

Relational Algebra

Chapter 4, Part A

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Relational Query Languages

- ❖ Query languages: Allow manipulation and **retrieval of data** from a database.
- ❖ Relational model supports simple, powerful QLs:
 - Strong formal foundation based on logic.
 - Allows for much optimization.
- ❖ Query Languages **!=** programming languages! 
 - QLs not expected to be “Turing complete”.
 - QLs not intended to be used for complex calculations.
 - QLs support easy, efficient access to large data sets.

Formal Relational Query Languages

- ❖ Two mathematical Query Languages form the basis for “real” languages (e.g. SQL), and for implementation:
 - Relational Algebra: More **operational**, very useful for representing execution plans.
 - Relational Calculus: Lets users describe what they want, rather than how to compute it. (**Non-operational**, declarative.)

Preliminaries

- ❖ A query is applied to *relation instances*, and the result of a query is also a relation instance.
 - *Schemas of input* relations for a query are *fixed* (but query will run regardless of instance!)
 - The *schema for the result* of a given query is also *fixed*! Determined by definition of query language constructs.
- ❖ Positional vs. named-field notation:
 - Positional notation easier for formal definitions, named-field notation more readable.
 - Both used in SQL

Example Schema

Sailors(sid: integer, sname: string, rating: integer, age: real)

Boats(bid: integer, bname: string, color: string)

Reserves(sid: integer, bid: integer, day: date).

Example Instances

R1

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

S1

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

- ❖ “Sailors” and “Reserves” relations for our examples.
- ❖ We’ll use positional or named field notation, assume that names of fields in query results are ‘inherited’ from names of fields in query input relations.

Relational Algebra

❖ Basic operations:

- Selection (σ) Selects a subset of rows from relation.
- Projection (π) Deletes unwanted columns from relation.
- Cross-product (\times) Allows us to combine two relations.
- Set-difference ($-$) Tuples in reln. 1, but not in reln. 2.
- Union (\cup) Tuples in reln. 1 and in reln. 2.

❖ Additional operations:

- Intersection, join, division, renaming: Not essential, but (very!) useful.

❖ Since each operation returns a relation, **operations can be composed!** (Algebra is “closed”.)

Projection

- ❖ Deletes attributes that are not in *projection list*.
- ❖ *Schema* of result contains exactly the fields in the projection list, with the same names that they had in the (only) input relation.
- ❖ Projection operator has to eliminate *duplicates*! (Why??)
 - Note: real systems typically don't do duplicate elimination unless the user explicitly asks for it. (Why not?)

sname	rating
yuppy	9
lubber	8
guppy	5
rusty	10

$\pi_{sname, rating}(S2)$

age
35.0
55.5

$\pi_{age}(S2)$

Selection

sid	sname	rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

- ❖ Selects rows that satisfy *selection condition*.

$$\sigma_{rating > 8}(S2)$$

- ❖ No duplicates in result! (Why?)

- ❖ *Schema* of result identical to schema of (only) input relation.

- ❖ Result relation can be the *input* for another relational algebra operation! (Operator composition.)

*select sname, rating
from S2
where rating > 8*

sname	rating
yuppy	9
rusty	10

σ_{rating > 8}(π_{sname, rating}(σ_{rating > 8}(S2)))

Union, Intersection, Set-Difference

- ❖ All of these operations take two input relations, which must be union-compatible:
 - Same number of fields.
 - ‘Corresponding’ fields have the same type.
- ❖ What is the *schema* of result?

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

$S1 \cup S2$

sid	sname	rating	age
22	dustin	7	45.0


$S1 - S2$

sid	sname	rating	age
31	lubber	8	55.5
58	rusty	10	35.0

$S1 \cap S2$

Cross-Product

- ❖ Each row of S2 is paired with each row of R1.
- ❖ *Result schema* has one field per field of S2 and R1, with field names 'inherited' if possible.
 - *Conflict*: Both S2 and R1 have a field called *sid*.



<u>(sid)</u>	sname	rating	age	<u>(sid)</u>	bid	day
22	dustin	7	45.0	22	101	10/10/96
<u>22</u>	dustin	7	45.0	<u>58</u>	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
<u>31</u>	lubber	8	55.5	<u>58</u>	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

$S_1 \times R_1$

- *Renaming operator*: $\rho (C(\underline{1} \rightarrow \underline{sid1}, \underline{5} \rightarrow \underline{sid2}), S1 \times R1)$

Joins

❖ Condition Join: $R \bowtie_c S = \sigma_c(R \times S)$

(sid)	sname	rating	age	(sid)	bid	day
<u>22</u>	dustin	7	45.0	<u>58</u>	103	11/12/96
<u>31</u>	lubber	8	55.5	<u>58</u>	103	11/12/96

$S1 \bowtie_{S1.sid < R1.sid} R1$

- ❖ *Result schema* same as that of cross-product.
- ❖ Fewer tuples than cross-product, might be able to compute more efficiently
- ❖ Sometimes called a *theta-join*.

Joins

- ❖ Equi-Join: A special case of condition join where the condition c contains only *equalities*.

sid	sname	rating	age	bid	day
22	dustin	7	45.0	101	10/10/96
58	rusty	10	35.0	103	11/12/96

$$S1 \bowtie_{sid} R1$$

- ❖ *Result schema* similar to cross-product, but only one copy of fields for which equality is specified.
- ❖ Natural Join: Equijoin on all common fields.

Find names of sailors who've reserved boat #103

❖ Solution 1:

$\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$

❖ Solution 2:

$\rho(Temp1, \sigma_{bid=103} Reserves)$

$\rho(Temp2, Temp1 \bowtie Sailors)$

$\pi_{sname}(Temp2)$

❖ Solution 3:

$\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$

Find names of sailors who've reserved a red boat
select s.name from Sailors S, Reserves R, Boats B where S.sid = R.sid and R.bid = B.bid and B.color = 'red'

❖ Information about boat color only available in Boats; so need an extra join:

$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$

❖ A more efficient solution:

$\pi_{sname}(\pi_{sid}((\pi_{bid}(\sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors))$

A query optimizer can find this, given the first solution!

Find sailors who've reserved a red or a green boat

- ❖ Can identify all red or green boats, then find sailors who've reserved one of these boats:

$$\rho \text{ (Tempboats, } (\sigma_{\text{color} = 'red' \vee \text{color} = 'green'} \text{Boats}))$$
$$\pi_{\text{sname}}(\text{Tempboats} \bowtie \text{Reserves} \bowtie \text{Sailors})$$

Empty?

- ❖ Can also define Tempboats using union! (How?)
- ❖ What happens if \vee is replaced by \wedge in this query?

Find sailors who've reserved a red and a green boat

- ❖ Previous approach won't work! Must identify sailors who've reserved red boats, sailors who've reserved green boats, then find the intersection (note that *sid* is a key for Sailors):

$\rho(\text{Tempred}, \pi_{sid}((\sigma_{\text{color} = 'red'} \text{Boats}) \bowtie \text{Reserves}))$

$\rho(\text{Tempgreen}, \pi_{sid}((\sigma_{\text{color} = 'green'} \text{Boats}) \bowtie \text{Reserves}))$

$\pi_{sname}((\text{Tempred} \cap \text{Tempgreen}) \bowtie \text{Sailors})$

Summary

- ❖ The relational model has rigorously defined query languages that are simple and powerful.
- ❖ Relational algebra is more operational; useful as internal representation for query evaluation plans.
- ❖ Several ways of expressing a given query; a query optimizer should choose the most efficient version.