

# Discrete Optimization Specialization: Workshop 0

## First Steps

### 1 Introduction

This workshop is simply about getting used to MiniZinc, and trying out a few trivial models.

#### 1.1 Hello World - `hello.mzn`

Build a MiniZinc model `hello.mzn` that outputs the result “Hello World”!

Test it from the IDE or from the command line using

```
minizinc hello.mzn
```

#### 1.2 Input and Output - `io.mzn`

Build a MiniZinc model `io.mzn` that takes a data file defining integer parameter  $n$  and outputs its value.

Test it using different values of  $d$  as the value for  $n$ , which it should print out. In the IDE, running the model should pop up a box asking you to input the value for  $n$ . Using the command line you can enter the value  $d$  for parameter  $n$  as follows:

```
minizinc io.mzn -D"n = d;"
```

#### 1.3 Simple Decision - `x110.mzn`

Build a MiniZinc model `x110.mzn` with a single decision variable  $x$  taking values from one to ten, which outputs its value.

Test that it prints out all solutions. In the IDE you can do this by in the Configuration tab, changing from “Default behavior” to “User-defined behavior” and change the number in “Stop after this many solutions (0 means ”all”)” to 0. You can test it on the command line using

```
minizinc x110.mzn -a
```

#### 1.4 Simple Optimization - `xopt.mzn`

Build a MiniZinc model `xopt.mzn` with a decision variable  $x$  taking values from 0 to 10, with constraints to ensure that  $x$  is divisible by 4, which outputs the value of  $x$  that gives the minimum value of  $(x - 7)^2$ .

Testing it in the IDE you should see that it prints out more than one solution. The last solution is the optimal, and the others are solutions found on the search to the optimal.

Or test it on the command line using

```
minizinc xopt.mzn
```

which should print out just the optimal solution, or instead

```
minizinc xopt.mzn -a
```

which should print out all the solutions it found on the way to the optimal. Notice how the `-a` flag means different things for satisfaction problems (all solutions to the problem) and optimization problems (all solutions found on the way to the optimal). In the IDE the default behavior for optimization problems is to print out all solutions on the way to the optimal.

*Question* Suppose you cannot use the `mod` function, how would you alternatively model that  $x$  is divisible by 4?

## 1.5 Arrays - array.mzn

Define a MiniZinc model `array.mzn` which takes an integer parameter  $n$  defining the length of an array of numbers  $x$  taking values from 0 to 9. Constrain the array so the sum of the numbers in the array is equal to the product of the numbers in the array. Output the resulting array.

Test it using the IDE set to print out all solutions as described for `x110.mzn`. Alternatively test your model from the command line using

```
minizinc array.mzn -a
```

which should print out all the solutions for  $x$ .

Add a constraint to ensure that the numbers in the array are non-decreasing, i.e.  $x[1] \leq x[2] \leq \dots \leq x[n]$ . This should reduce the number of similar solutions. This is an example of *symmetry breaking* which will be very useful.

How big a number can you solve with your model? Why do you think this happens?

## 1.6 A Sequence - seq.mzn

Define a MiniZinc model `seq.mzn` which takes a integer parameter  $n$  defining the length of an array of numbers  $x$  taking values from 0 to 3. Constrain the numbers so that the first number is zero, the last number is 3, and the sum of any two adjacent numbers in the array  $x$  is at most 3. Also constrain the value of  $x$  at positions divisible by 3 to be greater than or equal to 2. Maximize the sum of the numbers in the array  $x$ . The output should be of the form *sum = array of values*, e.g.

```
6 = [0,1,2,0,3]
```

given a solution  $x = [0, 1, 2, 0, 3]$  for  $n = 5$ .

Test your model for various values  $d$  of  $n$  using either the IDE pop up box to enter the value for  $n$ , or from the command line using

```
minizinc seq.mzn -D"n = d;"
```

Test out at least the values of  $d$  from 3 to 9.