 * (((x[1]) / (x[7])) ^ (0.67)) + 0.4 * (((x[2]) / (x[8])) ^ (0.67)) -
↳ x[1] - x[2] + 10.0;
con c1 : - 0.0588 * x[5] * x[7] - 0.1 * x[1] >= -1.0;
con c2 : - 0.0588 * x[6] * x[8] - 0.1 * x[1] - 0.1 * x[2] >= -1.0;
con c3 : - ((4 * x[3]) / (x[5])) - ((2) / ((x[3]) ^ (0.71) * x[5])) - 0.0588 *
↳ ((x[7]) / ((x[3]) ^ (1.3))) >= -1.0;
con c4 : - ((4 * x[4]) / (x[6])) - ((2) / ((x[4]) ^ (0.71) * x[6])) - 0.0588 *
↳ ((x[8]) / ((x[4]) ^ (1.3))) >= -1.0;
con frange : -9.9 <= 0.4 * (((x[1]) / (x[7])) ^ (0.67)) + 0.4 * (((x[2]) / (x[8]))
↳ ^ (0.67)) - x[1] - x[2] <= -5.8;
solve with nlp / algorithm=activeset;
create data solution from [i]= {1.._NVAR_} var=_VAR_.name value=_VAR_.lb_
↳ ub=_VAR_.ub rc=_VAR_.rc;
create data dual from [j] = {1.._NCON_} con=_CON_.name value=_CON_.body dual=_CON_.
↳ dual;

```

NOTE: Submitting OPTMODEL code to CAS server.

NOTE: Problem generation will use 8 threads.

NOTE: The problem has 8 variables (0 free, 0 fixed).

NOTE: The problem has 0 linear constraints (0 LE, 0 EQ, 0 GE, 0 range).

NOTE: The problem has 5 nonlinear constraints (0 LE, 0 EQ, 4 GE, 1 range).

NOTE: The OPTMODEL presolver removed 0 variables, 0 linear constraints, and 0
↳ nonlinear constraints.

NOTE: Using analytic derivatives for objective.

NOTE: Using analytic derivatives for nonlinear constraints.

NOTE: The NLP solver is called.

NOTE: The Active Set algorithm is used.

Iter	Objective		Optimality Error
	Value	Infeasibility	
0	3.65736570	0.41664483	0.24247905
1	3.65736570	0.41664483	0.24247905
2	3.40486061	0.10284726	0.18904638
3	3.51178229	0.07506389	0.18860455
4	4.23595983	0.03595983	0.60088809
5	4.16334906	0	0.47130008
6	4.03168584	0.00791810	0.13742971
7	3.88912660	0.11248991	0.06129662
8	3.89579714	0.09534670	0.05994916
9	3.95046640	0.02649207	0.06776850
10	3.92833580	0.03517161	0.06442935
11	3.95179326	0.00494247	0.05837915
12	3.94741555	0.00651989	0.05477333
13	3.95209064	0.00058609	0.05265725
14	3.95058104	0.00122758	0.04772557
15	3.95055959	0.00099113	0.04613473
16	3.95141460	0.00000381	0.04497006
17	3.95132211	0.0000005999371	0.07584723
18	3.95114031	0.00000941	0.04093117
19	3.95027690	0.00011307	0.00020755
20	3.95115797	0.0000007730235	0.00018707
21	3.95116558	0	0.00001366
22	3.95116364	0.0000000153799	0.00000814
23	3.95116355	0.0000000228326	0.00000595
24	3.95116352	0.0000000257138	0.00000337

(continues on next page)

(continued from previous page)

```

                25          3.95116349    0.0000000200547          0.00000132
                26          3.95116349    0.0000000192412          0.0000002015918
NOTE: Optimal.
NOTE: Objective = 3.9511634887.
NOTE: Objective of the best feasible solution found = 3.9511579677.
NOTE: The best feasible solution found is returned.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 8 rows and 6
↳columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 5 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4
↳columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 20 rows and 4
↳columns.
Selected Rows from Table PROBLEMSUMMARY

                                Value
Label
Objective Sense          Minimization
Objective Function              f1
Objective Type              Nonlinear

Number of Variables              8
Bounded Above                  0
Bounded Below                  0
Bounded Below and Above        8
Free                           0
Fixed                          0

Number of Constraints           5
Linear LE (<=)                 0
Linear EQ (=)                  0
Linear GE (>=)                 0
Linear Range                   0
Nonlinear LE (<=)              0
Nonlinear EQ (=)               0
Nonlinear GE (>=)              4
Nonlinear Range                1
Selected Rows from Table SOLUTIONSUMMARY

                                Value
Label
Solver                      NLP
Algorithm                    Active Set
Objective Function              f1
Solution Status              Best Feasible
Objective Value                3.9511579677

Optimality Error              0.0001050714
Infeasibility                  7.7302351E-7

Iterations                    26
Presolve Time                  0.00
Solution Time                  0.02
Selected Rows from Table SOLUTION

    var    value
0  x[1]  6.463315

```

(continues on next page)

(continued from previous page)

```

1  x[2]  2.234530
2  x[3]  0.667455
3  x[4]  0.595820
4  x[5]  5.932980
5  x[6]  5.527231
6  x[7]  1.013787
7  x[8]  0.400664
Out [8]: 3.951157967716

```

## 4.2.3 Nonlinear 2

### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpug&docsetTarget=ormpug\\_nlpsolver\\_examples02.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpug&docsetTarget=ormpug_nlpsolver_examples02.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/nlpse02.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/nlpse02.html)

### Model

```

import sasoptpy as so
import sasoptpy.abstract.math as sm

def test(cas_conn):

    m = so.Model(name='nlpse02', session=cas_conn)
    N = m.add_parameter(name='N', init=1000)
    x = m.add_variables(so.exp_range(1, N), name='x', init=1)
    m.set_objective(
        so.expr_sum(-4*x[i]+3 for i in so.exp_range(1, N-1)) +
        so.expr_sum((x[i]**2 + x[N]**2)**2 for i in so.exp_range(1, N-1)),
        name='f', sense=so.MIN)

    m.add_statement('print x;', after_solve=True)
    m.solve(options={'with': 'nlp'}, verbose=True)
    print(m.get_solution_summary())
    if m.get_session_type() == 'CAS':
        print(m.response['Print1.PrintTable'].head())

    # Model 2
    so.reset()
    m = so.Model(name='nlpse02_2', session=cas_conn)
    N = m.add_parameter(name='N', init=1000)
    x = m.add_variables(so.exp_range(1, N), name='x', lb=1, ub=2)
    m.set_objective(
        so.expr_sum(sm.cos(-0.5*x[i+1] - x[i]**2) for i in so.exp_range(
            1, N-1)), name='f2', sense=so.MIN)
    m.add_statement('print x;', after_solve=True)
    m.solve(verbose=True, options={'with': 'nlp', 'algorithm': 'activeset'})
    print(m.get_solution_summary())

    return m.get_objective_value()

```



## Output

```
In [1]: import os

In [2]: hostname = os.getenv('CASHOST')

In [3]: port = os.getenv('CASPORT')

In [4]: from swat import CAS

In [5]: cas_conn = CAS(hostname, port)

In [6]: import sasoptpy

In [7]: from examples.client_side.nonlinear_2 import test

In [8]: test(cas_conn)
NOTE: Initialized model nlpse02.
NOTE: Added action set 'optimization'.
NOTE: Converting model nlpse02 to OPTMODEL.
    num N init 1000;
    var x {{1..N}} init 1;
    min f = sum {i in 1..N-1} (- 4 * x[i] + 3) + sum {i in 1..N-1} ((x[i]) ^ (2) +
↪(x[N]) ^ (2)) ^ (2));
    solve with nlp / ;
    create data solution from [i]= {1..NVAR_} var=_VAR_.name value=_VAR_ lb=_VAR_.lb_
↪ub=_VAR_.ub rc=_VAR_.rc;
    create data dual from [j] = {1..NCON_} con=_CON_.name value=_CON_.body dual=_CON_.
↪dual;
    print x;

NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 1000 variables (1000 free, 0 fixed).
NOTE: The problem has 0 linear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver removed 0 variables, 0 linear constraints, and 0_
↪nonlinear constraints.
NOTE: Using analytic derivatives for objective.
NOTE: Using 2 threads for nonlinear evaluation.
NOTE: The NLP solver is called.
NOTE: The Interior Point Direct algorithm is used.
```

	Objective		Optimality
Iter	Value	Infeasibility	Error
0	2997.00000000	0	2.66666667
1	561.93750000	0	4.44444444
2	41.17478400	0	12.76397516
3	0.41230550	0	43.37933609
4	0.00005471	0	0.47005128
5	2.2737367544E-13	0	0.00006316
6	0	0	1.1527477269E-12

```
NOTE: Optimal.
NOTE: Objective = 0.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 1000 rows and 6_
↪columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 0 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4_
↪columns.
```

(continues on next page)

(continued from previous page)

```
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4
  columns.
Selected Rows from Table SOLUTIONSUMMARY

Label                                     Value
Solver                                     NLP
Algorithm      Interior Point Direct
Objective Function      f
Solution Status      Optimal
Objective Value      0

Optimality Error      1.152748E-12
Infeasibility      0

Iterations      6
Presolve Time      0.00
Solution Time      0.02
COL1      x
0      1.0      1.0
1      2.0      1.0
2      3.0      1.0
3      4.0      1.0
4      5.0      1.0
NOTE: Initialized model nlpse02_2.
NOTE: Added action set 'optimization'.
NOTE: Converting model nlpse02_2 to OPTMODEL.
  num N init 1000;
  var x {{1..N}} >= 1 <= 2;
  min f2 = sum {i in 1..N-1} (cos(- 0.5 * (x[i + 1]) - ((x[i]) ^ (2))));
  solve with nlp / algorithm=activeset;
  create data solution from [i]= {1..NVAR_} var=_VAR_.name value=_VAR_ lb=_VAR_.lb
  ub=_VAR_.ub rc=_VAR_.rc;
  create data dual from [j] = {1..NCON_} con=_CON_.name value=_CON_.body dual=_CON_.
  dual;
  print x;

NOTE: Submitting OPTMODEL code to CAS server.
NOTE: Problem generation will use 8 threads.
NOTE: The problem has 1000 variables (0 free, 0 fixed).
NOTE: The problem has 0 linear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver removed 0 variables, 0 linear constraints, and 0
  nonlinear constraints.
NOTE: Using analytic derivatives for objective.
NOTE: Using 3 threads for nonlinear evaluation.
NOTE: The NLP solver is called.
NOTE: The Active Set algorithm is used.
NOTE: Initial point was changed to be feasible to bounds.

Objective                                     Optimality
Iter      Value      Infeasibility      Error
0      70.66646447      0      1.24686873
1      70.66646439      0      1.24686873
2      -996.26893548      0      0.23815533
3      -998.99328004      0      0.10718277
4      -998.99999439      0      0.00379400
5      -999.00000000      0      0.00000393
```

(continues on next page)

(continued from previous page)

```

        6      -999.00000000      0  1.7018480129E-12
NOTE: Optimal.
NOTE: Objective = -999.
NOTE: The output table 'SOLUTION' in caslib 'CASUSER(casuser)' has 1000 rows and 6
      ↪ columns.
NOTE: The output table 'DUAL' in caslib 'CASUSER(casuser)' has 0 rows and 4 columns.
NOTE: The CAS table 'solutionSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4
      ↪ columns.
NOTE: The CAS table 'problemSummary' in caslib 'CASUSER(casuser)' has 12 rows and 4
      ↪ columns.
Selected Rows from Table SOLUTIONSUMMARY

              Value
Label
Solver              NLP
Algorithm            Active Set
Objective Function    f2
Solution Status       Optimal
Objective Value       -999

Optimality Error      1.701848E-12
Infeasibility         0

Iterations            6
Presolve Time         0.00
Solution Time         0.04
Out [8]: -999.0

```

## 4.3 SAS 9.4 Examples

### 4.3.1 Decentralization (SASPy)

#### Reference

SAS/OR example: [http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex\\_ex10\\_toc.htm&docsetVersion=15.1&locale=en](http://go.documentation.sas.com/?docsetId=ormpex&docsetTarget=ormpex_ex10_toc.htm&docsetVersion=15.1&locale=en)

SAS/OR code for example: [http://support.sas.com/documentation/onlinedoc/or/ex\\_code/151/mpex10.html](http://support.sas.com/documentation/onlinedoc/or/ex_code/151/mpex10.html)

#### Model

```

import sasoptpy as so
import pandas as pd

def test(cas_conn):

    m = so.Model(name='decentralization', session=cas_conn)

    DEPTS = ['A', 'B', 'C', 'D', 'E']
    CITIES = ['Bristol', 'Brighton', 'London']

```

(continues on next page)

(continued from previous page)

```

benefit_data = pd.DataFrame([
    ['Bristol', 10, 15, 10, 20, 5],
    ['Brighton', 10, 20, 15, 15, 15]],
    columns=['city'] + DEPTS).set_index('city')

comm_data = pd.DataFrame([
    ['A', 'B', 0.0],
    ['A', 'C', 1.0],
    ['A', 'D', 1.5],
    ['A', 'E', 0.0],
    ['B', 'C', 1.4],
    ['B', 'D', 1.2],
    ['B', 'E', 0.0],
    ['C', 'D', 0.0],
    ['C', 'E', 2.0],
    ['D', 'E', 0.7]], columns=['i', 'j', 'comm']).set_index(['i', 'j'])

cost_data = pd.DataFrame([
    ['Bristol', 'Bristol', 5],
    ['Bristol', 'Brighton', 14],
    ['Bristol', 'London', 13],
    ['Brighton', 'Brighton', 5],
    ['Brighton', 'London', 9],
    ['London', 'London', 10]], columns=['i', 'j', 'cost']).set_index(
    ['i', 'j'])

max_num_depts = 3

benefit = {}
for city in CITIES:
    for dept in DEPTS:
        try:
            benefit[dept, city] = benefit_data.loc[city, dept]
        except:
            benefit[dept, city] = 0

comm = {}
for row in comm_data.iterrows():
    (i, j) = row[0]
    comm[i, j] = row[1]['comm']
    comm[j, i] = comm[i, j]

cost = {}
for row in cost_data.iterrows():
    (i, j) = row[0]
    cost[i, j] = row[1]['cost']
    cost[j, i] = cost[i, j]

assign = m.add_variables(DEPTS, CITIES, vartype=so.BIN, name='assign')
IJKL = [(i, j, k, l)
         for i in DEPTS for j in CITIES for k in DEPTS for l in CITIES
         if i < k]
product = m.add_variables(IJKL, vartype=so.BIN, name='product')

totalBenefit = so.expr_sum(benefit[i, j] * assign[i, j]
                           for i in DEPTS for j in CITIES)

```

(continues on next page)

(continued from previous page)

```

totalCost = so.expr_sum(comm[i, k] * cost[j, l] * product[i, j, k, l]
                        for (i, j, k, l) in IJKL)

m.set_objective(totalBenefit-totalCost, name='netBenefit', sense=so.MAX)

m.add_constraints((so.expr_sum(assign[dept, city] for city in CITIES)
                  == 1 for dept in DEPTS), name='assign_dept')

m.add_constraints((so.expr_sum(assign[dept, city] for dept in DEPTS)
                  <= max_num_depts for city in CITIES), name='cardinality')

product_def1 = m.add_constraints((assign[i, j] + assign[k, l] - 1
                                <= product[i, j, k, l]
                                for (i, j, k, l) in IJKL),
                                name='pd1')

product_def2 = m.add_constraints((product[i, j, k, l] <= assign[i, j]
                                for (i, j, k, l) in IJKL),
                                name='pd2')

product_def3 = m.add_constraints((product[i, j, k, l] <= assign[k, l]
                                for (i, j, k, l) in IJKL),
                                name='pd3')

m.solve()
print(m.get_problem_summary())

m.drop_constraints(product_def1)
m.drop_constraints(product_def2)
m.drop_constraints(product_def3)

m.add_constraints((
    so.expr_sum(product[i, j, k, l]
                for j in CITIES if (i, j, k, l) in IJKL) == assign[k, l]
    for i in DEPTS for k in DEPTS for l in CITIES if i < k),
    name='pd4')

m.add_constraints((
    so.expr_sum(product[i, j, k, l]
                for l in CITIES if (i, j, k, l) in IJKL) == assign[i, j]
    for k in DEPTS for i in DEPTS for j in CITIES if i < k),
    name='pd5')

m.solve()
print(m.get_problem_summary())
totalBenefit.set_name('totalBenefit')
totalCost.set_name('totalCost')
print(so.get_solution_table(totalBenefit, totalCost))
print(so.get_solution_table(assign).unstack(level=-1))

return m.get_objective_value()

```

## Output

```
In [1]: import os

In [2]: import saspy

In [3]: config_file = os.path.abspath('../tests/examples/saspy_config.py')

In [4]: sas_conn = saspy.SASsession(cfgfile=config_file)
Using SAS Config named: sshsas
SAS Connection established. Subprocess id is 159

In [5]: import sasoptpy

In [6]: from examples.client_side.decentralization import test

In [7]: test(sas_conn)
NOTE: Initialized model decentralization.
NOTE: Converting model decentralization to OPTMODEL.
NOTE: Submitting OPTMODEL code to SAS instance.

NOTE: Writing HTML5(SASPY_INTERNAL) Body file: STDOUT
NOTE: Problem generation will use 4 threads.
NOTE: The problem has 105 variables (0 free, 0 fixed).
NOTE: The problem has 105 binary and 0 integer variables.
NOTE: The problem has 278 linear constraints (183 LE, 5 EQ, 90 GE, 0 range).
NOTE: The problem has 660 linear constraint coefficients.
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).
NOTE: The OPTMODEL presolver is disabled for linear problems.
NOTE: The initial MILP heuristics are applied.
NOTE: The MILP presolver value AUTOMATIC is applied.
NOTE: The MILP presolver removed 0 variables and 120 constraints.
NOTE: The MILP presolver removed 120 constraint coefficients.
NOTE: The MILP presolver added 120 constraint coefficients.
NOTE: The MILP presolver modified 0 constraint coefficients.
NOTE: The presolved problem has 105 variables, 158 constraints, and 540 constraint_
↪coefficients.
NOTE: The MILP solver is called.
NOTE: The parallel Branch and Cut algorithm is used.
NOTE: The Branch and Cut algorithm is using up to 4 threads.
```

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	2	-14.9000000	135.0000000	111.04%	0
0	1	2	-14.9000000	67.5000000	122.07%	0
0	1	2	-14.9000000	52.0000000	128.65%	0
0	1	3	8.1000000	52.0000000	84.42%	0
0	1	3	8.1000000	50.0000000	83.80%	0
0	1	3	8.1000000	48.2500000	83.21%	0
0	1	3	8.1000000	40.0000000	79.75%	0
0	1	3	8.1000000	39.2500000	79.36%	0
0	1	3	8.1000000	34.2000000	76.32%	0
0	1	3	8.1000000	33.6187500	75.91%	0
0	1	3	8.1000000	33.0761905	75.51%	0
0	1	3	8.1000000	32.6521739	75.19%	0
0	1	3	8.1000000	32.0142857	74.70%	0
0	1	3	8.1000000	31.8222222	74.55%	0
0	1	3	8.1000000	31.3333333	74.15%	0

(continues on next page)

(continued from previous page)

0	1	3	8.1000000	30.0000000	73.00%	0
0	1	3	8.1000000	28.5000000	71.58%	0
0	1	4	14.9000000	14.9000000	0.00%	0

NOTE: The MILP solver added 28 cuts with 146 cut coefficients at the root.  
NOTE: Optimal.  
NOTE: Objective = 14.9.  
NOTE: The data set WORK.PROB\_SUMMARY has 20 observations and 3 variables.  
NOTE: The data set WORK.SOL\_SUMMARY has 18 observations and 3 variables.  
NOTE: The data set WORK.SOLUTION has 105 observations and 6 variables.  
NOTE: The data set WORK.DUAL has 278 observations and 4 variables.  
NOTE: PROCEDURE OPTMODEL used (Total process time):  
real time 0.17 seconds  
cpu time 0.16 seconds

	Value
Label	
Objective Sense	Maximization
Objective Function	netBenefit
Objective Type	Linear
Number of Variables	105
Bounded Above	0
Bounded Below	0
Bounded Below and Above	105
Free	0
Fixed	0
Binary	105
Integer	0
Number of Constraints	278
Linear LE (<=)	183
Linear EQ (=)	5
Linear GE (>=)	90
Linear Range	0
Constraint Coefficients	660

NOTE: Converting model decentralization to OPTMODEL.  
NOTE: Submitting OPTMODEL code to SAS instance.

NOTE: Writing HTML5(SASPY\_INTERNAL) Body file: STDOUT  
NOTE: Problem generation will use 4 threads.  
NOTE: The problem has 105 variables (0 free, 0 fixed).  
NOTE: The problem has 105 binary and 0 integer variables.  
NOTE: The problem has 68 linear constraints (3 LE, 65 EQ, 0 GE, 0 range).  
NOTE: The problem has 270 linear constraint coefficients.  
NOTE: The problem has 0 nonlinear constraints (0 LE, 0 EQ, 0 GE, 0 range).  
NOTE: The OPTMODEL presolver is disabled for linear problems.  
NOTE: The initial MILP heuristics are applied.  
NOTE: The MILP presolver value AUTOMATIC is applied.  
NOTE: The MILP presolver removed 0 variables and 0 constraints.  
NOTE: The MILP presolver removed 0 constraint coefficients.  
NOTE: The MILP presolver modified 0 constraint coefficients.  
NOTE: The presolved problem has 105 variables, 68 constraints, and 270 constraint\_  
→coefficients.  
NOTE: The MILP solver is called.  
NOTE: The parallel Branch and Cut algorithm is used.

(continues on next page)

(continued from previous page)

NOTE: The Branch and Cut algorithm is using up to 4 threads.

Node	Active	Sols	BestInteger	BestBound	Gap	Time
0	1	2	-28.1000000	135.0000000	120.81%	0
0	1	2	-28.1000000	30.0000000	193.67%	0
0	1	3	-16.3000000	30.0000000	154.33%	0
0	1	4	14.9000000	14.9000000	0.00%	0

NOTE: Optimal.

NOTE: Objective = 14.9.

NOTE: The data set WORK.PROB\_SUMMARY has 20 observations and 3 variables.

NOTE: The data set WORK.SOL\_SUMMARY has 18 observations and 3 variables.

NOTE: The data set WORK.SOLUTION has 105 observations and 6 variables.

NOTE: The data set WORK.DUAL has 68 observations and 4 variables.

NOTE: PROCEDURE OPTMODEL used (Total process time):

real time	0.10 seconds
cpu time	0.08 seconds

Label	Value
Objective Sense	Maximization
Objective Function	netBenefit
Objective Type	Linear

Number of Variables	105
Bounded Above	0
Bounded Below	0
Bounded Below and Above	105
Free	0
Fixed	0
Binary	105
Integer	0

Number of Constraints	68
Linear LE (<=)	3
Linear EQ (=)	65
Linear GE (>=)	0
Linear Range	0

Constraint Coefficients	270
-------------------------	-----

	totalBenefit	totalCost
-	80.0	65.1
assign (A, Bristol)	1.0	
(A, Brighton)	0.0	
(A, London)	0.0	
(B, Bristol)	0.0	
(B, Brighton)	1.0	
(B, London)	0.0	
(C, Bristol)	0.0	
(C, Brighton)	1.0	
(C, London)	0.0	
(D, Bristol)	1.0	
(D, Brighton)	0.0	
(D, London)	0.0	
(E, Bristol)	0.0	
(E, Brighton)	1.0	
(E, London)	0.0	

dtype: float64

(continues on next page)



(continued from previous page)

```
Out [7]: 14.9
```



## API REFERENCE

### 5.1 Core

#### 5.1.1 Model

##### Constructor

---

<code>Model(**kwargs)</code>	Creates an optimization model
------------------------------	-------------------------------

---

##### `sasoptpy.Model`

**class** `Model` (*\*\*kwargs*)

Bases: `object`

Creates an optimization model

##### Parameters

**name** [string] Name of the model

**session** [`swat.cas.connection.CAS` or `saspy.SASsession`, optional] CAS or SAS  
Session object

##### Examples

```
>>> from swat import CAS
>>> import sasoptpy as so
>>> s = CAS('cas.server.address', port=12345)
>>> m = so.Model(name='my_model', session=s)
NOTE: Initialized model my_model
```

```
>>> mip = so.Model(name='mip')
NOTE: Initialized model mip
```

## Components

<code>Model.get_name(self)</code>	Returns model name
<code>Model.set_session(self, session)</code>	Sets the session of model
<code>Model.get_session(self)</code>	Returns the session of the model
<code>Model.get_session_type(self)</code>	Tests whether the model session is defined and still active
<code>Model.set_objective(self, expression, name)</code>	Specifies the objective function for the model
<code>Model.append_objective(self, expression, name)</code>	Appends a new objective to the model
<code>Model.get_objective(self)</code>	Returns the objective function as an <i>Expression</i> object
<code>Model.get_all_objectives(self)</code>	Returns a list of objectives in the model
<code>Model.add_variable(self, name[, vartype, ...])</code>	Adds a new variable to the model
<code>Model.add_variables(self, *argv, name[, ...])</code>	Adds a group of variables to the model
<code>Model.add_implicit_variable(self[, argv, name])</code>	Adds an implicit variable to the model
<code>Model.get_variable(self, name)</code>	Returns the reference to a variable in the model
<code>Model.get_variables(self)</code>	Returns a list of variables
<code>Model.get_grouped_variables(self)</code>	Returns an ordered dictionary of variables
<code>Model.get_implicit_variables(self)</code>	Returns a list of implicit variables
<code>Model.get_variable_coef(self, var)</code>	Returns the objective value coefficient of a variable
<code>Model.drop_variable(self, variable)</code>	Drops a variable from the model
<code>Model.drop_variables(self, *variables)</code>	Drops a variable group from the model
<code>Model.add_constraint(self, c, name)</code>	Adds a single constraint to the model
<code>Model.add_constraints(self, argv, name)</code>	Adds a set of constraints to the model
<code>Model.get_constraint(self, name)</code>	Returns the reference to a constraint in the model
<code>Model.get_constraints(self)</code>	Returns a list of constraints in the model
<code>Model.get_grouped_constraints(self)</code>	Returns an ordered dictionary of constraints
<code>Model.drop_constraint(self, constraint)</code>	Drops a constraint from the model
<code>Model.drop_constraints(self, *constraints)</code>	Drops a constraint group from the model
<code>Model.add_set(self, name[, init, value, settype])</code>	Adds a set to the model
<code>Model.add_parameter(self, *argv, name[, ...])</code>	Adds a <i>abstract.Parameter</i> object to the model
<code>Model.add_statement(self, statement[, ...])</code>	Adds a PROC OPTMODEL statement to the model
<code>Model.get_sets(self)</code>	Returns a list of Set objects in the model
<code>Model.get_parameters(self)</code>	Returns a list of <i>abstract.Parameter</i> and <i>abstract.ParameterGroup</i> objects in the model
<code>Model.get_statements(self)</code>	Returns a list of all statements inside the model
<code>Model.include(self, *argv)</code>	Adds existing variables and constraints to a model

### **sasoptpy.Model.get\_name**

`Model.get_name(self)`  
Returns model name

### **sasoptpy.Model.set\_session**

`Model.set_session(self, session)`  
Sets the session of model

#### **Parameters**

**session** [`swat.cas.connection.CAS` or `saspy.SASsession`] CAS or SAS Session object

#### **Notes**

- You can use CAS sessions (via SWAT package) or SAS sessions (via SASPy package)
- Session of a model can be set at initialization. See [Model](#).

### **sasoptpy.Model.get\_session**

`Model.get_session(self)`  
Returns the session of the model

#### **Returns**

**session** [`swat.cas.connection.CAS` or `saspy.SASsession`] Session of the model, or None

### **sasoptpy.Model.get\_session\_type**

`Model.get_session_type(self)`  
Tests whether the model session is defined and still active

#### **Returns**

**session** [string] 'CAS' for CAS sessions, 'SAS' for SAS sessions

### **sasoptpy.Model.set\_objective**

`Model.set_objective(self, expression, name, sense=None)`  
Specifies the objective function for the model

#### **Parameters**

**expression** [[Expression](#)] The objective function as an Expression

**name** [string] Name of the objective value

**sense** [string, optional] Objective value direction, `sasoptpy.MIN` or `sasoptpy.MAX`

#### **Returns**

**objective** [*Expression*] Objective function as an *Expression* object

See also:

*Model.append\_objective()*

## Notes

- Default objective sense is minimization *MIN*.
- This method replaces the existing objective of the model. When working with multiple objectives, use the *Model.append\_objective()* method.

## Examples

```
>>> profit = so.Expression(5 * sales - 2 * material, name='profit')
>>> m.set_objective(profit, so.MAX)
>>> print(m.get_objective())
- 2.0 * material + 5.0 * sales
```

```
>>> m.set_objective(4 * x - 5 * y, name='obj')
>>> print(repr(m.get_objective()))
sasoptpy.Expression(exp = 4.0 * x - 5.0 * y , name='obj')
```

```
>>> f1 = m.set_objective(2 * x + y, sense=so.MIN, name='f1')
>>> f2 = m.append_objective( (x - y) ** 2, sense=so.MIN, name='f2')
>>> print(m.to_optmodel(options={'with': 'blackbox', 'obj': (f1, f2)}))
proc optmodel;
var x;
var y;
min f1 = 2 * x + y;
min f2 = (x - y) ^ (2);
solve with blackbox obj (f1 f2);
print _var_.name _var_.lb _var_.ub _var_ _var_.rc;
print _con_.name _con_.body _con_.dual;
quit;
```

## sasoptpy.Model.append\_objective

**Model.append\_objective** (*self*, *expression*, *name*, *sense=None*)

Appends a new objective to the model

### Parameters

**expression** [*Expression*] The objective function as an *Expression*

**name** [string] Name of the objective value

**sense** [string, optional] Objective value direction, *sasoptpy.MIN* or *sasoptpy.MAX*

### Returns

**objective** [*Expression*] Objective function as an *Expression* object

See also:

*Model.set\_objective()*

## Notes

- Default objective sense is minimization *MIN*.

## Examples

```
>>> f1 = m.set_objective(2 * x + y, sense=so.MIN, name='f1')
>>> f2 = m.append_objective( (x - y) ** 2, sense=so.MIN, name='f2')
>>> print(m.to_optmodel(options={'with': 'blackbox', 'obj': (f1, f2)}))
proc optmodel;
var x;
var y;
min f1 = 2 * x + y;
min f2 = (x - y) ^ (2);
solve with blackbox obj (f1 f2);
print _var_.name _var_.lb _var_.ub _var_ _var_.rc;
print _con_.name _con_.body _con_.dual;
quit;
```

## sasoptpy.Model.get\_objective

`Model.get_objective(self)`

Returns the objective function as an *Expression* object

### Returns

**objective** [*Expression*] Objective function

## Examples

```
>>> m.set_objective(4 * x - 5 * y, name='obj')
>>> print(repr(m.get_objective()))
sasoptpy.Expression(exp = 4.0 * x - 5.0 * y, name='obj')
```

## sasoptpy.Model.get\_all\_objectives

`Model.get_all_objectives(self)`

Returns a list of objectives in the model

### Returns

**all\_objectives** [list] A list of *Objective* objects

## Examples

```
>>> m = so.Model(name='test_set_get_objective')
>>> x = m.add_variable(name='x')
>>> obj1 = m.set_objective(2 * x, sense=so.MIN, name='obj1')
>>> obj2 = m.set_objective(5 * x, sense=so.MIN, name='obj2') # Overrides obj1
>>> obj3 = m.append_objective(10 * x, sense=so.MIN, name='obj3')
>>> assertEquals(m.get_all_objectives(), [obj2, obj3])
True
```

## sasoptpy.Model.add\_variable

`Model.add_variable(self, name, vartype=None, lb=None, ub=None, init=None)`

Adds a new variable to the model

New variables can be created via this method or existing variables can be added to the model.

### Parameters

**name** [string] Name of the variable to be created

**vartype** [string, optional] Type of the variable, either *sasoptpy.BIN*, *sasoptpy.INT* or *sasoptpy.CONT*

**lb** [float, optional] Lower bound of the variable

**ub** [float, optional] Upper bound of the variable

**init** [float, optional] Initial value of the variable

### Returns

**var** [*Variable*] Variable that is added to the model

See also:

*Variable*, *Model.include()*

## Notes

- *name* is a mandatory field for this method.

## Examples

Adding a variable on the fly

```
>>> m = so.Model(name='demo')
>>> x = m.add_variable(name='x', vartype=so.INT, ub=10, init=2)
>>> print(repr(x))
NOTE: Initialized model demo
sasoptpy.Variable(name='x', lb=0, ub=10, init=2, vartype='INT')
```

Adding an existing variable to a model

```
>>> y = so.Variable(name='y', vartype=so.BIN)
>>> m = so.Model(name='demo')
>>> m.include(y)
```



**sasoptpy.Model.add\_variables**

`Model.add_variables` (*self*, \**argv*, *name*, *vartype=None*, *lb=None*, *ub=None*, *init=None*)

Adds a group of variables to the model

**Parameters**

**argv** [list, dict, `pandas.Index`] Loop index for variable group

**name** [string] Name of the variables

**vartype** [string, optional] Type of variables, *BIN*, *INT*, or *CONT*

**lb** [list, dict, `pandas.Series`] Lower bounds of variables

**ub** [list, dict, `pandas.Series`] Upper bounds of variables

**init** [list, dict, `pandas.Series`] Initial values of variables

See also:

*VariableGroup*, *Model.include()*

**Examples**

```
>>> production = m.add_variables(PERIODS, vartype=so.INT,
                                name='production', lb=min_production)
>>> print(production)
>>> print(repr(production))
Variable Group (production) [
  [Period1: production['Period1',]]
  [Period2: production['Period2',]]
  [Period3: production['Period3',]]
]
sasoptpy.VariableGroup(['Period1', 'Period2', 'Period3'],
name='production')
```

**sasoptpy.Model.add\_implicit\_variable**

`Model.add_implicit_variable` (*self*, *argv=None*, *name=None*)

Adds an implicit variable to the model

**Parameters**

**argv** [Generator-type object] Generator object where each item is an entry

**name** [string] Name of the implicit variable

## Notes

- Based on whether the implicit variables are generated by a regular or abstract expression, they can appear in generated OPTMODEL codes.

## Examples

```
>>> x = m.add_variables(range(5), name='x')
>>> y = m.add_implicit_variable((
>>>     x[i] + 2 * x[i+1] for i in range(4)), name='y')
>>> print(y[2])
x[2] + 2 * x[3]
```

```
>>> I = m.add_set(name='I')
>>> z = m.add_implicit_variable((x[i] * 2 + 2 for i in I), name='z')
>>> print(z._defn())
impvar z {i_1 in I} = 2 * x[i_1] + 2;
```

## sasoptpy.Model.get\_variable

`Model.get_variable(self, name)`

Returns the reference to a variable in the model

### Parameters

**name** [string] Name or key of the variable requested

### Returns

**variable** [*Variable*] Reference to the variable

## Examples

```
>>> m.add_variable(name='x', vartype=so.INT, lb=3, ub=5)
>>> var1 = m.get_variable('x')
>>> print(repr(var1))
sasoptpy.Variable(name='x', lb=3, ub=5, vartype='INT')
```

## sasoptpy.Model.get\_variables

`Model.get_variables(self)`

Returns a list of variables

### Returns

**variables** [list] List of variables in the model

## Examples

```
>>> x = m.add_variables(2, name='x')
>>> y = m.add_variable(name='y')
>>> print(m.get_variables())
[sasoptpy.Variable(name='x_0', vartype='CONT'),
 sasoptpy.Variable(name='x_1', vartype='CONT'),
 sasoptpy.Variable(name='y', vartype='CONT')]
```

## sasoptpy.Model.get\_grouped\_variables

`Model.get_grouped_variables(self)`

Returns an ordered dictionary of variables

### Returns

**grouped\_vars** [OrderedDict] Dictionary of variables and variable groups in the model

See also:

[`Model.get\_variables\(\)`](#), [`Model.get\_grouped\_constraints\(\)`](#)

## Examples

```
>>> m1 = so.Model(name='test_copy_model_1')
>>> x = m1.add_variable(name='x')
>>> y = m1.add_variables(2, name='y')
>>> vars = OrderedDict([('x', x), ('y', y)])
>>> self.assertEqual(m1.get_grouped_variables(), vars)
True
```

## sasoptpy.Model.get\_implicit\_variables

`Model.get_implicit_variables(self)`

Returns a list of implicit variables

### Returns

**implicit\_variables** [list] List of implicit variables in the model

## Examples

```
>>> m = so.Model(name='test_add_impvar')
>>> x = m.add_variables(5, name='x')
>>> y = m.add_implicit_variable((i * x[i] + x[i] ** 2 for i in range(5)),
                                name='y')
>>> assertEquals([y], m.get_implicit_variables())
True
```

### `sasoptpy.Model.get_variable_coef`

`Model.get_variable_coef(self, var)`

Returns the objective value coefficient of a variable

#### Parameters

**var** [*Variable* or string] Variable whose objective value is requested. It can be either the variable object itself, or the name of the variable.

#### Returns

**coef** [float] Objective value coefficient of the given variable

#### Examples

```
>>> x = m.add_variable(name='x')
>>> y = m.add_variable(name='y')
>>> m.set_objective(4 * x - 5 * y, name='obj', sense=so.MAX)
>>> print(m.get_variable_coef(x))
4.0
>>> print(m.get_variable_coef('y'))
-5.0
```

### `sasoptpy.Model.drop_variable`

`Model.drop_variable(self, variable)`

Drops a variable from the model

#### Parameters

**variable** [*Variable*] The variable to be dropped from the model

See also:

`Model.drop_variables()`

`Model.drop_constraint()`

`Model.drop_constraints()`

#### Examples

```
>>> x = m.add_variable(name='x')
>>> y = m.add_variable(name='y')
>>> print(m.get_variable('x'))
x
>>> m.drop_variable(x)
>>> print(m.get_variable('x'))
None
```

## sasoptpy.Model.drop\_variables

`Model.drop_variables(self, *variables)`

Drops a variable group from the model

### Parameters

**variables** [*VariableGroup*] The variable group to be dropped from the model

See also:

`Model.drop_variable()`

`Model.drop_constraint()`

`Model.drop_constraints()`

### Examples

```

>>> x = m.add_variables(3, name='x')
>>> print(m.get_variables())
[sasoptpy.Variable(name='x_0', vartype='CONT'),
 sasoptpy.Variable(name='x_1', vartype='CONT')]
>>> m.drop_variables(x)
>>> print(m.get_variables())
[]

```

## sasoptpy.Model.add\_constraint

`Model.add_constraint(self, c, name)`

Adds a single constraint to the model

### Parameters

**c** [*Constraint*] Constraint to be added to the model

**name** [string] Name of the constraint

### Returns

**c** [*Constraint*] Reference to the constraint

See also:

`Constraint`, `Model.include()`

### Examples

```

>>> x = m.add_variable(name='x', vartype=so.INT, lb=0, ub=5)
>>> y = m.add_variables(3, name='y', vartype=so.CONT, lb=0, ub=10)
>>> c1 = m.add_constraint(x + y[0] >= 3, name='c1')
>>> print(c1)
x + y[0] >= 3

```

```
>>> c2 = m.add_constraint(x - y[2] == [4, 10], name='c2')
>>> print(c2)
- y[2] + x = [4, 10]
```

## `sasoptpy.Model.add_constraints`

`Model.add_constraints` (*self, argv, name*)

Adds a set of constraints to the model

### Parameters

**argv** [Generator-type object] List of constraints as a generator-type Python object

**name** [string] Name for the constraint group and individual constraint prefix

### Returns

**cg** [`ConstraintGroup`] Reference to the `ConstraintGroup`

See also:

[`ConstraintGroup`](#), [`Model.include\(\)`](#)

## Examples

```
>>> x = m.add_variable(name='x', vartype=so.INT, lb=0, ub=5)
>>> y = m.add_variables(3, name='y', vartype=so.CONT, lb=0, ub=10)
>>> c = m.add_constraints((x + 2 * y[i] >= 2 for i in [0, 1, 2]),
                        name='c')
>>> print(c)
Constraint Group (c) [
  [0: 2.0 * y[0] + x >= 2]
  [1: 2.0 * y[1] + x >= 2]
  [2: 2.0 * y[2] + x >= 2]
]
```

```
>>> t = m.add_variables(3, 4, name='t')
>>> ct = m.add_constraints((t[i, j] <= x for i in range(3)
                        for j in range(4)), name='ct')
>>> print(ct)
Constraint Group (ct) [
  [(0, 0): - x + t[0, 0] <= 0]
  [(0, 1): t[0, 1] - x <= 0]
  [(0, 2): - x + t[0, 2] <= 0]
  [(0, 3): t[0, 3] - x <= 0]
  [(1, 0): t[1, 0] - x <= 0]
  [(1, 1): t[1, 1] - x <= 0]
  [(1, 2): - x + t[1, 2] <= 0]
  [(1, 3): - x + t[1, 3] <= 0]
  [(2, 0): - x + t[2, 0] <= 0]
  [(2, 1): t[2, 1] - x <= 0]
  [(2, 2): t[2, 2] - x <= 0]
  [(2, 3): t[2, 3] - x <= 0]
]
```

## sasoptpy.Model.get\_constraint

`Model.get_constraint(self, name)`

Returns the reference to a constraint in the model

### Parameters

**name** [string] Name of the constraint requested

### Returns

**constraint** [*Constraint*] Requested object

### Examples

```
>>> m.add_constraint(2 * x + y <= 15, name='c1')
>>> print(m.get_constraint('c1'))
2.0 * x + y <= 15
```

## sasoptpy.Model.get\_constraints

`Model.get_constraints(self)`

Returns a list of constraints in the model

### Returns

**constraints** [list] A list of Constraint objects

### Examples

```
>>> m.add_constraint(x[0] + y <= 15, name='c1')
>>> m.add_constraints((2 * x[i] - y >= 1 for i in [0, 1]), name='c2')
>>> print(m.get_constraints())
[sasoptpy.Constraint( x[0] + y <= 15, name='c1'),
 sasoptpy.Constraint( 2.0 * x[0] - y >= 1, name='c2_0'),
 sasoptpy.Constraint( 2.0 * x[1] - y >= 1, name='c2_1')]
```

## sasoptpy.Model.get\_grouped\_constraints

`Model.get_grouped_constraints(self)`

Returns an ordered dictionary of constraints

### Returns

**grouped\_cons** [OrderedDict] Dictionary of constraints and constraint groups in the model

See also:

*Model.get\_constraints()*, *Model.get\_grouped\_variables()*

## Examples

```
>>> m1 = so.Model(name='test_copy_model_1')
>>> x = m1.add_variable(name='x')
>>> y = m1.add_variables(2, name='y')
>>> c1 = m1.add_constraint(x + y[0] >= 2, name='c1')
>>> c2 = m1.add_constraints((x - y[i] <= 10 for i in range(2)), name='c2')
>>> cons = OrderedDict([('c1', c1), ('c2', c2)])
>>> self.assertEqual(m1.get_grouped_constraints(), cons)
True
```

## `sasoptpy.Model.drop_constraint`

`Model.drop_constraint` (*self*, *constraint*)

Drops a constraint from the model

### Parameters

**constraint** [*Constraint*] The constraint to be dropped from the model

See also:

`Model.drop_constraints()`

`Model.drop_variable()`

`Model.drop_variables()`

## Examples

```
>>> c1 = m.add_constraint(2 * x + y <= 15, name='c1')
>>> print(m.get_constraint('c1'))
2 * x + y <= 15
>>> m.drop_constraint(c1)
>>> print(m.get_constraint('c1'))
None
```

## `sasoptpy.Model.drop_constraints`

`Model.drop_constraints` (*self*, *\*constraints*)

Drops a constraint group from the model

### Parameters

**constraints** [*Constraint* or *ConstraintGroup*] Arbitrary number of constraints to be dropped

See also:

`Model.drop_constraints()`

`Model.drop_variable()`

`Model.drop_variables()`



## Examples

```
>>> c1 = m.add_constraints((x[i] + y <= 15 for i in [0, 1]), name='c1')
>>> print(m.get_constraints())
[sasoptpy.Constraint( x[0] + y <= 15, name='c1_0'),
 sasoptpy.Constraint( x[1] + y <= 15, name='c1_1')]
>>> m.drop_constraints(c1)
>>> print(m.get_constraints())
[]
```

## sasoptpy.Model.add\_set

`Model.add_set(self, name, init=None, value=None, settype=None)`

Adds a set to the model

### Parameters

**name** [string, optional] Name of the set

**init** [Set, optional] Initial value of the set

**value** [list, float, optional] Exact value of the set

**settype** [list, optional] Types of the set as a list

The list can have one more *num* (for float) and *str* (for string) values. You can use *sasoptpy.NUM* and *sasoptpy.STR* for floats and strings, respectively.

## Examples

```
>>> I = m.add_set(name='I')
>>> print(I._defn())
set I;
```

```
>>> J = m.add_set(name='J', settype=['str'])
>>> print(J._defn())
set <str> J;
```

```
>>> N = m.add_parameter(name='N', init=4)
>>> K = m.add_set(name='K', init=so.exp_range(1, N))
>>> print(K._defn())
set K = 1..N;
```

```
>>> m.add_set(name='W', settype=[so.STR, so.NUM])
>>> print(W._defn())
set <str, num> W;
```

## sasoptpy.Model.add\_parameter

`Model.add_parameter(self, *argv, name, init=None, value=None, p_type=None)`

Adds a `abstract.Parameter` object to the model

### Parameters

- argv** [Set, optional] Index or indices of the parameter
- name** [string] Name of the parameter
- init** [float or expression, optional] Initial value of the parameter
- p\_type** [string, optional] Type of the parameter, 'num' for floats or 'str' for strings

### Returns

- p** [`abstract.Parameter` or `abstract.ParameterGroup`] A single parameter or a parameter group

## Examples

```
>>> I = m.add_set(name='I')
>>> a = m.add_parameter(I, name='a', init=5)
>>> print(a._defn())
num a {I} init 5 ;
```

```
>>> I = m.add_set(name='I')
>>> J = m.add_set(name='J')
>>> p = m.add_parameter(I, J, name='p')
>>> print(p._defn())
num p {{I,J}};
```

## sasoptpy.Model.add\_statement

`Model.add_statement(self, statement, after_solve=None)`

Adds a PROC OPTMODEL statement to the model

### Parameters

- statement** [`Expression` or string] Statement object
- after\_solve** [boolean] Switch for appending the statement after the problem solution

### Notes

- If the statement string includes 'print', then the statement is automatically placed after the solve even if `after_solve` is `False`.

## Examples

```
>>> I = m.add_set(name='I')
>>> x = m.add_variables(I, name='x', vartype=so.INT)
>>> a = m.add_parameter(I, name='a')
>>> c = m.add_constraints((x[i] <= 2 * a[i] for i in I), name='c')
>>> m.add_statement('print x;', after_solve=True)
>>> print(m.to_optmodel())
proc optmodel;
min m_obj = 0;
set I;
var x {I} integer >= 0;
num a {I};
con c {i_1 in I} : x[i_1] - 2.0 * a[i_1] <= 0;
solve;
print _var_.name _var_.lb _var_.ub _var_ _var_.rc;
print _con_.name _con_.body _con_.dual;
print x;
quit;
```

## sasoptpy.Model.get\_sets

`Model.get_sets(self)`

Returns a list of `Set` objects in the model

### Returns

**set\_list** [list] List of sets in the model

## Examples

```
>>> m.get_sets()
[sasoptpy.abstract.Set(name=W, settype=['str', 'num']), sasoptpy.abstract.
↪Set(name=I, settype=['num']), sasoptpy.abstract.Set(name=J, settype=['num'])]
```

## sasoptpy.Model.get\_parameters

`Model.get_parameters(self)`

Returns a list of `abstract.Parameter` and `abstract.ParameterGroup` objects in the model

### Returns

**param\_list** [list] List of parameters in the model

## Examples

```
>>> for i in m.get_parameters():
...     print(i.get_name(), type(i))
p <class 'sasoptpy.abstract.parameter_group.ParameterGroup'>
r <class 'sasoptpy.abstract.parameter.Parameter'>
```

## sasoptpy.Model.get\_statements

`Model.get_statements(self)`

Returns a list of all statements inside the model

### Returns

**st\_list** [list] List of all statement objects

## Examples

```
>>> m.add_statement(so.abstract.LiteralStatement("expand;"))
>>> m.get_statements()
[<sasoptpy.abstract.statement.literal.LiteralStatement object at 0x7fe0202fc358>]
>>> print(m.to_optmodel())
proc optmodel;
var x;
min obj1 = x * x;
expand;
solve;
quit;
```

## sasoptpy.Model.include

`Model.include(self, *argv)`

Adds existing variables and constraints to a model

### Parameters

**argv** : Objects to be included in the model

## Notes

- Valid object types for *argv* parameter:
  - Model*  
Including a model causes all variables and constraints inside the original model to be included.
  - Variable*
  - Constraint*
  - VariableGroup*
  - ConstraintGroup*
  - Objective*

- Set
- Parameter
- ParameterGroup
- Statement and all subclasses
- ImplicitVar

## Examples

Adding an existing variable

```
>>> x = so.Variable(name='x', vartype=so.CONT)
>>> m.include(x)
```

Adding an existing constraint

```
>>> c1 = so.Constraint(x + y <= 5, name='c1')
>>> m.include(c1)
```

Adding an existing set of variables

```
>>> z = so.VariableGroup(3, 5, name='z', ub=10)
>>> m.include(z)
```

Adding an existing set of constraints

```
>>> c2 = so.ConstraintGroup((x + 2 * z[i, j] >= 2 for i in range(3)
                             for j in range(5)), name='c2')
>>> m.include(c2)
```

Adding an existing model (including all of its elements)

```
>>> new_model = so.Model(name='new_model')
>>> new_model.include(m)
```

## Solver calls

<code>Model.solve(self, \**kwargs)</code>	Solves the model by calling CAS or SAS optimization solvers
<code>Model.tune_parameters(self, \**kwargs)</code>	Tunes the model to find ideal solver parameters
<code>Model.get_solution(self[, vtype, solution, ...])</code>	Returns the primal and dual problem solutions
<code>Model.get_variable_value(self, var)</code>	Returns the value of a variable
<code>Model.get_objective_value(self)</code>	Returns the optimal objective value
<code>Model.get_solution_summary(self)</code>	Returns the solution summary table to the user
<code>Model.get_problem_summary(self)</code>	Returns the problem summary table to the user
<code>Model.get_tuner_results(self)</code>	Returns the tuning results
<code>Model.print_solution(self)</code>	Prints the current values of the variables
<code>Model.clear_solution(self)</code>	Clears the cached solution of the model

## sasoptpy.Model.solve

`Model.solve(self, **kwargs)`

Solves the model by calling CAS or SAS optimization solvers

### Parameters

**options** [dict, optional] Solver options as a dictionary object

**submit** [boolean, optional] When set to *True*, calls the solver

**name** [string, optional] Name of the table

**frame** [boolean, optional] When set to *True*, uploads the problem as a DataFrame in MPS format

**drop** [boolean, optional] When set to *True*, drops the MPS table after solve (only CAS)

**replace** [boolean, optional] When set to *True*, replaces an existing MPS table (only CAS and MPS)

**primalin** [boolean, optional] When set to *True*, uses initial values (only MILP)

**verbose** [boolean, optional (experimental)] When set to *True*, prints the generated OPTMODEL code

### Returns

**solution** [`pandas.DataFrame`] Solution of the optimization model

## Notes

- Some of the options listed under the `options` argument might not be passed, depending on which CAS action is being used.
- The `option` argument should be a dictionary, where keys are option names. For example, `m.solve(options={'maxtime': 600})` limits the solution time to 600 seconds.
- See [Solver Options](#) for a list of solver options.

## Examples

```
>>> m.solve()
NOTE: Initialized model food_manufacture_1
NOTE: Converting model food_manufacture_1 to DataFrame
NOTE: Added action set 'optimization'.
...
NOTE: Optimal.
NOTE: Objective = 107842.59259.
NOTE: The Dual Simplex solve time is 0.01 seconds.
```

```
>>> m.solve(options={'maxtime': 600})
```

```
>>> m.solve(options={'algorithm': 'ipm'})
```

## sasoptpy.Model.tune\_parameters

`Model.tune_parameters(self, **kwargs)`

Tunes the model to find ideal solver parameters

### Parameters

**kwargs** : Keyword arguments as defined in the optimization.tuner action.

Acceptable values are:

- **milpParameters**: Parameters for the solveMilp action, such as *maxTime*, *heuristics*, *feasTol*
- **tunerParameters**: Parameters for the tuner itself, such as *maxConfigs*, *printLevel*, *logFreq*
- **tuningParameters**: List of parameters to be tuned, such as *cutStrategy*, *presolver*, *restarts*

### Returns

**tunerResults** [`swat.dataframe.SASDataFrame`] Tuning results as a table

See also:

`Model.get_tuner_results()`

### Notes

- See [SAS Optimization documentation](#) for a full list of tunable parameters.
- See [Optimization Action Set documentation](#).

### Examples

```
>>> m = so.Model(name='model1')
>>> ...
>>> results = m.tune_parameters(tunerParameters={'maxConfigs': 10})
NOTE: Initialized model knapsack_with_tuner.
NOTE: Added action set 'optimization'.
NOTE: Uploading the problem DataFrame to the server.
NOTE: Cloud Analytic Services made the uploaded file available as table KNAPSACK_
↪WITH_TUNER in caslib CASUSER(casuser).
NOTE: The table KNAPSACK_WITH_TUNER has been created in caslib CASUSER(casuser)
↪from binary data uploaded to Cloud Analytic Services.
NOTE: Start to tune the MILP
```

SolveCalls	Configurations	BestTime	Time
1	1	0.21	0.26
2	2	0.19	0.50
3	3	0.19	0.72
4	4	0.19	0.95
5	5	0.19	1.17
6	6	0.19	1.56
7	7	0.18	1.76
8	8	0.17	1.96
9	9	0.17	2.16
10	10	0.17	2.35

```
NOTE: Configuration limit reached.
NOTE: The tuning time is 2.35 seconds.
```

(continues on next page)

(continued from previous page)

```
>>> print(results)
```

	Configuration	conflictSearch	...	Sum of Run Times	Percentage Successful
0	0.0	automatic	...	0.20	100.0
1	1.0	none	...	0.17	100.0
2	2.0	none	...	0.17	100.0
3	3.0	moderate	...	0.17	100.0
4	4.0	none	...	0.18	100.0
5	5.0	none	...	0.18	100.0
6	6.0	aggressive	...	0.18	100.0
7	7.0	moderate	...	0.18	100.0
8	8.0	aggressive	...	0.19	100.0
9	9.0	automatic	...	0.36	100.0

```
>>> results = m.tune_parameters(
    milpParameters={'maxtime': 10},
    tunerParameters={'maxConfigs': 20, 'logfreq': 5},
    tuningParameters=[
        {'option': 'presolver', 'initial': 'none', 'values': ['basic',
↪ 'aggressive', 'none']},
        {'option': 'cutStrategy'},
        {'option': 'strongIter', 'initial': -1, 'values': [-1, 100, 1000]}
    ])

```

NOTE: Added action set 'optimization'.

NOTE: Uploading the problem DataFrame to the server.

NOTE: Cloud Analytic Services made the uploaded file available as table KNAPSACK\_↪WITH\_TUNER in caslib CASUSER(casuser).

NOTE: The table KNAPSACK\_WITH\_TUNER has been created in caslib CASUSER(casuser) ↪↪from binary data uploaded to Cloud Analytic Services.

NOTE: Start to tune the MILP

SolveCalls	Configurations	BestTime	Time
5	5	0.17	1.01
10	10	0.17	2.00
15	15	0.17	2.98
20	20	0.17	3.95

NOTE: Configuration limit reached.

NOTE: The tuning time is 3.95 seconds.

```
>>> print(results)
```

	Configuration	conflictSearch	...	Sum of Run Times	Percentage Successful
0	0.0	automatic	...	0.17	100.0
1	1.0	none	...	0.16	100.0
2	2.0	none	...	0.16	100.0
3	3.0	none	...	0.16	100.0
4	4.0	none	...	0.16	100.0
5	5.0	none	...	0.17	100.0
6	6.0	none	...	0.17	100.0
7	7.0	none	...	0.17	100.0
8	8.0	none	...	0.17	100.0
9	9.0	none	...	0.17	100.0
10	10.0	none	...	0.17	100.0
11	11.0	aggressive	...	0.17	100.0
12	12.0	none	...	0.17	100.0
13	13.0	aggressive	...	0.17	100.0
14	14.0	automatic	...	0.17	100.0
15	15.0	none	...	0.17	100.0
16	16.0	none	...	0.17	100.0
17	17.0	moderate	...	0.17	100.0

(continues on next page)



(continued from previous page)

18	18.0	moderate	...	0.17	100.0
19	19.0	none	...	0.17	100.0

**sasoptpy.Model.get\_solution****Model.get\_solution** (*self*, *vtype*='Primal', *solution*=None, *pivot*=False)

Returns the primal and dual problem solutions

**Parameters****vtype** [string, optional] *Primal* or *Dual***solution** [integer, optional] Solution number to be returned (for the MILP solver)**pivot** [boolean, optional] When set to *True*, returns multiple solutions in columns as a pivot table**Returns****solution** [pandas.DataFrame] Primal or dual solution table returned from the CAS action**Notes**

- If the *Model.solve()* method is used with *frame=True* parameter, the MILP solver returns multiple solutions. You can retrieve different results by using the *solution* parameter.

**Examples**

```
>>> m.solve()
>>> print(m.get_solution('Primal'))
```

	var	lb	ub	value	solution
0	x[clock]	0.0	1.797693e+308	0.0	1.0
1	x[pc]	0.0	1.797693e+308	5.0	1.0
2	x[headphone]	0.0	1.797693e+308	2.0	1.0
3	x[mug]	0.0	1.797693e+308	0.0	1.0
4	x[book]	0.0	1.797693e+308	0.0	1.0
5	x[pen]	0.0	1.797693e+308	1.0	1.0
6	x[clock]	0.0	1.797693e+308	0.0	2.0
7	x[pc]	0.0	1.797693e+308	5.0	2.0
8	x[headphone]	0.0	1.797693e+308	2.0	2.0
9	x[mug]	0.0	1.797693e+308	0.0	2.0
10	x[book]	0.0	1.797693e+308	0.0	2.0
11	x[pen]	0.0	1.797693e+308	0.0	2.0
12	x[clock]	0.0	1.797693e+308	1.0	3.0
13	x[pc]	0.0	1.797693e+308	4.0	3.0
...					

```
>>> print(m.get_solution('Primal', solution=2))
```

	var	lb	ub	value	solution
6	x[clock]	0.0	1.797693e+308	0.0	2.0
7	x[pc]	0.0	1.797693e+308	5.0	2.0
8	x[headphone]	0.0	1.797693e+308	2.0	2.0
9	x[mug]	0.0	1.797693e+308	0.0	2.0

(continues on next page)

(continued from previous page)

```

10      x[book]  0.0  1.797693e+308  0.0  2.0
11      x[pen]  0.0  1.797693e+308  0.0  2.0

```

```

>>> print(m.get_solution(pivot=True))
solution      1.0  2.0  3.0  4.0  5.0
var
x[book]       0.0  0.0  0.0  1.0  0.0
x[clock]      0.0  0.0  1.0  1.0  0.0
x[headphone]  2.0  2.0  1.0  1.0  0.0
x[mug]        0.0  0.0  0.0  1.0  0.0
x[pc]         5.0  5.0  4.0  1.0  0.0
x[pen]        1.0  0.0  0.0  1.0  0.0

```

```

>>> print(m.get_solution('Dual'))
      con  value  solution
0      weight_con  20.0      1.0
1      limit_con[clock]  0.0      1.0
2      limit_con[pc]  5.0      1.0
3      limit_con[headphone]  2.0      1.0
4      limit_con[mug]  0.0      1.0
5      limit_con[book]  0.0      1.0
6      limit_con[pen]  1.0      1.0
7      weight_con  19.0      2.0
8      limit_con[clock]  0.0      2.0
9      limit_con[pc]  5.0      2.0
10     limit_con[headphone]  2.0      2.0
11     limit_con[mug]  0.0      2.0
12     limit_con[book]  0.0      2.0
13     limit_con[pen]  0.0      2.0
...

```

```

>>> print(m.get_solution('dual', pivot=True))
solution      1.0  2.0  3.0  4.0  5.0
con
limit_con[book]  0.0  0.0  0.0  1.0  0.0
limit_con[clock]  0.0  0.0  1.0  1.0  0.0
limit_con[headphone]  2.0  2.0  1.0  1.0  0.0
limit_con[mug]  0.0  0.0  0.0  1.0  0.0
limit_con[pc]  5.0  5.0  4.0  1.0  0.0
limit_con[pen]  1.0  0.0  0.0  1.0  0.0
weight_con  20.0  19.0  20.0  19.0  0.0

```

## sasoptpy.Model.get\_variable\_value

`Model.get_variable_value(self, var)`

Returns the value of a variable

### Parameters

**var** [*Variable* or string] Variable reference

## Notes

- It is possible to get a variable's value by using the `Variable.get_value()` method, as long as the variable is not abstract.
- This method is a wrapper around `Variable.get_value()` and an overlook function for model components.

## sasoptpy.Model.get\_objective\_value

`Model.get_objective_value(self)`

Returns the optimal objective value

### Returns

**objective\_value** [float] Optimal objective value at current solution

## Notes

- This method should be used for getting the objective value after solve.
- In order to get the current value of the objective after changing variable values, you can use `m.get_objective().get_value()`.

## Examples

```
>>> m.solve()
>>> print(m.get_objective_value())
42.0
```

## sasoptpy.Model.get\_solution\_summary

`Model.get_solution_summary(self)`

Returns the solution summary table to the user

### Returns

**ss** [`swat.dataframe.SASDataFrame`] Solution summary table, that is obtained after `Model.solve()`

## Examples

```
>>> m.solve()
>>> soln = m.get_solution_summary()
>>> print(type(soln))
<class 'swat.dataframe.SASDataFrame'>
```

```
>>> print(soln)
Solution Summary
Label
Solver
Value
LP
```

(continues on next page)

(continued from previous page)

Algorithm	Dual Simplex
Objective Function	obj
Solution Status	Optimal
Objective Value	10
Primal Infeasibility	0
Dual Infeasibility	0
Bound Infeasibility	0
Iterations	2
Presolve Time	0.00
Solution Time	0.01

```
>>> print(soln.index)
Index(['Solver', 'Algorithm', 'Objective Function', 'Solution Status',
      'Objective Value', '', 'Primal Infeasibility',
      'Dual Infeasibility', 'Bound Infeasibility', '', 'Iterations',
      'Presolve Time', 'Solution Time'],
      dtype='object', name='Label')
```

```
>>> print(soln.loc['Solution Status', 'Value'])
Optimal
```

## sasoptpy.Model.get\_problem\_summary

`Model.get_problem_summary(self)`

Returns the problem summary table to the user

### Returns

`ps` [`swat.dataframe.SASDataFrame`] Problem summary table, that is obtained after `Model.solve()`

## Examples

```
>>> m.solve()
>>> ps = m.get_problem_summary()
>>> print(type(ps))
<class 'swat.dataframe.SASDataFrame'>
```

```
>>> print(ps)
Problem Summary
                                Value
Label
Problem Name                    modell
Objective Sense                Maximization
Objective Function                obj
RHS                             RHS
Number of Variables              2
Bounded Above                   0
Bounded Below                   2
Bounded Above and Below         0
Free                             0
Fixed                           0
Number of Constraints            2
```

(continues on next page)

(continued from previous page)

LE (<=)	1
EQ (=)	0
GE (>=)	1
Range	0
Constraint Coefficients	4

```
>>> print(ps.index)
Index(['Problem Name', 'Objective Sense', 'Objective Function', 'RHS',
      '', 'Number of Variables', 'Bounded Above', 'Bounded Below',
      'Bounded Above and Below', 'Free', 'Fixed', '',
      'Number of Constraints', 'LE (<=)', 'EQ (=)', 'GE (>=)', 'Range', '',
      'Constraint Coefficients'],
      dtype='object', name='Label')
```

```
>>> print(ps.loc['Number of Variables'])
Value                2
Name: Number of Variables, dtype: object
```

```
>>> print(ps.loc['Constraint Coefficients', 'Value'])
4
```

## sasoptpy.Model.get\_tuner\_results

`Model.get_tuner_results(self)`

Returns the tuning results

### Returns

**tunerResults** [dict] Returns tuner results as a dictionary.

Its members are

- Performance Information
- Tuner Information
- Tuner Summary
- Tuner Results

See also:

[`Model.tune\_parameters\(\)`](#)

## Examples

```
>>> m.tune_parameters(tunerParameters={'maxConfigs': 10})
>>> results = m.get_tuner_results()
```

### **sasoptpy.Model.print\_solution**

`Model.print_solution(self)`

Prints the current values of the variables

**See also:**

*`Model.get_solution()`*

#### **Notes**

- This function might not work for abstract variables and nonlinear models.

#### **Examples**

```
>>> m.solve()
>>> m.print_solution()
x: 2.0
y: 0.0
```

### **sasoptpy.Model.clear\_solution**

`Model.clear_solution(self)`

Clears the cached solution of the model

#### **Notes**

- This method cleans the optimal objective value and solution time parameters of the model.

#### **Export**

<i><code>Model.to_mps(self, **kwargs)</code></i>	Returns the problem in MPS format
<i><code>Model.to_optmodel(self, **kwargs)</code></i>	Returns the model in OPTMODEL format

### **sasoptpy.Model.to\_mps**

`Model.to_mps(self, **kwargs)`

Returns the problem in MPS format

## Examples

```
>>> print(n.to_mps())
      Field1 Field2 Field3  Field4 Field5  Field6  _id_
0      NAME                n      0.0          0.0    1
1      ROWS                NaN          NaN    2
2      MIN  myobj          NaN          NaN    3
3  COLUMNS                NaN          NaN    4
4                y  myobj      2.0          NaN    5
5      RHS                NaN          NaN    6
6  RANGES                NaN          NaN    7
7  BOUNDS                NaN          NaN    8
8      FR      BND      y      NaN          NaN    9
9  ENDATA                0.0          0.0   10
```

## sasoptpy.Model.to\_optmodel

`Model.to_optmodel(self, **kwargs)`  
Returns the model in OPTMODEL format

## Examples

```
>>> print(n.to_optmodel())
proc optmodel;
var y init 2;
min myobj = 2 * y;
solve;
quit;
```

## Internal functions

---

<code>Model._is_linear(self)</code>	Checks whether the model can be written as a linear model (in MPS format)
-------------------------------------	---

---

## sasoptpy.Model.\_is\_linear

`Model._is_linear(self)`  
Checks whether the model can be written as a linear model (in MPS format)

### Returns

**is\_linear** [boolean] True if model does not have any nonlinear components or abstract operations, False otherwise

## Deprecated

Deprecated since version 1.0.0.

The following method(s) are deprecated and will be removed in future minor updates.

---

`Model.to_frame(self, **kwargs)`

---

## sasoptpy.Model.to\_frame

`Model.to_frame(self, **kwargs)`

## 5.1.2 Expression

### Constructor

<code>Expression([exp, name])</code>	Creates a mathematical expression to represent model components
<code>Auxiliary(base[, prefix, suffix, operator, ...])</code>	Represents an auxiliary expression, often as a symbolic attribute
<code>Symbol(name)</code>	Represents a symbolic string, to be evaluated on server-side

## sasoptpy.Expression

**class Expression** (*exp=None, name=None*)

Bases: `object`

Creates a mathematical expression to represent model components

#### Parameters

- exp** [`Expression`, optional] An existing expression where arguments are being passed
- name** [string, optional] A local name for the expression

#### Notes

- Two other classes (`Variable` and `Constraint`) are subclasses of this class.
- Expressions are created automatically after linear math operations with variables.
- An expression object can be called when defining constraints and other expressions.



## Examples

```
>>> x = so.Variable(name='x')
>>> y = so.VariableGroup(3, name='y')
>>> e = so.Expression(exp=x + 3 * y[0] - 5 * y[1], name='exp1')
>>> print(e)
- 5.0 * y[1] + 3.0 * y[0] + x
>>> print(repr(e))
sasoptpy.Expression(exp = - 5.0 * y[1] + 3.0 * y[0] + x ,
                    name='exp1')
```

```
>>> sales = so.Variable(name='sales')
>>> material = so.Variable(name='material')
>>> profit = 5 * sales - 3 * material
>>> print(profit)
5.0 * sales - 3.0 * material
>>> print(repr(profit))
sasoptpy.Expression(exp = 5.0 * sales - 3.0 * material , name=None)
```

```
>>> import sasoptpy.abstract.math as sm
>>> f = sm.sin(x) + sm.min(y[1],1) ** 2
>>> print(type(f))
<class 'sasoptpy.core.Expression'>
>>> print(f)
sin(x) + (min(y[1] , 1)) ** (2)
```

## sasoptpy.Auxiliary

**class Auxiliary** (*base, prefix=None, suffix=None, operator=None, value=None*)

Bases: `sasoptpy.core.expression.Expression`

Represents an auxiliary expression, often as a symbolic attribute

### Parameters

- base** [*Expression*] Original owner of the auxiliary value
- prefix** [string, optional] Prefix of the expression
- suffix** [string, optional] Suffix of the expression
- operator** [string, optional] Wrapping operator
- value** [float, optional] Initial value of the symbolic object

## Notes

- Auxiliary objects are for internal use

## sasoptpy.Symbol

**class** **Symbol** (*name*)

Bases: `sasoptpy.core.expression.Expression`

Represents a symbolic string, to be evaluated on server-side

### Parameters

**name** [string] String to be symbolized

### Notes

- A Symbol object can be used for any values that does not translate to a value on client-side, but has meaning on execution. For example, `_N_` is a SAS symbol, which can be used in PROC OPTMODEL strings.

## General methods

<code>Expression.set_name(self[, name])</code>	Specifies the name of the expression
<code>Expression.set_permanent(self)</code>	Converts a temporary expression into a permanent one
<code>Expression.set_temporary(self)</code>	Converts expression into a temporary expression to enable in-place operations
<code>Expression.get_name(self)</code>	Returns the name of the object
<code>Expression.get_value(self)</code>	Calculates and returns the value of the linear expression
<code>Expression.get_dual(self)</code>	Returns the dual value

## sasoptpy.Expression.set\_name

`Expression.set_name` (*self*, *name=None*)

Specifies the name of the expression

### Parameters

**name** [string] Name of the expression

### Returns

**name** [string] Name of the expression after resolving conflicts

## Examples

```
>>> x = so.Variable(name='x')
>>> e = x**2 + 2*x + 1
>>> e.set_name('expansion')
```

### **sasoptpy.Expression.set\_permanent**

`Expression.set_permanent(self)`

Converts a temporary expression into a permanent one

#### **Parameters**

**name** [string, optional] Name of the expression

#### **Returns**

**name** [string] Name of the expression in the namespace

### **sasoptpy.Expression.set\_temporary**

`Expression.set_temporary(self)`

Converts expression into a temporary expression to enable in-place operations

### **sasoptpy.Expression.get\_name**

`Expression.get_name(self)`

Returns the name of the object

#### **Returns**

**name** [string] Name of the object

#### **Examples**

```
>>> m = so.Model()
>>> var1 = m.add_variables(name='x')
>>> print(var1.get_name())
x
```

### **sasoptpy.Expression.get\_value**

`Expression.get_value(self)`

Calculates and returns the value of the linear expression

#### **Returns**

**v** [float] Value of the expression

#### **Examples**

```
>>> sales = so.Variable(name='sales', init=10)
>>> material = so.Variable(name='material', init=3)
>>> profit = so.Expression(5 * sales - 3 * material)
>>> print(profit.get_value())
41
```

## sasoptpy.Expression.get\_dual

`Expression.get_dual(self)`

Returns the dual value

### Returns

**dual** [float] Dual value of the object

## Operations

<code>Expression.add(self, other[, sign])</code>	Combines two expressions and produces a new one
<code>Expression.copy(self[, name])</code>	Returns a copy of the <i>Expression</i> object
<code>Expression.mult(self, other)</code>	Multiplies the <i>Expression</i> by a scalar value
<code>Expression.get_member(self, key)</code>	Returns the requested member of the expression
<code>Expression.get_member_dict(self)</code>	Returns an ordered dictionary of elements
<code>Expression.get_member_value(self, key)</code>	Returns coefficient of requested member
<code>Expression.get_constant(self)</code>	Returns the constant term in the expression
<code>Expression.set_member(self, key, ref, val[, op])</code>	Adds a new member or changes an existing member
<code>Expression.set_member_value(self, key, value)</code>	Changes the coefficient of the requested member
<code>Expression.add_to_member_value(self, key, value)</code>	Adds <i>value</i> to the coefficient of the requested member
<code>Expression.mult_member_value(self, key, value)</code>	Multiplies the coefficient of the requested member by the specified <i>value</i>
<code>Expression.copy_member(self, key, exp)</code>	Copies the member of another expression
<code>Expression.delete_member(self, key)</code>	Deletes the requested member from the core dictionary

## sasoptpy.Expression.add

`Expression.add(self, other, sign=1)`

Combines two expressions and produces a new one

### Parameters

**other** [float or *Expression*] Second expression or constant value to be added

**sign** [int, optional] Sign of the addition, 1 or -1

### Returns

**r** [*Expression*] Reference to the outcome of the operation

## Notes

- It is preferable to use regular Python operation, instead of calling this method:

```
>>> e = x - y
>>> f = 3 * x + 2 * y
>>> g = e + f
>>> print(g)
4 * x + y
```

**sasoptpy.Expression.copy**`Expression.copy (self, name=None)`Returns a copy of the *Expression* object**Parameters****name** [string, optional] Name for the copy**Returns****r** [*Expression*] Copy of the object**Examples**

```

>>> x = so.Variable(name='x')
>>> y = so.VariableGroup(1, name='y')
>>> e = so.Expression(7 * x - y[0], name='e')
>>> print(repr(e))
sasoptpy.Expression(exp = - y[0] + 7.0 * x , name='e')
>>> f = e.copy(name='f')
>>> print(repr(f))
sasoptpy.Expression(exp = - y[0] + 7.0 * x , name='f')

```

**sasoptpy.Expression.mult**`Expression.mult (self, other)`Multiplies the *Expression* by a scalar value**Parameters****other** [*Expression* or int] Second expression to be multiplied**Returns****r** [*Expression*] A new *Expression* that represents the multiplication**Notes**

- This method is mainly for internal use.
- It is preferable to use regular Python operation, instead of calling this method:

```

>>> e = 3 * (x-y)
>>> f = 3
>>> g = e*f
>>> print(g)
9 * x - 9 * y

```

### **sasoptpy.Expression.get\_member**

`Expression.get_member(self, key)`

Returns the requested member of the expression

#### **Parameters**

**key** [string] Identifier of the member, name for single objects

#### **Returns**

**member** [dict] A dictionary of coefficient, operator, and reference of member

### **sasoptpy.Expression.get\_member\_dict**

`Expression.get_member_dict(self)`

Returns an ordered dictionary of elements

### **sasoptpy.Expression.get\_member\_value**

`Expression.get_member_value(self, key)`

Returns coefficient of requested member

#### **Parameters**

**key** [string] Identifier of the member

#### **Returns**

**value** [float] Coefficient value of the requested member

### **sasoptpy.Expression.get\_constant**

`Expression.get_constant(self)`

Returns the constant term in the expression

#### **Examples**

```
>>> x = so.Variable(name='x')
>>> e = 2 * x + 5
>>> print(e.get_constant())
5
```

### **sasoptpy.Expression.set\_member**

`Expression.set_member(self, key, ref, val, op=None)`

Adds a new member or changes an existing member

#### **Parameters**

**key** [string] Identifier of the new or existing member

**ref** [Object] A reference to the new or existing member

**val** [float] Initial coefficient of the new or existing member

**op** [string, optional] Operator, if member has multiple children

### **sasoptpy.Expression.set\_member\_value**

`Expression.set_member_value(self, key, value)`

Changes the coefficient of the requested member

#### **Parameters**

**key** [string] Identifier of the member

**value** [float] New coefficient value of the member

### **sasoptpy.Expression.add\_to\_member\_value**

`Expression.add_to_member_value(self, key, value)`

Adds *value* to the coefficient of the requested member

#### **Parameters**

**key** [string] Identifier of the member

**value** [float] Value to be added

### **sasoptpy.Expression.mult\_member\_value**

`Expression.mult_member_value(self, key, value)`

Multiplies the coefficient of the requested member by the specified *value*

#### **Parameters**

**key** [string] Identifier of the member

**value** [float] Value to be multiplied with

### **sasoptpy.Expression.copy\_member**

`Expression.copy_member(self, key, exp)`

Copies the member of another expression

#### **Parameters**

**key** [string] Identifier of the member

**exp** [*Expression*] Other expression to be copied from

**sasoptpy.Expression.delete\_member**

`Expression.delete_member` (*self*, *key*)  
Deletes the requested member from the core dictionary

**Class methods**

---

`Expression.to_expression`(*obj*)

---

**sasoptpy.Expression.to\_expression**

**classmethod** `Expression.to_expression` (*obj*)

**Private Methods**

<code>Expression._expr</code> ( <i>self</i> )	Generates the OPTMODEL-compatible string representation of the object
<code>Expression._is_linear</code> ( <i>self</i> )	Checks whether the expression is composed of linear components
<code>Expression._relational</code> ( <i>self</i> , <i>other</i> , <i>direction_</i> )	Creates a logical relation between <i>Expression</i> objects
<code>Expression.__repr__</code> ( <i>self</i> )	Returns a string representation of the object
<code>Expression.__str__</code> ( <i>self</i> )	Generates a representation string that is Python-compatible

**sasoptpy.Expression.\_expr**

`Expression._expr` (*self*)  
Generates the OPTMODEL-compatible string representation of the object

**Examples**

```
>>> x = so.Variable(name='x')
>>> y = so.Variable(name='y')
>>> f = x + y ** 2
>>> print(f)
x + (y) ** (2)
>>> print(f._expr())
x + (y) ^ (2)
```



**sasoptpy.Expression.\_is\_linear**

Expression.**\_is\_linear** (*self*)

Checks whether the expression is composed of linear components

**Returns**

**is\_linear** [boolean] True if the expression is linear, False otherwise

**Examples**

```
>>> x = so.Variable()
>>> e = x*x
>>> print(e.is_linear())
False
```

```
>>> f = x*x + x*x - 2*x*x + 5
>>> print(f.is_linear())
True
```

**sasoptpy.Expression.\_relational**

Expression.**\_relational** (*self*, *other*, *direction\_*)

Creates a logical relation between *Expression* objects

**Parameters**

**other** [*Expression*] Expression on the other side of the relation with respect to self

**direction\_** [string] Direction of the logical relation, either *E*, *L*, or *G*

**Returns**

**generated\_constraint** [*Constraint*] Constraint generated as a result of linear relation

**sasoptpy.Expression.\_\_repr\_\_**

Expression.**\_\_repr\_\_** (*self*)

Returns a string representation of the object

**Examples**

```
>>> x = so.Variable(name='x')
>>> y = so.Variable(name='y')
>>> f = x + y ** 2
>>> print(repr(f))
sasoptpy.Expression(exp = x + (y) ** (2), name=None)
```

## sasoptpy.Expression.\_\_str\_\_

Expression.\_\_str\_\_(self)  
Generates a representation string that is Python-compatible

### Examples

```
>>> f = x + y ** 2
>>> print(str(f))
x + (y) ** (2)
```

## 5.1.3 Objective

### Constructor

---

<i>Objective</i> (**kwargs)	Objective represents expressions with sense and used as target value in optimization
-----------------------------	--

---

## sasoptpy.Objective

**class Objective**(\*\*kwargs)  
Bases: sasoptpy.core.expression.Expression  
Objective represents expressions with sense and used as target value in optimization

### Parameters

**exp** [*Expression*] Objective as an expression  
**name** [string] Unique name of the expression  
**sense** [string, optional] Direction of the objective, sasoptpy.MIN (default) or sasoptpy.MAX

### Examples

```
>>> m = so.Model(name='test_objective')
>>> x = m.add_variable(name='x')
>>> obj = m.set_objective(2 * x - x ** 3, sense=so.MIN, name='new_obj')
>>> str(m.get_objective())
2 * x - (x) ** (3)
>>> type(obj)
sasoptpy.Objective
```

## Methods

<code>Objective.set_sense(self, sense)</code>	Specifies the objective sense (direction)
<code>Objective.get_sense(self)</code>	Returns the objective sense (direction)

### `sasoptpy.Objective.set_sense`

`Objective.set_sense(self, sense)`  
Specifies the objective sense (direction)

#### Parameters

**sense** [string] `sasoptpy.MIN` or `sasoptpy.MAX`

### `sasoptpy.Objective.get_sense`

`Objective.get_sense(self)`  
Returns the objective sense (direction)

## 5.1.4 Variable

### Constructor

<code>Variable(**kwargs)</code>	Creates an optimization variable to be used inside models
---------------------------------	---

### `sasoptpy.Variable`

**class Variable** (*\*\*kwargs*)  
Bases: `sasoptpy.core.expression.Expression`  
Creates an optimization variable to be used inside models

#### Parameters

**name** [string] Name of the variable

**vartype** [string, optional] Type of the variable

**lb** [float, optional] Lower bound of the variable

**ub** [float, optional] Upper bound of the variable

**init** [float, optional] Initial value of the variable

**abstract** [boolean, optional] When set to *True*, indicates that the variable is abstract

See also:

`sasoptpy.Model.add_variable()`

## Examples

```
>>> x = so.Variable(name='x', lb=0, ub=20, vartype=so.CONT)
>>> print(repr(x))
sasoptpy.Variable(name='x', lb=0, ub=20, vartype='CONT')
```

```
>>> y = so.Variable(name='y', init=1, vartype=so.INT)
>>> print(repr(y))
sasoptpy.Variable(name='y', lb=0, ub=inf, init=1, vartype='INT')
```

## Attributes

**lb** Lower bound of the variable

**ub** Upper bound of the variable

## Methods

<code>Variable.set_bounds(self, \*[, lb, ub])</code>	Changes bounds on a variable
<code>Variable.set_init(self[, init])</code>	Changes initial value of a variable
<code>Variable.get_type(self)</code>	Returns the type of variable
<code>Variable.get_attributes(self)</code>	Returns an ordered dictionary of main attributes

## `sasoptpy.Variable.set_bounds`

`Variable.set_bounds` (*self*, \*, *lb=None*, *ub=None*)  
Changes bounds on a variable

### Parameters

**lb** [float or *Expression*] Lower bound of the variable

**ub** [float or *Expression*] Upper bound of the variable

## Examples

```
>>> x = so.Variable(name='x', lb=0, ub=20)
>>> print(repr(x))
sasoptpy.Variable(name='x', lb=0, ub=20, vartype='CONT')
>>> x.set_bounds(lb=5, ub=15)
>>> print(repr(x))
sasoptpy.Variable(name='x', lb=5, ub=15, vartype='CONT')
```

### sasoptpy.Variable.set\_init

`Variable.set_init(self, init=None)`

Changes initial value of a variable

#### Parameters

**init** [float or None] Initial value of the variable

#### Examples

```
>>> x = so.Variable(name='x')
>>> x.set_init(5)
```

```
>>> y = so.Variable(name='y', init=3)
>>> y.set_init()
```

### sasoptpy.Variable.get\_type

`Variable.get_type(self)`

Returns the type of variable

Valid values are:

- `sasoptpy.CONT`
- `sasoptpy.INT`
- `sasoptpy.BIN`

### sasoptpy.Variable.get\_attributes

`Variable.get_attributes(self)`

Returns an ordered dictionary of main attributes

#### Returns

**attributes** [OrderedDict] Dictionary consists of *init*, *lb*, and *ub* attributes

### Inherited Methods

<code>Variable.copy(self[, name])</code>	Returns a copy of the <i>Expression</i> object
<code>Variable.get_dual(self)</code>	Returns the dual value
<code>Variable.get_name(self)</code>	Returns the name of the object
<code>Variable.get_value(self)</code>	Returns the value of the variable

### `sasoptpy.Variable.copy`

`Variable.copy` (*self*, *name=None*)

Returns a copy of the *Expression* object

#### Parameters

**name** [string, optional] Name for the copy

#### Returns

**r** [*Expression*] Copy of the object

### Examples

```
>>> x = so.Variable(name='x')
>>> y = so.VariableGroup(1, name='y')
>>> e = so.Expression(7 * x - y[0], name='e')
>>> print(repr(e))
sasoptpy.Expression(exp = - y[0] + 7.0 * x , name='e')
>>> f = e.copy(name='f')
>>> print(repr(f))
sasoptpy.Expression(exp = - y[0] + 7.0 * x , name='f')
```

### `sasoptpy.Variable.get_dual`

`Variable.get_dual` (*self*)

Returns the dual value

#### Returns

**dual** [float] Dual value of the object

### `sasoptpy.Variable.get_name`

`Variable.get_name` (*self*)

Returns the name of the object

#### Returns

**name** [string] Name of the object

### Examples

```
>>> m = so.Model()
>>> var1 = m.add_variables(name='x')
>>> print(var1.get_name())
x
```

**sasoptpy.Variable.get\_value**`Variable.get_value(self)`

Returns the value of the variable

**Returns****value** [float] Value of the variable**Examples**

```
>>> x.set_value(20)
>>> x.get_value()
20
```

**5.1.5 Variable Group****Constructor**


---

<code>VariableGroup(**kwargs)</code>	Creates a group of <i>Variable</i> objects
--------------------------------------	--

---

**sasoptpy.VariableGroup****class VariableGroup** (*\*\*kwargs*)Bases: `sasoptpy.core.group.Group`Creates a group of *Variable* objects**Parameters****argv** [list, dict, int, `pandas.Index`] Loop index for variable group**name** [string, optional] Name (prefix) of the variables**vartype** [string, optional] Type of variables, *BIN*, *INT*, or *CONT***lb** [list, dict, `pandas.Series`, optional] Lower bounds of variables**ub** [list, dict, `pandas.Series`, optional] Upper bounds of variables**init** [float, optional] Initial values of variables

See also:

`sasoptpy.Model.add_variables()``sasoptpy.Model.include()`

## Notes

- When working with a single model, use the `sasoptpy.Model.add_variables()` method.
- If a variable group object is created, it can be added to a model using the `sasoptpy.Model.include()` method.
- An individual variable inside the group can be accessed using indices.

```
>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z', lb=0, ub=10)
>>> print(repr(z[0, 'a']))
sasoptpy.Variable(name='z_0_a', lb=0, ub=10, vartype='CONT')
```

## Examples

```
>>> PERIODS = ['Period1', 'Period2', 'Period3']
>>> production = so.VariableGroup(PERIODS, vartype=so.INT,
                                name='production', lb=10)

>>> print(production)
Variable Group (production) [
  [Period1: production['Period1']]
  [Period2: production['Period2']]
  [Period3: production['Period3']]
]
```

```
>>> x = so.VariableGroup(4, vartype=so.BIN, name='x')
>>> print(x)
Variable Group (x) [
  [0: x[0]]
  [1: x[1]]
  [2: x[2]]
  [3: x[3]]
]
```

```
>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z')
>>> print(z)
Variable Group (z) [
  [(0, 'a'): z[0, 'a']]
  [(0, 'b'): z[0, 'b']]
  [(0, 'c'): z[0, 'c']]
  [(1, 'a'): z[1, 'a']]
  [(1, 'b'): z[1, 'b']]
  [(1, 'c'): z[1, 'c']]
]
>>> print(repr(z))
sasoptpy.VariableGroup([0, 1], ['a', 'b', 'c'], name='z')
```



## Methods

<code>VariableGroup.get_name(self)</code>	Returns the name of the variable group
<code>VariableGroup.get_attributes(self)</code>	Returns an ordered dictionary of main attributes
<code>VariableGroup.get_type(self)</code>	Returns the type of variable
<code>VariableGroup.get_members(self)</code>	Returns a dictionary of members
<code>VariableGroup.set_bounds(self[, lb, ub, members])</code>	Specifies or updates bounds for the variable group
<code>VariableGroup.set_init(self, init)</code>	Specifies or updates the initial values
<code>VariableGroup.mult(self, vector)</code>	Quick multiplication method for the variable groups
<code>VariableGroup.sum(self, \*argv)</code>	Quick sum method for the variable groups

### sasoptpy.VariableGroup.get\_name

`VariableGroup.get_name(self)`  
Returns the name of the variable group

#### Returns

**name** [string] Name of the variable group

#### Examples

```
>>> m = so.Model(name='m')
>>> var1 = m.add_variables(4, name='x')
>>> print(var1.get_name())
x
```

### sasoptpy.VariableGroup.get\_attributes

`VariableGroup.get_attributes(self)`  
Returns an ordered dictionary of main attributes

#### Returns

**attributes** [OrderedDict] The dictionary consists of *init*, *lb*, and *ub* attributes

### sasoptpy.VariableGroup.get\_type

`VariableGroup.get_type(self)`  
Returns the type of variable

Possible values are:

- `sasoptpy.CONT`
- `sasoptpy.INT`
- `sasoptpy.BIN`

## Examples

```
>>> z = so.VariableGroup(3, name='z', vartype=so.INT)
>>> z.get_type()
'INT'
```

### `sasoptpy.VariableGroup.get_members`

`VariableGroup.get_members` (*self*)  
Returns a dictionary of members

### `sasoptpy.VariableGroup.set_bounds`

`VariableGroup.set_bounds` (*self*, *lb=None*, *ub=None*, *members=True*)  
Specifies or updates bounds for the variable group

#### Parameters

**lb** [float, `pandas.Series`, optional] Lower bound

**ub** [float, `pandas.Series`, optional] Upper bound

## Examples

```
>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z', lb=0, ub=10)
>>> print(repr(z[0, 'a']))
sasoptpy.Variable(name='z_0_a', lb=0, ub=10, vartype='CONT')
>>> z.set_bounds(lb=3, ub=5)
>>> print(repr(z[0, 'a']))
sasoptpy.Variable(name='z_0_a', lb=3, ub=5, vartype='CONT')
```

```
>>> u = so.VariableGroup(['a', 'b', 'c', 'd'], name='u')
>>> lb_vals = pd.Series([1, 4, 0, -1], index=['a', 'b', 'c', 'd'])
>>> u.set_bounds(lb=lb_vals)
>>> print(repr(u['b']))
sasoptpy.Variable(name='u_b', lb=4, ub=inf, vartype='CONT')
```

### `sasoptpy.VariableGroup.set_init`

`VariableGroup.set_init` (*self*, *init*)  
Specifies or updates the initial values

#### Parameters

**init** [float, list, dict, `pandas.Series`] Initial value of the variables

## Examples

```
>>> m = so.Model(name='m')
>>> y = m.add_variables(3, name='y')
>>> print(y._defn())
var y {{0,1,2}};
>>> y.set_init(5)
>>> print(y._defn())
var y {{0,1,2}} init 5;
```

## sasoptpy.VariableGroup.mult

VariableGroup.**mult** (*self*, *vector*)

Quick multiplication method for the variable groups

### Parameters

**vector** [list, dictionary, `pandas.Series`, or `pandas.DataFrame`] Vector to be multiplied with the variable group

### Returns

**r** [*Expression*] An expression that is the product of the variable group with the specified vector

## Examples

Multiplying with a list

```
>>> x = so.VariableGroup(4, vartype=so.BIN, name='x')
>>> e1 = x.mult([1, 5, 6, 10])
>>> print(e1)
10.0 * x[3] + 6.0 * x[2] + x[0] + 5.0 * x[1]
```

Multiplying with a dictionary

```
>>> y = so.VariableGroup([0, 1], ['a', 'b'], name='y', lb=0, ub=10)
>>> dvals = {(0, 'a'): 1, (0, 'b'): 2, (1, 'a'): -1, (1, 'b'): 5}
>>> e2 = y.mult(dvals)
>>> print(e2)
2.0 * y[0, 'b'] - y[1, 'a'] + y[0, 'a'] + 5.0 * y[1, 'b']
```

Multiplying with a `pandas.Series` object

```
>>> u = so.VariableGroup(['a', 'b', 'c', 'd'], name='u')
>>> ps = pd.Series([0.1, 1.5, -0.2, 0.3], index=['a', 'b', 'c', 'd'])
>>> e3 = u.mult(ps)
>>> print(e3)
1.5 * u['b'] + 0.1 * u['a'] - 0.2 * u['c'] + 0.3 * u['d']
```

Multiplying with a `pandas.DataFrame` object

```
>>> data = np.random.rand(3, 3)
>>> df = pd.DataFrame(data, columns=['a', 'b', 'c'])
>>> print(df)
```

(continues on next page)

(continued from previous page)

```

NOTE: Initialized model model1
      a      b      c
0  0.966524  0.237081  0.944630
1  0.821356  0.074753  0.345596
2  0.065229  0.037212  0.136644
>>> y = m.add_variables(3, ['a', 'b', 'c'], name='y')
>>> e = y.mult(df)
>>> print(e)
0.9665237354418064 * y[0, 'a'] + 0.23708064143289442 * y[0, 'b'] +
0.944629500537536 * y[0, 'c'] + 0.8213562592159828 * y[1, 'a'] +
0.07475256894157478 * y[1, 'b'] + 0.3455957019116668 * y[1, 'c'] +
0.06522945752546017 * y[2, 'a'] + 0.03721153533250843 * y[2, 'b'] +
0.13664422498043194 * y[2, 'c']

```

## sasoptpy.VariableGroup.sum

VariableGroup.**sum**(*self*, \**argv*)

Quick sum method for the variable groups

### Parameters

**argv** [Arguments] List of indices for the sum

### Returns

**r** [*Expression*] Expression that represents the sum of all variables in the group

## Examples

```

>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z', lb=0, ub=10)
>>> e1 = z.sum('*', '*')
>>> print(e1)
z[1, 'c'] + z[1, 'a'] + z[1, 'b'] + z[0, 'a'] + z[0, 'b'] +
z[0, 'c']
>>> e2 = z.sum('*', 'a')
>>> print(e2)
z[1, 'a'] + z[0, 'a']
>>> e3 = z.sum('*', ['a', 'b'])
>>> print(e3)
z[1, 'a'] + z[0, 'b'] + z[1, 'b'] + z[0, 'a']

```

## 5.1.6 Constraint

### Constructor

---

*Constraint*(\*\*kwargs)

Creates a linear or quadratic constraint for optimization models

---

## sasoptpy.Constraint

**class Constraint** (\*\*kwargs)

Bases: `sasoptpy.core.expression.Expression`

Creates a linear or quadratic constraint for optimization models

Constraints should be created by adding logical relations to *Expression* objects.

### Parameters

**exp** [*Expression*] A logical expression that forms the constraint

**direction** [string, optional] Direction of the logical expression

Possible values are

- *E* for equality (=) constraints
- *L* for less than or equal to (<=) constraints
- *G* for greater than or equal to (>=) constraints

**name** [string, optional] Name of the constraint object

**crange** [float, optional] Range for ranged constraints

See also:

*sasoptpy.Model.add\_constraint()*

## Notes

- A constraint can be generated in two different ways:
  - Using the *sasoptpy.Model.add\_constraint()* method

```
>>> m = so.Model(name='m')
>>> c1 = m.add_constraint(3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint( - 5.0 * y + 3.0 * x <= 10, name='c1')
```

- Using the constructor

```
>>> c1 = sasoptpy.Constraint(3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint( - 5.0 * y + 3.0 * x <= 10, name='c1')
```

- The same constraint can be included into other models using the *Model.include()* method.

## Examples

```
>>> x = so.Variable(name='x')
>>> y = so.Variable(name='y')
>>> c1 = so.Constraint( 3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint( - 5.0 * y + 3.0 * x <= 10, name='c1')
```

```
>>> c2 = so.Constraint( - x + 2 * y - 5, direction='L', name='c2')
sasoptpy.Constraint( - x + 2.0 * y <= 5, name='c2')
```

## Methods

<code>Constraint.get_value(self[, rhs])</code>	Returns the current value of the constraint
<code>Constraint.get_dual(self)</code>	Returns the dual value if exists
<code>Constraint.set_block(self, block_number)</code>	Sets the decomposition block number for a constraint
<code>Constraint.set_direction(self, direction)</code>	Changes the direction of a constraint
<code>Constraint.set_rhs(self, value)</code>	Changes the constant value (right-hand side) of a constraint
<code>Constraint.update_var_coef(self, var, value)</code>	Updates the coefficient of a variable inside the constraint

## sasoptpy.Constraint.get\_value

`Constraint.get_value(self, rhs=False)`  
Returns the current value of the constraint

### Parameters

**rhs** [boolean, optional] When set to *True*, includes constant values to the value of the constraint. Default is *False*.

## Examples

```
>>> x = so.Variable(name='x', init=2)
>>> c = so.Constraint(x ** 2 + 2 * x <= 15, name='c')
>>> print(c.get_value())
8
>>> print(c.get_value(rhs=True))
-7
```

**sasoptpy.Constraint.get\_dual**

`Constraint.get_dual(self)`  
Returns the dual value if exists

**Returns**

**dual** [float] Dual value of the constraint

**sasoptpy.Constraint.set\_block**

`Constraint.set_block(self, block_number)`  
Sets the decomposition block number for a constraint

**Parameters**

**block\_number** [int] Block number of the constraint

**Examples**

```
>>> c1 = m.add_constraints((x + 2 * y[i] <= 5 for i in NODES),
                           name='c1')
>>> for i in NODES:
    c1[i].set_block(i)
```

**sasoptpy.Constraint.set\_direction**

`Constraint.set_direction(self, direction)`  
Changes the direction of a constraint

**Parameters**

**direction** [string] Direction of the constraint

Possible values are

- *E* for equality (=) constraints
- *L* for less than or euqal to (<=) constraints
- *G* for greater than or equal to (>=) constraints

**Examples**

```
>>> c1 = so.Constraint(exp=3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint( 3.0 * x - 5.0 * y <= 10, name='c1')
>>> c1.set_direction('G')
>>> print(repr(c1))
sasoptpy.Constraint( 3.0 * x - 5.0 * y >= 10, name='c1')
```

### `sasoptpy.Constraint.set_rhs`

`Constraint.set_rhs(self, value)`

Changes the constant value (right-hand side) of a constraint

#### Parameters

**value** [float] New right-hand side value for the constraint

#### Examples

```
>>> x = m.add_variable(name='x')
>>> y = m.add_variable(name='y')
>>> c = m.add_constraint(x + 3*y <= 10, name='con_1')
>>> print(c)
x + 3.0 * y <= 10
>>> c.set_rhs(5)
>>> print(c)
x + 3.0 * y <= 5
```

### `sasoptpy.Constraint.update_var_coef`

`Constraint.update_var_coef(self, var, value)`

Updates the coefficient of a variable inside the constraint

#### Parameters

**var** [*Variable*] Variable to be updated

**value** [float] Coefficient of the variable in the constraint

See also:

`sasoptpy.Model.set_coef()`

#### Examples

```
>>> c1 = so.Constraint(exp=3 * x - 5 * y <= 10, name='c1')
>>> print(repr(c1))
sasoptpy.Constraint(- 5.0 * y + 3.0 * x <= 10, name='c1')
>>> c1.update_var_coef(x, -1)
>>> print(repr(c1))
sasoptpy.Constraint(- 5.0 * y - x <= 10, name='c1')
```



## 5.1.7 Constraint Group

### Constructor

<code>ConstraintGroup(**kwargs)</code>	Creates a group of <i>Constraint</i> objects
--	--

### sasoptpy.ConstraintGroup

**class** `ConstraintGroup` (*\*\*kwargs*)

Bases: `sasoptpy.core.group.Group`

Creates a group of *Constraint* objects

#### Parameters

**argv** [Generator-type object] A Python generator that includes *Expression* objects

**name** [string, optional] Name (prefix) of the constraints

See also:

`sasoptpy.Model.add_constraints()`

`sasoptpy.Model.include()`

#### Notes

Use `sasoptpy.Model.add_constraints()` when working with a single model.

#### Examples

```
>>> var_ind = ['a', 'b', 'c', 'd']
>>> u = so.VariableGroup(var_ind, name='u')
>>> t = so.Variable(name='t')
>>> cg = so.ConstraintGroup((u[i] + 2 * t <= 5 for i in var_ind), name='cg')
>>> print(cg)
Constraint Group (cg) [
  [a: 2.0 * t + u['a'] <= 5]
  [b: u['b'] + 2.0 * t <= 5]
  [c: 2.0 * t + u['c'] <= 5]
  [d: 2.0 * t + u['d'] <= 5]
]
```

```
>>> z = so.VariableGroup(2, ['a', 'b', 'c'], name='z', lb=0, ub=10)
>>> cg2 = so.ConstraintGroup((2 * z[i, j] + 3 * z[i-1, j] >= 2 for i in
                             [1] for j in ['a', 'b', 'c']), name='cg2')
>>> print(cg2)
Constraint Group (cg2) [
  [(1, 'a'): 3.0 * z[0, 'a'] + 2.0 * z[1, 'a'] >= 2]
  [(1, 'b'): 2.0 * z[1, 'b'] + 3.0 * z[0, 'b'] >= 2]
  [(1, 'c'): 2.0 * z[1, 'c'] + 3.0 * z[0, 'c'] >= 2]
]
```

## Methods

<code>ConstraintGroup.get_name(self)</code>	Returns the name of the constraint group
<code>ConstraintGroup.get_all_keys(self)</code>	Returns a list of all keys (indices) in the group
<code>ConstraintGroup.get_expressions(self[, rhs])</code>	Returns constraints as a list of expressions
<code>ConstraintGroup.get_members(self)</code>	Returns a dictionary of members

### `sasoptpy.ConstraintGroup.get_name`

`ConstraintGroup.get_name(self)`  
Returns the name of the constraint group

#### Returns

**name** [string] Name of the constraint group

### Examples

```
>>> m = so.Model(name='m')
>>> x = m.add_variable(name='x')
>>> indices = ['a', 'b', 'c']
>>> y = m.add_variables(indices, name='y')
>>> c1 = m.add_constraints((x + y[i] <= 4 for i in indices),
                           name='con1')
>>> print(c1.get_name())
con1
```

### `sasoptpy.ConstraintGroup.get_all_keys`

`ConstraintGroup.get_all_keys(self)`  
Returns a list of all keys (indices) in the group

### `sasoptpy.ConstraintGroup.get_expressions`

`ConstraintGroup.get_expressions(self, rhs=False)`  
Returns constraints as a list of expressions

#### Parameters

**rhs** [boolean, optional] When set to *True*, passes the the constant part (rhs) of the constraint

#### Returns

**df** [`pandas.DataFrame`] Returns a DataFrame that consists of constraints as expressions

## Examples

```
>>> m = so.Model(name='m')
>>> var_ind = ['a', 'b', 'c', 'd']
>>> u = m.add_variables(var_ind, name='u')
>>> t = m.add_variable(name='t')
>>> cg = so.ConstraintGroup((u[i] + 2 * t <= 5 for i in var_ind),
                             name='cg')
>>> ce = cg.get_expressions()
>>> print(ce)
              cg
a  u[a] + 2 * t
b  u[b] + 2 * t
c  u[c] + 2 * t
d  u[d] + 2 * t
>>> ce_rhs = cg.get_expressions(rhs=True)
>>> print(ce_rhs)
              cg
a  u[a] + 2 * t - 5
b  u[b] + 2 * t - 5
c  u[c] + 2 * t - 5
d  u[d] + 2 * t - 5
```

## sasoptpy.ConstraintGroup.get\_members

`ConstraintGroup.get_members(self)`

Returns a dictionary of members

## 5.1.8 Workspace

### Constructor

---

*Workspace*(name[, session])

---

Workspace represents an OPTMODEL block that allows multiple solves

---

## sasoptpy.Workspace

**class Workspace** (name, session=None)

Bases: `object`

Workspace represents an OPTMODEL block that allows multiple solves

### Parameters

**name** [string] Name of the workspace

**session** [`saspy.SASsession` or `swat.cas.connection.CAS`, optional] Session to be submitted

## Methods

<code>Workspace.get_elements(self)</code>	Returns a list of elements in the workspace
<code>Workspace.set_active_model(self, model)</code>	Marks the specified model as active; to be used in solve statements
<code>Workspace.append(self, element)</code>	Appends a new element (operation or statement) to the workspace
<code>Workspace.submit(self, <i>\**kwargs</i>)</code>	Submits the workspace as an OPTMODEL block and returns solutions
<code>Workspace.parse_solve_responses(self)</code>	Retrieves the solutions to all solve statements
<code>Workspace.parse_print_responses(self)</code>	Retrieves responses to all print statements
<code>Workspace.get_variable(self, name)</code>	Obtains the value of a specified variable name
<code>Workspace.set_variable_value(self, name, value)</code>	Specifies the value of a variable
<code>Workspace.to_optmodel(self)</code>	Returns equivalent OPTMODEL code of the workspace

### `sasoptpy.Workspace.get_elements`

`Workspace.get_elements(self)`  
Returns a list of elements in the workspace

### `sasoptpy.Workspace.set_active_model`

`Workspace.set_active_model(self, model)`  
Marks the specified model as active; to be used in solve statements

#### Parameters

**model** [*Model*] Model to be activated

### `sasoptpy.Workspace.append`

`Workspace.append(self, element)`  
Appends a new element (operation or statement) to the workspace

#### Parameters

**element** [*sasoptpy.abstract.Statement*] Any statement that can be appended

### `sasoptpy.Workspace.submit`

`Workspace.submit(self, **kwargs)`  
Submits the workspace as an OPTMODEL block and returns solutions

**sasoptpy.Workspace.parse\_solve\_responses**

`Workspace.parse_solve_responses` (*self*)  
Retrieves the solutions to all solve statements

**sasoptpy.Workspace.parse\_print\_responses**

`Workspace.parse_print_responses` (*self*)  
Retrieves responses to all print statements

**sasoptpy.Workspace.get\_variable**

`Workspace.get_variable` (*self*, *name*)  
Obtains the value of a specified variable name

**Parameters**

**name** [string] Name of the variable

**sasoptpy.Workspace.set\_variable\_value**

`Workspace.set_variable_value` (*self*, *name*, *value*)  
Specifies the value of a variable

**Parameters**

**name** [string] Name of the variable

**value** [float] New value of the variable

**sasoptpy.Workspace.to\_optmodel**

`Workspace.to_optmodel` (*self*)  
Returns equivalent OPTMODEL code of the workspace

**Returns**

**optmodel** [string] Generated OPTMODEL code of the workspace object

## 5.2 Abstract

### 5.2.1 Abstract

**Main classes**

<code>Parameter(**kwargs)</code>	Represents a problem input parameter
<code>ParameterGroup(**kwargs)</code>	Represents a group of input parameters
<code>Set(**kwargs)</code>	Creates an index set to be represented inside PROC OPTMODEL

Continued on next page

Table 25 – continued from previous page

<code>SetIterator</code> (initset[, name, datatype])	Creates an iterator object for a given Set
<code>SetIteratorGroup</code> (initset[, datatype, names])	Creates a group of set iterator objects for multi-dimensional sets
<code>Statement</code> ()	Creates a statement to be executed at the server
<code>ImplicitVar</code> (**kwargs)	Creates an implicit variable

## **sasoptpy.abstract.Parameter**

**class** `Parameter` (\*\*kwargs)

Bases: `sasoptpy.core.expression.Expression`

Represents a problem input parameter

### **Parameters**

**name** [string] Name of the parameter

**ptype** [string, optional] Type of the parameter. Possible values are `sasoptpy.STR` and `sasoptpy.NUM`

**value** [float, optional] Value of the parameter

**init** [float, optional] Initial value of the parameter

### **Examples**

```
>>> with so.Workspace('w') as w:
...     p = so.Parameter(name='p', init=3)
...     p.set_value(5)
...
<sasoptpy.abstract.statement.assignment.Assignment object at 0x7f7952e9bb38>
>>> print(so.to_optmodel(w))
proc optmodel;
  num p init 3;
  p = 5;
quit;
```

## **sasoptpy.abstract.ParameterGroup**

**class** `ParameterGroup` (\*\*kwargs)

Bases: `object`

Represents a group of input parameters

### **Parameters**

**index\_key** [iterable] Index key of the group members

**name** [string] Name of the parameter group

**ptype** [string, optional] Type of the parameters. Possible values are `sasoptpy.STR` and `sasoptpy.NUM`

**value** [float, optional] Value of the parameter

**init** [float, optional] Initial value of the parameter

## Examples

```
>>> from sasoptpy.actions import for_loop
>>> with so.Workspace('w') as w:
...     p = so.ParameterGroup(so.exp_range(1, 6), name='p', init=3)
...     p[0].set_value(3)
...     S = so.Set(name='S', value=so.exp_range(1, 6))
...     for i in for_loop(S):
...         p[i].set_value(1)
...
>>> print(so.to_optmodel(w))
proc optmodel;
    num p {1..5} init 3;
    p[0] = 3;
    set S = 1..5;
    for {o13 in S} do;
        p[o13] = 1;
    end;
quit;
```

## sasoptpy.abstract.Set

**class** `Set` (*\*\*kwargs*)

Bases: `object`

Creates an index set to be represented inside PROC OPTMODEL

### Parameters

**name** [string] Name of the parameter

**init** [Expression, optional] Initial value expression of the parameter

**settype** [list, optional] List of types for the set, consisting of 'num' and 'str' values

## Examples

```
>>> I = so.Set('I')
>>> print(I._defn())
set I;
```

```
>>> J = so.Set('J', settype=['num', 'str'])
>>> print(J._defn())
set <num, str> J;
```

```
>>> N = so.Parameter(name='N', init=5)
>>> K = so.Set('K', init=so.exp_range(1,N))
>>> print(K._defn())
set K = 1..N;
```

## sasoptpy.abstract.SetIterator

**class** `SetIterator` (*initset*, *name=None*, *datatype=None*)

Bases: `sasoptpy.core.expression.Expression`

Creates an iterator object for a given Set

### Parameters

**initset** [*Set*] Set to be iterated on

**name** [string, optional] Name of the iterator

**datatype** [string, optional] Type of the iterator

### Notes

- `abstract.SetIterator` objects are created automatically when iterating over a `abstract.Set` object

### Examples

```
>>> S = so.Set(name='S')
>>> for i in S:
...     print(i.get_name(), type(i))
o19 <class 'sasoptpy.abstract.set_iterator.SetIterator'>
```

## sasoptpy.abstract.SetIteratorGroup

**class** `SetIteratorGroup` (*initset*, *datatype=None*, *names=None*)

Bases: `collections.OrderedDict`, `sasoptpy.core.expression.Expression`

Creates a group of set iterator objects for multi-dimensional sets

### Parameters

**initset** [*Set*] Set to be iterated on

**names** [string, optional] Names of the iterators

**datatype** [string, optional] Types of the iterators

### Examples

```
>>> T = so.Set(name='T', settype=[so.STR, so.NUM])
>>> for j in T:
...     print(j.get_name(), type(j))
...     for k in j:
...         print(k.get_name(), type(k))
o5 <class 'sasoptpy.abstract.set_iterator.SetIteratorGroup'>
o6 <class 'sasoptpy.abstract.set_iterator.SetIterator'>
o8 <class 'sasoptpy.abstract.set_iterator.SetIterator'>
```



## sasoptpy.abstract.Statement

### class Statement

Bases: `abc.ABC`

Creates a statement to be executed at the server

This class is an abstract base class for all statement types.

## sasoptpy.abstract.ImplicitVar

### class ImplicitVar(\*\*kwargs)

Bases: `object`

Creates an implicit variable

#### Parameters

**argv** [Generator, optional] Generator object for the implicit variable

**name** [string, optional] Name of the implicit variable

## Notes

- If the loop inside generator is over an abstract object, a definition for the object will be created inside `Model.to_optmodel()` method.

## Examples

### Regular Implicit Variable

```
>>> I = range(5)
>>> x = so.Variable(name='x')
>>> y = so.VariableGroup(I, name='y')
>>> z = so.ImplicitVar((x + i * y[i] for i in I), name='z')
>>> for i in z:
>>>     print(i, z[i])
(0,) x
(1,) x + y[1]
(2,) x + 2 * y[2]
(3,) x + 3 * y[3]
(4,) x + 4 * y[4]
```

### Abstract Implicit Variable

```
>>> I = so.Set(name='I')
>>> x = so.Variable(name='x')
>>> y = so.VariableGroup(I, name='y')
>>> z = so.ImplicitVar((x + i * y[i] for i in I), name='z')
>>> print(z._defn())
impvar z {i_1 in I} = x + i_1 * y[i_1];
>>> for i in z:
>>>     print(i, z[i])
(sasoptpy.abstract.SetIterator(name=i_1, ...),) x + i_1 * y[i_1]
```

## Statements

The following list of classes define the underlying structure for the abstract functions. See [Abstract Actions](#) to see how you can use abstract functions and statements.

---

<i>Assignment</i> (identifier, expression[, keyword])
<i>CoForLoopStatement</i> (*args)
<i>CreateDataStatement</i> (table, index[, columns])
<i>DropStatement</i> (**kwargs)
<i>ForLoopStatement</i> (*args)
<i>IfElseStatement</i> (logic_expression, if_statement)
<i>LiteralStatement</i> (**kwargs)
<i>ObjectiveStatement</i> (expression, **kwargs)
<i>ReadDataStatement</i> (table, index[, columns])
<i>SolveStatement</i> (*args, **kwargs)
<i>FixStatement</i> (*elements)
<i>UnfixStatement</i> (*elements)
<i>PrintStatement</i> (*args)

---

### sasoptpy.abstract.statement.Assignment

```
class Assignment (identifier, expression, keyword=None)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

### sasoptpy.abstract.statement.CoForLoopStatement

```
class CoForLoopStatement (*args)
    Bases: sasoptpy.abstract.statement.for_loop.ForLoopStatement
```

### sasoptpy.abstract.statement.CreateDataStatement

```
class CreateDataStatement (table, index, columns=None)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

### sasoptpy.abstract.statement.DropStatement

```
class DropStatement (**kwargs)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.ForLoopStatement**

```
class ForLoopStatement (*args)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.IfElseStatement**

```
class IfElseStatement (logic_expression, if_statement, else_statement=None)
    Bases: sasoptpy.abstract.statement.if_else.NestedConditions
```

**sasoptpy.abstract.statement.LiteralStatement**

```
class LiteralStatement (**kwargs)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.ObjectiveStatement**

```
class ObjectiveStatement (expression, **kwargs)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.ReadDataStatement**

```
class ReadDataStatement (table, index, columns=None)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.SolveStatement**

```
class SolveStatement (*args, **kwargs)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.FixStatement**

```
class FixStatement (*elements)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.UnfixStatement**

```
class UnfixStatement (*elements)
    Bases: sasoptpy.abstract.statement.statement_base.Statement
```

**sasoptpy.abstract.statement.PrintStatement****class PrintStatement** (\*args)

Bases: sasoptpy.abstract.statement.statement\_base.Statement

## 5.3 Interface

### 5.3.1 Interface

**CAS (Viya)**

---

<i>CASMediator</i> (caller, cas_session)	Handles the connection between sasoptpy and the SAS Viya (CAS) server
--	---

---

**sasoptpy.interface.CASMediator****class CASMediator** (caller, cas\_session)

Bases: sasoptpy.interface.solver.mediator.Mediator

Handles the connection between sasoptpy and the SAS Viya (CAS) server

**Parameters****caller** [*sasoptpy.Model* or *sasoptpy.Workspace*] Model or workspace that mediator belongs to**cas\_session** [*swat.cas.connection.CAS*] CAS connection**Notes**

- CAS Mediator is used by *sasoptpy.Model* and *sasoptpy.Workspace* objects internally.

**Model**

---

<i>CASMediator.solve</i> (self, <i>\*\*kwargs</i> )	Solve action for Model objects
<i>CASMediator.tune</i> (self, <i>\*\*kwargs</i> )	Wrapper for the MILP tuner
<i>CASMediator.tune_problem</i> (self, <i>\*\*kwargs</i> )	Calls optimization.tuner CAS action to finds out the ideal configuration
<i>CASMediator.solve_with_mps</i> (self, <i>\*\*kwargs</i> )	Submits the problem in MPS (DataFrame) format, supported by old versions
<i>CASMediator.solve_with_optmodel</i> (self, <i>\*\*kwargs</i> )	Submits the problem in OPTMODEL format
<i>CASMediator.parse_cas_solution</i> (self)	Performs post-solve operations
<i>CASMediator.parse_cas_table</i> (self, table)	Converts requested <i>swat.cas.table.CASTable</i> objects to <i>swat.dataframe.SASDataFrame</i>
<i>CASMediator.set_variable_values</i> (self, solution)	Performs post-solve assignment of variable values

---

Continued on next page

Table 28 – continued from previous page

<code>CASMediator.set_constraint_values(self, solution)</code>	Performs post-solve assignment of constraint values
<code>CASMediator.set_model_objective_value(self, value)</code>	Performs post-solve assignment of objective values
<code>CASMediator.set_variable_init_values(self, values)</code>	Performs post-solve assignment of variable initial values
<code>CASMediator.upload_user_blocks(self)</code>	Uploads user-defined decomposition blocks to the CAS server
<code>CASMediator.upload_model(self[, name, ...])</code>	Converts internal model to MPS table and upload to CAS session

**sasoptpy.interface.CASMediator.solve**

`CASMediator.solve(self, **kwargs)`  
Solve action for Model objects

**sasoptpy.interface.CASMediator.tune**

`CASMediator.tune(self, **kwargs)`  
Wrapper for the MILP tuner

**sasoptpy.interface.CASMediator.tune\_problem**

`CASMediator.tune_problem(self, **kwargs)`  
Calls optimization.tuner CAS action to finds out the ideal configuration

**sasoptpy.interface.CASMediator.solve\_with\_mps**

`CASMediator.solve_with_mps(self, **kwargs)`  
Submits the problem in MPS (DataFrame) format, supported by old versions

**Parameters**

**kwargs** [dict] Keyword arguments for solver settings and options

**Returns**

**primal\_solution** [`swat.dataframe.SASDataFrame`] Solution of the model or None

**sasoptpy.interface.CASMediator.solve\_with\_optmodel**

`CASMediator.solve_with_optmodel(self, **kwargs)`  
Submits the problem in OPTMODEL format

**Parameters**

**kwargs** [dict] Keyword arguments for solver settings and options

**Returns**

**primal\_solution** [`swat.dataframe.SASDataFrame`] Solution of the model or None

### **sasoptpy.interface.CASMediator.parse\_cas\_solution**

`CASMediator.parse_cas_solution(self)`

Performs post-solve operations

#### **Returns**

**solution** [`swat.dataframe.SASDataFrame`] Solution of the problem

### **sasoptpy.interface.CASMediator.parse\_cas\_table**

`CASMediator.parse_cas_table(self, table)`

Converts requested `swat.cas.table.CASTable` objects to `swat.dataframe.SASDataFrame`

### **sasoptpy.interface.CASMediator.set\_variable\_values**

`CASMediator.set_variable_values(self, solution)`

Performs post-solve assignment of variable values

#### **Parameters**

**solution** [`class:swat.dataframe.SASDataFrame`] Primal solution of the problem

### **sasoptpy.interface.CASMediator.set\_constraint\_values**

`CASMediator.set_constraint_values(self, solution)`

Performs post-solve assignment of constraint values

#### **Parameters**

**solution** [`class:swat.dataframe.SASDataFrame`] Primal solution of the problem

### **sasoptpy.interface.CASMediator.set\_model\_objective\_value**

`CASMediator.set_model_objective_value(self)`

Performs post-solve assignment of objective values

#### **Parameters**

**solution** [`class:swat.dataframe.SASDataFrame`] Primal solution of the problem

### **sasoptpy.interface.CASMediator.set\_variable\_init\_values**

`CASMediator.set_variable_init_values(self)`

Performs post-solve assignment of variable initial values

#### **Parameters**

**solution** [`class:swat.dataframe.SASDataFrame`] Primal solution of the problem

**sasoptpy.interface.CASMediator.upload\_user\_blocks**`CASMediator.upload_user_blocks` (*self*)

Uploads user-defined decomposition blocks to the CAS server

**Returns****name** [string] CAS table name of the user-defined decomposition blocks**Examples**

```
>>> userblocks = m.upload_user_blocks()
>>> m.solve(milp={'decomp': {'blocks': userblocks}})
```

**sasoptpy.interface.CASMediator.upload\_model**`CASMediator.upload_model` (*self*, *name=None*, *replace=True*, *constant=False*, *verbose=False*)

Converts internal model to MPS table and upload to CAS session

**Parameters****name** [string, optional] Desired name of the MPS table on the server**replace** [boolean, optional] Option to replace the existing MPS table**Returns****frame** [`swat.cas.table.CASTable`] Reference to the uploaded CAS Table**Notes**

- This method returns `None` if the model session is not valid.
- Name of the table is randomly assigned if *name* argument is `None` or not given.
- This method should not be used if `Model.solve()` is going to be used. `Model.solve()` calls this method internally.

**Workspace**

<code>CASMediator.submit</code> ( <i>self</i> , <i>kwargs</i> )	Submit action for custom input and <i>sasoptpy.Workspace</i> objects
<code>CASMediator.submit_optmodel_code</code> ( <i>self</i> , ...)	Converts caller into OPTMODEL code and submits using <code>optimization.runOptmodel</code> action
<code>CASMediator.parse_cas_workspace_response</code> ( <i>self</i> )	Parses results of workspace submission
<code>CASMediator.set_workspace_variable_value</code> ( <i>self</i> , ...)	Performs post-solve assignment of <i>sasoptpy.Workspace</i> variable values

**sasoptpy.interface.CASMediator.submit**

`CASMediator.submit(self, **kwargs)`  
Submit action for custom input and *sasoptpy.Workspace* objects

**sasoptpy.interface.CASMediator.submit\_optmodel\_code**

`CASMediator.submit_optmodel_code(self, **kwargs)`  
Converts caller into OPTMODEL code and submits using `optimization.runOptmodel` action

**Parameters**

**kwargs** : Solver settings and options

**sasoptpy.interface.CASMediator.parse\_cas\_workspace\_response**

`CASMediator.parse_cas_workspace_response(self)`  
Parses results of workspace submission

**sasoptpy.interface.CASMediator.set\_workspace\_variable\_values**

`CASMediator.set_workspace_variable_values(self, solution)`  
Performs post-solve assignment of *sasoptpy.Workspace* variable values

**SAS**

---

<i>SASMediator</i> (caller, sas_session)	Handles the connection between sasoptpy and SAS instance
--	--

---

**sasoptpy.interface.SASMediator**

**class SASMediator** (caller, sas\_session)  
Bases: `sasoptpy.interface.solver.mediator.Mediator`

Handles the connection between sasoptpy and SAS instance

**Parameters**

**caller** [*sasoptpy.Model* or *sasoptpy.Workspace*] Model or workspace that mediator belongs to  
**sas\_session** [*saspy.SASsession*] SAS session object



## Notes

- SASMediator is used by `sasoptpy.Model` and `sasoptpy.Workspace` objects internally.

## Model

<code>SASMediator.solve(self, **kwargs)</code>	Solve action for Model objects
<code>SASMediator.solve_with_mps(self, **kwargs)</code>	Submits the problem in MPS (DataFrame) format, supported by old versions
<code>SASMediator.solve_with_optmodel(self, **kwargs)</code>	Submits the problem in OPTMODEL format
<code>SASMediator.parse_sas_mps_solution(self)</code>	Parses MPS solution after <i>solve</i> and returns solution
<code>SASMediator.parse_sas_solution(self)</code>	Performs post-solve operations
<code>SASMediator.parse_sas_table(self, table_name)</code>	Converts requested table name into <code>pandas.DataFrame</code>
<code>SASMediator.convert_to_original(self, table)</code>	Converts variable names to their original format if a placeholder gets used
<code>SASMediator.perform_postsolve_operations(self)</code>	Performs post-solve operations for proper output display

### sasoptpy.interface.SASMediator.solve

`SASMediator.solve(self, **kwargs)`  
Solve action for Model objects

### sasoptpy.interface.SASMediator.solve\_with\_mps

`SASMediator.solve_with_mps(self, **kwargs)`  
Submits the problem in MPS (DataFrame) format, supported by old versions

#### Parameters

**kwargs** [dict] Keyword arguments for solver settings and options

#### Returns

**primal\_solution** [`pandas.DataFrame`] Solution of the model or None

### sasoptpy.interface.SASMediator.solve\_with\_optmodel

`SASMediator.solve_with_optmodel(self, **kwargs)`  
Submits the problem in OPTMODEL format

#### Parameters

**kwargs** [dict] Keyword arguments for solver settings and options

#### Returns

**primal\_solution** [`pandas.DataFrame`] Solution of the model or None

**sasoptpy.interface.SASMediator.parse\_sas\_mps\_solution**

`SASMediator.parse_sas_mps_solution(self)`  
Parses MPS solution after *solve* and returns solution

**sasoptpy.interface.SASMediator.parse\_sas\_solution**

`SASMediator.parse_sas_solution(self)`  
Performs post-solve operations

**Returns**

**solution** [`pandas.DataFrame`] Solution of the problem

**sasoptpy.interface.SASMediator.parse\_sas\_table**

`SASMediator.parse_sas_table(self, table_name)`  
Converts requested table name into `pandas.DataFrame`

**sasoptpy.interface.SASMediator.convert\_to\_original**

`SASMediator.convert_to_original(self, table)`  
Converts variable names to their original format if a placeholder gets used

**sasoptpy.interface.SASMediator.perform\_postsolve\_operations**

`SASMediator.perform_postsolve_operations(self)`  
Performs post-solve operations for proper output display

**Workspace**

<code>SASMediator.submit(self, \*\*kwargs)</code>	Submit action for custom input and <i>sasoptpy.Workspace</i> objects
<code>SASMediator.submit_optmodel_code(self, ...)</code>	Submits given <i>sasoptpy.Workspace</i> object in OPTMODEL format
<code>SASMediator.parse_sas_workspace_response(self)</code>	Parses results of workspace submission
<code>SASMediator.set_workspace_variable_values(self)</code>	Performs post-solve assignment of <i>sasoptpy.Workspace</i> variable values

**sasoptpy.interface.SASMediator.submit**

`SASMediator.submit(self, **kwargs)`

Submit action for custom input and *sasoptpy.Workspace* objects

**sasoptpy.interface.SASMediator.submit\_optmodel\_code**

`SASMediator.submit_optmodel_code(self, **kwargs)`

Submits given *sasoptpy.Workspace* object in OPTMODEL format

**Parameters**

**kwargs** : Solver settings and options

**sasoptpy.interface.SASMediator.parse\_sas\_workspace\_response**

`SASMediator.parse_sas_workspace_response(self)`

Parses results of workspace submission

**sasoptpy.interface.SASMediator.set\_workspace\_variable\_values**

`SASMediator.set_workspace_variable_values(self, solution)`

Performs post-solve assignment of *sasoptpy.Workspace* variable values

## 5.4 Functions

### 5.4.1 Functions

#### Utility Functions

<code>dict_to_frame(dictobj[, cols])</code>	Converts dictionaries to DataFrame objects for pretty printing
<code>exp_range(start, stop[, step])</code>	Creates a set within specified range
<code>flatten_frame(df[, swap])</code>	Converts a <code>pandas.DataFrame</code> object into <code>pandas.Series</code>
<code>get_value_table(*args, **kwargs)</code>	Returns values of the given arguments as a merged pandas DataFrame
<code>expr_sum(argv)</code>	Summation function for <i>Expression</i> objects
<code>quick_sum(argv)</code>	Summation function for <i>Expression</i> objects
<code>reset()</code>	Resets package configs and internal counters

## `sasoptpy.dict_to_frame`

**dict\_to\_frame** (*dictobj*, *cols=None*)

Converts dictionaries to DataFrame objects for pretty printing

### Parameters

**dictobj** [dict] Dictionary to be converted

**cols** [list, optional] Column names

### Returns

**frobj** [DataFrame] DataFrame representation of the dictionary

### Examples

```
>>> d = {'coal': {'period1': 1, 'period2': 5, 'period3': 7},
>>>        'steel': {'period1': 8, 'period2': 4, 'period3': 3},
>>>        'copper': {'period1': 5, 'period2': 7, 'period3': 9}}
>>> df = so.dict_to_frame(d)
>>> print(df)
   period1  period2  period3
coal         1         5         7
copper        5         7         9
steel         8         4         3
```

## `sasoptpy.exp_range`

**exp\_range** (*start*, *stop*, *step=1*)

Creates a set within specified range

### Parameters

**start** [*Expression*] First value of the range

**stop** [*Expression*] Last value of the range

**step** [*Expression*, optional] Step size of the range

### Returns

**exset** [Set] Set that represents the range

### Examples

```
>>> N = so.Parameter(name='N')
>>> p = so.exp_range(1, N)
>>> print(p._defn())
set 1..N;
```

## sasoptpy.flatten\_frame

**flatten\_frame** (*df*, *swap=False*)

Converts a `pandas.DataFrame` object into `pandas.Series`

### Parameters

**df** [`pandas.DataFrame`] DataFrame to be flattened

**swap** [boolean, optional] Option to use columns as first index

### Returns

**new\_frame** [`pandas.DataFrame`] A new DataFrame where indices consist of index and columns names as tuples

## Examples

```
>>> price = pd.DataFrame([
>>>     [1, 5, 7],
>>>     [8, 4, 3],
>>>     [5, 7, 9]], columns=['period1', 'period2', 'period3']).\
>>>     set_index(['coal', 'steel', 'copper'])
>>> print('Price data: \n{}'.format(price))
>>> price_f = so.flatten_frame(price)
>>> print('Price data: \n{}'.format(price_f))
Price data:
      period1  period2  period3
coal         1         5         7
steel        8         4         3
copper        5         7         9
Price data:
(coal, period1)      1
(coal, period2)      5
(coal, period3)      7
(steel, period1)     8
(steel, period2)     4
(steel, period3)     3
(copper, period1)    5
(copper, period2)    7
(copper, period3)    9
dtype: int64
```

## sasoptpy.get\_value\_table

**get\_value\_table** (*\*args*, *\*\*kwargs*)

Returns values of the given arguments as a merged pandas DataFrame

### Parameters

**key** [list, optional] Keys for objects

**rhs** [bool, optional] Option for including constant values

### Returns

**table** [`pandas.DataFrame`] DataFrame object that holds object values

## sasoptpy.expr\_sum

**expr\_sum** (*argv*)

Summation function for *Expression* objects

### Returns

**exp** [*Expression*] Sum of given arguments

### Notes

This function is faster for expressions compared to Python's native `sum()` function.

### Examples

```
>>> x = so.VariableGroup(10000, name='x')
>>> y = so.expr_sum(2*x[i] for i in range(10000))
```

## sasoptpy.quick\_sum

**quick\_sum** (*argv*)

Summation function for *Expression* objects

### Notes

This method will deprecate in future versions. Use `expr_sum()` instead.

## sasoptpy.reset

**reset** ()

Resets package configs and internal counters

## Abstract Actions

<code>actions.read_data</code> (table, index, columns)	Reads data tables inside Set and Parameter objects
<code>actions.create_data</code> (table, index, columns)	Creates data tables from variables, parameters, and expressions
<code>actions.solve</code> ([options, primalin])	Solves the active optimization problem and generates results
<code>actions.for_loop</code> (\*args)	Creates a for-loop container to be executed on the server
<code>actions.cofor_loop</code> (\*args)	Creates a cofor-loop to be executed on the server concurrently
<code>actions.if_condition</code> (logic_expression, ...)	Creates an if-else block
<code>actions.switch_conditions</code> (\*\*args)	Creates several if-else blocks by using the specified arguments
<code>actions.set_value</code> (left, right)	Creates an assignment statement
<code>actions.fix</code> (\*args)	Fixes values of variables to the specified values

Continued on next page

Table 34 – continued from previous page

<code>actions.unfix(*args)</code>	Unfixes values of variables
<code>actions.set_objective(expression, name, sense)</code>	Specifies the objective function
<code>actions.print_item(*args)</code>	Prints the specified argument list on server
<code>actions.put_item(*args[, names])</code>	Prints the specified item values to the output log
<code>actions.expand()</code>	Prints expanded problem to output
<code>actions.drop(*args)</code>	Drops the specified constraints or constraint groups from model
<code>actions.restore(*args)</code>	Restores dropped constraint and constraint groups
<code>actions.union(*args)</code>	Aggregates the specified sets and set expressions
<code>actions.diff(left, right)</code>	Gets the difference between set and set expressions
<code>actions.substring(main_string, first_pos, ...)</code>	Gets the substring of the specified positions
<code>actions.use_problem(problem)</code>	Changes the currently active problem

## sasoptpy.actions.read\_data

**read\_data** (*table, index, columns*)

Reads data tables inside Set and Parameter objects

### Parameters

**table** [string or `swat.cas.table.CASTable`] Table object or name to be read, case-insensitive

**index** [dict] Index properties of the table

Has two main members:

- **target** [`sasoptpy.abstract.Set`] Target Set object to be read into
- **key** [string, list or None] Column name to be read from.

For multiple indices, key should be a list of string or `sasoptpy.abstract.SetIterator` objects

For a given set *YEAR* and column name *year\_no*, the index dictionary should be written as:

```
>>> {'target': YEAR, 'key': 'year_no'}
```

If index is simply the row number, use *'key': so.N* which is equivalent to the special *\_N\_* character in the SAS language.

**columns** [list] A list of dictionaries, each holding column properties.

Columns are printed in the specified order. Each column should be represented as a dictionary with following fields:

- **target** [`sasoptpy.abstract.ParameterGroup`] Target parameter object to be read into
- **column** [string] Column name to be read from
- **index** [`sasoptpy.SetIterator`, optional] Subindex for specific column, needed for complex operations

If the name of the `sasoptpy.abstract.Parameter` object is same as the column name, the following call is enough:

```
>>> p = so.Parameter(name='price')
>>> read_data(..., columns=[{'target': p}])
```

For reading a different column name, *column* field should be specified:

```
>>> {'target': p, 'column': 'price_usd'}
```

When working with `ParameterGroup` objects, sometimes a secondary loop is needed. This is achieved by using the *index* field, along with the `sasoptpy.abstract.statement.ReadDataStatement.append()` method.

### Returns

**r** [`sasoptpy.abstract.statement.ReadDataStatement`] Read data statement object, which includes all properties

Additional columns can be added using the `sasoptpy.abstract.statement.ReadDataStatement.append()` function.

See also:

`tests.abstract.statement.test_read_data.TestReadData`

### Examples

Reading a regular set:

```
>>> with Workspace('test_workspace') as ws:
>>>     ITEMS = Set(name='ITEMS')
>>>     value = ParameterGroup(ITEMS, name='value', init=0)
>>>     get = VariableGroup(ITEMS, name='get', vartype=so.INT, lb=0)
>>>     read_data(
...         table="values",
...         index={'target': ITEMS, 'key': None},
...         columns=[{'target': value}])
>>> print(so.to_optmodel(w))
proc optmodel;
  set ITEMS;
  num value {ITEMS} init 0;
  var get {{ITEMS}} integer >= 0;
  read data values into ITEMS value;
quit;
```

Reading with row index:

```
>>> with so.Workspace('test_read_data_n') as ws:
>>>     ASSETS = so.Set(name='ASSETS')
>>>     ret = so.ParameterGroup(ASSETS, name='return', ptype=so.NUM)
>>>     read_data(
...         table='means',
...         index={'target': ASSETS, 'key': so.N},
...         columns=[{'target': ret}]
...     )
>>> print(so.to_optmodel(w))
proc optmodel;
  set ASSETS;
  num return {ASSETS};
```

(continues on next page)



(continued from previous page)

```

    read data means into ASSETS=[_N_] return;
quit;

```

Reading with no index set and subindex:

```

>>> with so.Workspace('test_read_data_no_index_expression') as ws:
>>>     ASSETS = so.Set(name='ASSETS')
>>>     cov = so.ParameterGroup(ASSETS, ASSETS, name='cov', init=0)
>>>     with iterate(ASSETS, 'asset1') as asset1, iterate(ASSETS, 'asset2') as
    ↪asset2:
>>>         read_data(
...             table='covdata',
...             index={'key': [asset1, asset2]},
...             columns=[
...                 {'target': cov},
...                 {'target': cov[asset2, asset1]},
...                 {'column': 'cov'}])
>>> print(so.to_optmodel(w))
proc optmodel;
    set ASSETS;
    num cov {ASSETS, ASSETS} init 0;
    read data covdata into [asset1 asset2] cov cov[asset2, asset1]=cov;
quit;

```

Reading a column with multiple indices:

```

>>> with so.Workspace(name='test_read_data_idx_col') as ws:
>>>     dow = so.Set(name='DOW', value=so.exp_range(1, 6))
>>>     locs = so.Set(name='LOCS', settype=so.STR)
>>>     demand = so.ParameterGroup(locs, dow, name='demand')
>>>     with iterate(locs, name='loc') as loc:
>>>         r = read_data(
...             table='dmnd',
...             index={'target': locs, 'key': loc}
...         )
>>>         with iterate(dow, name='d') as d:
>>>             r.append({
...                 'index': d,
...                 'target': demand[loc, d],
...                 'column': concat('day', d)
...             })
>>> optmodel_code = so.to_optmodel(ws)
proc optmodel;
    set DOW = 1..5;
    set <str> LOCS;
    num demand {LOCS, DOW};
    read data dmnd into LOCS=[loc] {d in DOW} < demand[loc, d]=col('day' || d) >;
quit;

```

## sasoptpy.actions.create\_data

**create\_data** (*table, index, columns*)

Creates data tables from variables, parameters, and expressions

### Parameters

**table** [string] Name of the table to be created

**index** [dict] Table index properties

This dictionary can be empty if no index is needed. It can have following fields:

- **key** [list] List of index keys. Keys can be string or `sasoptpy.abstract.SetIterator` objects
- **set** [list] List of sets that is being assigned to keys

**columns** [list] List of columns. Columns can be `sasoptpy.abstract.Parameter`, `sasoptpy.abstract.ParameterGroup` objects or dictionaries. If specified as a dictionary, each can have following keys:

- **name** [string] Name of the column in output table
- **expression** [`sasoptpy.core.Expression`] Any expression
- **index** [list or `sasoptpy.abstract.SetIterator`] Index for internal loops

The *index* field can be used when a subindex is needed. When specified as a list, members should be `sasoptpy.abstract.SetIterator` objects. See examples for more details.

See also:

`tests.abstract.statement.test_create_data.TestCreateData`

## Examples

Regular column:

```
>>> with so.Workspace('w') as w:
>>>     m = so.Parameter(name='m', value=7)
>>>     n = so.Parameter(name='n', value=5)
>>>     create_data(table='example', index={}, columns=[m, n])
>>> print(so.to_optmodel(w))
proc optmodel;
    num m = 7;
    num n = 5;
    create data example from m n;
quit;
```

Column with name:

```
>>> with so.Workspace('w') as w:
>>>     m = so.Parameter(name='m', value=7)
>>>     n = so.Parameter(name='n', value=5)
>>>     create_data(table='example', index={}, columns=[
...         {'name': 'ratio', 'expression': m/n}
...     ])
>>> print(so.to_optmodel(w))
```

(continues on next page)

(continued from previous page)

```
proc optmodel;
  num m = 7;
  num n = 5;
  create data example from ratio=((m) / (n));
quit;
```

Column name with concat:

```
>>> from sasoptpy.util import concat
>>> with so.Workspace('w') as w:
>>>     m = so.Parameter(name='m', value=7)
>>>     n = so.Parameter(name='n', value=5)
>>>     create_data(table='example', index={}, columns=[
...         {'name': concat('s', n), 'expression': m+n}
...     ])
>>> print(so.to_optmodel(w))
proc optmodel;
  num m = 7;
  num n = 5;
  create data example from col('s' || n)=(m + n);
quit;
```

Table with index:

```
>>> with so.Workspace('w') as w:
>>>     m = so.ParameterGroup(
>>>         so.exp_range(1, 6), so.exp_range(1, 4), name='m', init=0)
>>>     m[1, 1] = 1
>>>     m[4, 1] = 1
>>>     S = so.Set(name='ISET', value=[i*2 for i in range(1, 3)])
>>>     create_data(
...         table='example',
...         index={'key': ['i', 'j'], 'set': [S, [1, 2]]},
...         columns=[m]
...     )
>>> print(so.to_optmodel(w))
proc optmodel;
  num m {1..5, 1..3} init 0;
  m[1, 1] = 1;
  m[4, 1] = 1;
  set ISET = {1,4};
  create data example from [i j] = {{ISET,{1,2}}} m;
quit;
```

Index over Python range:

```
>>> with so.Workspace('w') as w:
>>>     s = so.Set(name='S', value=so.exp_range(1, 6))
>>>     x = so.VariableGroup(s, name='x')
>>>     x[1] = 1
>>>     create_data(table='example',
...         index={'key': ['i'], 'set': so.exp_range(1, 4)}, columns=[x])
>>> print(so.to_optmodel(w))
proc optmodel;
  set S = 1..5;
  var x {{S}};
  x[1] = 1;
```

(continues on next page)

(continued from previous page)

```

    create data example from [i] = {1..3} x;
quit;

```

Append column with index:

```

>>> from sasoptpy.util import iterate, concat
>>> with so.Workspace('w', session=session) as w:
>>>     alph = so.Set(name='alph', settype=so.string, value=['a', 'b', 'c'])
>>>     x = so.VariableGroup([1, 2, 3], alph, name='x', init=2)
>>>     with iterate(so.exp_range(1, 4), name='i') as i:
>>>         c = create_data(
>>>             table='example',
>>>             index={'key': [i], 'set': [i.get_set()]})
>>>         with iterate(alph, name='j') as j:
>>>             c.append(
>>>                 {'name': concat('x', j),
>>>                  'expression': x[i, j],
>>>                  'index': j})
>>> print(so.to_optmodel(w))
proc optmodel;
    set <str> alph = {'a','b','c'};
    var x {{1,2,3}, {alph}} init 2;
    create data example from [i] = {{1..3}} {j in alph} < col('x' || j)=(x[i, j])_
↪>;
quit;

```

Multiple column indices:

```

>>> from sasoptpy.util import concat, iterate
>>> with so.Workspace('w') as w:
>>>     S = so.Set(name='S', value=[1, 2, 3])
>>>     T = so.Set(name='T', value=[1, 3, 5])
>>>     x = so.VariableGroup(S, T, name='x', init=1)
>>>     with iterate(S, name='i') as i, iterate(T, name='j') as j:
>>>         create_data(
>>>             table='out',
>>>             index={},
>>>             columns=[
>>>                 {'name': concat('x', concat(i, j)), 'expression': x[i, j],
>>>                  'index': [i, j]})
>>> print(so.to_optmodel(w))
proc optmodel;
    set S = {1,2,3};
    set T = {1,3,5};
    var x {{S}, {T}} init 1;
    create data out from {i in S, j in T} < col('x' || i || j)=(x[i, j]) >;
quit;

```

## sasoptpy.actions.solve

**solve** (*options=None, primalin=False*)

Solves the active optimization problem and generates results

### Parameters

**options** [dict, optional] Solver options

This dictionary can have several fields.

- **with** [string] Name of the solver, see possible values under Notes.

See [Solver Options](#) for a list of solver options. All fields in options (except *with*) is passed directly to the solver.

**primalin** [bool, optional] When set to *True*, uses existing variable values as an initial point in MILP solver

### Returns

**ss** [*sasoptpy.abstract.statement.SolveStatement*] Solve statement object.

Contents of the response can be retrieved using *get\_response* function.

## Notes

Possible solver names for *with* parameter:

- *lp* : Linear programming
- *milp* : Mixed integer linear programming
- *nlp* : General nonlinear programming
- *qp* : Quadratic programming
- *blackbox* : Black-box optimization

SAS Optimization also has a constraint programming solver (clp), and network solver (network) but they are not currently supported by sasoptpy.

## Examples

Regular solve:

```
>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x', lb=1, ub=10)
>>>     o = so.Objective(2*x, sense=so.maximize, name='obj')
>>>     s = solve()
>>>     p = print_item(x)
>>> print(so.to_optmodel(w))
proc optmodel;
    var x >= 1 <= 10;
    max obj = 2 * x;
    solve;
    print x;
quit;
```

Option alternatives:

```
>>> with so.Workspace('w') as w:
>>>     # Problem declaration, etc..
>>>     solve()
>>>     solve(options={'with': 'milp'})
>>>     solve(options={'with': 'milp'}, primalin=True)
>>>     solve(options={'with': 'milp', 'presolver': None, 'feastol': 1e-6,
>>>                     'logfreq': 2, 'maxsols': 3, 'scale': 'automatic',
>>>                     'restarts': None, 'cutmir': 'aggressive'})
>>> print(so.to_optmodel(w))
proc optmodel;
    solve;
    solve with milp;
    solve with milp / primalin;
    solve with milp / presolver=None feastol=1e-06 logfreq=2 maxsols=3_
    ↪scale=automatic restarts=None cutmir=aggressive;
quit;
```

## sasoptpy.actions.for\_loop

**for\_loop**(\*args)

Creates a for-loop container to be executed on the server

### Parameters

**args** [*sasoptpy.abstract.Set* objects] Any number of *sasoptpy.abstract.Set* objects can be given

### Returns

**set\_iterator** [*sasoptpy.abstract.SetIterator*, *sasoptpy.abstract.SetIteratorGroup*] Set iterators to be used inside for-loop

See also:

*sasoptpy.actions.cofor\_loop()*

## Notes

For tasks that can be run concurrently, consider using *sasoptpy.actions.cofor\_loop()*

## Examples

Regular for loop:

```
>>> with so.Workspace('w') as w:
>>>     r = so.exp_range(1, 11)
>>>     x = so.VariableGroup(r, name='x')
>>>     for i in for_loop(r):
>>>         x[i] = 1
>>> print(so.to_optmodel(w))
proc optmodel;
    var x {{1,2,3,4,5,6,7,8,9,10}};
    for {o13 in 1..10} do;
        x[o13] = 1;
```

(continues on next page)

(continued from previous page)

```

    end;
quit;

```

Nested for loops:

```

>>> from sasoptpy.actions import put_item
>>> with so.Workspace('w') as w:
>>>     for i in for_loop(range(1, 3)):
>>>         for j in for_loop(['a', 'b']):
>>>             put_item(i, j)
>>> print(so.to_optmodel(w))
proc optmodel;
    for {o2 in 1..2} do;
        for {o5 in {'a', 'b'}} do;
            put o2 o5;
        end;
    end;
quit;

```

Multiple set for-loops:

```

>>> with so.Workspace('w') as w:
>>>     r = so.Set(name='R', value=range(1, 11))
>>>     c = so.Set(name='C', value=range(1, 6))
>>>     a = so.ParameterGroup(r, c, name='A', ptype=so.number)
>>>     for (i, j) in for_loop(r, c):
>>>         a[i, j] = 1
>>> print(so.to_optmodel(w))
proc optmodel;
    set R = 1..10;
    set C = 1..5;
    num A {R, C};
    for {o5 in R, o7 in C} do;
        A[o5, o7] = 1;
    end;
quit;

```

## sasoptpy.actions.cofor\_loop

**cofor\_loop** (\*args)

Creates a cofor-loop to be executed on the server concurrently

### Parameters

**args** [*sasoptpy.abstract.Set* objects] Any number of *sasoptpy.abstract.Set* objects can be specified

### Returns

**set\_iterator** [*sasoptpy.abstract.SetIterator*, *sasoptpy.abstract.SetIteratorGroup*] Set iterators to be used inside cofor-loop

See also:

*sasoptpy.actions.for\_loop()*

## Notes

A cofor-loop runs its content concurrently. For tasks that depend on each other, consider using `sasoptpy.actions.for_loop()`

## Examples

```
>>> with so.Workspace('w') as w:
>>>     x = so.VariableGroup(6, name='x', lb=0)
>>>     so.Objective(
>>>         so.expr_sum(x[i] for i in range(6)), name='z', sense=so.MIN)
>>>     a1 = so.Constraint(x[1] + x[2] + x[3] <= 4, name='a1')
>>>     for i in cofor_loop(so.exp_range(3, 6)):
>>>         fix(x[1], i)
>>>         solve()
>>>         put_item(i, x[1], so.Symbol('_solution_status_'), names=True)
>>> print(so.to_optmodel(w))
proc optmodel;
  var x {{0,1,2,3,4,5}} >= 0;
  min z = x[0] + x[1] + x[2] + x[3] + x[4] + x[5];
  con a1 : x[1] + x[2] + x[3] <= 4;
  cofor {o13 in 3..5} do;
    fix x[1]=o13;
    solve;
    put o13= x[1]= _solution_status_;
  end;
quit;
```

## sasoptpy.actions.if\_condition

**if\_condition** (*logic\_expression*, *if\_statement*, *else\_statement=None*)

Creates an if-else block

### Parameters

**logic\_expression** [*sasoptpy.Constraint* or *sasoptpy.abstract.Condition*]  
Logical condition for the True case

For the condition, it is possible to combine constraints, such as

```
>>> a = so.Parameter(value=5)
>>> if_condition((a < 3) | (a > 6), func1, func2)
```

Constraints should be combined using bitwise operators (& for *and*, | for *or*).

**if\_statement** [function or *IfElseStatement*] Python function or if-else statement to be called if the condition is True

**else\_statement** [function or *IfElseStatement*, optional] Python function or if-else statement to be called if the condition is False



## Examples

Regular condition:

```
>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x')
>>>     x.set_value(0.5)
>>>     def func1():
>>>         x.set_value(1)
>>>     def func2():
>>>         x.set_value(0)
>>>     if_condition(x > 1e-6, func1, func2)
>>> print(so.to_optmodel(w))
proc optmodel;
    var x;
    x = 0.5;
    if x > 1e-06 then do;
        x = 1;
    end;
    else do;
        x = 0;
    end;
quit;
```

Combined conditions:

```
>>> with so.Workspace('w') as w:
>>>     p = so.Parameter(name='p')
>>>     def case1():
>>>         p.set_value(10)
>>>     def case2():
>>>         p.set_value(20)
>>>     r = so.Parameter(name='r', value=10)
>>>     if_condition((r < 5) | (r > 10), case1, case2)
>>> print(so.to_optmodel(w))
proc optmodel;
    num p;
    num r = 10;
    if (r < 5) or (r > 10) then do;
        p = 10;
    end;
    else do;
        p = 20;
    end;
quit;
```

## sasoptpy.actions.switch\_conditions

**switch\_conditions** (\*\*args)

Creates several if-else blocks by using the specified arguments

### Parameters

**args** : Several arguments can be passed to the function

Each case should follow a condition. You can use `sasoptpy.Constraint` objects as conditions, and Python functions for the cases.

## Examples

```
>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x')
>>>     p = so.Parameter(name='p')
>>>     x.set_value(2.5)
>>>     def func1():
>>>         p.set_value(1)
>>>     def func2():
>>>         p.set_value(2)
>>>     def func3():
>>>         p.set_value(3)
>>>     def func4():
>>>         p.set_value(0)
>>>     switch_conditions(x < 1, func1, x < 2, func2, x < 3, func3, func4)
>>> print(to.optmodel(w))
proc optmodel;
  var x;
  num p;
  x = 2.5;
  if x < 1 then do;
    p = 1;
  end;
  else if x < 2 then do;
    p = 2;
  end;
  else if x < 3 then do;
    p = 3;
  end;
  else do;
    p = 0;
  end;
quit;
```

## sasoptpy.actions.set\_value

**set\_value** (*left*, *right*)

Creates an assignment statement

### Parameters

**left** [*sasoptpy.Expression*] Any expression (variable or parameter)

**right** [*sasoptpy.Expression* or float] Right-hand-side expression

## Examples

```
>>> with so.Workspace('ex_9_1_matirx_sqrt', session=None) as w:
>>>     so.LiteralStatement('call streaminit(1);')
>>>     n = so.Parameter(name='n', value=5)
>>>     rn = so.Set(name='RN', value=so.exp_range(1, n))
>>>     A = so.ParameterGroup(rn, rn, name='A', value="10-20*rand('UNIFORM')")
>>>     P = so.ParameterGroup(rn, rn, name='P')
>>>     for i in for_loop(rn):
>>>         for j in for_loop(so.exp_range(i, n)):
```

(continues on next page)

(continued from previous page)

```

>>>         set_value(P[i, j], so.expr_sum(A[i, k] * A[j, k] for k in rn))
>>> print(so.to_optmodel(w))
proc optmodel;
  call streaminit(1);
  num n = 5;
  set RN = 1..n;
  num A {RN, RN} = 10-20*rand('UNIFORM');
  num P {RN, RN};
  for {o7 in RN} do;
    for {o10 in o7..n} do;
      P[o7, o10] = sum {k in RN} (A[o7, k] * A[o10, k]);
    end;
  end;
quit;

```

## sasoptpy.actions.fix

**fix** (\*args)

Fixes values of variables to the specified values

### Parameters

**args** [*sasoptpy.Variable*, float, *sasoptpy.Expression*, tuple] Set of arguments to be fixed

Arguments get paired (if not given in tuples) to allow several fix operations

See also:

*sasoptpy.actions.unfix()*

*tests.abstract.statement.test\_fix\_unfix.TestFix*

## Examples

Regular fix statement:

```

>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x')
>>>     fix(x, 1)
>>>     solve()
>>>     unfix(x)
>>> print(so.to_optmodel(w))
proc optmodel;
  var x;
  fix x=1;
  solve;
  unfix x;
quit;

```

Multiple fix-unfix:

```

>>> with so.Workspace('w') as w:
>>>     x = so.VariableGroup(4, name='x')
>>>     for i in cofor_loop(range(4)):

```

(continues on next page)

(continued from previous page)

```

>>>         fix((x[0], i), (x[1], 1))
>>>         solve()
>>>         unfix(x[0], (x[1], 2))
>>> print(so.to_optmodel(w))
proc optmodel;
  var x {{0,1,2,3}};
  cofor {o7 in 0..3} do;
    fix x[0]=o7 x[1]=1;
    solve;
    unfix x[0] x[1]=2;
  end;
quit;

```

## sasoptpy.actions.unfix

**unfix**(\*args)

Unfixes values of variables

### Parameters

**args** [*sasoptpy.Variable* objects] Set of arguments to be unfixed

See also:

*sasoptpy.actions.fix()*

*tests.abstract.statement.test\_fix\_unfix.TestFix*

## Examples

Regular unfix statement:

```

>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x')
>>>     fix(x, 1)
>>>     solve()
>>>     unfix(x)
>>> print(so.to_optmodel(w))
proc optmodel;
  var x;
  fix x=1;
  solve;
  unfix x;
quit;

```

Multiple fix-unfix:

```

>>> with so.Workspace('w') as w:
>>>     x = so.VariableGroup(4, name='x')
>>>     for i in cofor_loop(range(4)):
>>>         fix((x[0], i), (x[1], 1))
>>>         solve()
>>>         unfix(x[0], (x[1], 2))
>>> print(so.to_optmodel(w))
proc optmodel;

```

(continues on next page)

(continued from previous page)

```

var x {{0,1,2,3}};
cofor {o7 in 0..3} do;
    fix x[0]=o7 x[1]=1;
    solve;
    unfix x[0] x[1]=2;
end;
quit;

```

## sasoptpy.actions.set\_objective

**set\_objective** (*expression, name, sense*)

Specifies the objective function

### Parameters

**expression** [*sasoptpy.Expression*] Objective function

**name** [string] Name of the objective function

**sense** [string] Direction of the objective function, *so.MAX* or *so.MIN*

## Examples

```

>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x', lb=1)
>>>     set_objective(x ** 3, name='xcube', sense=so.minimize)
>>>     solve()
>>> print(so.to_optmodel(w))
proc optmodel;
    var x >= 1;
    MIN xcube = (x) ^ (3);
    solve;
quit;

```

## sasoptpy.actions.print\_item

**print\_item** (*\*args*)

Prints the specified argument list on server

### Parameters

**args** [*sasoptpy.Variable, sasoptpy.Expression*] Arbitrary number of arguments to be printed

These values are printed on the server, but can be retrieved after execution

### Returns

**ps** [*sasoptpy.abstract.statement.PrintStatement*] Print statement object.

Contents of the response can be retrieved using *get\_response* function.

## Examples

```
>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x', lb=1, ub=10)
>>>     o = so.Objective(2*x, sense=so.maximize, name='obj')
>>>     s = solve()
>>>     p = print_item(x)
>>> print(so.to_optmodel(w))
proc optmodel;
    var x >= 1 <= 10;
    max obj = 2 * x;
    solve;
    print x;
quit;
>>> print(p.get_response())
           x
0  10.0
```

## sasoptpy.actions.put\_item

**put\_item** (\*args, names=None)

Prints the specified item values to the output log

### Parameters

**args** [*sasoptpy.Expression*, string] Arbitrary elements to be put into log

Variables, variable groups, and expressions can be printed to log

**names** [bool, optional] When set to *True*, prints the name of the arguments in the log

## Examples

Regular operation:

```
>>> with so.Workspace('w') as w:
>>>     for i in for_loop(range(1, 3)):
>>>         for j in for_loop(['a', 'b']):
>>>             put_item(i, j)
>>> print(so.to_optmodel(w))
proc optmodel;
    for {o2 in 1..2} do;
        for {o5 in {'a', 'b'}} do;
            put o2 o5;
        end;
    end;
quit;
```

Print with names:

```
>>> with so.Workspace('w') as w:
>>>     x = so.VariableGroup(6, name='x', lb=0)
>>>     so.Objective(
>>>         so.expr_sum(x[i] for i in range(6)), name='z', sense=so.MIN)
>>>     a1 = so.Constraint(x[1] + x[2] + x[3] <= 4, name='a1')
>>>     for i in cofor_loop(so.exp_range(3, 6)):
```

(continues on next page)

(continued from previous page)

```

>>>         fix(x[1], i)
>>>         solve()
>>>         put_item(i, x[1], so.Symbol('_solution_status_'), names=True)
proc optmodel;
  var x {{0,1,2,3,4,5}} >= 0;
  min z = x[0] + x[1] + x[2] + x[3] + x[4] + x[5];
  con a1 : x[1] + x[2] + x[3] <= 4;
  cofor {o13 in 3..5} do;
    fix x[1]=o13;
    solve;
    put o13= x[1]= _solution_status_;
  end;
quit;

```

## sasoptpy.actions.expand

### expand()

Prints expanded problem to output

### Examples

```

>>> with so.Workspace(name='w') as w:
>>>     x = so.VariableGroup(3, name='x')
>>>     self.assertEqual(x[0].sym.get_conditions_str(), '')
>>>     # solve
>>>     x[0].set_value(1)
>>>     x[1].set_value(5)
>>>     x[2].set_value(0)
>>>     c = so.ConstraintGroup(None, name='c')
>>>     with iterate([0, 1, 2], 's') as i:
>>>         with condition(x[i].sym > 0):
>>>             c[i] = x[i] >= 1
>>>     set_objective(x[0], name='obj', sense=so.MIN)
>>>     expand()
>>>     solve()
>>> print(so.to_optmodel(w))
proc optmodel;
  var x {{0,1,2}};
  x[0] = 1;
  x[1] = 5;
  x[2] = 0;
  con c {s in {0,1,2}: x[s].sol > 0} : x[s] >= 1;
  MIN obj = x[0];
  expand;
  solve;
quit;

```

## **sasoptpy.actions.drop**

**drop** (\*args)

Drops the specified constraints or constraint groups from model

### **Parameters**

**args** [*sasoptpy.Constraint*, *sasoptpy.ConstraintGroup*] Constraints to be dropped

See also:

*sasoptpy.actions.restore()*

### **Examples**

```
>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x', lb=1)
>>>     y = so.Variable(name='y', lb=0)
>>>     c = so.Constraint(sm.sqrt(x) >= 5, name='c')
>>>     o = so.Objective(x + y, sense=so.MIN, name='obj')
>>>     s = solve()
>>>     drop(c)
>>>     o2 = so.Objective(x, sense=so.MIN, name='obj2')
>>>     s2 = solve()
>>> print(so.to_optmodel(w))
proc optmodel;
  var x >= 1;
  var y >= 0;
  con c : sqrt(x) >= 5;
  min obj = x + y;
  solve;
  drop c;
  min obj2 = x;
  solve;
quit;
```

## **sasoptpy.actions.restore**

**restore** (\*args)

Restores dropped constraint and constraint groups

### **Parameters**

**args** [*sasoptpy.Constraint*, *sasoptpy.ConstraintGroup*] Constraints to be restored

See also:

*sasoptpy.actions.drop()*



## Examples

```
>>> with so.Workspace('w') as w:
>>>     x = so.Variable(name='x', lb=-1)
>>>     set_objective(x**3, name='xcube', sense=so.minimize)
>>>     c = so.Constraint(x >= 1, name='xbound')
>>>     solve()
>>>     drop(c)
>>>     solve()
>>>     restore(c)
>>>     solve()
>>> print(so.to_optmodel(w))
proc optmodel;
    var x >= -1;
    MIN xcube = (x) ^ (3);
    con xbound : x >= 1;
    solve;
    drop xbound;
    solve;
    restore xbound;
    solve;
quit;
```

## sasoptpy.actions.union

**union** (\*args)

Aggregates the specified sets and set expressions

### Parameters

**args** [*sasoptpy.abstract.Set* and *sasoptpy.abstract.InlineSet*] Objects to be aggregated

## Examples

```
>>> from sasoptpy.actions import union, put_item
>>> with so.Workspace('w') as w:
>>>     n = so.Parameter(name='n', value=11)
>>>     S = so.Set(name='S', value=so.exp_range(1, n))
>>>     T = so.Set(name='T', value=so.exp_range(n+1, 20))
>>>     U = so.Set(name='U', value=union(S, T))
>>>     put_item(U, names=True)
>>> print(so.to_optmodel(w))
proc optmodel;
    num n = 11;
    set S = 1..n;
    set T = n+1..20;
    set U = S union T;
    put U;
quit;
```

## sasoptpy.actions.diff

**diff** (*left*, *right*)

Gets the difference between set and set expressions

### Parameters

**left** [*sasoptpy.abstract.Set*] Left operand

**right** [*sasoptpy.abstract.Set*] Right operand

### Examples

```
>>> from sasoptpy.actions import diff, put_item
>>> with so.Workspace('w') as w:
>>>     S = so.Set(name='S', value=so.exp_range(1, 20))
>>>     T = so.Set(name='T', value=so.exp_range(1, 15))
>>>     U = so.Set(name='U', value=diff(S, T))
>>>     put_item(U, names=True)
>>> print(so.to_optmodel(w))
proc optmodel;
  set S = 1..19;
  set T = 1..14;
  set U = S diff T;
  put U;
quit;
```

## sasoptpy.actions.substring

**substring** (*main\_string*, *first\_pos*, *last\_pos*)

Gets the substring of the specified positions

### Parameters

**main\_string** [*sasoptpy.abstract.Parameter* or string] Main string

**first\_pos** [integer] First position of the substring, starting from 1

**last\_pos** [integer] Last position of the substring

### Examples

```
>>> with so.Workspace('w') as w:
>>>     p = so.Parameter(name='p', value='random_string', ptype=so.STR)
>>>     r = so.Parameter(name='r', value=substring(p, 1, 6), ptype=so.STR)
>>>     put_item(r)
>>> print(so.to_optmodel(w))
proc optmodel;
  str p = 'random_string';
  str r = substr(p, 1, 6);
  put r;
quit;
```

## sasoptpy.actions.use\_problem

**use\_problem** (*problem*)

Changes the currently active problem

### Parameters

**problem** [*sasoptpy.Model*] Model to be activated

### Examples

```

>>> from sasoptpy.actions import use_problem
>>> with so.Workspace('w') as w:
>>>     m = so.Model(name='m')
>>>     m2 = so.Model(name='m2')
>>>     use_problem(m)
>>>     x = so.Variable(name='x')
>>>     use_problem(m2)
>>>     m.solve()
>>>     m2.solve()
>>> print(so.to_optmodel(w))
proc optmodel;
  problem m;
  problem m2;
  use problem m;
  var x;
  use problem m2;
  use problem m;
  solve;
  use problem m2;
  solve;
quit;

```

## Math Functions

<i>math.math_func</i> (exp, op, \*args)	Function wrapper for math functions
<i>math.abs</i> (exp)	Absolute value function
<i>math.log</i> (exp)	Natural logarithm function
<i>math.log2</i> (exp)	Logarithm function in base 2
<i>math.log10</i> (exp)	Logarithm function in base 10
<i>math.exp</i> (exp)	Exponential function
<i>math.sqrt</i> (exp)	Square root function
<i>math.mod</i> (exp, divisor)	Modulo function
<i>math.int</i> (exp)	Integer value function
<i>math.sign</i> (exp)	Sign value function
<i>math.max</i> (exp, \*args)	Largest value function
<i>math.min</i> (exp, \*args)	Smallest value function
<i>math.sin</i> (exp)	Sine function
<i>math.cos</i> (exp)	Cosine function
<i>math.tan</i> (exp)	Tangent function

### **sasoptpy.math.math\_func**

**math\_func** (*exp*, *op*, \**args*)

Function wrapper for math functions

#### **Parameters**

**exp** [Expression] Expression where the math function will be applied

**op** [string] String representation of the math function

**args** [float, optional] Additional arguments

### **sasoptpy.math.abs**

**abs** (*exp*)

Absolute value function

### **sasoptpy.math.log**

**log** (*exp*)

Natural logarithm function

### **sasoptpy.math.log2**

**log2** (*exp*)

Logarithm function in base 2

### **sasoptpy.math.log10**

**log10** (*exp*)

Logarithm function in base 10

### **sasoptpy.math.exp**

**exp** (*exp*)

Exponential function

### **sasoptpy.math.sqrt**

**sqrt** (*exp*)

Square root function

**sasoptpy.math.mod**

**mod** (*exp*, *divisor*)  
Modulo function

**Parameters**

**exp** [Expression] Dividend  
**divisor** [Expression] Divisor

**sasoptpy.math.int**

**int** (*exp*)  
Integer value function

**sasoptpy.math.sign**

**sign** (*exp*)  
Sign value function

**sasoptpy.math.max**

**max** (*exp*, \**args*)  
Largest value function

**sasoptpy.math.min**

**min** (*exp*, \**args*)  
Smallest value function

**sasoptpy.math.sin**

**sin** (*exp*)  
Sine function

**sasoptpy.math.cos**

**cos** (*exp*)  
Cosine function

## sasoptpy.math.tan

**tan** (*exp*)  
Tangent function

## 5.5 Tests

### 5.5.1 Unit Tests

#### Core

<code>test_expression.</code> <code>TestExpression([methodName])</code>	Unit tests for <i>sasoptpy.Expression</i> objects
<code>test_objective.TestObjective([methodName])</code>	Unit tests for <i>sasoptpy.Objective</i> objects
<code>test_model.TestModel([methodName])</code>	Unit tests for <i>sasoptpy.Model</i> objects
<code>test_variable.TestVariable([methodName])</code>	Unit tests for <i>sasoptpy.Variable</i> objects
<code>test_variable_group.</code> <code>TestVariableGroup([...])</code>	Unit tests for <i>sasoptpy.VariableGroup</i> objects
<code>test_constraint.</code> <code>TestConstraint([methodName])</code>	Unit tests for <i>sasoptpy.Constraint</i> objects
<code>test_constraint_group.</code> <code>TestConstraintGroup([...])</code>	Unit tests for <i>sasoptpy.ConstraintGroup</i> objects
<code>test_util.TestUtil([methodName])</code>	Unit tests for core utility functions

#### tests.core.test\_expression.TestExpression

**class TestExpression** (*methodName='runTest'*)  
Bases: `unittest.case.TestCase`  
Unit tests for *sasoptpy.Expression* objects

#### tests.core.test\_objective.TestObjective

**class TestObjective** (*methodName='runTest'*)  
Bases: `unittest.case.TestCase`  
Unit tests for *sasoptpy.Objective* objects

#### tests.core.test\_model.TestModel

**class TestModel** (*methodName='runTest'*)  
Bases: `unittest.case.TestCase`  
Unit tests for *sasoptpy.Model* objects

**tests.core.test\_variable.TestVariable**

**class TestVariable** (*methodName='runTest'*)  
 Bases: `unittest.case.TestCase`  
 Unit tests for *sasoptpy.Variable* objects

**tests.core.test\_variable\_group.TestVariableGroup**

**class TestVariableGroup** (*methodName='runTest'*)  
 Bases: `unittest.case.TestCase`  
 Unit tests for *sasoptpy.VariableGroup* objects

**tests.core.test\_constraint.TestConstraint**

**class TestConstraint** (*methodName='runTest'*)  
 Bases: `unittest.case.TestCase`  
 Unit tests for *sasoptpy.Constraint* objects

**tests.core.test\_constraint\_group.TestConstraintGroup**

**class TestConstraintGroup** (*methodName='runTest'*)  
 Bases: `unittest.case.TestCase`  
 Unit tests for *sasoptpy.ConstraintGroup* objects

**tests.core.test\_util.TestUtil**

**class TestUtil** (*methodName='runTest'*)  
 Bases: `unittest.case.TestCase`  
 Unit tests for core utility functions

**Abstract**

<i>test_math.TestAbstractMath</i> ( <i>methodName</i> )	Unit tests for mathematical functions
<i>test_set.TestSet</i> ( <i>methodName</i> )	Unit tests for <i>sasoptpy.abstract.Set</i> objects
<i>test_set_iterator.TestSetIterator</i> ( <i>methodName</i> )	Unit tests for <i>sasoptpy.abstract.SetIterator</i> objects
<i>test_parameter.TestParameter</i> ( <i>methodName</i> )	
<i>test_implicit_variable.TestImplicitVariable</i> ( <i>...</i> )	Unit tests for <i>sasoptpy.abstract.ImplicitVar</i> objects
<i>test_condition.TestCondition</i> ( <i>methodName</i> )	Unit tests for abstract conditions to be executed on the server
<i>statement.test_assignment.TestAssignment</i> ( <i>...</i> )	Unit tests for assignment statements

Continued on next page

Table 37 – continued from previous page

<code>statement.test_cofor_loop.</code> <code>TestCoforLoop([...])</code>	Unit tests for concurrent for (COFOR) statements
<code>statement.test_create_data.</code> <code>TestCreateData([...])</code>	Unit tests for CREATE DATA statements
<code>statement.test_drop_restore.</code> <code>TestDropRestore([...])</code>	Unit tests for DROP and RESTORE statements
<code>statement.test_fix_unfix.</code> <code>TestFix([methodName])</code>	Unit tests for FIX and UNFIX statements
<code>statement.test_for_loop.</code> <code>TestForLoop([methodName])</code>	Unit tests for FOR statements
<code>statement.test_if_else.</code> <code>TestIfElse([methodName])</code>	Unit tests for IF/ELSE and SWITCH statements
<code>statement.test_literal.</code> <code>TestLiteral([methodName])</code>	Unit tests for literal statements
<code>statement.test_read_data.</code> <code>TestReadData([...])</code>	Unit tests for READ DATA statements
<code>statement.test_solve.</code> <code>TestSolve([methodName])</code>	Unit tests for SOLVE statements

### tests.abstract.test\_math.TestAbstractMath

**class** **TestAbstractMath** (*methodName='runTest'*)

Bases: `unittest.case.TestCase`

Unit tests for mathematical functions

### tests.abstract.test\_set.TestSet

**class** **TestSet** (*methodName='runTest'*)

Bases: `unittest.case.TestCase`

Unit tests for `sasoptpy.abstract.Set` objects

### tests.abstract.test\_set\_iterator.TestSetIterator

**class** **TestSetIterator** (*methodName='runTest'*)

Bases: `unittest.case.TestCase`

Unit tests for `sasoptpy.abstract.SetIterator` objects

### tests.abstract.test\_parameter.TestParameter

**class** **TestParameter** (*methodName='runTest'*)

Bases: `unittest.case.TestCase`



**tests.abstract.test\_implicit\_variable.TestImplicitVariable**

```
class TestImplicitVariable (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for sasoptpy.abstract.ImplicitVar objects
```

**tests.abstract.test\_condition.TestCondition**

```
class TestCondition (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for abstract conditions to be executed on the server
```

**tests.abstract.statement.test\_assignment.TestAssignment**

```
class TestAssignment (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for assignment statements
```

**tests.abstract.statement.test\_cofor\_loop.TestCoforLoop**

```
class TestCoforLoop (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for concurrent for (COFOR) statements
```

**tests.abstract.statement.test\_create\_data.TestCreateData**

```
class TestCreateData (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for CREATE DATA statements
```

**tests.abstract.statement.test\_drop\_restore.TestDropRestore**

```
class TestDropRestore (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for DROP and RESTORE statements
```

### **tests.abstract.statement.test\_fix\_unfix.TestFix**

```
class TestFix (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for FIX and UNFIX statements
```

### **tests.abstract.statement.test\_for\_loop.TestForLoop**

```
class TestForLoop (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for FOR statements
```

### **tests.abstract.statement.test\_if\_else.TestIfElse**

```
class TestIfElse (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for IF/ELSE and SWITCH statements
```

### **tests.abstract.statement.test\_literal.TestLiteral**

```
class TestLiteral (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for literal statements
```

### **tests.abstract.statement.test\_read\_data.TestReadData**

```
class TestReadData (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for READ DATA statements
```

### **tests.abstract.statement.test\_solve.TestSolve**

```
class TestSolve (methodName='runTest')  
    Bases: unittest.case.TestCase  
    Unit tests for SOLVE statements
```

## Interface

---

<code>test_cas_interface.</code>	Unit tests for the CAS interface
<code>TestCASInterface([methodName])</code>	
<code>test_sas_interface.</code>	Unit tests for the SAS interface
<code>TestSASInterface([methodName])</code>	

---

### tests.interface.test\_cas\_interface.TestCASInterface

```
class TestCASInterface (methodName='runTest')
    Bases: unittest.case.TestCase
    Unit tests for the CAS interface
```

### tests.interface.test\_sas\_interface.TestSASInterface

```
class TestSASInterface (methodName='runTest')
    Bases: unittest.case.TestCase
    Unit tests for the SAS interface
```

## Session

---

<code>test_workspace.TestWorkspace([methodName])</code>	Unit tests for the <i>sasoptpy.Workspace</i> objects
---	--

---

### tests.session.test\_workspace.TestWorkspace

```
class TestWorkspace (methodName='runTest')
    Bases: unittest.case.TestCase
    Unit tests for the sasoptpy.Workspace objects
```



## VERSION HISTORY

This page outlines changes from each release.

### 6.1 v0.2.1 (February 26, 2019)

#### 6.1.1 New Features

- Support for evaluating nonlinear expressions is added, see `Expression.get_value()` and `utils._evaluate()`
- Support for multiple objectives is added for LSO solver, see `Model.set_objective()` and *Multiobjective* example
- Support for spaces inside variable indices is added
- Experimental RESTful API is added

#### 6.1.2 Changes

- Dictionaries inside components are replaced with ordered dictionaries to preserve deterministic behavior
- Math operators are added into the keys of linear coefficient dictionaries
- Some iterators are rewritten by using the *yield* keyword for performance
- `key_name` and `col_names` parameters are added into `read_table()`

#### 6.1.3 Bug Fixes

- Fixed: Using a single variable as an objective is producing incorrect input
- Fixed: `Expression.get_value()` fails to evaluate expressions with operators
- Fixed: `Expression.add()` overrides operators in some instances
- Fixed: Expressions with same components but different operators get summed incorrectly
- Fixed: New version of Viya complains about `pandas.DataFrame` column types
- Syntax fixes for **PEP 8** compliance

### 6.1.4 Notes

- A Jupyter notebook example of the Diet Problem is added
- A new example is added to show usage of experimental RESTful API
- Unit tests are added for development repository
- CI/CD integration is added for the development repository on Gitlab
- Generated models can be checked by using the hash values inside tests.responses

## 6.2 v0.2.0 (July 30, 2018)

### 6.2.1 New Features

- Support for the new runOptmodel CAS action is added
- Nonlinear optimization model building support is added for both SAS 9.4 and SAS Viya solvers
- Abstract model building support is added when using SAS Viya solvers
- New object types, `Set`, `SetIterator`, `Parameter`, `ParameterValue`, `ImplicitVar`, `ExpressionDict`, and `Statement` are added for abstract model building
- `Model.to_optmodel()` method is added for exporting model objects into PROC OPTMODEL code as a string
- Wrapper functions `read_table()` and `read_data()` are added to read CASTable and DataFrame objects into the models
- Math function wrappers are added
- `_expr` and `_defn` methods are added to all object types for producing OPTMODEL expression and definitions
- Multiple solutions are now returned when using `solveMilp` action and can be retrieved by using `Model.get_solution()` method
- `Model.get_variable_value()` is added to get solution values of abstract variables

### 6.2.2 Changes

- Variable and constraint naming schemes are replaced with OPTMODEL equivalent versions
- Variables and constraints now preserve the order in which they are inserted to the problem
- `Model.to_frame()` method is updated to reflect changes to `VariableGroup` and `ConstraintGroup` orderings
- Two solve methods, `solve_on_cas` and `solve_on_viya` are merged into `Model.solve()`
- `Model.solve()` method checks the available CAS actions and uses the runOptmodel action whenever possible
- As part of the merging process, `lp` and `milp` arguments are replaced with `options` argument in `Model.solve()` and `Model.to_optmodel()`
- An optional argument `frame` is added to `Model.solve()` for forcing use of MPS mode and `solveLp-solveMilp` actions
- Minor changes are applied to `__str__` and `__repr__` methods
- Creation indices for objects are being kept by using the return of the `register_name()` function

- Objective constant values are now being passed by using new CAS action arguments when possible
- A linearity check is added for models
- Test folder is added to the repository

### 6.2.3 Bug Fixes

- Nondeterministic behavior when generating MPS files is fixed.

### 6.2.4 Notes

- Abstract and nonlinear models can be solved on Viya only if the `runOptmodel` action is available on the CAS server.
- Three new examples are added which demonstrate abstract model building.
- Some minor changes are applied to the existing examples.

## 6.3 v0.1.2 (April 24, 2018)

### 6.3.1 New Features

- As an experimental feature, sasoptpy now supports *SASPy* connections
- `Model.solve_local()` method is added for solving optimization problems by using SAS 9.4 installations
- `Model.drop_variable()`, `Model.drop_variables()`, `Model.drop_constraint()`, `Model.drop_constraints()` methods are added
- `Model.get_constraint()` and `Model.get_constraints()` methods are added to retrieve *Constraint* objects in a model
- `Model.get_variables()` method is added
- `_dual` attribute is added to the *Expression* objects
- `Variable.get_dual()` and `Constraint.get_dual()` methods are added
- `Expression.set_name()` method is added

### 6.3.2 Changes

- Session argument accepts `saspy.SASsession` objects
- `VariableGroup.mult()` method now supports `pandas.DataFrame`
- Type check for the `Model.set_session()` is removed to support new session types
- Problem and solution summaries are not being printed by default anymore, see `Model.get_problem_summary()` and `Model.get_solution_summary()`
- The default behavior of dropping the table after each solve is changed, but can be controlled with the `drop` argument of the `Model.solve()` method

### 6.3.3 Bug Fixes

- Fixed: Variables do not appear in MPS files if they are not used in the model
- Fixed: `Model.solve()` primalin argument does not pass into options

### 6.3.4 Notes

- A `.gitignore` file is added to the repository.
- A new example is added: Decentralization. Both *CAS* and *SAS* versions of the new example are added.
- There is a known issue with the nondeterministic behavior when creating MPS tables. This will be fixed with a hotfix after the release.
- A new option (no-ex) is added to makedocs script for skipping examples when building docs.

## 6.4 v0.1.1 (February 26, 2018)

### 6.4.1 New Features

- Initial value argument 'init' is added for *Variable* objects
- `Variable.set_init()` method is added for variables
- Initial value option 'primalin' is added to `Model.solve()` method
- Table name argument 'name', table drop option 'drop', and replace option 'replace' are added to `Model.solve()` method
- Decomposition block implementation is rewritten; block numbers does not need to be consecutive and ordered `Model.upload_user_blocks()`
- `VariableGroup.get_name()` and `ConstraintGroup.get_name()` methods are added
- `Model.test_session()` method is added for checking if session is defined for models
- `expr_sum()` function is added for faster summation of *Expression* objects

### 6.4.2 Changes

- `methods.py` is renamed to `utils.py`

### 6.4.3 Bug Fixes

- Fixed: Crash in VG and CG when a key not in the list is called
- Fixed: `get_value` of pandas is deprecated
- Fixed: Variables can be set as temporary expressions
- Fixed: Ordering in `get_solution_table()` is incorrect for multiple entries



## 6.5 v0.1.0 (December 22, 2017)

- Initial release



## PYTHON MODULE INDEX

### S

`sasoptpy`, [1](#)



## Symbols

`__repr__()` (*Expression method*), 205  
`__str__()` (*Expression method*), 206  
`_expr()` (*Expression method*), 204  
`_is_linear()` (*Expression method*), 205  
`_is_linear()` (*Model method*), 195  
`_relational()` (*Expression method*), 205

## A

`abs()` (*in module sasoptpy.math*), 264  
`add()` (*Expression method*), 200  
`add_constraint()` (*Model method*), 177  
`add_constraints()` (*Model method*), 178  
`add_implicit_variable()` (*Model method*), 173  
`add_parameter()` (*Model method*), 182  
`add_set()` (*Model method*), 181  
`add_statement()` (*Model method*), 182  
`add_to_member_value()` (*Expression method*), 203  
`add_variable()` (*Model method*), 172  
`add_variables()` (*Model method*), 173  
`append()` (*Workspace method*), 224  
`append_objective()` (*Model method*), 170  
`Assignment` (*class in sasoptpy.abstract.statement*), 230  
`Auxiliary` (*class in sasoptpy*), 197

## C

`CASMediator` (*class in sasoptpy.interface*), 232  
`clear_solution()` (*Model method*), 194  
`cofor_loop()` (*in module sasoptpy.actions*), 251  
`CoForLoopStatement` (*class in sasoptpy.abstract.statement*), 230  
`Constraint` (*class in sasoptpy*), 217  
`ConstraintGroup` (*class in sasoptpy*), 221  
`convert_to_original()` (*SASMediator method*), 238  
`copy()` (*Expression method*), 201  
`copy()` (*Variable method*), 210  
`copy_member()` (*Expression method*), 203  
`cos()` (*in module sasoptpy.math*), 265  
`create_data()` (*in module sasoptpy.actions*), 246

`CreateDataStatement` (*class in sasoptpy.abstract.statement*), 230

## D

`delete_member()` (*Expression method*), 204  
`dict_to_frame()` (*in module sasoptpy*), 240  
`diff()` (*in module sasoptpy.actions*), 262  
`drop()` (*in module sasoptpy.actions*), 260  
`drop_constraint()` (*Model method*), 180  
`drop_constraints()` (*Model method*), 180  
`drop_variable()` (*Model method*), 176  
`drop_variables()` (*Model method*), 177  
`DropStatement` (*class in sasoptpy.abstract.statement*), 230

## E

`exp()` (*in module sasoptpy.math*), 264  
`exp_range()` (*in module sasoptpy*), 240  
`expand()` (*in module sasoptpy.actions*), 259  
`expr_sum()` (*in module sasoptpy*), 242  
`Expression` (*class in sasoptpy*), 196

## F

`fix()` (*in module sasoptpy.actions*), 255  
`FixStatement` (*class in sasoptpy.abstract.statement*), 231  
`flatten_frame()` (*in module sasoptpy*), 241  
`for_loop()` (*in module sasoptpy.actions*), 250  
`ForLoopStatement` (*class in sasoptpy.abstract.statement*), 231

## G

`get_all_keys()` (*ConstraintGroup method*), 222  
`get_all_objectives()` (*Model method*), 171  
`get_attributes()` (*Variable method*), 209  
`get_attributes()` (*VariableGroup method*), 213  
`get_constant()` (*Expression method*), 202  
`get_constraint()` (*Model method*), 179  
`get_constraints()` (*Model method*), 179  
`get_dual()` (*Constraint method*), 219  
`get_dual()` (*Expression method*), 200  
`get_dual()` (*Variable method*), 210

[get\\_elements\(\)](#) (*Workspace method*), 224  
[get\\_expressions\(\)](#) (*ConstraintGroup method*), 222  
[get\\_grouped\\_constraints\(\)](#) (*Model method*), 179  
[get\\_grouped\\_variables\(\)](#) (*Model method*), 175  
[get\\_implicit\\_variables\(\)](#) (*Model method*), 175  
[get\\_member\(\)](#) (*Expression method*), 202  
[get\\_member\\_dict\(\)](#) (*Expression method*), 202  
[get\\_member\\_value\(\)](#) (*Expression method*), 202  
[get\\_members\(\)](#) (*ConstraintGroup method*), 223  
[get\\_members\(\)](#) (*VariableGroup method*), 214  
[get\\_name\(\)](#) (*ConstraintGroup method*), 222  
[get\\_name\(\)](#) (*Expression method*), 199  
[get\\_name\(\)](#) (*Model method*), 169  
[get\\_name\(\)](#) (*Variable method*), 210  
[get\\_name\(\)](#) (*VariableGroup method*), 213  
[get\\_objective\(\)](#) (*Model method*), 171  
[get\\_objective\\_value\(\)](#) (*Model method*), 191  
[get\\_parameters\(\)](#) (*Model method*), 183  
[get\\_problem\\_summary\(\)](#) (*Model method*), 192  
[get\\_sense\(\)](#) (*Objective method*), 207  
[get\\_session\(\)](#) (*Model method*), 169  
[get\\_session\\_type\(\)](#) (*Model method*), 169  
[get\\_sets\(\)](#) (*Model method*), 183  
[get\\_solution\(\)](#) (*Model method*), 189  
[get\\_solution\\_summary\(\)](#) (*Model method*), 191  
[get\\_statements\(\)](#) (*Model method*), 184  
[get\\_tuner\\_results\(\)](#) (*Model method*), 193  
[get\\_type\(\)](#) (*Variable method*), 209  
[get\\_type\(\)](#) (*VariableGroup method*), 213  
[get\\_value\(\)](#) (*Constraint method*), 218  
[get\\_value\(\)](#) (*Expression method*), 199  
[get\\_value\(\)](#) (*Variable method*), 211  
[get\\_value\\_table\(\)](#) (*in module sasoptpy*), 241  
[get\\_variable\(\)](#) (*Model method*), 174  
[get\\_variable\(\)](#) (*Workspace method*), 225  
[get\\_variable\\_coef\(\)](#) (*Model method*), 176  
[get\\_variable\\_value\(\)](#) (*Model method*), 190  
[get\\_variables\(\)](#) (*Model method*), 174

## I

[if\\_condition\(\)](#) (*in module sasoptpy.actions*), 252  
[IfElseStatement](#) (*class in sasoptpy.abstract.statement*), 231  
[ImplicitVar](#) (*class in sasoptpy.abstract*), 229  
[include\(\)](#) (*Model method*), 184  
[int\(\)](#) (*in module sasoptpy.math*), 265

## L

[LiteralStatement](#) (*class in sasoptpy.abstract.statement*), 231  
[log\(\)](#) (*in module sasoptpy.math*), 264  
[log10\(\)](#) (*in module sasoptpy.math*), 264

[log2\(\)](#) (*in module sasoptpy.math*), 264

## M

[math\\_func\(\)](#) (*in module sasoptpy.math*), 264  
[max\(\)](#) (*in module sasoptpy.math*), 265  
[min\(\)](#) (*in module sasoptpy.math*), 265  
[mod\(\)](#) (*in module sasoptpy.math*), 265  
[Model](#) (*class in sasoptpy*), 167  
[mult\(\)](#) (*Expression method*), 201  
[mult\(\)](#) (*VariableGroup method*), 215  
[mult\\_member\\_value\(\)](#) (*Expression method*), 203

## O

[Objective](#) (*class in sasoptpy*), 206  
[ObjectiveStatement](#) (*class in sasoptpy.abstract.statement*), 231

## P

[Parameter](#) (*class in sasoptpy.abstract*), 226  
[ParameterGroup](#) (*class in sasoptpy.abstract*), 226  
[parse\\_cas\\_solution\(\)](#) (*CASMediator method*), 234  
[parse\\_cas\\_table\(\)](#) (*CASMediator method*), 234  
[parse\\_cas\\_workspace\\_response\(\)](#) (*CASMediator method*), 236  
[parse\\_print\\_responses\(\)](#) (*Workspace method*), 225  
[parse\\_sas\\_mps\\_solution\(\)](#) (*SASMediator method*), 238  
[parse\\_sas\\_solution\(\)](#) (*SASMediator method*), 238  
[parse\\_sas\\_table\(\)](#) (*SASMediator method*), 238  
[parse\\_sas\\_workspace\\_response\(\)](#) (*SASMediator method*), 239  
[parse\\_solve\\_responses\(\)](#) (*Workspace method*), 225  
[perform\\_postsolve\\_operations\(\)](#) (*SASMediator method*), 238  
[print\\_item\(\)](#) (*in module sasoptpy.actions*), 257  
[print\\_solution\(\)](#) (*Model method*), 194  
[PrintStatement](#) (*class in sasoptpy.abstract.statement*), 232  
[put\\_item\(\)](#) (*in module sasoptpy.actions*), 258  
[Python Enhancement Proposals](#)  
     PEP 498, 5  
     PEP 8, 273

## Q

[quick\\_sum\(\)](#) (*in module sasoptpy*), 242

## R

[read\\_data\(\)](#) (*in module sasoptpy.actions*), 243  
[ReadDataStatement](#) (*class in sasoptpy.abstract.statement*), 231

`reset()` (in module *sasoptpy*), 242  
`restore()` (in module *sasoptpy.actions*), 260

## S

*SASMediator* (class in *sasoptpy.interface*), 236  
*sasoptpy* (module), 1  
*Set* (class in *sasoptpy.abstract*), 227  
`set_active_model()` (*Workspace* method), 224  
`set_block()` (*Constraint* method), 219  
`set_bounds()` (*Variable* method), 208  
`set_bounds()` (*VariableGroup* method), 214  
`set_constraint_values()` (*CASMediator* method), 234  
`set_direction()` (*Constraint* method), 219  
`set_init()` (*Variable* method), 209  
`set_init()` (*VariableGroup* method), 214  
`set_member()` (*Expression* method), 202  
`set_member_value()` (*Expression* method), 203  
`set_model_objective_value()` (*CASMediator* method), 234  
`set_name()` (*Expression* method), 198  
`set_objective()` (in module *sasoptpy.actions*), 257  
`set_objective()` (*Model* method), 169  
`set_permanent()` (*Expression* method), 199  
`set_rhs()` (*Constraint* method), 220  
`set_sense()` (*Objective* method), 207  
`set_session()` (*Model* method), 169  
`set_temporary()` (*Expression* method), 199  
`set_value()` (in module *sasoptpy.actions*), 254  
`set_variable_init_values()` (*CASMediator* method), 234  
`set_variable_value()` (*Workspace* method), 225  
`set_variable_values()` (*CASMediator* method), 234  
`set_workspace_variable_values()` (*CASMediator* method), 236  
`set_workspace_variable_values()` (*SASMediator* method), 239  
*SetIterator* (class in *sasoptpy.abstract*), 228  
*SetIteratorGroup* (class in *sasoptpy.abstract*), 228  
`sign()` (in module *sasoptpy.math*), 265  
`sin()` (in module *sasoptpy.math*), 265  
`solve()` (*CASMediator* method), 233  
`solve()` (in module *sasoptpy.actions*), 249  
`solve()` (*Model* method), 186  
`solve()` (*SASMediator* method), 237  
`solve_with_mps()` (*CASMediator* method), 233  
`solve_with_mps()` (*SASMediator* method), 237  
`solve_with_optmodel()` (*CASMediator* method), 233  
`solve_with_optmodel()` (*SASMediator* method), 237  
*SolveStatement* (class in *sasoptpy.abstract.statement*), 231

`sqrt()` (in module *sasoptpy.math*), 264  
*Statement* (class in *sasoptpy.abstract*), 229  
`submit()` (*CASMediator* method), 236  
`submit()` (*SASMediator* method), 239  
`submit()` (*Workspace* method), 224  
`submit_optmodel_code()` (*CASMediator* method), 236  
`submit_optmodel_code()` (*SASMediator* method), 239  
`substring()` (in module *sasoptpy.actions*), 262  
`sum()` (*VariableGroup* method), 216  
`switch_conditions()` (in module *sasoptpy.actions*), 253  
*Symbol* (class in *sasoptpy*), 198

## T

`tan()` (in module *sasoptpy.math*), 266  
*TestAbstractMath* (class in *tests.abstract.test\_math*), 268  
*TestAssignment* (class in *tests.abstract.statement.test\_assignment*), 269  
*TestCASInterface* (class in *tests.interface.test\_cas\_interface*), 271  
*TestCoforLoop* (class in *tests.abstract.statement.test\_cofor\_loop*), 269  
*TestCondition* (class in *tests.abstract.test\_condition*), 269  
*TestConstraint* (class in *tests.core.test\_constraint*), 267  
*TestConstraintGroup* (class in *tests.core.test\_constraint\_group*), 267  
*TestCreateData* (class in *tests.abstract.statement.test\_create\_data*), 269  
*TestDropRestore* (class in *tests.abstract.statement.test\_drop\_restore*), 269  
*TestExpression* (class in *tests.core.test\_expression*), 266  
*TestFix* (class in *tests.abstract.statement.test\_fix\_unfix*), 270  
*TestForLoop* (class in *tests.abstract.statement.test\_for\_loop*), 270  
*TestIfElse* (class in *tests.abstract.statement.test\_if\_else*), 270  
*TestImplicitVariable* (class in *tests.abstract.test\_implicit\_variable*), 269  
*TestLiteral* (class in *tests.abstract.statement.test\_literal*), 270  
*TestModel* (class in *tests.core.test\_model*), 266  
*TestObjective* (class in *tests.core.test\_objective*), 266

TestParameter (class in *tests.abstract.test\_parameter*), 268

TestReadData (class in *tests.abstract.statement.test\_read\_data*), 270

TestSASInterface (class in *tests.interface.test\_sas\_interface*), 271

TestSet (class in *tests.abstract.test\_set*), 268

TestSetIterator (class in *tests.abstract.test\_set\_iterator*), 268

TestSolve (class in *tests.abstract.statement.test\_solve*), 270

TestUtil (class in *tests.core.test\_util*), 267

TestVariable (class in *tests.core.test\_variable*), 267

TestVariableGroup (class in *tests.core.test\_variable\_group*), 267

TestWorkspace (class in *tests.session.test\_workspace*), 271

to\_expression() (*Expression* class method), 204

to\_frame() (*Model* method), 196

to\_mps() (*Model* method), 194

to\_optmodel() (*Model* method), 195

to\_optmodel() (*Workspace* method), 225

tune() (*CASMediator* method), 233

tune\_parameters() (*Model* method), 187

tune\_problem() (*CASMediator* method), 233

## U

unfix() (*in module sasoptpy.actions*), 256

UnfixStatement (class in *sasoptpy.abstract.statement*), 231

union() (*in module sasoptpy.actions*), 261

update\_var\_coef() (*Constraint* method), 220

upload\_model() (*CASMediator* method), 235

upload\_user\_blocks() (*CASMediator* method), 235

use\_problem() (*in module sasoptpy.actions*), 263

## V

Variable (class in *sasoptpy*), 207

VariableGroup (class in *sasoptpy*), 211

## W

Workspace (class in *sasoptpy*), 223