

Part I

Introduction to Modeling & Simulation

Stochastic Discrete Event Simulation

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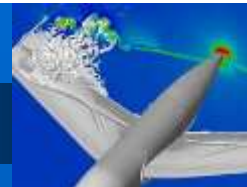
UMR CNRS 6158

Laboratoire d'Informatique de Modélisation
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Part I.A

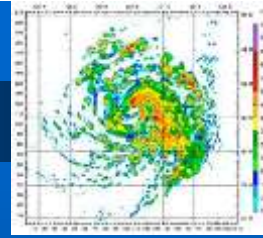
Simulation ?



Aeronautic air tremble
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- In Computer Science:
Simulation is the imitation of the operation of a system or a real world process over time.
- The **system** is a collection of interacting **objects** (cf. dictionary definition)
- The system can be existing or not :
 - « A priori » modelling (non existing)
 - « A posteriori » modelling (existing)

And what about Models ?



- A **model** is a representation of a **system**
- In Matter, Mind and Models (published by MIT Press in 1965) by Marvin L. Minsky we find the following definition :

To an observer B,
an object A* is a model of an object A
to the extent that B can use A*
to answer questions that interest him about A

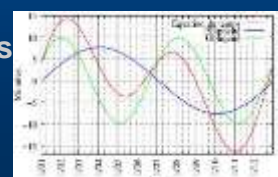
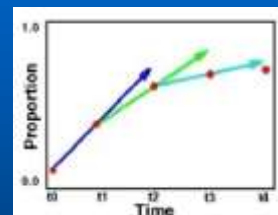
- It implies that :
 - A model is built with an intended **goal** in mind.
 - A the model should be complex enough to answer the **questions** raised.

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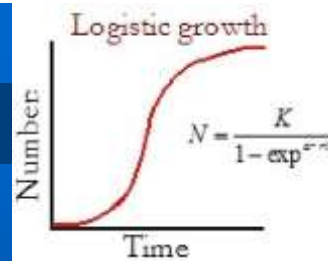
Continuous vs. Discrete Simulation

$$\begin{aligned} \frac{\partial}{\partial t} M(t) &= \frac{\partial}{\partial t} \int_{\Omega} f(x,t) dx \\ \frac{\partial}{\partial t} \ln f_{u,v}(t) &= \left(\frac{\partial}{\partial t} \right)_{u,v} \left\{ \frac{\partial}{\partial t} \ln f_{u,v}(t) \right\} \\ \int_{\Omega} f(x,t) \frac{\partial}{\partial t} \ln f_{u,v}(t) dx &= M(t) \left(\frac{\partial}{\partial t} \right)_{u,v} \left\{ \frac{\partial}{\partial t} \ln f_{u,v}(t) \right\} \\ \int_{\Omega} f(x,t) \left(\frac{\partial}{\partial t} \ln f_{u,v}(t) \right) dx &= M(t) \left(\frac{\partial}{\partial t} \right)_{u,v} \left\{ \frac{\partial}{\partial t} \ln f_{u,v}(t) \right\} \\ \frac{\partial}{\partial t} M(t) &= \frac{\partial}{\partial t} \int_{\Omega} f(x,t) dx = \int_{\Omega} \frac{\partial}{\partial t} f(x,t) dx \end{aligned}$$

- The **system state** is defined by a collection of **variables** that describe a system at any time :
 - With a discrete **event** simulation, the model **state variables** change only at discrete points in **time**
 - In a continuous simulation the systems state changes continuously according to a mathematical model (equation or set of equations)
- We can find **combined simulation** with both discrete and continuous components
- Remark: At the quantic level, everything is finally discrete.



Continuous vs. Discrete (Analytical vs. Algorithmic)

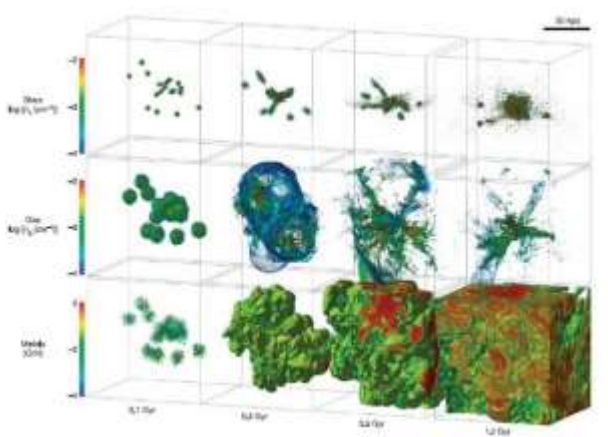


- **Analytical Model** : the model rely on a mathematical “formula” often named “closed form” mathematical solution – named analytical solution.
 - Advantage: a fast computing of the solution
 - Drawback: limited to a small set of systems
- **Computer Simulation Model** : we rely on a simulation algorithm to compute a solution for which we do not have an “Analytical solution”
 - Drawback: often slow to compute solutions.
 - Advantage : fits with all types of systems



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Ex: Simulations of galaxies



Sept. 27th 2012,
Two astronomers have made one of the largest ever conducted simulations in astrophysics to model the growth of galaxies. Masao Mori (LA Univ.) and Masayuki Umemura (Tsukuba Univ.) are able to simulate galaxy evolution since 300 million years after the Big Bang until today. Their results show that galaxies may have evolved much faster than previously thought. ⁶

ISIMA - F2 (inside)

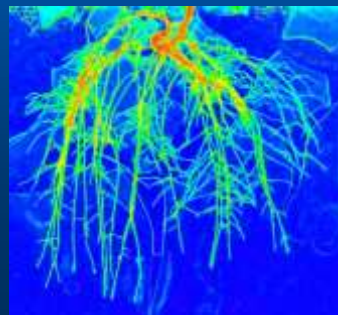


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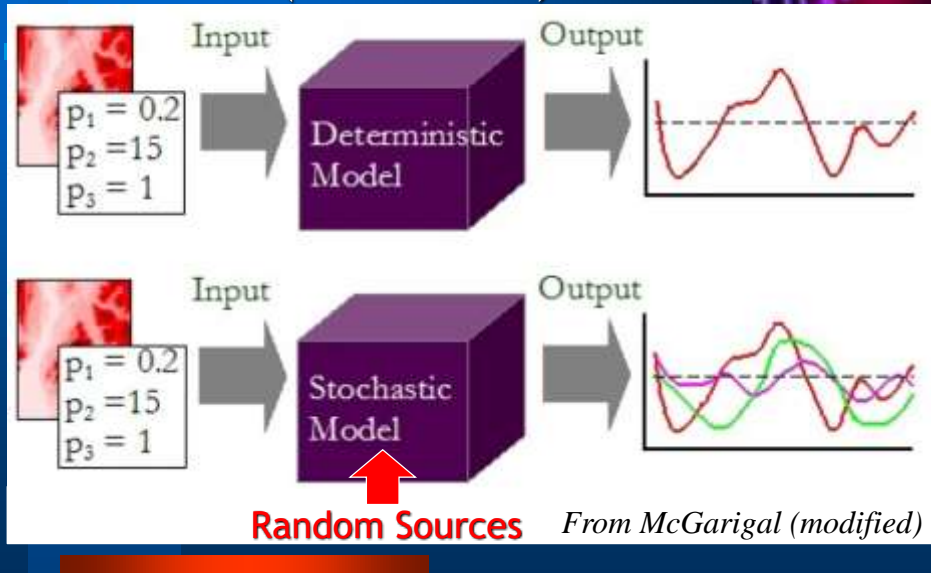
Simulations Deterministic vs. Stochastic



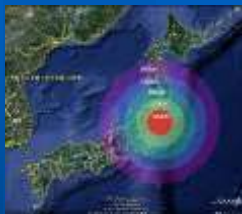
- **Deterministic** simulation : the output of the model is precisely determined by its structure and its parameter values
- **Stochastic** modeling : use of a random source
 - New scientific barriers to break are sometimes behind our best deterministic models
 - The assessment of stochastic parallel simulations is tough and this domain is less studied



Simulations - Deterministic vs. Stochastic (continued)



Monte Carlo (MC) simulation: Every simulation making a smart (stochastic) use of a random source can be considered as MC simulation



- Stochastic models of normal plant operation
- System reliability Monte Carlo models
- Simulation of ground motion using stochastic method
- Nonstationary stochastic model of earthquake motions...
- Shock wave modeling...



University of Toulouse

We still need to increase reliability...



- Monte Carlo (MC) simulations helps increasing model precisions with spatial constraints but they can be very slow

- In many industries stochastic models are more widely used for risk assessment (and to take into account rare & random events)
- Quantitative risk analysis can be improved with Monte Carlo simulations

with no pilot, no eletro-mechanic controls or cables, auto landing...

Ex: problems with the Mediator drug in France
(and with more than 200 other drugs)



- Multi-scale stochastic drug release model
- Stochastic model for the origin and treatment of tumors containing drug-resistant cells
- Comparison of stochastic models to predict the influence of drug distribution, enzyme heterogeneity...
- ...

