

Data Structures and Algorithms¹

A Study Guide for Students of Sorsogon State
University - Bulan Campus²

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²This book is a study guide for students of Sorsogon State University - Bulan Campus taking up the course Data Structures and Algorithms.

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Preface

“Bad programmers worry about the code. Good programmers worry about data structures and their relationships.”

– Linus Torvalds

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