

# Gametheory and Cybersecurity: a study Fliplt and multiple resources

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hoofdspecialisatie Veilige software

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Voorafgaande schriftelijke toestemming van de promotor is eveneens vereist voor het aanwenden van de in deze masterproef beschreven (originele) methoden, producten, schakelingen en programma's voor industrieel of commercieel nut en voor de inzending van deze publicatie ter deelname aan wetenschappelijke prijzen of wedstrijden.

# Voorwoord

I would like to thank everybody who kept me busy the last year, especially my promotor and my assistants. I would also like to thank the jury for reading the text. My sincere gratitude also goes to my wife and the rest of my family.

*Sophie Marien*

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# Samenvatting

In this thesis I present a work of gametheory merged with cybersecurity. The **abstract** environment contains a more extensive overview of the work. But it should be limited to one page.

# Samenvatting

In dit **abstract** environment wordt een al dan niet uitgebreide Nederlandse samenvatting van het werk gegeven. Wanneer de tekst voor een Nederlandstalige master in het Engels wordt geschreven, wordt hier normaal een uitgebreide samenvatting verwacht, bijvoorbeeld een tiental bladzijden.

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# List of Abbreviations and Symbols

## Abbreviations

LoG	Laplacian-of-Gaussian
MSE	Mean Square error
PSNR	Peak Signal-to-Noise ratio



# Hoofdstuk 1

## Introduction

The first contains a general introduction to the work. The goals are defined and the modus operandi is explained.

bib referenties  
in orde brengen

### 1.1 Introduction

Security is an important asset in the computer science. Technology is growing fast and so are the malicious people. Defending a network of a company is not very easy. It makes use of firewalls, routers, IDS systems, virus scans, and so on. Protecting a company network is difficult job. They are often the victim of targetted attacks. In a security report of 2014, , state that 80% of the companies are the vitims of targeted attacks. Many corporate networks have to continuously defend themselves against outside invaders such as viruses and worms. The network administrator will try to keep the network to malware-free as possible. If still there is an intruder managed to penetrate the network then the network manager this intruder trying to get out as quickly as possible. This is not always easy. Especially when the intruders secretly sneak and then spread rapidly. In this paper we will work further on the work made by Marten van Dijk, Ari Juels, Alina Oprea and Ronals L. Rivest who wrote a report on the Game FlipIt. FlipIt is a the game of "Stealthy Takeovers". It models a game by means of two players, the attacker and the defender. Both can gain control over a single shared resource by flipping it. The most important property of the game is that the flipping happens stealthy. This means that the players have no clue about when the other player moves. The goal of the game is to maximise the time the player controls the resource minus the average cost of the flipping.

verwijzing naar  
report

verwijzing naar  
FlipIT

#### 1.1.1 Motivation of the game

#### 1.1.2 Contributions and results

#### 1.1.3 Conclusions

The "I love you"virus is an example of a virus that spreads quickly. This virus propagates via mail systems. If someone opens an email with "I love you"virus in

## 1. INTRODUCTION

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annex this virus spreads itself by sending a mail itself to everyone in your contact list. So the virus can multiply rapidly and eventually a business network shut down by the heavy traffic. In this example, there is a need human interaction to spread the virus to do. If no one opens the virus can not spread the mail. Unfortunately, there are viruses that can spread without human interaction. These viruses are referred to as worms. A worm is also a computer program that replicates itself to spread to other computers so. Via a computer network, copies of the worm forwarded without an intermediary is used for. The worm will use vulnerabilities to infect other computers. Most worms are designed to spread out and just try not to make any changes to the systems that they pass. These worms can still inflict damage by increased network traffic they generate. Worms that contain Harm damage a program to install a backdoor or a rootkit on the infected computers. Backdoors and rootkits ensure that future use can be made of the infected computers. The Stuxnetworm is a very famous worm. Initially this worm spread via infected USB sticks and from then it could spread through the Internet to other computers. The purpose of the Stuxnetworm was broken to run the centrifuges in nuclear reactors. Many reactors have been infected. From the standpoint of the defender, it is very important to respond as quickly as possible so that the worm can not spread quickly.

## Hoofdstuk 2

# Introduction to Game Theory

In the following paragraph an introduction to game theory is given based on the work of [?] and [?]. For a more detailed and full introduction to game theory, the reader is referred to [?].

### 2.1 Intro Game Theory

Game theory studies the interaction between independent and self-interested agents. It is a mathematical way of modelling the interactions between two or more agents where the outcomes depend on what everybody does and how it should be structured to lead to good outcomes. For this reason it is very important for economics and also for politics, biology, computer science, philosophy and a variety of other disciplines.

One of the assumptions underlying game theory is that the players of the game, the agents, are independent and self-interested. This does not necessarily mean that they want to harm other agents or that they only care about themselves. Instead it means that each agent has preferences about the states of the world he likes. These preferences are mapped to natural numbers and are called the utility function. The numbers are interpreted as a mathematical measure to tell you how much an agent likes or dislikes the states of the world.

It also explains the impact of uncertainty. When an agent is uncertain about a distribution of outcomes, his utility will describe the expected value of the utility function with respect to the probability of the distribution of the outcomes. For example: with 0.7 probability it will be 7 degrees outside and 0.3 probability it will be 10 degrees. The agent can have a different opinion about that distribution versus another distribution. ().

In a decision game theoretic approach an agent will try to act in such a way to maximise his expected or average utility function. It becomes more complicated when two or more agents want to maximise their utility and whose actions can affect each other utilities. This kind of games are referred to as non cooperative game theory, where the basic modelling unit is the group of agents. The individualistic approach, where the basic modelling is only one agent, is referred as cooperative

uitleggen aan  
de hand van een  
voorbeeld

game theory.

There are two standard representations for games. The first one is the Normal Form. The second one is the Extensive Form.

In the following list a couple of terms that will be used throughout the paper.

*Players:* players are referred as the ones who are the decision makers. It can be a person, a company or an animal.

*Actions:* actions are what the player can do.

*Outcomes:*

*Utility function:* the utility function is the mapping of the level of happiness of an agent about the state of the world to natural numbers.

*Strategies:* A strategy is the combination of different actions. A pure strategy is only one action.

A game in game theory consists of multiple agents and every agent has a set of actions that he can play.

## 2.2 Virusses

Stealth Regin's developers put considerable effort into making it highly inconspicuous. Its low key nature means it can potentially be used in espionage campaigns lasting several years. Even when its presence is detected, it is very difficult to ascertain what it is doing. Symantec was only able to analyze the payloads after it decrypted sample files.

It has several "stealth" features. These include anti-forensics capabilities, a custom-built encrypted virtual file system (EVFS), and alternative encryption in the form of a variant of RC5, which isn't commonly used. Regin uses multiple sophisticated means to covertly communicate with the attacker including via ICMP/ping, embedding commands in HTTP cookies, and custom TCP and UDP protocols Ways of defending a network:

- Self-defending networks: The next generation of network security
- Honeynet games: a game theoretic approach to defending network monitors

Many network security threats today are spread over the Internet. The most common include:

Viruses, worms, and Trojan horses Spyware and adware Zero-day attacks, also called zero-hour attacks Hacker attacks Denial of service attacks Data interception and theft Identity theft

Computer virus through mail. Though virus spreading through email is an old technique, it is still effective and is widely used by current viruses and worms. Sending viruses through email has some advantages that are attractive to virus

writers: Sending viruses through email does not require any security holes in computer operating systems or software. Almost everyone who uses computers uses email service. A large number of users have little knowledge of email viruses and trust most email they receive, especially email from their friends [28][29]. Email are private properties like post office letters. Thus correspondent laws or policies are required to permit checking email content for detecting viruses before end users receive email [18].

Send a email with malicious attachment. Only again infected if attachment again opened. Thus this is the action of attacking every neighbour node + also can attack again the node where the virus was coming from. There are also email viruses where the malicious program is hidden in the txt and the attachment does not need to be opened.

### 2.2.1 Malware

Relevant researches:

- How Viruses and worm can be detected. Difference between UDP en TCP worm propagation

## 2.3 Conclusion

The final section of the chapter gives an overview of the important results of this chapter. This implies that the introductory chapter and the concluding chapter don't need a conclusion.





## Hoofdstuk 3

# The FlipIt game

### 3.1 Extensions on FlipIt

There are various possible ways to extend FlipIt. For instance Laszka et al. extended the basic FlipIt game to multiple resources. The incentive is that for compromising a system in a real case it needs more than just taking over one resource. An example is gaining access to a system and breaking the password. The model is called FlipThem [2]. Two ways of flipping the resources are used: the AND and the OR control model. In the AND model the attacker only controls the system if he controls all the resources of the system, whereas in the OR model the attacker only needs to compromise one resource to be in control of the entire system. The difference with FlipThem and this paper is that we introduce a Graph Model in the beginning. Another extension on FlipIt is done by Pham[?] [1]. Beside the action Flip there is another action Test. The basic idea is to test with an extra action if the resource has been compromised or not. This action involves also an extra cost. This model is useful if somebody wants to know for example if his password has been compromised or wants to assess the periodic security of a system. In [?] [?] Laszka et al. they also consider non targeted attacks by non-strategic players and .

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len

In this section, we introduce the game FlipIt [4]. FlipIt is a game introduced by .. and Rivest. First we explain the framework of FlipIt and after that the formulas and assumptions that we will make for the game for during the whole paper.

### 3.2 The First Topic of this Chapter

FlipIt is a two-players game with a shared (single) resource that the players want to control as long as possible. The shared resource can be a password, a network or a secret key depending on the setting being modelled. In the rest of the paper we will call the players the Attacker and the Defender. To get the control over the resource, players can flip the resource at any given time. Each move will imply a certain cost. The unique feature of FlipIt is that the move will happen in a stealthy way, meaning that the other player has no clue that the other player has flipped the

### 3. THE FLIPIT GAME

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resource. For instance, the defender will not find out if the resource has already been compromised by the attacker, but he can only potentially know it after he flips the resource himself. The goal of the player is to maximize the time that he or she has control over the resource while minimizing total cost of the moves. Players won't move to frequently. A move can also result in a "wasted move", called a flop. It may happen that the resource was already under control by the defender. If the defender moves when he or she has already control over the resource, he or she would have wasted move since it does not result in a change of ownership.

Because the players move in a stealthy way, there are different types of feedback that a player can get while moving:

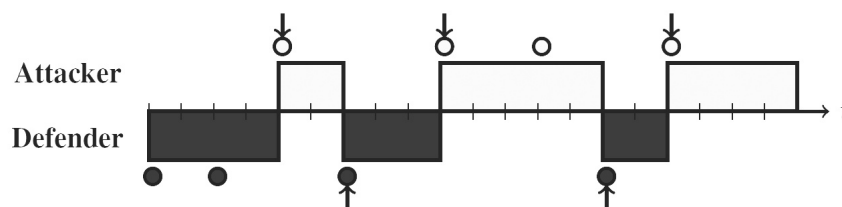
- Non-adaptive (NA): The player does not receive any feedback during the game while flipping.
- Last move (LM): When a player flips it will find out the exact time that the opponent played the last time.
- Full History (FH): When a player flips it will find out the whole history of the opponents move.

The game can be extended by the amount of information that a player receives. It can also be possible for a player to get information at the start of the game. Both interesting cases are:

- Rate-of-play (RP): The player finds out the exact rate of play of the opponent.
- Knowledge-of-strategy (KS): The player finds out the complete information of the strategy that the opponent is playing.

In our assumption the strategy of both players will be non-adaptive. None of the players has information of the strategy of the opponent.

### 3.3 Figures



FIGUUR 3.1: The FlipIt game where both players are playing periodically

Categories	Classes of Strategies
Non-adaptive (NA)	Exponential
	Periodic
	Renewal
	General non-adaptive
Adaptive (AD)	Last move (LM)
	Full History (FH)

TABLE 3.1: Classes of strategies in FlipIt

### 3.3.1 Strategies

In this subsection we go through the strategies used in FlipIt and the most important results.

There are two different kinds of strategies, the *non-adaptive strategies* and the *renewal strategies*. If there is no need for feedback for both of the players, we say that we have a non-adaptive strategy. Because the player does not receive any feedback during the game it will play in the same manner against every opponent. They are not dependent on the opponents movements. This means that they can already generate the time sequence for all the moves in advance. But they can depend on some randomness because the non-adaptive strategies can be randomised. In this paper we will focus in the beginning on the non-adaptive strategies. Reasons behind this is that a player (defender or attacker) rarely knows what the strategies are of his opponent. [If the attacker wants to move stealthily, it might have limited attack options FLIPTHEM].

A renewal strategy is a non-adaptive strategy where the time intervals between two consecutive moves are generated by a renewal process.

nog redenen  
zoeken

Periodic

Non-Arithmetic Renewal

Exponential

### 3.3.2 Actions of the attacker

A virus has different kind of ways of making his way through a company network. We will describe the different ways of how the virus can propagate. For start we will say that the virus or worm will be dropped on Node  $i$  and that it has  $k$  numbers of neighbours.

1. Node  $i$  is infected and will spread the virus or worm to every  $k$  neighbours and will stop infecting the neighbours in the next step
2. Node  $i$  is infected and will spread the virus or worm to every  $k$  neighbours and will keep on spreading the virus in every next step

3. Node  $i$  is infected and will spread the virus to only one of the  $k$  neighbours and will stop infecting another one in the next step
4. Node  $i$  is infected and will spread the virus to only one of the  $k$  neighbours and in the next step it will infect another one of the  $k$  neighbours

In the game that will be modelled in the paper we will use the settings of the 1 spreading method. We will not use method 2 because this kind of propagation will float the network. Because we use the settings of a mail system and contact in a mailing list the method of 3 and 4 are not used.

In the first method the node that has been infected can be again infected. If one of the neighbours infect the node again the node will infect his neighbours again. By using this spreading method we have three states of a node. An infected state, a clean state and a spreading state. And infected state means that the node is infected and will not spread itself again to its neighbours, a clean state means that there is no virus or worm on the node and a spreading state means that the node is infected and that it will spread itself in the next step to its neighbours. We can argument this kind of propagation through a mail worm.

We will model two kind of attacks of the attacker:

1. The attacker drops the virus on a random node on the network
2. The attacker drops the virus on a targeted node on the network

The attacker in this game will put a virus or worm on one of the nodes in the network. This will happen at random. The attacker does not know on which node the virus will be dropped. We will use this randomness because most viruses are spread via a usb stick or a shared resource. If we use this spreading method where we have a targeted attack the attacker will have more information about the network.

The attacker can choose at which rate it will drop a virus on one of the nodes on the network. The cost of dropping a virus will be the same. It will not increase. If it will increase this means that the attacker will eventually drop out of the game because it becomes to expensive.

The attacker is in control over the game if it manages to infect a subset of all the resources of the company network.

#### 3.3.3 Actions of the defender

The attacker wants to protect all the nodes of his network. It can do so by getting back control over the resources. We will assume that the defender of the network has knowledge over his own network. Which is convenient in the real world because a company has to know how his infrastructure looks like.

The defender has two possible ways of defending its network:

1. The defender flips all the nodes of his network

voorbeeld ge-  
ven van zo een  
worm

feit uit security  
rapport syman-  
tec

2. The defender will flip a subset of the nodes of his network

The cost of flipping all the nodes of the network will be greater than the cost of flipping a subset of nodes. We make this assumption because otherwise it will be beneficial for the defender to always flip all the nodes in the network.

We will also make the assumption that as a defender flips a node the node can get infected again. A flip will not be correlated to a patch but to a clean-up. Another setting of the game can be that the flip of the defender is equal to a patch and that the resource cannot be infected any more. But with this case we deviate from the flipIt game, because the attacker cannot flip the resource any more. Unless we work with different viruses every time the attacker flips. We start with the less complex game of flipping is equal to a clean-up.

waarom geen patch, wormen kunnen veranderen gaandeweg

andere mogelijkheid:

### 3.3.4 Strategies of both players

We explained what the actions of each player are.

## 3.4 Formal definition Game

In this section we provide a formal definition of the game and the notation that we will use throughout the paper.

*Players* There are two players in the game, one is the defender and the other one is the attacker. They are respectively identified by 0 and 1.

*Time* The game starts at  $t = 0$  and continues indefinitely as  $t \rightarrow \infty$ . The game is a continuous game.

*Graph* We represent the company network as a Graph  $G = \langle V, E \rangle$ .  $G$  is an ordered pair where  $V$  denotes the set of resources or nodes in the network and  $E$  denotes the set of connections or links, which are a two-element subset of  $V$ . We use the notations resources and nodes interleaving in this paper.

We have  $N$  resources in the network.  $N \in \mathbb{N}$ . This means we can denote the resources by:

aanvullen

$$V \in V_0, V_1, V_2, \dots, V_N$$

The set  $E$  of connections indicates if there is a link between two resources. We see the links as bidirectional so the total graph is undirected. If there is a link between resource  $V_n$  and  $V_{n+1}$  then there is also a link between  $V_{n+1}$  and  $V_n$ .

*Game State* There is also a time-dependent variable that represents the state of the game.  $C = C(t)$  is either 0 if the game is under control by the defender and 1 if the Game is under control by the attacker.

We start at  $t = 0$  with the defender who has control over the game. We do this

### 3. THE FLIPIT GAME

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because we assume that the defender will only put the network online without having a virus or worm in it. The Attacker can gain control over the game when it compromises a subset  $s$  of the resources. The subset  $s$  is a minimum of 1 resource and a maximum of all the resources  $N$ .

We can also define the state of each resource by  $C_N^A$  and  $C_N^D$ . If  $C_N^A = 1$  then this means that the attacker has control over the resource, and 0 otherwise. For  $C_N^D$  it is visa versa,  $C_N^D = 1 - C_N^A$ .

deze variabele  
nodig ja of nee  
? JA

*Moves* Both players can make a move in the game. Moves done in a finite numbers of time in any finite time interval. Both players can play at any time they want, they can also play at the same time. If this happens the one that has control over the resource will keep having control over the resource. This makes the game fully symmetric. The sequence of move times are denoted by the following infinite sequence:

beter uitleggen

$$t = t_1, t_2, t_3, ..$$

Two move times can be the same because we allow players to move at the same time. We can also denote the infinite sequence of times when player  $i$  moves. We write this as :

$$t = t_{i,1}, t_{i,2}, t_{i,3}, .. \text{ with } i \in \{0, 1\}$$

The sequences  $t_1$  and  $t_0$  are disjoint subsets of the sequent  $t$ . We can also denote who made the  $k$ th move by defining a sequence  $p$  that denotes the sequence of who played:

$$p = p_1, p_2, p_3, .. \text{ with } p_k \in \{0, 1\}$$

*Number of moves*  $n_i(t)$  denotes the number of moves made by player  $i$  up to and including time  $t$ . This means that

$$n(t) = n_1(t) + n_0(t)$$

is the sum of the number of moves made by the defender and the attacker up to and including time  $t$ .

*Average move rate* We denote  $\alpha_i(t)$  as the average move rate by player  $i$ :

$$\alpha_i(t) = n_i(t)/t \text{ with } t > 0 \text{ and } i \in \{0, 1\}$$

*Period* We can also define the period in terms of the average move rate:

$$\delta_i = 1/\alpha_i$$

*Who played last* We know who played last by taking the modulo with the period.  $Z_i$  represents the time since the last flip of player i. We can also denote the time since the last flip of player i on resource r by  $Z_i^N$ . For a non adaptive game, period deterministic: At time  $t = n$  is  $Z_i = n \bmod i$ .

*Cost* The cost is an important property of the game. In FlipIt for every player the cost of a move is denoted by  $k_i$ . These costs can be very different for every player. In this game we denote the players flipping cost for resource  $V_N$  by  $c_i^{V_N}$ .

For the defender the cost will be either the cost of flipping every resource or the cost of flipping a subgroup of the resources.

For the attacker the cost will be the cost of dropping a virus on a node. The spreading of the virus will not imply an extra cost.

*Utility* In FlipIt the Gain definition is the utility function. The Gain denotes the total time a player i has gained control over a resource. The Gain  $G_i$  denotes players  $i$  total gain of a game, which is the total time the player has gained control over a subset of resources thus controlling the game. This is denoted by the following:

$$G_i(t) = \int_0^t C_i(x) dx$$

If we sum up the total Gain of the attacker and the defender we end up with the time:

$$G_1(t) + G_0(t) = t$$

*Average gain rate* The average gain rate for player i is defined as

$$\gamma_i(t) = G_i(t)/t$$

### 3.4.1 Formal definition

*Graph Matrix* We represent the graph of the network through a matrix  $A = |V| \times |V|$ . The (i,j)-entry of the matrix A will have a 1 if there is a connection between node  $V_i$  and node  $V_j$ . If we are working with an undirected graph the matrix will be symmetric.

*Attack Vector* We denote  $X = 1 \times |V|$  as the attack vector. It will be a vector with only zeros. The attacker will place a virus on a node V. This will be denoted by the Vth entry in the vector that is changed by a 1.

*Reset vector* The reset vector will make sure that the right entries in the matrix become zero. If the defender flips every node every time it flips then the attack vector will be 0.

*Cummulative Matrix* This matrix will keep record of the propagation of the virus through the network.

er kan nog steeds tegelijk geflipt zijn maar dan hebben ze wel geflipt

nu gain van een resource, moet voor verschillende resources zijn

*State Matrix* The State matrix  $T(t) = 1 \times |V|$  will keep at every time  $t$  the state of the game and denote which node at time  $t$  is infected with the virus. At time  $t = 0$  the State Matrix will be the null matrix.

De eerste infectie is de attack vector \* Graph matrix .

## 3.5 Conclusion

The final section of the chapter gives an overview of the important results of this chapter. This implies that the introductory chapter and the concluding chapter don't need a conclusion.



## Hoofdstuk 4

# Introduction to GameTheory

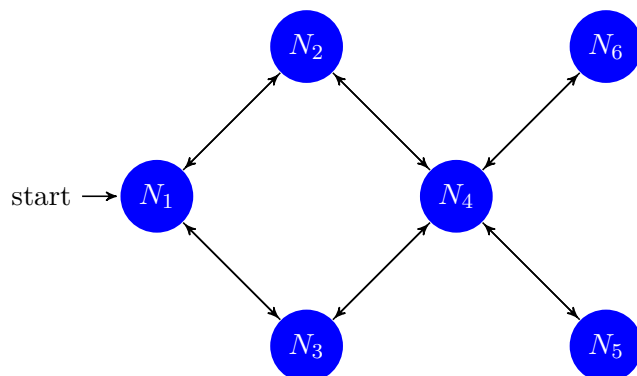
### 4.1 Write down the settings of the game

source: [http://en.wikipedia.org/wiki/Adjacency\\_matrix](http://en.wikipedia.org/wiki/Adjacency_matrix)

We model the network through an undirected Graph  $G = \langle V, E \rangle$  where  $|V|$  denotes the number of resources in the network and  $|E|$  the number of connections. We can convert this to an adjacent matrix where we can represent which vertices of the graph are neighbours of other vertices.

For our graph we have an  $|V| \times |V|$  matrix with on every entry  $a_{ij}$  a 1 as value if there is a connection between node  $V_i$  and  $V_j$  and with zeros its diagonal. Because our graph is undirected we have a symmetric matrix.

*"If  $A$  is the adjacency matrix of the directed or undirected graph  $G$ , then the matrix  $A^n$  (i.e., the matrix product of  $n$  copies of  $A$ ) has an interesting interpretation: the entry in row  $i$  and column  $j$  gives the number of (directed or undirected) walks of length  $n$  from vertex  $i$  to vertex  $j$ . If  $n$  is the smallest nonnegative integer, such that for all  $i, j$ , the  $(i, j)$ -entry of  $A^n > 0$ , then  $n$  is the distance between vertex  $i$  and vertex  $j$ ." [Wikipedia]*



The adjacent matrix becomes this matrix  $[A]$ :

$$\begin{array}{c}
 N_1 \quad N_2 \quad N_3 \quad N_4 \quad N_5 \quad N_6 \\
 \begin{array}{c} N_1 \\ N_2 \\ N_3 \\ N_4 \\ N_5 \\ N_6 \end{array} \begin{pmatrix} 0 & 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{pmatrix}
 \end{array}$$

Matrix  $A \times A = A^2$  becomes the matrix with the number of paths with 2 steps from  $N_i$  to  $N_j$ : We denote this matrix as matrix  $[B]$

$$\begin{array}{c}
 N_1 \quad N_2 \quad N_3 \quad N_4 \quad N_5 \quad N_6 \\
 \begin{array}{c} N_1 \\ N_2 \\ N_3 \\ N_4 \\ N_5 \\ N_6 \end{array} \begin{pmatrix} 2 & 0 & 0 & 2 & 0 & 0 \\ 0 & 2 & 2 & 0 & 1 & 1 \\ 0 & 2 & 2 & 0 & 1 & 1 \\ 2 & 0 & 0 & 4 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 1 & 1 \end{pmatrix}
 \end{array}$$

Matrix  $A^2 \times A = A^3$  becomes the matrix with the number of paths with 3 steps from  $N_i$  to  $N_j$ : We denote this matrix as matrix  $[C]$

$$\begin{array}{c}
 N_1 \quad N_2 \quad N_3 \quad N_4 \quad N_5 \quad N_6 \\
 \begin{array}{c} N_1 \\ N_2 \\ N_3 \\ N_4 \\ N_5 \\ N_6 \end{array} \begin{pmatrix} 0 & 4 & 4 & 0 & 2 & 2 \\ 4 & 0 & 0 & 6 & 0 & 0 \\ 4 & 0 & 0 & 6 & 0 & 0 \\ 0 & 6 & 6 & 0 & 4 & 4 \\ 2 & 0 & 0 & 4 & 0 & 0 \\ 2 & 0 & 0 & 4 & 0 & 0 \end{pmatrix}
 \end{array}$$

So for  $A^N$  every  $a_{ij}$  entry gives the number of paths with N steps from  $N_i$  to  $N_j$ .

With this knowledge we can calculate in how many steps a node is infected.  $A$  calculates which nodes are infected after 1 step,  $A^N$  calculates which nodes are infected in N steps.. So if we want to know how many nodes are infected after 3 steps we have to add every matrix ( $A + A^2 + A^3$ ) and see which entry is a non zero entry.

What do we need for an algorithm

Graph network  $G = \langle V, E \rangle$

Graph matrix  $[A]$  which is  $|V| \times |V|$

Attack vector  $[X]$  which is  $1 \times |V|$

cummulative matrix  $[M]$  which is  $|V| \times |V|$

state matrix  $[T]$  which is  $|V| \times |V|$

Reset vector  $[R]$

duration  $d$

time  $n$

rate  $\delta_0$  of defender and  $\delta_1$  of attacker

Initialisation algorithm:

```

initialisatie
d=0
A=basismatrix
M=A^{0}
n=0
\delta_{0}
\delta_{1}
X
R
controller = defender

```

Algorithm

```

n:= n + 1;
Check who is in control? ( through modulo )
if ( defender & controller=defender)
d:= d + 1;

if ( defender & controller=attacker )
G = X \times R (flippen ten voordele van defender)
d = 0
controller = defender

if ( attacker & controller=defender )
controller=attacker
..

if ( attacker & controller=attacker )
d:= d + 1
M = M x A
T = T + M
G = X x T

```



## Hoofdstuk 5

# The Final Chapter

### 5.1 chap



## Hoofdstuk 6

# Conclusion

The final chapter contains the overall conclusion. It also contains suggestions for future work and industrial applications.

### 6.1 trala





# Bijlagen



# Bijlage A

## The First Appendix

Appendices hold useful data which is not essential to understand the work done in the master thesis. An example is a (program) source. An appendix can also have sections as well as figures and references<sup>[1]</sup>.

### A.1 More Lorem



## Bijlage B

# The Last Appendix

Appendices are numbered with letters, but the sections and subsections use arabic numerals, as can be seen below.

### B.1 Lorem 20-24



# Bibliografie

[1]

[2] M. F. L. B. Aron Laszka, Gabor Horvath. *5th International Conference, GameSec 2014, Los Angeles, CA, USA, November 6-7, 2014. Proceedings*, page 175.

[3] D. A. Craig and H. T. Nguyen. Wireless Real-Time Head Movement System Using a Personal Digital Assistant (PDA) for Control of a Power Wheelchair. *Conference proceedings : ... Annual International Conference of the IEEE Engineering in Medicine and Biology Society. IEEE Engineering in Medicine and Biology Society. Conference*, 1:772–775, 2005.

[4] R. G. A. J. A. O. R. L. R. Kevin D. Brouwers, Marten van Dijk and N. Triandopoulos. Defending Against the Unkown Enemy: Applying FlipIt to System Security. *Third International Conference, GameSec 2012, Budapest, Hungary, November 5-6, 2012. Proceedings*, 7638:248–263, 2012.

[5] R. G. A. J. A. O. R. L. R. Kevin D. Brouwers, Marten van Dijk and N. Triandopoulos. Defending Against the Unkown Enemy: Applying FlipIt to System Security. *Third International Conference, GameSec 2012, Budapest, Hungary, November 5-6, 2012. Proceedings*, 7638:248–263, 2012.

## Fiche masterproef

*Student:* Sophie Marien

*Titel:* Gametheory and Cybersecurity: a study FlipIt and multiple resources

*Engelse titel:* Beste masterproef ooit al geschreven

*UDC:* 621.3

*Korte inhoud:*

Hier komt een heel bondig abstract van hooguit 500 woorden.  $\text{\LaTeX}$  commando's mogen hier gebruikt worden. Blanco lijnen (of het commando `\par`) zijn wel niet toegelaten!

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

Thesis voorgedragen tot het behalen van de graad van Master of Science in de ingenieurswetenschappen: computerwetenschappen, hoofdspecialisatie Veilige software

*Promotor:* Prof. dr. ir. Tom Holvoet

*Assessoren:* Ir. W. Eetveel  
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