

Solving Proximity Constraints

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- 2 System Model
- 3 Workflow
- 4 Usage and Experience with the presented Tools

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For proving theorems, a frequently occurring problem is to find common instances of formulae.

Example 1

Let f be a function, a, b constants and x a variable. The two expressions

$$f(a,x)$$
 and $f(a,b)$

can be unified with $\{x \mapsto b\}$.

Motivation

Introduction

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For proving theorems, a frequently occurring problem is to find common instances of formulae.

Example 2

Let f, g be functions, a, b constants and x a variable. The two expressions

$$f(a,x)$$
 and $g(a,b)$

cannot be unified as $f \neq g$.



Motivation

In 1965 Robinson presented his unification algorithm and solved this problem, his algorithm was improved for better(=faster) performance since.

If we consider now the unification problem

$$f(a,x) \simeq^{?} g(a,b)$$

again, we might wonder, if we could not ignore $f \neq g$, if they are "close" to each other, i.e. if they are equal in a fuzzy logic sense. Being close is represented as a proximity relation, which are symmetric and reflexive, but not necessarily transitive. C. Pau and T. Kutsia solved this problem, presenting an algorithm, which we implemented.

Introduction

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The Algorithm consists of two sub-algorithms and works on (modifies) 4 sets:

- P: unification problem to be solved ,
- C: neighbourhood constraint,
- \bullet σ : set of pre-unifier,
- Φ: name-class mapping,

where Algorithm 1 modifies P, C, and σ and Algorithm 2 modifies C and Φ . If Algorithm 1 was successful, $P = \emptyset$, if Algorithm 2 was successful $C = \emptyset$.



pre-Unification rules

Introduction

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(Tri)
$$\{x \simeq^{?} x\} \uplus P; C; \sigma \Rightarrow P; C; \sigma$$

(Dec) $\{F(\overline{s_n}) \simeq^{?} G(\overline{t_n})\} \uplus P; C; \sigma \Rightarrow \{\overline{s_n} \simeq^{?} t_n\} \cup P; \{F \approx^{?} G\} \cup C; \sigma$
(VE) $\{x \simeq^{?} t\} \uplus P; C; \sigma \Rightarrow \{t' \simeq^{?} t\} \cup Px \mapsto t'; C; \sigma\{x \mapsto t'\}$
(Ori) $\{t \simeq^{?} x\} \uplus P; C; \sigma \Rightarrow \{x \simeq^{?} t\} \cup P; C; \sigma$
(Cla) $\{F(\overline{s_n}) \simeq^{?} G(\overline{t_n})\} \uplus P; C; \sigma \Rightarrow \bot$ if $m \neq n$
(Occ) $\{x \simeq^{?} t\} \uplus P; C; \sigma \Rightarrow \bot$ if there is an occurrence cycle of x in t
(VO) $\{x \simeq^{?} v, \overline{x_n} \simeq^{?} \overline{y_n}\}; C; \sigma \Rightarrow \{\overline{x_n} \simeq^{?} \overline{y_n}\}\{x \mapsto v\}; C; \sigma\{x \mapsto v\}$

Rules for Neighbourhood Constraints

(FFS)
$$\{f \approx^? g\} \uplus C; \Phi \Rightarrow C; \Phi; \text{ if } \mathcal{R}(f,g) \geq \lambda$$

(NFS)
$$\{N \approx^? g\} \uplus C; \Phi \Rightarrow C; update(\Phi, N \rightarrow pc(g, \mathcal{R}, \lambda))$$

(FSN)
$$\{g \approx^? N\} \uplus C; \Phi \Rightarrow \{N \approx^? g\} \cup C; \Phi$$

(NN1)

$$\{N \approx^? M\} \uplus C; \Phi \Rightarrow C; update(\Phi, N \rightarrow \{f\}, M \rightarrow pc(f, \mathcal{R}, \lambda)),$$
 where $N \in dom(\Phi), f \in \Phi(N)$

(NN2)
$$\{M \approx^? N\} \uplus C; \Phi \Rightarrow \{N \approx^? M\} \cup C; \Phi$$
, where $M \notin dom(\Phi), N \in dom(\Phi)$

(Fail1)
$$\{f \approx^? g\} \uplus C; \Phi \Rightarrow \bot$$
, if $\mathcal{R}(f,g) < \lambda$

(Fail2)
$$C$$
; $\Phi \Rightarrow \bot$, if there exists $N \in dom(\Phi)$ such that $\Phi(N) = \emptyset$

Simple example about how both algorithms work

Example 3

Introduction

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Let p, q and f be functions, b, c, c' constants and x, z variables. Then the following unification problem has a solution:

$$p(x,z) = {}^{?} q(f(b), f(x))$$
 with $R = \{(b,c'), (c',c), (p,q)\}$



Simple example

Introduction

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Example - both success

$$p(x,z) = q(f(b), f(x))$$
 and $R = \{(b,c'), (c',c), (p,q)\}$

pre-Unification

$$P = \{p \simeq^{?} q\}$$

$$C = \{\}$$

$$\sigma = \{\}$$

$$\Rightarrow^{\text{Dec}}$$

$$P = \{x \simeq^{?} f, z \simeq^{?} f\}$$

$$C = \{p \approx^{?} q\}$$

$$\sigma = \{\}$$

$$\Rightarrow^{\text{VE}}$$

Introduction

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$$P = \{N_{1}(N_{2}) \simeq^{?} f(b), z \simeq^{?} f(N_{1}(N_{2}))\}$$

$$C = \{p \approx^{?} q\}$$

$$\sigma = \{x \mapsto N_{1}(N_{2})\}$$

$$\Rightarrow^{Dec^{2}}$$

$$p(x, z) =^{?} q(f(b), f(x)); R = \{(a, a'), (a', b), (b, c'), (c', c), (p, q)\}$$

$$P = \{z \simeq^{?} f\}$$

$$C = \{p \approx^{?} q, N_{1} \approx^{?} f, N_{2} \approx^{?} b\}$$

$$\sigma = \{x \mapsto N_{1}(N_{2})\}$$

$$\Rightarrow^{VE}$$

$$P = \{N_{3}(N_{4}(N_{5})) \simeq^{?} f(N_{1}(N_{2}))\}$$

$$C = \{p \approx^{?} q, N_{1} \approx^{?} f, N_{2} \approx^{?} b\}$$

$$\sigma = \{x \mapsto N_{1}(N_{2}), z \mapsto N_{3}(N_{4}(N_{5}))\}$$

$$\Rightarrow^{Dec^{3}}$$

Usage and Experience with the presented Tools

Introduction 00000000000

$$P = \{\}$$

$$C = \{p \approx^{?} q, N_{1} \approx^{?} f, N_{2} \approx^{?} b, N_{3} \approx^{?} f, N_{4} \approx^{?} N_{1}, N_{5} \approx^{?} N_{2} \}$$

$$\sigma = \{x \mapsto N_{1}(N_{2}), z \mapsto N_{3}(N_{4}(N_{5})) \}$$

Constraint Simplification

$$C = \{p \approx^{?} q, N_{1} \approx^{?} f, N_{2} \approx^{?} b, N_{3} \approx^{?} f, N_{4} \approx^{?} N_{1}, N_{5} \approx^{?} N_{2}\}$$

$$\Phi = \{\}$$

$$\Rightarrow FFS$$

$$C = \{N_{1} \approx^{?} f, N_{2} \approx^{?} b, N_{3} \approx^{?} f, N_{4} \approx^{?} N_{1}, N_{5} \approx^{?} N_{2}\}$$

$$\Phi = \{\}$$

$$\Rightarrow NFS^{3}$$

Usage and Experience with the presented Tools

Introduction

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$$C = \{N_4 \approx^? N_1, N_5 \approx^? N_2\}$$

$$\Phi = \{N1 \mapsto \{f\}, N2 \mapsto \{b, c'\}, N3 \mapsto \{f\}\}$$

$$\Rightarrow^{NN2}$$

$$C = \{N_1 \approx^? N_4, N_5 \approx^? N_2\}$$

$$\Phi = \{N1 \mapsto \{f\}, N2 \mapsto \{b, c'\}, N3 \mapsto \{f\}\}$$

$$\Rightarrow^{NN1}$$

$$C = \{N_5 \approx^? N_2\}$$

$$\Phi = \{N1 \mapsto \{f\}, N2 \mapsto \{b, c'\}, N3 \mapsto \{f\}, N4 \mapsto \{f\}\}$$

 $R = \{(b, c'), (c', c), (p, q)\}$

Usage and Experience with the presented Tools

→NN2,NN1



$$C = \{\}$$

$$\Phi_1 = \{N1 \mapsto \{f\}, N2 \mapsto \{b\}, N3 \mapsto \{f\}, N4 \mapsto \{f\}, N5 \mapsto \{b, c'\}\}$$

$$\{b, c'\}\}$$

$$\Phi_2 = \{N1 \mapsto \{f\}, N2 \mapsto \{c'\}, N3 \mapsto \{f\}, N4 \mapsto \{f\}, N5 \mapsto \{b, c', c\}\}$$

Solution

$$\Phi_{1} = \{N1 \mapsto \{f\}, N2 \mapsto \{b\}, N3 \mapsto \{f\}, N4 \mapsto \{f\}, N5 \mapsto \{b, c'\}\}
\Phi_{2} = \{N1 \mapsto \{f\}, N2 \mapsto \{c'\}, N3 \mapsto \{f\}, N4 \mapsto \{f\}, N5 \mapsto \{b, c', c\}\}
\sigma = \{x \mapsto N_{1}(N_{2}), z \mapsto N_{3}(N_{4}(N_{5}))\}$$

Simple example - pre-Unification fails

Example [Fail pU]

Introduction 0000000000

Examples where the pre-Unification algorithm fails:

$$(Occ) \quad p(x) = q(f(x)) \tag{1}$$

Usage and Experience with the presented Tools

(Cla)
$$p(a,b) = q(f(x))$$
 (2)

Simple example - Constraint Simplification fails

Example [Fail CS]

Introduction

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Let p and f be functions, a, b constants and x, y variables. Then for the following unification problem only the pre-Unification algorithm is successful:

$$p(a, x, a) = (y, b, x)$$
 with $R = \{(b, c), (p, q)\}$

pre-Unification

Introduction

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$$\textit{C} = \{\textit{p} \approx^? \textit{q}, \textit{N}_1 \approx^? \textit{a}, \textit{N}_2 \approx^? \textit{b}, \textit{a} \approx^? \textit{N}_2\}$$

Constraint Simplification

$$C = \{p \approx^{?} q, N_{1} \approx^{?} a, N_{2} \approx^{?} b, a \approx^{?} N_{2}\}$$

$$\Phi = \{\}$$

$$\Rightarrow^{\mathsf{FFS}}$$

$$C = \{N_{1} \approx^{?} a, N_{2} \approx^{?} b, a \approx^{?} N_{2}\}$$

$$\Phi = \{\}$$

$$\Rightarrow^{\mathsf{NFS}^{2}}$$



Simple example cont.

$$C = \{a \approx^{?} N_{2}\}$$

$$\Phi = \{N_{1} \mapsto \{a\}, N_{2} \mapsto \{b, c\}\}$$

$$\Rightarrow^{FSN}$$

$$C = \{N_{2} \approx^{?} a\}$$

$$\Phi = \{N_{1} \mapsto \{a\}, N_{2} \mapsto \{b, c\}\}$$

$$\Rightarrow^{NFS}$$

$$C = \{\}$$

$$\Phi = \{N_{1} \mapsto \{a\}, N_{2} \mapsto \emptyset\}$$

$$\Rightarrow^{Fail2}$$

- 2 System Model

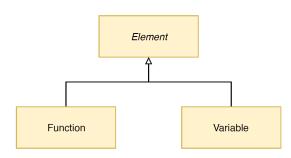


System Model

Project consists of 4 packages:

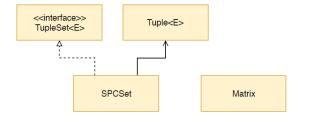
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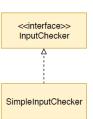
- elements : contains all needed types
- tool : offers important tools (e.g. read input)
- unificationProblem : has the core features
- userInterfaces : provide user interfaces





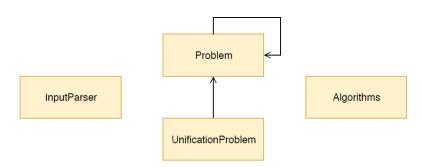
Package tool







Package unificationProblem





Package userInterfaces

Introduction

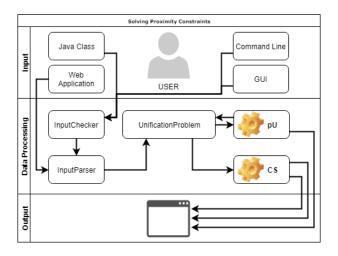
SPC_CL

SPC_GUI

WebInterface

- 2 System Model
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Workflow





- 2 System Model
- 3 Workflow
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Redmine/UML

We found Redmine and its features very helpful for Software development. Mainly, we used it to keep track of work that has to be done, that was done, and also see what the other person is working on. We also tried out the Forum, to communicate when we needed, but we found Whatsapp more suitable for this. For communication: In our opinion, communication is one of the most important things when working in a team, but we tried to restrict ourselves to the communications channels offered by the lecture, so basically Redmine, meeting a few minutes before the lecture, and Whatsapp that is like the Forum + notification when read.

From a very early stage on, we also used UML, to express and communicate our ideas about the project and the implementation as well as to structure it.



Redmine/UML

- Redmine useful feature
- Communication:
 - Redmine forum
 - Whatsapp
 - meetings before the lectures
- UML
 - used it from the beginning
 - to express and communicate our ideas

Git/Javadoc

As it is a requirement for the project, we of course used git a lot. We tried to use branches and merge. As suggested, we committed (and most of the times also pushed) as soon as we further developed the project. As we did not work on the project for 8 hours straight every day in the week, this pretty much models the usage in a company, where you pull at the beginning, then work/commit to save your work and at the end of the day (or at a "milestone") push.

It was very important to us to use Javadoc from the beginning on for almost each method. The reason for that was that eclipse has the nice feature of displaying it as a tooltip, and so you can understand easily the behaviour of the method, even if the other person implemented it.

Git/Javadoc

- Git
 - own Git repository for the project
 - merged branches
 - committed continuously
- Javadoc
 - used it from the beginning
 - displaying it as a tooltip



JUnit/Jenkins

For testing, that was very necessary, to find bugs, we used JUnit 5, although we later found out it is not too easy to use it from command line/Jenkins. It also was a good feeling, that whenever one had altered parts of the code, and run JUnit everything worked out again. At the beginning we had the feeling that Jenkins would not be as useful in our project as it might be in others, but actually, it was nice to use it to simply run all tests. Even though realizing that JUnit 5 has (also) strict naming conventions for test classes took us some time.



JUnit/Jenkins

- JUnit 5
- good to find bugs
- not easy to call from the CMD/Jenkins
- JUnit 5 strict naming of test classes