

Data Structures and Algorithms¹

A Study Guide for Students of Sorsogon State University - Bulan Campus²

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²This book is a study guide for students of Sorsogon State University - Bulan Campus taking up the course Data Structures and Algorithms.

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Contents

Contents	ii
List of Figures	ix
List of Tables	x
1 Introduction to Data Structures and Algorithms	2
1.1 Introduction	2
1.2 Setup and Installation	2
1.2.1 C++ Compiler Installation	2
1.2.1.1 Windows	2
1.2.2 Visual Studio Code Installation	3
1.2.3 Testing the Installation	3
1.3 What are Data Structures?	4
1.4 What are Algorithms?	4
1.5 Why Study Data Structures and Algorithms?	4
1.6 Basic Terminologies	4
1.6.1 Data	4
1.6.2 Data Object	4
1.6.3 Data Type	4
1.6.3.1 Primitive Data Types	5
1.6.3.1.1 Integer (int)	5
1.6.3.1.2 Character (char)	5
1.6.3.1.3 Boolean (bool)	5
1.6.3.1.4 Floating-Point (float)	5
1.6.3.1.5 Double (double)	6
1.6.3.2 Non-primitive Data Types	6
1.6.3.2.1 Array (int, float, char, etc.)	6
1.6.3.2.2 String (char)	6
1.6.3.2.3 Structure	6
1.6.3.2.4 Class	7
1.6.3.2.5 Vector	7
1.6.3.2.6 List	7
1.6.3.2.6.1 Singly Linked List	7
1.6.3.2.6.2 Doubly Linked List	8
1.6.3.2.6.3 Circular Linked List	8
1.6.3.2.6.4 Circular Doubly Linked List	8
1.6.3.2.7 Stack	9
1.6.3.2.8 Queue	9
1.6.3.2.8.1 Circular Queue	9

1.6.3.2.8.2	Priority Queue	9
1.6.3.2.8.3	Double-Ended Queue (Deque)	10
1.6.3.2.9	Tree	10
1.6.3.2.10	Graph	10
1.6.3.2.11	Hash Map or Hash Table	11
1.6.3.2.12	Set	11
1.6.4	Abstract Data Type	12
1.6.5	Pointers	12
1.6.5.1	Declaring Pointers	13
1.6.5.2	Initializing Pointers	13
1.6.5.3	Dereferencing Pointers	13
1.6.5.4	Pointer Arithmetic	14
1.6.5.5	Pointer to Pointer	14
1.7	Asymptotic Notations	15
1.7.1	Big-O Notation	15
1.7.2	Omega Notation	15
1.7.3	Theta Notation	16
1.7.4	Complexity of an Algorithm	16
1.7.4.1	Time Complexity	16
1.7.4.1.1	Constant Time Complexity ($O(1)$)	16
1.7.4.1.2	Logarithmic Time Complexity ($O(\log n)$)	17
1.7.4.1.3	Linear Time Complexity ($O(n)$)	17
1.7.4.1.4	Linearithmic Time Complexity ($O(n \log n)$)	17
1.7.4.1.5	Quadratic Time Complexity ($O(n^2)$)	18
1.7.4.1.6	Exponential Time Complexity ($O(2^n)$)	19
1.7.4.1.7	Factorial Time Complexity ($O(n!)$)	19
1.7.4.2	Space Complexity	19
1.7.4.2.1	Constant Space Complexity ($O(1)$)	19
1.7.4.2.2	Linear Space Complexity ($O(n)$)	20
1.7.4.2.3	Quadratic Space Complexity ($O(n^2)$)	20
1.7.4.2.4	Exponential Space Complexity ($O(2^n)$)	21
1.7.4.2.5	Factorial Space Complexity ($O(n!)$)	21
1.8	Summary	21
2	Arrays and Linked Lists	22
2.1	Introduction	22
2.2	Arrays	22
2.2.1	Types of Arrays	24
2.2.1.1	One-dimensional Array	24
2.2.1.2	Multi-dimensional Array	25
2.2.2	Array Operations	27
2.2.2.1	Insertion	27
2.2.2.2	Deletion	27
2.2.2.3	Searching	27
2.2.3	Complexity Analysis of Arrays	27
2.3	Linked Lists	27
2.3.1	Types of Linked Lists	27
2.3.1.1	Singly Linked List	27
2.3.1.2	Doubly Linked List	27
2.3.1.3	Circular Linked List	27
2.3.2	Operations on Linked Lists	27

2.3.2.1	Insertion	27
2.3.2.2	Deletion	27
2.3.2.3	Searching	27
2.3.3	Complexity Analysis of Linked Lists	27
2.4	Comparison of Arrays and Linked Lists	27
2.5	Summary	27
3	Stacks and Queues	28
3.1	Introduction	29
3.2	Stacks	29
3.2.1	Operations on Stacks	29
3.2.1.1	Push	29
3.2.1.2	Pop	29
3.2.1.3	Peek	29
3.2.1.4	isEmpty	29
3.2.1.5	isFull	29
3.2.2	Complexity Analysis of Stacks	29
3.2.3	Implementation of Stacks Using Arrays	29
3.2.4	Implementation of Stacks Using Linked Lists	29
3.3	Queues	29
3.3.1	Types of Queues	29
3.3.1.1	Linear Queue	29
3.3.1.2	Circular Queue	29
3.3.1.3	Priority Queue	29
3.3.1.4	Double-ended Queue (Deque)	29
3.3.2	Operations on Queues	29
3.3.2.1	Enqueue	29
3.3.2.2	Dequeue	29
3.3.2.3	Front	29
3.3.2.4	Rear	29
3.3.3	Complexity Analysis of Queues	29
3.3.4	Implementation of Queues Using Arrays	29
3.3.5	Implementation of Queues Using Linked Lists	29
3.4	Comparison of Stacks and Queues	29
3.5	Summary	29
4	Trees	30
4.1	Introduction	31
4.2	Properties of Trees	31
4.2.1	Root Node	31
4.2.2	Parent Node	31
4.2.3	Child Node	31
4.2.4	Leaf Node	31
4.2.5	Ancestors	31
4.2.6	Siblings	31
4.2.7	Descendants	31
4.2.8	Height of a Tree	31
4.2.9	Depth of a Node	31
4.2.10	Degree of a Node	31
4.2.11	Level of a Node	31
4.2.12	Subtree	31
4.3	Types of Trees	31

4.3.1	Binary Tree	31
4.3.1.1	Types of Binary Trees	31
4.3.1.1.1	Left-skewed Binary Tree	31
4.3.1.1.2	Right-skewed Binary Tree	31
4.3.1.1.3	Complete Binary Tree	31
4.3.2	Ternary Tree	31
4.3.3	N-ary Tree	31
4.3.4	Binary Search Tree	31
4.3.5	AVL Tree	31
4.3.6	Red-Black Tree	31
4.4	Basic Operations on Trees	31
4.4.1	Creation of a Tree	31
4.4.2	Insertion	31
4.4.3	Deletion	31
4.4.4	Searching	31
4.4.5	Traversal	31
4.4.5.1	Preorder Traversal	31
4.4.5.2	Inorder Traversal	31
4.4.5.3	Postorder Traversal	31
4.4.5.4	Level-order Traversal	31
4.5	Complexity Analysis of Trees	31
4.6	Summary	31
5	Graphs	32
5.1	Introduction	33
5.2	Properties of Graphs	33
5.2.1	Vertex	33
5.2.2	Edge	33
5.2.3	Degree of a Vertex	33
5.2.4	Path	33
5.3	Types of Graphs	33
5.3.1	Finite Graph	33
5.3.2	Infinite Graph	33
5.3.3	Trivial Graph	33
5.3.4	Simple Graph	33
5.3.5	Multi Graph	33
5.3.6	Null Graph	33
5.3.7	Complete Graph	33
5.3.8	Pseudo Graph	33
5.3.9	Regular Graph	33
5.3.10	Bipartite Graph	33
5.3.11	Labelled Graph	33
5.3.12	Weighted Graph	33
5.3.13	Directed Graph	33
5.3.14	Undirected Graph	33
5.3.15	Connected Graph	33
5.3.16	Disconnected Graph	33
5.3.17	Cyclic Graph	33
5.3.18	Acyclic Graph	33
5.3.19	Directed Acyclic Graph (DAG)	33
5.3.20	Digraph	33

5.3.21	Subgraph	33
5.4	Operations on Graphs	33
5.4.1	Creation of a Graph	33
5.4.2	Insertion	33
5.4.2.1	Insertion of a Vertex	33
5.4.2.2	Insertion of an Edge	33
5.4.3	Deletion	33
5.4.3.1	Deletion of a Vertex	33
5.4.3.2	Deletion of an Edge	33
5.4.4	Traversal	33
5.4.4.1	Depth First Search (DFS)	33
5.4.4.2	Breadth First Search (BFS)	33
5.4.5	Shortest Path	33
5.4.6	Minimum Spanning Tree	33
5.5	Complexity Analysis of Graphs	33
5.6	Summary	33
6	Sorting and Searching	34
6.1	Introduction	35
6.2	Sorting	35
6.2.1	Types of Sorting Algorithms	35
6.2.1.1	Bubble Sort	35
6.2.1.2	Selection Sort	35
6.2.1.3	Insertion Sort	35
6.2.1.4	Merge Sort	35
6.2.1.5	Quick Sort	35
6.2.1.6	Heap Sort	35
6.2.1.7	Radix Sort	35
6.2.1.8	Counting Sort	35
6.2.1.9	Bucket Sort	35
6.2.2	Comparison of Sorting Algorithms	35
6.3	Searching	35
6.3.1	Types of Searching Algorithms	35
6.3.1.1	Linear Search	35
6.3.1.2	Binary Search	35
6.3.1.3	Jump Search	35
6.3.1.4	Interpolation Search	35
6.3.1.5	Exponential Search	35
6.3.1.6	Fibonacci Search	35
6.3.1.7	Ternary Search	35
6.3.2	Comparison of Searching Algorithms	35
6.4	Summary	35
7	Hashing	36
7.1	Introduction	36
7.2	Hash Table	36
7.3	Hash Function	36
7.4	Collision Resolution Techniques	36
7.4.1	Separate Chaining	36
7.4.2	Open Addressing	36
7.4.2.1	Linear Probing	36
7.4.2.2	Quadratic Probing	36

7.4.2.3	Double Hashing	36
7.5	Complexity Analysis of Hashing	36
7.6	Summary	36
8	Advanced Data Structures and Algorithms	37
8.1	Introduction	38
8.2	Advanced Data Structures	38
8.2.1	Segment Tree	38
8.2.2	Fenwick Tree	38
8.2.3	Suffix Tree	38
8.2.4	Suffix Array	38
8.2.5	Trie	38
8.2.6	Heap	38
8.2.7	Disjoint Set	38
8.2.8	Skip List	38
8.2.9	Splay Tree	38
8.2.10	Bloom Filter	38
8.2.11	KD Tree	38
8.2.12	Quad Tree	38
8.2.13	Octree	38
8.2.14	B-Tree	38
8.2.15	B+ Tree	38
8.2.16	R-Tree	38
8.2.17	X-Tree	38
8.2.18	Y-Tree	38
8.2.19	Z-Tree	38
8.3	Advanced Algorithms	38
8.3.1	Dynamic Programming	38
8.3.2	Greedy Algorithms	38
8.3.3	Backtracking	38
8.3.4	Divide and Conquer	38
8.3.5	Branch and Bound	38
8.3.6	Randomized Algorithms	38
8.3.7	Approximation Algorithms	38
8.3.8	String Matching Algorithms	38
8.3.9	Pattern Searching Algorithms	38
8.3.10	Cryptography Algorithms	38
8.3.11	Geometric Algorithms	38
8.3.12	Graph Algorithms	38
8.3.13	Network Flow Algorithms	38
8.3.14	Game Theory Algorithms	38
8.3.15	Quantum Algorithms	38
8.4	Summary	38
9	Applications of Data Structures and Algorithms	39
9.1	Applications in Computer Science	40
9.1.1	Operating Systems	40
9.1.2	Database Management Systems	40
9.1.3	Compiler Design	40
9.1.4	Networking	40
9.1.5	Artificial Intelligence	40
9.1.6	Machine Learning	40

9.1.7	Computer Graphics	40
9.1.8	Computer Vision	40
9.1.9	Robotics	40
9.1.10	Web Development	40
9.1.11	Mobile Development	40
9.1.12	Game Development	40
9.1.13	Cybersecurity	40
9.1.14	Quantum Computing	40
9.2	Applications in Real Life	40
9.2.1	Social Media	40
9.2.2	E-commerce	40
9.2.3	Healthcare	40
9.2.4	Finance	40
9.2.5	Transportation	40
9.2.6	Education	40
9.2.7	Agriculture	40
9.2.8	Manufacturing	40
9.2.9	Entertainment	40
9.2.10	Sports	40
9.2.11	Travel	40
9.2.12	Telecommunications	40
9.2.13	Energy	40
9.2.14	Environment	40
9.2.15	Politics	40
9.2.16	Military	40
9.3	Summary	40
10	References	41

List of Figures

1	Pointer Example	12
2	Dereferencing Pointers	13
3	Pointer Arithmetic	14
4	Pointer to Pointer	15
5	Asymptotic Notation	16
6	Elements of an array in C++	22
7	Initializing Array Elements	23
8	Initializing Array Elements with Empty Members	24
9	One-dimensional Array in C++	25
10	Two-dimensional Array in C++	25

List of Tables

List of Codes

1.1	Hello World Program	3
1.2	Compiling the Program	3
1.3	Running the Program	3
1.4	Integer Data Type	5
1.5	Character Data Type	5
1.6	Boolean Data Type	5
1.7	Floating-Point Data Type	5
1.8	Double Data Type	6
1.9	Array Data Type	6
1.10	String Data Type	6
1.11	Structure Data Type	6
1.12	Class Data Type	7
1.13	Vector Data Type	7
1.14	List Data Type	7
1.15	Singly Linked List Data Type	8
1.16	Doubly Linked List Data Type	8
1.17	Circular Linked List Data Type	8
1.18	Circular Doubly Linked List Data Type	8
1.19	Stack Data Type	9
1.20	Queue Data Type	9
1.21	Priority Queue Data Type	10
1.22	Deque Data Type	10
1.23	Tree Data Type	10
1.24	Graph Data Type	11
1.25	Ordered Map Data Type	11
1.26	Unordered Map Data Type	11
1.27	Ordered Set Data Type	11
1.28	Unordered Set Data Type	12
1.29	Pointer Data Type	12
1.30	Declaring Pointers	13
1.31	Initializing Pointers	13
1.32	Dereferencing Pointers	13
1.33	Pointer Arithmetic	14
1.34	Pointer to Pointer Data Type	15
1.35	Constant Time Complexity	16
1.36	Logarithmic Time Complexity	17
1.37	Linear Time Complexity	17
1.38	Linearithmic Time Complexity	17
1.39	Quadratic Time Complexity	18
1.40	Exponential Time Complexity	19
1.41	Factorial Time Complexity	19

1.42	Constant Space Complexity	19
1.43	Linear Space Complexity	20
1.44	Quadratic Space Complexity	20
1.45	Exponential Space Complexity	21
1.46	Factorial Space Complexity	21
2.1	Array Declaration	22
2.2	Assigning Values to Array Elements	23
2.3	Initializing Array Elements	23
2.4	Initializing Array Elements with Unspecified Size	23
2.5	Initializing Array Elements with Empty Members	24
2.6	One-dimensional Array	25
2.7	Two-dimensional Array	25
2.8	Two-dimensional Array with Empty Members	26

Preface

“Bad programmers worry about the code. Good programmers worry about data structures and their relationships.”

– Linus Torvalds

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1

Introduction to Data Structures and Algorithms

1.1 Introduction

Data structures and algorithms are one of the fundamental components of computer science. They are essential for solving complex problems efficiently and effectively. Data structures are used to store and organize data in a computer so that it can be accessed and manipulated efficiently. Algorithms are step-by-step procedures or formulas for solving a problem. They are the instructions that tell a computer how to perform a task.

In this course, we will learn about the fundamental data structures and algorithms that are used in computers. We will study how to design, implement, and analyze data structures and algorithms to solve real-world problems. By the end of this course, you will have a solid foundation in data structures and algorithms that will help you become a better programmer and problem solver.

1.2 Setup and Installation

In this course, we will be using the C++ programming language to implement data structures and algorithms. C++ is a powerful and versatile programming language that is widely used in the field of computer science. To get started, you will need to install a C++ compiler and an integrated development environment (IDE) on your computer.

1.2.1 C++ Compiler Installation

The first step is to install a C++ compiler on your computer. A compiler is a program that translates source code written in a programming language into machine code that can be executed by a computer. There are several C++ compilers available, but we recommend using the GNU Compiler Collection (GCC) which is a free and open-source compiler that supports multiple programming languages including C++.

1.2.1.1 Windows

To install GCC on Windows, you can use the MinGW (Minimalist GNU for Windows) project which provides a port of GCC to Windows. You can download the MinGW installer from the MinGW website and follow the installation instructions. You can install MinGW

by following the instructions here: https://code.visualstudio.com/docs/languages/cpp#_example-install-mingwx64-on-windows

1.2.2 Visual Studio Code Installation

The next step is to install an integrated development environment (IDE) on your computer. An IDE is a software application that provides comprehensive facilities to computer programmers for software development. We recommend using Visual Studio Code which is a free and open-source IDE developed by Microsoft. You can download Visual Studio Code from the official website and follow the installation instructions: <https://code.visualstudio.com/Download>

Other than Visual Studio Code, you also need to install the C/C++ extension for Visual Studio Code. You can install the C/C++ extension by following the instructions here: <https://code.visualstudio.com/docs/languages/cpp>

1.2.3 Testing the Installation

To test if the installation was successful, you can create a simple C++ program and compile it using the C++ compiler. Open Visual Studio Code and create a new file with the following C++ code:

```
1 #include <iostream>
2 namespace std;
3
4 int main() {
5     cout << "Hello, World!" << endl;
6     return 0;
7 }
```

Code 1.1: Hello World Program

Save the file with a .cpp extension (e.g., hello.cpp) and open a terminal window in Visual Studio Code. Compile the program using the following command:

```
1 g++ hello.cpp -o hello
```

Code 1.2: Compiling the Program

If there are no errors, you can run the program by executing the following command:

```
1 ./hello
```

Code 1.3: Running the Program

If everything is set up correctly, you should see the output "Hello, World!" printed on the screen.

1.3 What are Data Structures?

A **data structure** is a way of organizing and storing data in a computer so that it can be accessed and manipulated efficiently. Data structures provide a way to manage large amounts of data effectively for various applications. They define the relationship between the data, and the operations that can be performed on the data. There are many different types of data structures that are used in computer science, each with its own strengths and weaknesses. The use of the right data structure can significantly improve the performance of an algorithm and make it more efficient.

1.4 What are Algorithms?

An **algorithm** is a step-by-step procedure or formula for solving a problem. It is a sequence of well-defined instructions that take some input and produce an output. Algorithms are used to solve complex problems and perform various tasks efficiently. They are the instructions that tell a computer how to perform a task. Algorithms are essential for writing computer programs and developing software applications. The efficiency of an algorithm is measured by its time complexity and space complexity.

1.5 Why Study Data Structures and Algorithms?

Data structures and algorithms are essential topics in computer science and software engineering. They are one of the fundamental components of computer science and are used in various applications such as operating systems, database management systems, networking, artificial intelligence, and many others. A good understanding of data structures and algorithms will help you become a better programmer and problem solver. In addition, many companies use data structures and algorithms as part of their technical interviews to assess the problem-solving skills of candidates. Therefore, studying data structures and algorithms is essential for anyone pursuing a career in software engineering or software development.

1.6 Basic Terminologies

Before we dive into the details of data structures and algorithms, let's understand some basic terminologies that might be helpful in understanding the concepts better.

1.6.1 Data

Data is a collection of facts, figures, or information that can be used for analysis or reference. It can be in the form of numbers, text, images, audio, video, or any other format. Data is the raw material that is processed by a computer to produce meaningful information.

1.6.2 Data Object

A **data object** is an instance of a data structure that contains data along with the operations that can be performed on the data. It is an abstraction of a real-world entity that is represented in a computer program.

1.6.3 Data Type

A **data type** is a classification of data that tells the compiler or interpreter how the programmer intends to use the data. It defines the operations that can be performed on the data, the values that can be stored in the data, and the memory space required to store the data.

1.6.3.1 Primitive Data Types

Primitive data types are the basic data types that are built into the programming language. They are used to store simple values such as integers, floating-point numbers, characters, and booleans. Examples of primitive data types include `int`, `float`, `char`, and `bool`. The following are the common primitive data types used in programming:

1.6.3.1.1 Integer (`int`)

The *integer* data type is used to store whole numbers without any decimal points. It can be either signed or unsigned, depending on whether it can store negative values or not. An integer's value can range from -2,147,483,648 to 2,147,483,647 and takes 4 bytes of memory.

```
1 int x = 10;
```

Code 1.4: Integer Data Type

1.6.3.1.2 Character (`char`)

The *character* data type is used to store a single character such as a letter, digit, or special symbol. It is represented by a single byte of memory. A `char` value can range from -128 to 127 or 0 to 255, depending on whether it is signed or unsigned. These values are represented using ASCII codes.

```
1 char c = 'A';
```

Code 1.5: Character Data Type

1.6.3.1.3 Boolean (`bool`)

The *boolean* data type is used to store true or false values. It is represented by a single byte of memory. A `bool` value can be either true or false.

```
1 bool flag = true;
```

Code 1.6: Boolean Data Type

1.6.3.1.4 Floating-Point (`float`)

The *floating-point* data type is used to store real numbers with decimal points. It can represent both integer and fractional parts of a number. It can be either single precision or double precision, depending on the number of bits used to store the value. A `float` value can range from 1.2E-38 to 3.4E+38 and takes 4 bytes of memory.

```
1 float y = 3.14;
```

Code 1.7: Floating-Point Data Type

1.6.3.1.5 Double (double)

The **double** data type is used to store real numbers with double precision. It can represent both integer and fractional parts of a number with higher precision than the float data type. A double value can range from 2.3E-308 to 1.7E+308 and takes 8 bytes of memory.

```
1 double z = 3.14159;
```

Code 1.8: Double Data Type

1.6.3.2 Non-primitive Data Types

Non-primitive data types are more complex data types that are derived from primitive data types. They are used to store collections of values or objects. Examples of non-primitive data types include arrays, strings, structures, classes, and pointers.

1.6.3.2.1 Array (int, float, char, etc.)

An **array** is a collection of elements of the same data type that are stored in contiguous memory locations. It is used to store multiple values of the same type under a single name. The elements of an array can be accessed using an index value. In C++, arrays are zero-indexed, which means the first element is at index 0. Arrays also have a fixed size that is specified at the time of declaration. If you need a dynamic size array, you can use a vector in C++.

```
1 int arr[5] = {1, 2, 3, 4, 5};
```

Code 1.9: Array Data Type

1.6.3.2.2 String (char)

A **string** is a collection of characters that are stored as a sequence of characters terminated by a null character '\0'. It is used to represent text in a computer program. Strings are treated as arrays of characters in C++.

```
1 char str[] = "Hello, World!";
```

Code 1.10: String Data Type

1.6.3.2.3 Structure

A **structure** is a user-defined data type that is used to store a collection of different data types under a single name. It is used to represent a record that contains multiple fields or members. Each field in a structure can have a different data type.

```
1 struct Person {  
2     char name[50];  
3     int age;  
4     float height;  
5 };
```

Code 1.11: Structure Data Type

1.6.3.2.4 Class

A *class* is a user-defined data type that is used to define objects that contain data members and member functions. It is used to implement object-oriented programming concepts such as encapsulation, inheritance, and polymorphism.

```
1 class Circle {  
2     private:  
3         float radius;  
4     public:  
5         float getArea() {  
6             return 3.14 * radius * radius;  
7         }  
8 };
```

Code 1.12: Class Data Type

1.6.3.2.5 Vector

A *vector* is a dynamic array that can grow or shrink in size dynamically. It is a part of the Standard Template Library (STL) in C++ and provides a more flexible alternative to fixed-size arrays. Vectors are used to store a collection of elements of the same data type.

```
1 vector<int> vec = {1, 2, 3, 4, 5};
```

Code 1.13: Vector Data Type

1.6.3.2.6 List

A *list* is a linear data structure that is used to store a collection of elements in a sequential order. It is a part of the Standard Template Library (STL) in C++ and provides operations to insert, delete, and access elements in the list. Lists are used to implement linked lists in C++.

```
1 list<int> lst = {1, 2, 3, 4, 5};
```

Code 1.14: List Data Type

There are different types of lists in C++, such as singly linked list, doubly linked list, circular linked list, and circular doubly linked list, that provide different operations and performance characteristics.

1.6.3.2.6.1 Singly Linked List

A *singly linked list* is a linear data structure that is used to store a collection of elements in a sequential order. Each element in the list is stored in a node that contains the data and a

pointer to the next node in the list.

```
1 struct Node {  
2     int data;  
3     Node *next;  
4 };
```

Code 1.15: Singly Linked List Data Type

1.6.3.2.6.2 Doubly Linked List

A *doubly linked list* is a linear data structure that is used to store a collection of elements in a sequential order. Each element in the list is stored in a node that contains the data, a pointer to the next node, and a pointer to the previous node in the list.

```
1 struct Node {  
2     int data;  
3     Node *next;  
4     Node *prev;  
5 };
```

Code 1.16: Doubly Linked List Data Type

1.6.3.2.6.3 Circular Linked List

A *circular linked list* is a linear data structure that is used to store a collection of elements in a circular order. Each element in the list is stored in a node that contains the data and a pointer to the next node in the list. The last node in the list points back to the first node, creating a circular structure.

```
1 struct Node {  
2     int data;  
3     Node *next;  
4 };
```

Code 1.17: Circular Linked List Data Type

1.6.3.2.6.4 Circular Doubly Linked List

A *circular doubly linked list* is a linear data structure that is used to store a collection of elements in a circular order. Each element in the list is stored in a node that contains the data, a pointer to the next node, and a pointer to the previous node in the list. The last node in the list points back to the first node, creating a circular structure.

```
1 struct Node {  
2     int data;  
3     Node *next;  
4     Node *prev;
```

```
5 };
```

Code 1.18: Circular Doubly Linked List Data Type

1.6.3.2.7 Stack

A **stack** is a linear data structure that follows the Last In First Out (LIFO) principle. It is used to store a collection of elements in a sequential order. The main operations on a stack are push (to insert an element) and pop (to remove an element).

```
1 stack<int> stk;  
2 stk.push(1);  
3 stk.push(2);  
4 stk.push(3);  
5 stk.push(4);  
6 stk.pop();
```

Code 1.19: Stack Data Type

1.6.3.2.8 Queue

A **queue** is a linear data structure that follows the First In First Out (FIFO) principle. It is used to store a collection of elements in a sequential order. The main operations on a queue are enqueue (to insert an element) and dequeue (to remove an element).

```
1 queue<int> que;  
2 que.push(1);  
3 que.push(2);  
4 que.push(3);  
5 que.push(4);  
6 que.pop();
```

Code 1.20: Queue Data Type

There are different types of queues in C++, such as linear queue, circular queue, priority queue, and double-ended queue (deque), that provide different operations and performance characteristics.

1.6.3.2.8.1 Circular Queue

A **circular queue** is a type of queue that uses a circular structure to store elements. Unlike a linear queue, a circular queue does not have a fixed front and rear end. Instead, the front and rear ends wrap around the ends of the queue. This allows the queue to reuse the space freed up by dequeued elements. In C++, there is no built-in circular queue data type, but you can implement one using an array and a few pointers.

1.6.3.2.8.2 Priority Queue

A **priority queue** is a type of queue that stores elements based on their priority. The element with the highest priority is dequeued first. Priority queues are typically implemented using

heaps, which are a type of binary tree data structure.

```
1 priority_queue<int> pq;  
2 pq.push(1);  
3 pq.push(4);  
4 pq.push(2);  
5 pq.push(3);  
6 pq.pop();
```

Code 1.21: Priority Queue Data Type

1.6.3.2.8.3 Double-Ended Queue (Deque)

A *double-ended queue* or *deque* is a type of queue that allows elements to be inserted and removed from both ends. It is a generalization of both stacks and queues and provides more flexibility in manipulating elements.

```
1 deque<int> dq;  
2 dq.push_front(1);  
3 dq.push_back(2);  
4 dq.push_front(3);  
5 dq.push_back(4);  
6 dq.pop_front();
```

Code 1.22: Deque Data Type

1.6.3.2.9 Tree

A *tree* is a non-linear data structure that is used to store a collection of elements in a hierarchical order. It consists of nodes that are connected by edges. The topmost node in a tree is called the root node, and the nodes below it are called child nodes. Trees are used to represent hierarchical relationships between elements.

```
1 struct Node {  
2     int data;  
3     Node *left;  
4     Node *right;  
5 };
```

Code 1.23: Tree Data Type

There are different types of trees in computer science, such as binary trees, binary search trees, AVL trees, red-black trees, and many others, that provide different operations and performance characteristics.

1.6.3.2.10 Graph

A *graph* is a non-linear data structure that is used to store a collection of elements and the relationships between them. It consists of nodes (vertices) that are connected by edges.

Graphs are used to represent networks, social relationships, maps, and many other real-world applications.

```
1 struct Graph {  
2     int V;  
3     list<int> *adj;  
4 };
```

Code 1.24: Graph Data Type

There are different types of graphs in computer science, such as directed graphs, undirected graphs, weighted graphs, and many others, each with its own set of advantages and disadvantages.

Another important thing to note is that “Every tree is a graph, but not every graph is a tree.”

1.6.3.2.11 Hash Map or Hash Table

A *Hash Map* is a data structure that is used to store a collection of key-value pairs. It uses a hash function to map keys to values and stores them in an array. Hash maps provide fast access to elements and are used to implement associative arrays, sets, and dictionaries.

There are two ways to implement a hash map in C++: the ordered map using the `map` class or using the `unordered_map` class.

```
1 map<string, int> mp;  
2 mp["one"] = 1;  
3 mp["two"] = 2;  
4 mp["three"] = 3;
```

Code 1.25: Ordered Map Data Type

```
1 unordered_map<string, int> ump;  
2 ump["one"] = 1;  
3 ump["two"] = 2;  
4 ump["three"] = 3;
```

Code 1.26: Unordered Map Data Type

1.6.3.2.12 Set

A *set* is a data structure that is used to store a collection of unique elements. It is used to implement the mathematical set abstraction and provides operations to insert, delete, and search for elements.

There are two ways to implement a set in C++: the ordered set using the `set` class or using the `unordered_set` class.

```
1 set<int> st;  
2 st.insert(1);
```



```

3 st.insert(2);
4 st.insert(3);

```

Code 1.27: Ordered Set Data Type

```

1 unordered_set<int> ust;
2 ust.insert(1);
3 ust.insert(2);
4 ust.insert(3);

```

Code 1.28: Unordered Set Data Type

1.6.4 Abstract Data Type

An *abstract data type (ADT)* is a mathematical model that defines a set of data values and operations that can be performed on those values. It is an abstraction of a data structure that specifies the operations that can be performed on the data without specifying how they are implemented. *Abstraction* refers to the process of hiding the implementation details of a data structure and exposing only the essential features. An ADT is defined by its interface, which includes the data values and operations that can be performed on those values.

1.6.5 Pointers

A *pointer* is a special type of data type that stores the memory address of another data type. An “address” is a unique number that identifies a location in memory. The memory address of a variable is the location in memory where the variable is stored. Pointers are used to store the address of a variable or object in memory. Pointers are used to implement dynamic memory allocation and to pass parameters by reference.

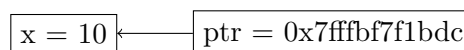


Figure 1: Pointer Example

Figure 1 shows an example of a pointer in C++. The variable `x` stores the value 10, and the pointer `ptr` stores the memory address of the variable `x`. The memory address is represented as a hexadecimal number `0x7ffbf7f1bdc`.

```

1 int main() {
2     int x = 10;
3     int *ptr = &x;
4
5     cout << *ptr; // Output: 10
6
7     return 0;
8 }

```

Code 1.29: Pointer Data Type

In the above example, the pointer `ptr` stores the memory address of the variable `x`. The `*` operator is used to dereference the pointer and access the value stored at the memory address.

An example of an address of a variable is `0x7ffbf7f1bdc`. When you dereference the pointer, you get the value stored at that address.

1.6.5.1 Declaring Pointers

To declare a pointer, you need to specify the data type of the variable or object it points to. You can declare a pointer using the following syntax:

```
1 int *ptr;
```

Code 1.30: Declaring Pointers

In the above example, the pointer `ptr` is declared to point to an integer variable. You can also declare a pointer to a structure, class, or any other data type.

1.6.5.2 Initializing Pointers

To initialize a pointer, you need to assign it the memory address of a variable or object. You can initialize a pointer using the address-of operator `&`. You can also initialize a pointer to `NULL` or `nullptr` to indicate that it does not point to any memory location.

```
1 int x = 10;
2 int *ptr = &x;
```

Code 1.31: Initializing Pointers

In the above example, the pointer `ptr` is initialized with the memory address of the variable `x`.

1.6.5.3 Dereferencing Pointers

To access the value stored at the memory address pointed to by a pointer, you need to dereference the pointer using the dereference operator `*`. The dereference operator is used to access the value stored at the memory address.

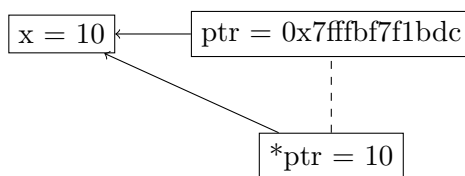


Figure 2: Dereferencing Pointers

Figure 2 shows an example of dereferencing a pointer in C++. The pointer `ptr` points to the variable `x`, and the dereference operator `*` is used to access the value stored at the memory address.

```
1 int x = 10;
2 int *ptr = &x;
3
4 cout << *ptr; // Output: 10
5
```

```

6 *ptr = 20;
7
8 cout << x; // Output: 20

```

Code 1.32: Dereferencing Pointers

In the above example, the pointer `ptr` points to the variable `x`. You can use the dereference operator `*` to access the value stored at the memory address. You can also use the dereference operator to modify the value stored at the memory address.

1.6.5.4 Pointer Arithmetic

Pointer arithmetic is a feature of pointers that allows you to perform arithmetic operations on pointers. You can add or subtract an integer value from a pointer to move it to a different memory location. Pointer arithmetic is used to access elements in an array or to iterate over a data structure.

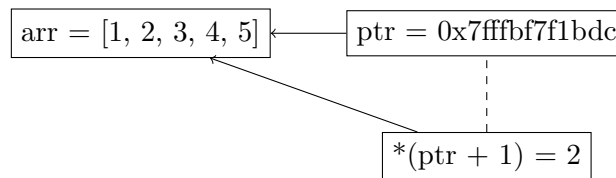


Figure 3: Pointer Arithmetic

Figure 3 shows an example of pointer arithmetic in C++. The pointer `ptr` points to the first element of the array `arr`, and the pointer arithmetic operation `*(ptr + 1)` is used to access the second element of the array.

```

1 int main() {
2     int arr[5] = {1, 2, 3, 4, 5};
3     int *ptr = arr;
4
5     cout << *ptr; // Output: 1
6     cout << *(ptr + 1); // Output: 2
7
8     return 0;
9 }

```

Code 1.33: Pointer Arithmetic

In the above example, the pointer `ptr` points to the first element of the array `arr`. You can use pointer arithmetic to access the elements of the array by adding an integer value to the pointer.

1.6.5.5 Pointer to Pointer

A *pointer to pointer* is a special type of pointer that stores the memory address of another pointer. It is used to store the address of a pointer variable in memory. Pointer to pointer is used to implement multiple levels of indirection and to create dynamic data structures such as linked lists and trees.

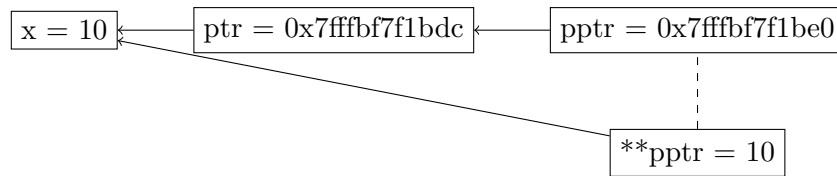


Figure 4: Pointer to Pointer

Figure 4 shows an example of a pointer to pointer in C++. The pointer `ptr` stores the memory address of the variable `x`, and the pointer `pptr` stores the memory address of the pointer `ptr`. The double dereference operator `**` is used to access the value stored at the memory address.

```

1 int main() {
2     int x = 10;
3     int *ptr = &x;
4     int **pptr = &ptr;
5
6     cout << **pptr; // Output: 10
7
8     return 0;
9 }
  
```

Code 1.34: Pointer to Pointer Data Type

In the above example, the pointer `ptr` stores the memory address of the variable `x`, and the pointer `pptr` stores the memory address of the pointer `ptr`. You can use the double dereference operator `**` to access the value stored at the memory address.

1.7 Asymptotic Notations

Asymptotic notations are mathematical notations used to describe the limiting behavior of a function as the input size approaches infinity. They are used to analyze the complexity of algorithms and to compare the performance of different algorithms. The three most common asymptotic notations used in computer science are big-O notation, omega notation, and theta notation.

1.7.1 Big-O Notation

The *big-O notation* is used to describe the upper bound on the growth rate of an algorithm as the input size approaches infinity. It provides an upper limit on the worst-case time complexity of an algorithm. The big-O notation is used to analyze the efficiency of an algorithm in terms of the number of basic operations it performs.

1.7.2 Omega Notation

The *omega notation* or *big-omega notation* is used to describe the lower bound on the growth rate of an algorithm as the input size approaches infinity. It provides a lower limit on the best-case time complexity of an algorithm. The omega notation is used to analyze the efficiency of an algorithm in terms of the minimum number of basic operations it performs.

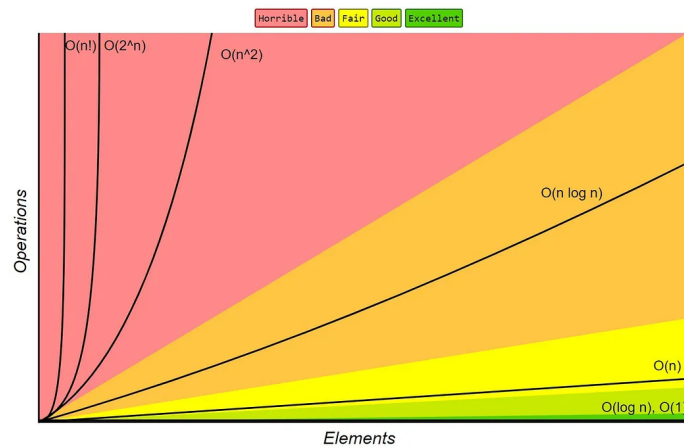


Figure 5: Asymptotic Notation

Big-O Complexity Analysis Chart from freeCodeCamp

1.7.3 Theta Notation

The *theta notation* or *big-theta notation* is used to describe the tight bound on the growth rate of an algorithm as the input size approaches infinity. It provides an upper and lower limit on the time complexity of an algorithm. The theta notation is used to analyze the efficiency of an algorithm in terms of the average number of basic operations it performs.

1.7.4 Complexity of an Algorithm

The *complexity of an algorithm* is a measure of the amount of time and space required to execute the algorithm as a function of the input size. It is used to analyze the efficiency of an algorithm and to compare different algorithms for the same problem. The complexity of an algorithm is usually expressed using big-O notation, which provides an upper bound on the growth rate of the algorithm as the input size increases.

1.7.4.1 Time Complexity

The *time complexity* of an algorithm is a measure of the amount of time required to execute the algorithm as a function of the input size. It is used to analyze the efficiency of an algorithm in terms of the number of basic operations it performs. The time complexity of an algorithm is usually expressed using big-O notation, which provides an upper bound on the growth rate of the algorithm as the input size increases.

1.7.4.1.1 Constant Time Complexity ($O(1)$)

An algorithm is said to have a *constant time complexity* if the execution time of the algorithm does not depend on the input size. It means that the algorithm takes the same amount of time to execute regardless of the input size. An example of an algorithm with constant time complexity is accessing an element in an array using its index.

```
1 int arr[5] = {1, 2, 3, 4, 5};
2 int x = arr[2]; // Accessing the element at index 2
```

Code 1.35: Constant Time Complexity

1.7.4.1.2 Logarithmic Time Complexity ($O(\log n)$)

An algorithm is said to have a **logarithmic time complexity** if the execution time of the algorithm grows logarithmically as the input size increases. An example of an algorithm with logarithmic time complexity is binary search, where the input size is halved at each step.

```
1 int binarySearch(int arr[], int n, int x) {  
2     int low = 0, high = n - 1;  
3     while (low <= high) {  
4         int mid = low + (high - low) / 2;  
5         if (arr[mid] == x) return mid;  
6         else if (arr[mid] < x) low = mid + 1;  
7         else high = mid - 1;  
8     }  
9     return -1;  
10 }
```

Code 1.36: Logarithmic Time Complexity

1.7.4.1.3 Linear Time Complexity ($O(n)$)

An algorithm is said to have a **linear time complexity** if the execution time of the algorithm grows linearly as the input size increases. It means that the algorithm takes a constant amount of time to process each element in the input. An example of an algorithm with linear time complexity is traversing an array to find the maximum element.

```
1 int findMax(int arr[], int n) {  
2     int max = arr[0];  
3     for (int i = 1; i < n; i++) {  
4         if (arr[i] > max) max = arr[i];  
5     }  
6     return max;  
7 }
```

Code 1.37: Linear Time Complexity

1.7.4.1.4 Linearithmic Time Complexity ($O(n \log n)$)

An algorithm is said to have a **linearithmic time complexity** if the execution time of the algorithm grows linearithmically as the input size increases. An example of an algorithm with linearithmic time complexity is sorting an array using the merge sort algorithm.

```
1 void merge(int arr[], int l, int m, int r) {  
2     // Merge two subarrays of arr[]  
3     int i, j, k;  
4     int n1 = m - l + 1;  
5     int n2 = r - m;  
6  
7     int *L = new int[n1];  
8     int *R = new int[n2];
```

```

9
10     for (i = 0; i < n1; i++) L[i] = arr[l + i];
11     for (j = 0; j < n2; j++) R[j] = arr[m + 1 + j];
12
13     i = 0; j = 0; k = l;
14     while (i < n1 && j < n2) {
15         if (L[i] <= R[j]) arr[k++] = L[i++];
16         else arr[k++] = R[j++];
17     }
18
19     while (i < n1) arr[k++] = L[i++];
20     while (j < n2) arr[k++] = R[j++];
21 }
22
23 void mergeSort(int arr[], int l, int r) {
24     if (l < r) {
25         int m = l + (r - l) / 2;
26         mergeSort(arr, l, m);
27         mergeSort(arr, m + 1, r);
28         merge(arr, l, m, r);
29     }
30 }

```

Code 1.38: Linearithmic Time Complexity

1.7.4.1.5 Quadratic Time Complexity ($O(n^2)$)

An algorithm is said to have a *quadratic time complexity* if the execution time of the algorithm grows quadratically as the input size increases. It means that the time taken by the algorithm to process each element in the input is proportional to the square of the input size. An example of an algorithm with quadratic time complexity is the bubble sort algorithm.

```

1 void bubbleSort(int arr[], int n) {
2     for (int i = 0; i < n - 1; i++) {
3         for (int j = 0; j < n - i - 1; j++) {
4             if (arr[j] > arr[j + 1]) {
5                 int temp = arr[j];
6                 arr[j] = arr[j + 1];
7                 arr[j + 1] = temp;
8             }
9         }
10    }
11 }

```

Code 1.39: Quadratic Time Complexity

Another common example of an algorithm with quadratic time complexity is a nested loop that iterates over all pairs of elements in an array.

1.7.4.1.6 Exponential Time Complexity ($O(2^n)$)

An algorithm is said to have an *exponential time complexity* if the execution time of the algorithm grows exponentially as the input size increases. It means that the time taken by the algorithm increases exponentially with each additional element in the input. An example of an algorithm with exponential time complexity is the recursive Fibonacci sequence algorithm.

```
1 int fibonacci(int n) {  
2     if (n <= 1) return n;  
3     return fibonacci(n - 1) + fibonacci(n - 2);  
4 }
```

Code 1.40: Exponential Time Complexity

1.7.4.1.7 Factorial Time Complexity ($O(n!)$)

An algorithm is said to have a *factorial time complexity* if the execution time of the algorithm grows factorially as the input size increases. It means that the time taken by the algorithm increases a factorial number of times with each additional element in the input. An example of an algorithm with factorial time complexity is the permutation algorithm that generates all possible permutations of a set of elements.

```
1 void permute(string str, int l, int r) {  
2     if (l == r) cout << str << endl;  
3     else {  
4         for (int i = l; i <= r; i++) {  
5             swap(str[l], str[i]);  
6             permute(str, l + 1, r);  
7             swap(str[l], str[i]);  
8         }  
9     }  
10 }
```

Code 1.41: Factorial Time Complexity

1.7.4.2 Space Complexity

The *space complexity* of an algorithm is a measure of the amount of memory required to execute the algorithm as a function of the input size. It is used to analyze the efficiency of an algorithm in terms of the amount of memory it uses. The space complexity of an algorithm is usually expressed using big-O notation, which provides an upper bound on the amount of memory the algorithm uses as the input size increases.

1.7.4.2.1 Constant Space Complexity ($O(1)$)

An algorithm is said to have a *constant space complexity* if the amount of memory required to execute the algorithm does not depend on the input size. It means that the algorithm uses a fixed amount of memory to process the input. An example of an algorithm with constant space complexity is swapping two variables without using a temporary variable.


```
1 void swap(int &a, int &b) {  
2     a = a + b;  
3     b = a - b;  
4     a = a - b;  
5 }
```

Code 1.42: Constant Space Complexity

1.7.4.2.2 Linear Space Complexity ($O(n)$)

An algorithm is said to have a **linear space complexity** if the amount of memory required to execute the algorithm grows linearly as the input size increases. It means that the algorithm uses a memory space that is proportional to the input size. An example of an algorithm with linear space complexity is storing the elements of an array in a separate array in reverse order.

```
1 void reverseArray(int arr[], int n) {  
2     int start = 0, end = n - 1;  
3     while (start < end) {  
4         int temp = arr[start];  
5         arr[start] = arr[end];  
6         arr[end] = temp;  
7         start++;  
8         end--;  
9     }  
10 }
```

Code 1.43: Linear Space Complexity

1.7.4.2.3 Quadratic Space Complexity ($O(n^2)$)

An algorithm is said to have a **quadratic space complexity** if the amount of memory required to execute the algorithm grows quadratically as the input size increases. It means that the algorithm uses a memory space that is proportional to the square of the input size. An example of an algorithm with quadratic space complexity is storing all pairs of elements in an array in a separate array.

```
1 void allPairs(int arr[], int n) {  
2     vector<int> pairs(n * n);  
3     for (int i = 0; i < n; i++) {  
4         for (int j = 0; j < n; j++) {  
5             pairs[i * n + j] = arr[i] + arr[j];  
6         }  
7     }  
8 }
```

Code 1.44: Quadratic Space Complexity

1.7.4.2.4 Exponential Space Complexity ($O(2^n)$)

An algorithm is said to have an **exponential space complexity** if the amount of memory required to execute the algorithm grows exponentially as the input size increases. An example of an algorithm with exponential space complexity is generating all subsets of a set of elements.

```
1 void generateSubsets(int arr[], int n) {  
2     for (int i = 0; i < (1 << n); i++) {  
3         for (int j = 0; j < n; j++) {  
4             if (i & (1 << j)) cout << arr[j] << " ";  
5         }  
6         cout << endl;  
7     }  
8 }
```

Code 1.45: Exponential Space Complexity

1.7.4.2.5 Factorial Space Complexity ($O(n!)$)

An algorithm is said to have a **factorial space complexity** if the amount of memory required to execute the algorithm grows factorially as the input size increases. An example of an algorithm with factorial space complexity is generating all permutations of a set of elements.

```
1 void permute(string str, int l, int r) {  
2     if (l == r) cout << str << endl;  
3     else {  
4         for (int i = l; i <= r; i++) {  
5             swap(str[l], str[i]);  
6             permute(str, l + 1, r);  
7             swap(str[l], str[i]);  
8         }  
9     }  
10 }
```

Code 1.46: Factorial Space Complexity

1.8 Summary

In this chapter, we introduced the fundamental concepts of data structures and algorithms. We discussed the importance of data structures and algorithms in computer science and software engineering. We also covered some basic terminologies related to data structures and algorithms, such as data, data object, data type, abstract data type, and complexity of an algorithm. We introduced the concept of asymptotic notations, such as big-O notation, omega notation, and theta notation, and discussed the time complexity of algorithms in terms of big-O notation. We covered common time complexity ranges from best to worst performance, such as constant time complexity, logarithmic time complexity, linear time complexity, linearithmic time complexity, quadratic time complexity, exponential time complexity, and factorial time complexity.

2

Arrays and Linked Lists

2.1 Introduction

Some of the most basic and fundamental data structures in computer science are arrays and linked lists. These data structures are used to store and manipulate collections of elements in a computer program. In this chapter, we will discuss the properties, operations, and complexity analysis of arrays and linked lists.

2.2 Arrays

An **array** is a collection of elements of the same data type that are stored in contiguous memory locations. It is used to store multiple values of the same type under a single name. The elements of an array can be accessed using an index value. In C++, arrays are zero-indexed, which means the first element is at index 0. Arrays also have a fixed size that is specified at the time of declaration.

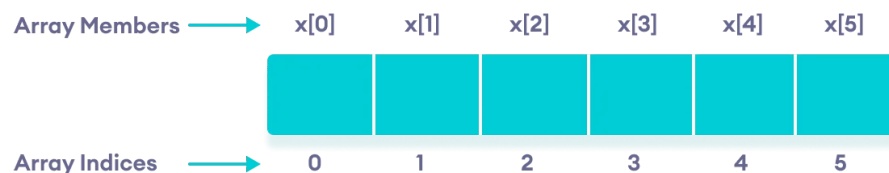


Figure 6: Elements of an array in C++

Elements of an array in C++ from Programiz

Figure 6 shows the visual representation of the elements of an array in C++. It shows the array members and indices.

```
1 // array.cpp
2 int main() {
3     int arr[6];
4     return 0;
5 }
```

Code 2.1: Array Declaration

The above code snippet declares an array named `arr` of size 6 that can store 6 integer values. The elements of the array are accessed using index values from 0 to 5 as shown in Figure 6.

```
1 // array_assign.cpp
2 int main() {
3     int arr[6];
4     arr[0] = 19;
5     arr[1] = 10;
6     arr[2] = 8;
7     return 0;
8 }
```

Code 2.2: Assigning Values to Array Elements

The above code snippet assigns values to the elements of the array `arr` at index 0, 1, and 2. The elements of the array can be accessed and modified using their index values. Array elements that are not explicitly initialized are assigned default values based on their data type. For example, integer elements are initialized to 0.



Figure 7: Initializing Array Elements

Initializing Array Elements from Programiz

Figure 7 shows the code for initializing array elements in C++. The array elements are initialized using curly braces `{}` with the values separated by commas. When the size of the array is specified, the number of elements in the initialization list must match the size of the array. If the size of the array is not specified, the size is automatically determined based on the number of elements in the array during initialization.

```
1 int main() {
2     int arr[6] = {19, 10, 8, 17, 9, 15};
3     return 0;
4 }
```

Code 2.3: Initializing Array Elements

The above code snippet initializes the elements of the array `arr` with the values 19, 10, 8, 17, 9, and 15. The size of the array is specified as 6, and the number of elements in the initialization list matches the size of the array.

```
1 int main() {
2     int arr[] = {19, 10, 8, 17, 9, 15};
```

```

3   return 0;
4 }

```

Code 2.4: Initializing Array Elements with Unspecified Size

The above code snippet initializes the elements of the array `arr` with the values 19, 10, 8, 17, 9, and 15. The size of the array is not specified and is automatically determined based on the number of elements in the initialization list.



Figure 8: Initializing Array Elements with Empty Members

Initializing Array Elements with Empty Members from Programiz

Figure 8 shows the code for initializing array elements with empty members in C++. The array elements are initialized using curly braces `{}` with empty members. Empty members only appear at the end of the initialization list and are assigned default values based on their data type. For example, integer elements are initialized to 0.

```

1 int main() {
2     int arr[6] = {19, 10, 8};
3     return 0;
4 }

```

Code 2.5: Initializing Array Elements with Empty Members

The above code snippet initializes the first three elements of the array `arr` with the values 19, 10, and 8. The remaining elements of the array are initialized to 0, which is the default value for integer elements.

2.2.1 Types of Arrays

There are two main types of arrays in C++: one-dimensional arrays and multi-dimensional arrays.

2.2.1.1 One-dimensional Array

A *one-dimensional array* is a collection of elements of the same data type that are stored in a single row. It is the most common type of array used in computer programming. The elements of a one-dimensional array are accessed using a single index value.

Figure 9 shows the visual representation of a one-dimensional array in C++. As shown in the figure, the elements of the array are stored in a single row, and each element is accessed using a single index value.

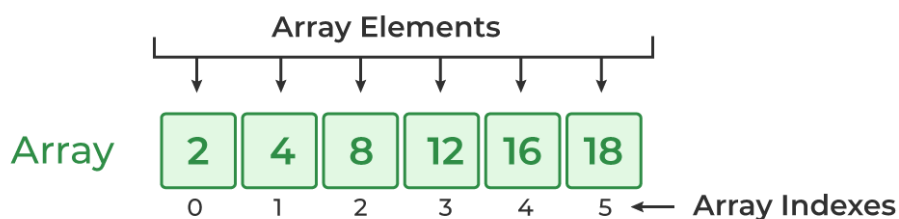


Figure 9: One-dimensional Array in C++

One-dimensional Array in C++ from GeekforGeeks

```

1 int main() {
2     int arr[6] = {2, 4, 8, 12, 16, 18};
3     return 0;
4 }

```

Code 2.6: One-dimensional Array

The above code snippet declares and initializes a one-dimensional array named `arr` with 6 integer elements. A one-dimensional array only has one set of square brackets `[]`. One set of square brackets signifies that the array is one-dimensional.

2.2.1.2 Multi-dimensional Array

A *multi-dimensional array* is a collection of elements of the same data type that are stored in multiple rows and columns. It is used to store data in a tabular format. The elements of a multi-dimensional array are accessed using multiple index values.

	Column 0	Column 1	Column 2
Row 0	<code>x[0][0]</code>	<code>x[0][1]</code>	<code>x[0][2]</code>
Row 1	<code>x[1][0]</code>	<code>x[1][1]</code>	<code>x[1][2]</code>
Row 2	<code>x[2][0]</code>	<code>x[2][1]</code>	<code>x[2][2]</code>

Figure 10: Two-dimensional Array in C++

Two-dimensional Array in C++ from GeekforGeeks

Figure 10 shows the visual representation of a two-dimensional array in C++. As shown in the figure, the elements of the array are stored in multiple rows and columns, and each element is accessed using two index values. The number of elements in a two-dimensional array is determined by the number of rows and columns.

```
1 int main() {  
2     int arr[3][4] = {  
3         {1, 2, 3, 4},  
4         {5, 6, 7, 8},  
5         {9, 10, 11, 12}  
6     };  
7     return 0;  
8 }
```

Code 2.7: Two-dimensional Array

The above code snippet declares and initializes a two-dimensional array named `arr` with 3 rows and 4 columns. A two-dimensional array has two sets of square brackets `[] []`. Two sets of square brackets signify that the array is two-dimensional. The number of rows and columns in a two-dimensional array is specified within the square brackets. The first set of square brackets specifies the number of rows, and the second set of square brackets specifies the number of columns. Thus, in the above example, the array `arr` has 3 rows and 4 columns.

```
1 int main() {  
2     int arr[3][4] = {  
3         {1, 2},  
4         {5, 6, 7},  
5         {9}  
6     };  
7     return 0;  
8 }
```

Code 2.8: Two-dimensional Array with Empty Members

2.2.2 Array Operations

2.2.2.1 Insertion

2.2.2.2 Deletion

2.2.2.3 Searching

2.2.3 Complexity Analysis of Arrays

2.3 Linked Lists

2.3.1 Types of Linked Lists

2.3.1.1 Singly Linked List

2.3.1.2 Doubly Linked List

2.3.1.3 Circular Linked List

2.3.2 Operations on Linked Lists

2.3.2.1 Insertion

2.3.2.2 Deletion

2.3.2.3 Searching

2.3.3 Complexity Analysis of Linked Lists

2.4 Comparison of Arrays and Linked Lists

2.5 Summary

3

Stacks and Queues

3.1 Introduction

3.2 Stacks

3.2.1 Operations on Stacks

3.2.1.1 Push

3.2.1.2 Pop

3.2.1.3 Peek

3.2.1.4 isEmpty

3.2.1.5 isFull

3.2.2 Complexity Analysis of Stacks

3.2.3 Implementation of Stacks Using Arrays

3.2.4 Implementation of Stacks Using Linked Lists

3.3 Queues

3.3.1 Types of Queues

3.3.1.1 Linear Queue

3.3.1.2 Circular Queue

3.3.1.3 Priority Queue

3.3.1.4 Double-ended Queue (Deque)

3.3.2 Operations on Queues

3.3.2.1 Enqueue

3.3.2.2 Dequeue

3.3.2.3 Front

3.3.2.4 Rear

3.3.3 Complexity Analysis of Queues

3.3.4 Implementation of Queues Using Arrays

3.3.5 Implementation of Queues Using Linked Lists

3.4 Comparison of Stacks and Queues

4

Trees

4.1 Introduction

4.2 Properties of Trees

4.2.1 Root Node

4.2.2 Parent Node

4.2.3 Child Node

4.2.4 Leaf Node

4.2.5 Ancestors

4.2.6 Siblings

4.2.7 Descendants

4.2.8 Height of a Tree

4.2.9 Depth of a Node

4.2.10 Degree of a Node

4.2.11 Level of a Node

4.2.12 Subtree

4.3 Types of Trees

4.3.1 Binary Tree

4.3.1.1 Types of Binary Trees

4.3.1.1.1 Left-skewed Binary Tree

4.3.1.1.2 Right-skewed Binary Tree

4.3.1.1.3 Complete Binary Tree

4.3.2 Ternary Tree

4.3.3 N-ary Tree

4.3.4 Binary Search Tree

4.3.5 AVL Tree

4.3.6 Red-Black Tree

4.4 Basic Operations on Trees

5

Graphs

5.1 Introduction

5.2 Properties of Graphs

5.2.1 Vertex

5.2.2 Edge

5.2.3 Degree of a Vertex

5.2.4 Path

5.3 Types of Graphs

5.3.1 Finite Graph

5.3.2 Infinite Graph

5.3.3 Trivial Graph

5.3.4 Simple Graph

5.3.5 Multi Graph

5.3.6 Null Graph

5.3.7 Complete Graph

5.3.8 Pseudo Graph

5.3.9 Regular Graph

5.3.10 Bipartite Graph

5.3.11 Labelled Graph

5.3.12 Weighted Graph

5.3.13 Directed Graph

5.3.14 Undirected Graph

5.3.15 Connected Graph

5.3.16 Disconnected Graph

5.3.17 Cyclic Graph

5.3.18 Acyclic Graph

5.3.19 Directed Acyclic Graph (DAG)

6

Sorting and Searching

6.1 Introduction

6.2 Sorting

6.2.1 Types of Sorting Algorithms

6.2.1.1 Bubble Sort

6.2.1.2 Selection Sort

6.2.1.3 Insertion Sort

6.2.1.4 Merge Sort

6.2.1.5 Quick Sort

6.2.1.6 Heap Sort

6.2.1.7 Radix Sort

6.2.1.8 Counting Sort

6.2.1.9 Bucket Sort

6.2.2 Comparison of Sorting Algorithms

6.3 Searching

6.3.1 Types of Searching Algorithms

6.3.1.1 Linear Search

6.3.1.2 Binary Search

6.3.1.3 Jump Search

6.3.1.4 Interpolation Search

6.3.1.5 Exponential Search

6.3.1.6 Fibonacci Search

6.3.1.7 Ternary Search

6.3.2 Comparison of Searching Algorithms

6.4 Summary

7

Hashing

7.1 Introduction

7.2 Hash Table

7.3 Hash Function

7.4 Collision Resolution Techniques

7.4.1 Separate Chaining

7.4.2 Open Addressing

7.4.2.1 Linear Probing

7.4.2.2 Quadratic Probing

7.4.2.3 Double Hashing

7.5 Complexity Analysis of Hashing

7.6 Summary

8

Advanced Data Structures and Algorithms

8.1 Introduction

8.2 Advanced Data Structures

8.2.1 Segment Tree

8.2.2 Fenwick Tree

8.2.3 Suffix Tree

8.2.4 Suffix Array

8.2.5 Trie

8.2.6 Heap

8.2.7 Disjoint Set

8.2.8 Skip List

8.2.9 Splay Tree

8.2.10 Bloom Filter

8.2.11 KD Tree

8.2.12 Quad Tree

8.2.13 Octree

8.2.14 B-Tree

8.2.15 B+ Tree

8.2.16 R-Tree

8.2.17 X-Tree

8.2.18 Y-Tree

8.2.19 Z-Tree

8.3 Advanced Algorithms

8.3.1 Dynamic Programming

8.3.2 Greedy Algorithms

9

Applications of Data Structures and Algorithms

9.1 Applications in Computer Science

9.1.1 Operating Systems

9.1.2 Database Management Systems

9.1.3 Compiler Design

9.1.4 Networking

9.1.5 Artificial Intelligence

9.1.6 Machine Learning

9.1.7 Computer Graphics

9.1.8 Computer Vision

9.1.9 Robotics

9.1.10 Web Development

9.1.11 Mobile Development

9.1.12 Game Development

9.1.13 Cybersecurity

9.1.14 Quantum Computing

9.2 Applications in Real Life

9.2.1 Social Media

9.2.2 E-commerce

9.2.3 Healthcare

9.2.4 Finance

9.2.5 Transportation

9.2.6 Education

9.2.7 Agriculture

9.2.8 Manufacturing

9.2.9 Entertainment

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