

# Solving Proximity Constraints

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## 1 Introduction

## 2 System Model

## 3 Workflow

## 4 Usage and Experience with the presented Tools

# Motivation

For proving theorems, a frequently occurring problem is to find common instances of formulae.

## Example 1

Let  $f$  be a function,  $a, b$  constants and  $x$  a variable. The two expressions

$$f(a, x) \quad \text{and} \quad f(a, b)$$

can be unified with  $\{x \mapsto b\}$ .

# Motivation

For proving theorems, a frequently occurring problem is to find common instances of formulae.

## Example 2

Let  $f, g$  be functions,  $a, b$  constants and  $x$  a variable. The two expressions

$$f(a, x) \quad \text{and} \quad g(a, b)$$

cannot be unified as  $f \neq g$ .

# Motivation

In 1965 Robinson presented his unification algorithm and solved this problem, his algorithm was improved for better(=faster) performance since.

If we consider now the unification problem

$$f(a, x) \simeq^? g(a, b)$$

again, we might wonder, if we could not ignore  $f \neq g$ , if they are “close” to each other, i.e. if they are equal in a fuzzy logic sense. Being close is represented as a proximity relation, which are symmetric and reflexive, but not necessarily transitive. C. Pau and T. Kutsia solved this problem, presenting an algorithm, which we implemented.

# Introduction

The Algorithm consists of two sub-algorithms and works on (modifies) 4 sets:

- $P$ : unification problem to be solved ,
- $C$ : neighbourhood constraint,
- $\sigma$ : set of pre-unifier,
- $\Phi$ : name-class mapping,

where Algorithm 1 modifies  $P$ ,  $C$ , and  $\sigma$  and Algorithm 2 modifies  $C$  and  $\Phi$ . If Algorithm 1 was successful,  $P = \emptyset$ , if Algorithm 2 was successful  $C = \emptyset$ .

## pre-Unification rules

$$\text{(Tri)} \{x \simeq^? x\} \uplus P; C; \sigma \Rightarrow P; C; \sigma$$

(Dec)

$$\{F(\overline{s_n}) \simeq^? G(\overline{t_n})\} \uplus P; C; \sigma \Rightarrow \{\overline{s_n \simeq^? t_n}\} \cup P; \{F \approx^? G\} \cup C; \sigma$$

$$\text{(VE)} \{x \simeq^? t\} \uplus P; C; \sigma \Rightarrow \{t' \simeq^? t\} \cup P; x \mapsto t'; C; \sigma \{x \mapsto t'\}$$

$$\text{(Ori)} \{t \simeq^? x\} \uplus P; C; \sigma \Rightarrow \{x \simeq^? t\} \cup P; C; \sigma$$

$$\text{(Cla)} \{F(\overline{s_n}) \simeq^? G(\overline{t_n})\} \uplus P; C; \sigma \Rightarrow \perp \text{ if } m \neq n$$

(Occ)

$$\{x \simeq^? t\} \uplus P; C; \sigma \Rightarrow \perp \text{ if there is an occurrence cycle of } x \text{ in } t$$

(VO)

$$\{x \simeq^? y, \overline{x_n \simeq^? y_n}\}; C; \sigma \Rightarrow \{\overline{x_n \simeq^? y_n}\} \{x \mapsto y\}; C; \sigma \{x \mapsto y\}$$

## Rules for Neighbourhood Constraints

(FFS)  $\{f \approx^? g\} \uplus C; \Phi \Rightarrow C; \Phi$ ; if  $\mathcal{R}(f, g) \geq \lambda$

(NFS)  $\{N \approx^? g\} \uplus C; \Phi \Rightarrow C; \text{update}(\Phi, N \rightarrow \mathbf{pc}(g, \mathcal{R}, \lambda))$

(FSN)  $\{g \approx^? N\} \uplus C; \Phi \Rightarrow \{N \approx^? g\} \cup C; \Phi$

(NN1)

$\{N \approx^? M\} \uplus C; \Phi \Rightarrow C; \text{update}(\Phi, N \rightarrow \{f\}, M \rightarrow \mathbf{pc}(f, \mathcal{R}, \lambda))$ ,  
where  $N \in \text{dom}(\Phi)$ ,  $f \in \Phi(N)$

(NN2)  $\{M \approx^? N\} \uplus C; \Phi \Rightarrow \{N \approx^? M\} \cup C; \Phi$ , where  
 $M \notin \text{dom}(\Phi)$ ,  $N \in \text{dom}(\Phi)$

(Fail1)  $\{f \approx^? g\} \uplus C; \Phi \Rightarrow \perp$ , if  $\mathcal{R}(f, g) < \lambda$

(Fail2)  $C; \Phi \Rightarrow \perp$ , if there exists  $N \in \text{dom}(\Phi)$  such that  $\Phi(N) = \emptyset$



# Simple example about how both algorithms work

## Example 3

Let  $p, q$  and  $f$  be functions,  $b, c, c'$  constants and  $x, z$  variables.  
Then the following unification problem has a solution:

$$p(x, z) =^? q(f(b), f(x)) \quad \text{with} \quad R = \{(b, c'), (c', c), (p, q)\}$$

# Simple example - pre-Unification fails

## Example [Fail pU]

Examples where the pre-Unification algorithm fails:

$$(Occ) \quad p(x) =^? q(f(x)) \quad (1)$$

$$(Cla) \quad p(a, b) =^? q(f(x)) \quad (2)$$

# Simple example - Constraint Simplification fails

## Example [Fail CS]

Let  $p$  and  $f$  be functions,  $a, b$  constants and  $x, y$  variables. Then for the following unification problem only the pre-Unification algorithm is successful:

$$p(a, x, a) =^? q(y, b, x) \quad \text{with} \quad R = \{(b, c), (p, q)\}$$

# Simple example cont.

## pre-Unification

...

$$C = \{p \approx^? q, N_1 \approx^? a, N_2 \approx^? b, a \approx^? N_2\}$$

## Constraint Simplification

$$C = \{p \approx^? q, N_1 \approx^? a, N_2 \approx^? b, a \approx^? N_2\}$$

$$\Phi = \{\}$$

$\Rightarrow_{\text{FFS}}$

$$C = \{N_1 \approx^? a, N_2 \approx^? b, a \approx^? N_2\}$$

$$\Phi = \{\}$$

$\Rightarrow_{\text{NFS}^2}$

## Simple example cont.

$$C = \{a \approx^? N_2\}$$

$$\Phi = \{N_1 \mapsto \{a\}, N_2 \mapsto \{b, c\}\}$$

$$\Rightarrow_{\text{FSN}}$$

$$C = \{N_2 \approx^? a\}$$

$$\Phi = \{N_1 \mapsto \{a\}, N_2 \mapsto \{b, c\}\}$$

$$\Rightarrow_{\text{NFS}}$$

$$C = \{\}$$

$$\Phi = \{N_1 \mapsto \{a\}, N_2 \mapsto \emptyset\}$$

$$\Rightarrow_{\text{Fail2}}$$

$$\perp$$

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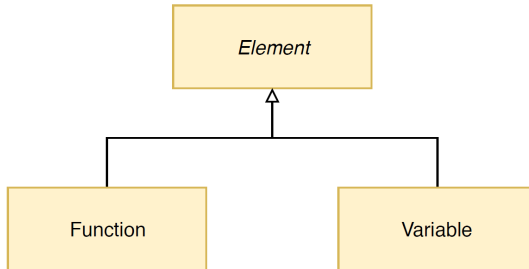
## 4 Usage and Experience with the presented Tools

# System Model

Project consists of 4 packages:

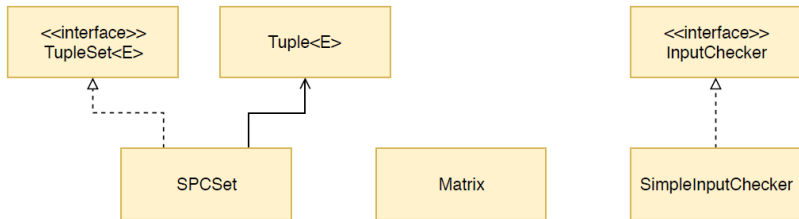
- elements : contains all needed types
- tool : offers important tools (e.g. read input)
- unificationProblem : has the core features
- userInterfaces : provide user interfaces

# Package elements

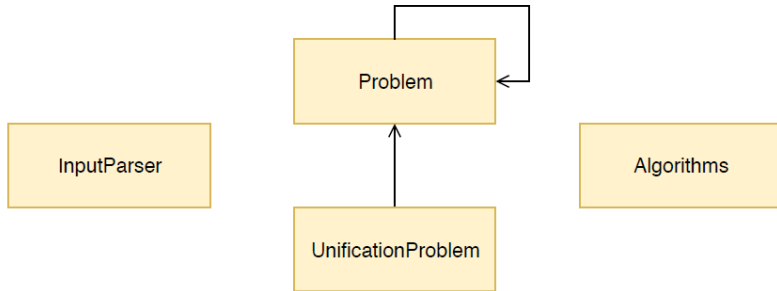




# Package tool



# Package unificationProblem



# Package userInterfaces

SPC\_CL

SPC\_GUI

WebInterface

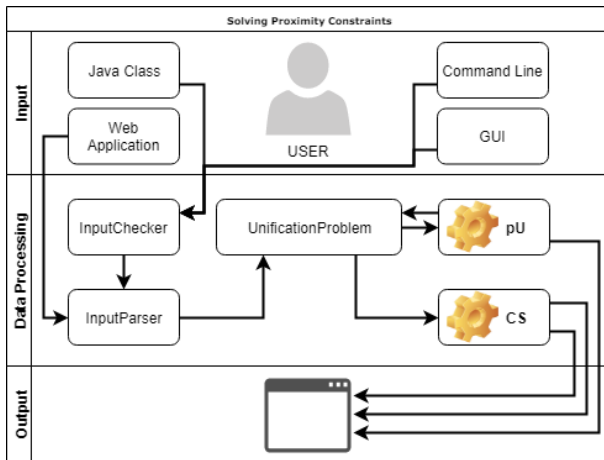
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# Workflow



## 1 Introduction

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## 4 Usage and Experience with the presented Tools

# Redmine/UML

- Redmine - useful feature
- Communication:
  - Redmine forum
  - Whatsapp
  - meetings before the lectures
- UML
  - used it from the beginning
  - to express and communicate our ideas

# Git/Javadoc

- Git
  - own Git repository for the project
  - merged branches
  - committed continuously
- Javadoc
  - used it from the beginning
  - displaying it as a tooltip



# JUnit/Jenkins

- JUnit 5
- good to find bugs
- not easy to call from the CMD/Jenkins
- JUnit 5 - strict naming of test classes