

Solving Proximity Constraints

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- 2 System Model
- 3 Workflow
- 4 Usage and Experience with the presented Tools

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For proving theorems, a frequently occurring problem is to find common instances of formulae.

Example 1

Let f be a function, a, b constants and x a variable. The two expressions

$$f(a,x)$$
 and $f(a,b)$

can be unified with $\{x \mapsto b\}$.



Motivation

Introduction

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For proving theorems, a frequently occurring problem is to find common instances of formulae.

Example 2

Let f, g be functions, a, b constants and x a variable. The two expressions

$$f(a,x)$$
 and $g(a,b)$

cannot be unified as $f \neq g$.

Motivation

Introduction

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In 1965 Robinson presented his unification algorithm and solved this problem, his algorithm was improved for better(=faster) performance since.

If we consider now the unification problem

$$f(a,x) \simeq^{?} g(a,b)$$

again, we might wonder, if we could not ignore $f \neq g$, if they are "close" to each other, i.e. if they are equal in a fuzzy logic sense. Being close is represented as a proximity relation, which are symmetric and reflexive, but not necessarily transitive. C. Pau and T. Kutsia solved this problem, presenting an algorithm, which we implemented.

Introduction

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The Algorithm consists of two sub-algorithms and works on (modifies) 4 sets:

- P: unification problem to be solved ,
- C: neighbourhood constraint,
- \bullet σ : set of pre-unifier,
- Φ: name-class mapping,

where Algorithm 1 modifies P, C, and σ and Algorithm 2 modifies C and Φ . If Algorithm 1 was successful, $P = \emptyset$, if Algorithm 2 was successful $C = \emptyset$.



pre-Unification rules

(Tri)
$$\{x \simeq^{?} x\} \uplus P; C; \sigma \Rightarrow P; C; \sigma$$

(Dec) $\{F(\overline{s_n}) \simeq^{?} G(\overline{t_n})\} \uplus P; C; \sigma \Rightarrow \{\overline{s_n} \simeq^{?} \overline{t_n}\} \cup P; \{F \approx^{?} G\} \cup C; \sigma$
(VE) $\{x \simeq^{?} t\} \uplus P; C; \sigma \Rightarrow \{t' \simeq^{?} t\} \cup Px \mapsto t'; C; \sigma\{x \mapsto t'\}$
(Ori) $\{t \simeq^{?} x\} \uplus P; C; \sigma \Rightarrow \{x \simeq^{?} t\} \cup P; C; \sigma$
(Cla) $\{F(\overline{s_n}) \simeq^{?} G(\overline{t_n})\} \uplus P; C; \sigma \Rightarrow \bot$ if $m \neq n$
(Occ) $\{x \simeq^{?} t\} \uplus P; C; \sigma \Rightarrow \bot$ if there is an occurrence cycle of x in t
(VO) $\{x \simeq^{?} v, \overline{x_n} \simeq^{?} \overline{y_n}\}; C; \sigma \Rightarrow \{\overline{x_n} \simeq^{?} \overline{y_n}\}\{x \mapsto v\}; C; \sigma\{x \mapsto v\}$

Rules for Neighbourhood Constraints

(FFS)
$$\{f \approx^? g\} \uplus C; \Phi \Rightarrow C; \Phi; \text{ if } \mathcal{R}(f,g) \geq \lambda$$

(NFS)
$$\{N \approx^? g\} \uplus C; \Phi \Rightarrow C; update(\Phi, N \rightarrow pc(g, \mathcal{R}, \lambda))$$

(FSN)
$$\{g \approx^? N\} \uplus C; \Phi \Rightarrow \{N \approx^? g\} \cup C; \Phi$$

(NN1)

$$\{N \approx^? M\} \uplus C; \Phi \Rightarrow C; update(\Phi, N \rightarrow \{f\}, M \rightarrow pc(f, \mathcal{R}, \lambda)),$$

where $N \in dom(\Phi), f \in \Phi(N)$

(NN2)
$$\{M \approx^? N\} \uplus C; \Phi \Rightarrow \{N \approx^? M\} \cup C; \Phi$$
, where $M \notin dom(\Phi), N \in dom(\Phi)$

(Fail1)
$$\{f \approx^? g\} \uplus C; \Phi \Rightarrow \bot$$
, if $\mathcal{R}(f,g) < \lambda$

(Fail2) C; $\Phi \Rightarrow \perp$, if there exists $N \in dom(\Phi)$ such that $\Phi(N) = \emptyset$



Simple example about how both algorithms work

Example 3

Introduction

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Let p, q and f be functions, b, c, c' constants and x, z variables. Then the following unification problem has a solution:

$$p(x,z) = {}^{?} q(f(b), f(x))$$
 with $R = \{(b,c'), (c',c), (p,q)\}$

Example [Fail pU]

Introduction 00000000000

Examples where the pre-Unification algorithm fails:

$$(Occ) \quad p(x) = q(f(x)) \tag{1}$$

(Cla)
$$p(a,b) = q(f(x))$$
 (2)

Example [Fail CS]

Introduction

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Let p and q be functions, a, b, c constants and x, y variables. Then for the following unification problem only the pre-Unification algorithm is successful:

$$p(a, x, a) = (y, b, x)$$
 with $R = \{(b, c), (p, q)\}$

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Simple example cont.

pre-Unification

Introduction

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$$\textit{C} = \{\textit{p} \approx^? \textit{q}, \textit{N}_1 \approx^? \textit{a}, \textit{N}_2 \approx^? \textit{b}, \textit{a} \approx^? \textit{N}_2\}$$

Constraint Simplification

$$C = \{p \approx^? q, N_1 \approx^? a, N_2 \approx^? b, a \approx^? N_2\}$$

$$\Phi = \{\}$$

$$\Rightarrow^{FFS}$$

$$C = \{N_1 \approx^? a, N_2 \approx^? b, a \approx^? N_2\}$$

$$\Phi = \{\}$$

$$\Rightarrow^{NFS^2}$$

Simple example cont.

$$C = \{a \approx^{?} N_{2}\}$$

$$\Phi = \{N_{1} \mapsto \{a\}, N_{2} \mapsto \{b, c\}\}$$

$$\Rightarrow^{FSN}$$

$$C = \{N_{2} \approx^{?} a\}$$

$$\Phi = \{N_{1} \mapsto \{a\}, N_{2} \mapsto \{b, c\}\}$$

$$\Rightarrow^{NFS}$$

$$C = \{\}$$

$$\Phi = \{N_{1} \mapsto \{a\}, N_{2} \mapsto \emptyset\}$$

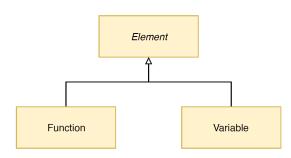
$$\Rightarrow^{Fail2}$$

- 2 System Model

System Model

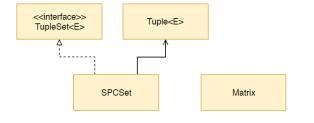
Project consists of 4 packages:

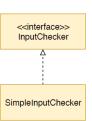
- elements : contains all needed types
- tool : offers important tools (e.g. store proximity relations)
- unificationProblem : has the core features
- userInterfaces : provide user interfaces



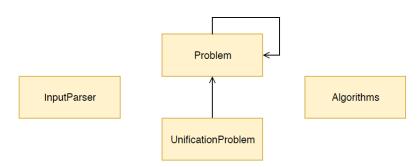


Package tool





Package unificationProblem





Package userInterfaces

Introduction

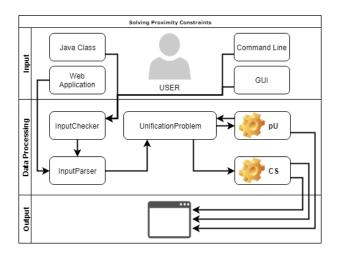
SPC_CL

SPC_GUI

WebInterface

- 2 System Model
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- 4 Usage and Experience with the presented Tool

Workflow



- 2 System Model
- 3 Workflow
- 4 Usage and Experience with the presented Tools



Redmine/UML

- Redmine useful feature
- Communication:
 - Redmine forum
 - Whatsapp
 - meetings before the lectures
- UMI
 - used it from the beginning
 - to express and communicate our ideas

Git

- own Git repository for the project
- merged branches
- committed continuously
- Javadoc
 - used it from the beginning
 - displaying it as a tooltip

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JUnit/Jenkins

- JUnit 5
- good to find bugs
- not easy to call from the CMD/Jenkins
- JUnit 5 strict naming of test classes